

Ch 5.

rule: last in first out (LIFO)

Applications of Stacks:

- (1) Check for balanced braces 檢查成對括號
- (2) Recognize strings in a language 辨識語言
- (3) Algebraic expression evaluation 代數運算式求解
- (4) Search a path 搜尋一條路徑

Operation for ADT stack:

- isEmpty() 是否為空
 - push (in newItem: StackItemType) 新增一筆
 - pop() 移除最近一筆
 - getTop (out stackTop: StackItemType) 擷取最近一筆
 - pop (out stackTop: StackItemType) 擷取後移除最近一筆
- } throw StackException

Examples of checking for balanced braces

```
while (not end of string) {  
    if (ch == "{")  
        aStack.push(ch)  
    else if (ch == "}")  
        aStack.pop()  
}
```

```
while (not end of string) {  
    if (ch == "{")  
        aStack.push(ch)  
    else if (ch == "}") {  
        if (!aStack.isEmpty())  
            aStack.pop()  
        else return false  
    }  
}
```

```
while (not end of string && count >= 0) {  
    get next ch;  
    switch (ch) {  
        case "{": count ++  
        case "}": count --  
    }  
}
```

rule: first in first out (FIFO)

• Applications of Queue

- (1) Reading a string of characters 讀入字串
- (2) Recognize a palindrome 辨識迴文
- (3) Simulation 模擬

• A queue:

- New items enter at the back, or rear, of the queue.
- Items leave from the front of the queue.
- First in first out (FIFO) property

• Queues:

- Are appropriate for many real-world situations
- Have applications in computer science
- Simulation
 - A study to show how to reduced the wait involved in an application (自然界或人類的行為)

• Operations for ADT queue:

- is Empty() 是否為空
- enqueue (in newItem: QueueItemType) 新增
- dequeue() 移除
- getFront (out queueFront: QueueItemType) 擷取
- dequeue (out queueFront: QueueItemType) 擷取後移除

} throw QueueException

• Simulation

- A technique for modeling the behavior of both natural and human-made systems (行為模型)
- Goal:
 - Generate statistics that summarize the performance of an existing system
 - Predict the performance of a proposed system

- Analysis of algorithms

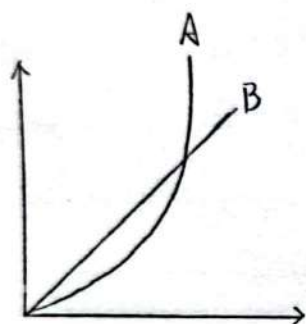
- Time efficiency
- Space efficiency

- A comparison of algorithms:

- Should focus on significant differences in efficiency
- Should not consider reductions in computing costs due to clever coding tricks

- 3 difficulties with comparing programs of algorithms:

- (1) specific implementation 実作
- (2) computer 電腦設備
- (3) data 資料



Algorithm A requires time proportional to n^2 growth-rate functions

Algorithm B requires time proportional to n

Algorithm A: $O(n^2)$, Algorithm B: $O(n)$ — Big O notation

- Growth-rate function $f(n)$

- A mathematical function used to specify an algorithm's order in terms of the size of the problem

- Definition of the order of an algorithm

- Algorithm A is order $f(n)$ — denoted $O(f(n))$

$O(1)$ $O(\lg n)$ $O(n)$ $O(n \lg n)$ $O(n^2)$ $O(n^3)$ $O(2^n)$
 優 ← ————— → 劣
 $O(f(n)) + O(g(n)) = O(f(n) + g(n))$

- Worst case: maximum amount of time an algorithm requires to solve problems of size n .
- Average case: average amount of time an algorithm requires to solve problems of size n .
- Best case: minimum amount of time an algorithm requires to solve problems of size n .

• Stable sort vs Unstable sort

bubble
insertion
merge
radix

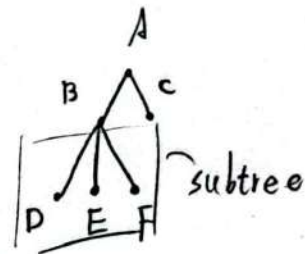
quick
selection
heap

if $a=b$, 排序完後仍保持
 a, b 的順序 \rightarrow stable

	worst	best
bubble	$O(n^2)$	$O(n^2)$
insertion	$O(n^2)$	$O(n)$
merge	$O(n \log n)$	$O(n \log n)$
radix	$O(d(n+r))$	$O(d(n+r))$
quick	$O(n^2)$	$O(n \log n)$
selection	$O(n^2)$	$O(n)$

Ch 8

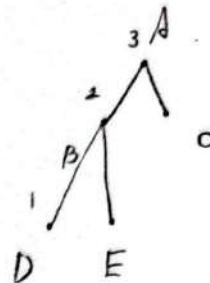
- Trees are composed of nodes and edges
- Trees are hierarchical
 - Parent-child relationship between 2 nodes
 - Ancestor-descendant relationships among nodes



- Subtree :
 - Any node and its descendants
- Leaf :
 - A node with no children
- Siblings :
 - Nodes with a common parent
- Ancestor of node B :
 - A node on the path from root to B
- Descendant of node B :
 - A node on the path from B to leaf
- Root
 - The only node in the tree with no parent

• Binary tree:

- A binary tree is a set T of nodes such that either
 - T is empty or
 - T is partitioned into three disjoint subsets:
 - (1) a single node r , the root
 - (2) 2 possibly empty sets that are binary trees, called the left subtree of r and the right subtree of r



• Height of a tree:

- Number of nodes along the longest path from the root to a leaf

• Level of a node in a tree T :

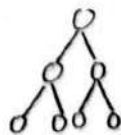
- If n is the root of T , it's at level 1
- If n isn't the root, its level is 1 greater than the level of its parent

• Height of a tree T defined in terms of the levels of its nodes

- If T is empty, its height is 0
- If T isn't empty, its height is equal to the maximum level of its nodes

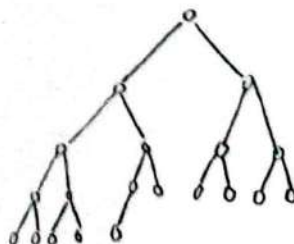
• Full Binary Tree

- A binary tree of height h is full if nodes at levels $< h$ have 2 children nodes



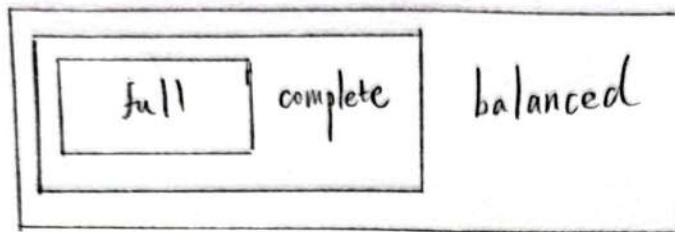
• Complete Binary Tree

- A binary tree of height h is complete if
 - (1) All nodes at levels $\leq h-2$ have 2 children
 - (2) When a node at level $h-1$ has children, all nodes to its left at the same level have 2 children
 - (3) When a node at level $h-1$ has 1 child, it's a left child



- Balanced binary tree

- A binary tree is balanced if the height of any node's 2 subtrees differ by no more than 1



- Traversals of a binary tree

- Preorder Traversal

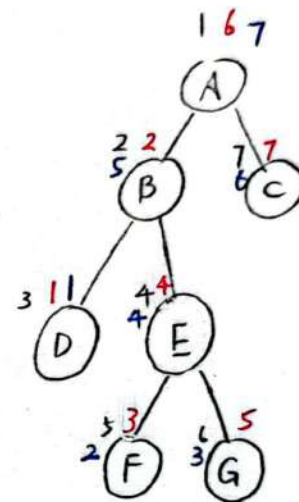
- Visit root before visiting its subtrees
- Before the recursive calls

- Inorder Traversal

- Visit root between visiting its subtrees
- Between the recursive calls

- Postorder Traversal

- Visit root after visiting its subtrees
- After the recursive calls



Preorder : 1 2 3 4 5 6 7

Inorder : 3 2 4 1 5 6 7

Postorder : 3 2 4 5 6 7 1