

佇列 Queue

- First in First out

EX: Convert a sequence of digits into the decimal value

247.53

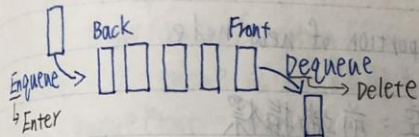
```
do { aQueue.dequeue(ch) // 移除空格
} while (ch is blank)
n = 0
done = false
while (!done && ch is digit) {
    n = n * 10 + integer of ch
    if (aQueue.isEmpty()) // 判斷是否為空
        done = true
    else aQueue.dequeue(ch) // 移除佇列最前面 ch
} // while
if (!done && ch == '.') {
    aQueue.dequeue(ch) // 移除小數點
    // 判斷小數後有幾位
    p = 0
    while (!done && ch is digit) {
        n = n * 10 + integer of ch
        p++
        if (aQueue.isEmpty())
            done = true
        else aQueue.dequeue(ch)
    } // while
    n = n * (0.1)p
} // if
```

判斷迴文：比較 stack 頂端和 queue 前端

EX: Recognizing Palindromes.

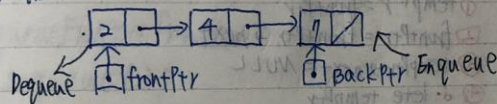
```
isPal  
aQueue.createQueue()  
aStack.createStack()  
for (the next character ch in str) {  
    aQueue.enqueue(ch)  
    aStack.push(ch)  
} // for  
charEqual = true  
while (!aQueue.isEmpty() && charEqual) {  
    <法1> aQueue.getFront(front) <法2> aQueue.dequeue(front)  
    aStack.getTop(top) aStack.pop(top)  
    if (front == top) {  
        aQueue.dequeue()  
        aStack.pop()  
    } // if  
    else charEqual = false  
} // while
```

Implementations of the ADT Queue

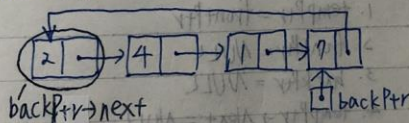


- A circular linked list with one external reference
 - Only a reference to the back (環狀: 只有後端)
- 優: 只有一個變數

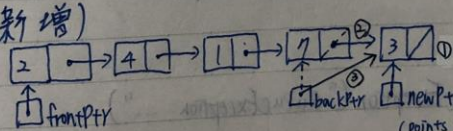
linked list



Circular linked list

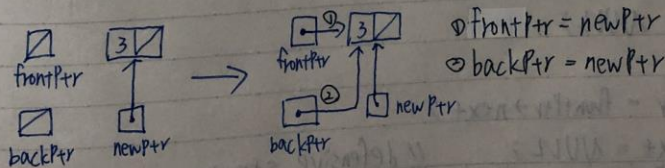


Enqueue (新增)



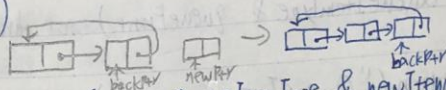
- ① $newPtr \rightarrow next = NULL$
- ② $backPtr \rightarrow next = newPtr$
- ③ $backPtr = newPtr$
(points to new node)

若一開始為空



- ① $frontPtr = newPtr$
- ② $backPtr = newPtr$

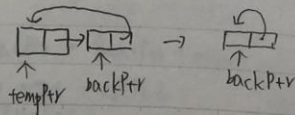
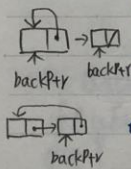
Circular (環狀)



```
void Queue::enqueue(const QueueItemType & newItem) { // 新增
    QueueNode * newPtr = new QueueNode;
    newPtr->item = newItem;
    if (isEmpty()) // 0 -> 1 node
        newPtr->next = newPtr; // point to itself
    else { // k -> k+1 nodes, k > 0
        newPtr->next = backPtr->next; // point to the front
        backPtr->next = newPtr; // put behind the back
    } // else
    backPtr = newPtr; // new node at the back
} // enqueue
```

```
void Queue::dequeue() throw (QueueException) { // 移除
    if (isEmpty())
        throw ...;
    else {
```

```
        QueueNode * tempPtr = backPtr->next; // tempPtr 指向 front
        if (backPtr == backPtr->next) // 只有一個節點
            backPtr = NULL; // one node -> empty
        else // the next front
            backPtr->next = tempPtr->next;
        tempPtr->next = NULL; // defensive strategy
        delete tempPtr; // release space
    } // else
} // dequeue
```

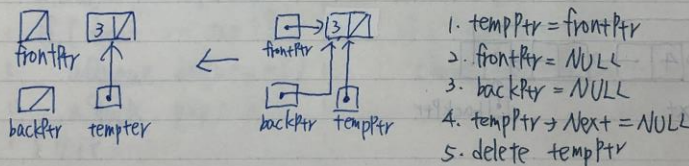
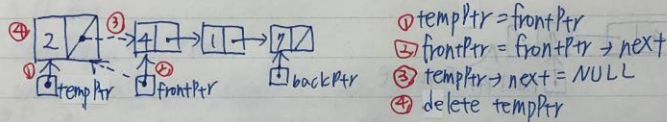


```

void Queue::enqueue (const QueueItemType & newItem) { // 擷取後移除
    QueueNode * newPtr = new QueueNode;
    newPtr->item = newItem; // set data portion of new node
    newPtr->next = NULL; // 新節點及指標
    if (isEmpty()) frontPtr = newPtr; // 至空: 前端指標
    else backPtr->next = newPtr; // 非空: 後端指標下一個
    backPtr = newPtr; // new node is at the back
} // enqueue

```

Dequeue (移除)



```

void Queue::dequeue() {
    if (isEmpty()) throw QueueException("QueueException: ...");
    else {
        QueueNode * tempPtr = frontPtr;
        if (frontPtr == backPtr) { // one node only
            frontPtr = NULL;
            backPtr = NULL;
        } // if
        else frontPtr = frontPtr->next;
        tempPtr->next = NULL; // defensive strategy
        delete tempPtr; // 釋放空間
    } // else
} // dequeue

```


陣列實作佇列ADT (使用環狀陣列)

To initialize the queue:

front = 0

back = Max-Queue - 1

count = 0

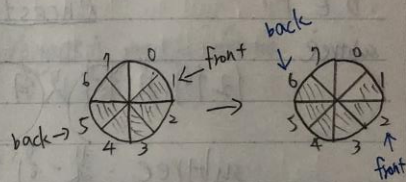
Insert:

$back = (back + 1) \% \text{Max_QUEUE};$

items[back] = newItem;

++count;

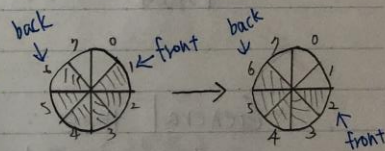
back 初始值 = Max-Queue - 1



Deleting:

$front = (front + 1) \% \text{Max_QUEUE};$

--count;

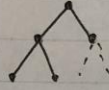


全空條件: count = 0

全滿條件: count = Max-QUEUE

Binary Tree

最多 2 個 node

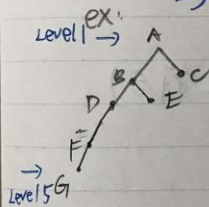


left subtree
right subtree

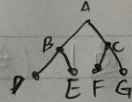
* Height of a tree (樹高)

→ number of nodes along the longest path from root to a leaf

→ 影響效率 (越小越好)



height 5



height 3

* Level of a node n in a tree T (階層)

* 最大階層 = 樹高

$$\text{height}(T) = 1 + \max \{ \text{height}(T_L), \text{height}(T_R) \}$$

* 樹裡無 cycle

Full Binary Tree (完全樹)



height h is full

- nodes at levels $< h$ have two children each

complete Binary Tree (完整樹)

① full to level-1 ex: level=5, level 4 is full binary tree

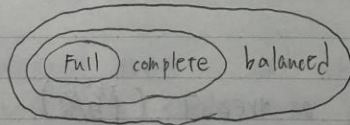
② Level h is filled from left to right

③ at levels $< h-2$ have two children each

balanced

→ 左樹高, 右樹高差距不超過 1. (每個點都要符合)

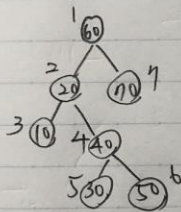
→ 效率穩定, 省空間



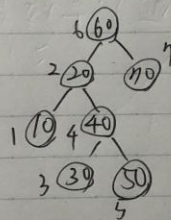
Traversal

- preorder \Rightarrow visit root before visiting its subtrees.
- Inorder \Rightarrow visit root between visiting its subtrees.
- Postorder \Rightarrow visit root after visiting its subtrees

Preorder

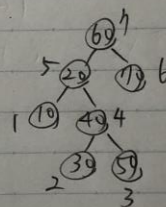


Inorder



左邊先

Postorder

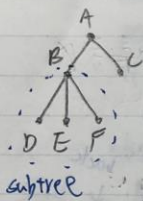


Inorder \equiv sort

Trees

目的: 紀錄資料關係 (= 維)

內容導向



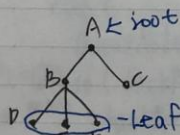
Trees are hierarchical

- Parent-child relationship between two nodes
- Ancestor-descendant relationship among nodes

任何資料只有一個直屬長官適用於 trees

subtree: 某部份資料形成小樹
子樹

General tree: one or more nodes
root: a single node



Parent of node B: A

- leaf 葉節點: A node with no children

siblings 兄弟節點: Node with a common parent
(父節點為同一人)

Ancestor of node B 祖先節點 A D

Decendant of node B 子孫節點 D A