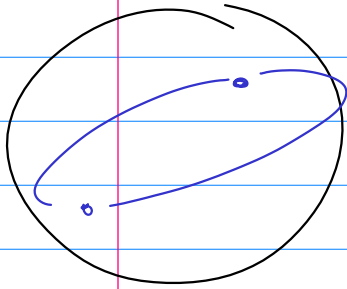


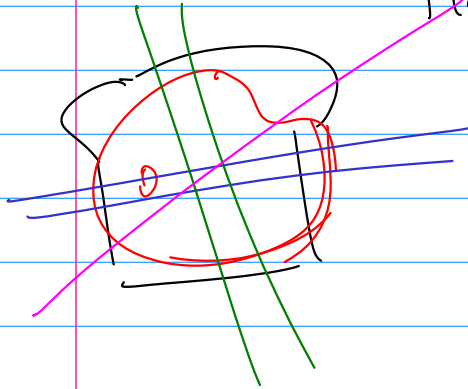
Thm



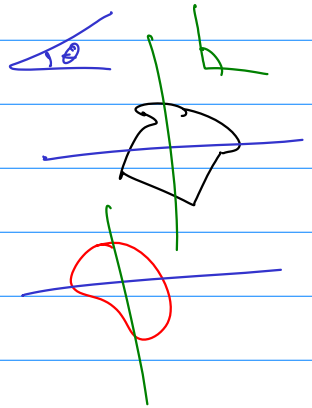
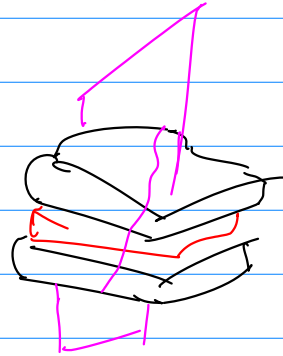
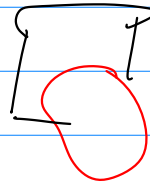
Antipodes

On earth,  
At any given time, there exists  
a pair of antipodes  
at which the temp and the pressure  
are the same.

Ham sandwich theorem



3-d variant



1.5 : If two one-sided limits exist and equal  $L$ ,  
then the overall limit exists and equals  $L$ .

1.8 : If the overall limit exists and equals  $L$ ,  
and the function at the same place equals  $L$ ,  
then the function is continuous there.

$$\lim_{x \rightarrow a} f(x) = f(a)$$

$\Updownarrow$   
f is cont.  
at a

Just defined

or

Just limit  
existing

alone do not imply continuity!

1.7 The precise def of a limit...

1.6 ... gives us limit laws,  
and the direct subst-property for

- Polynomials
  - Rational functions
  - Root functions
  - Trig functions
- } continuous on their domains, and the DSP works on their domains.

$$\lim_{x \rightarrow 1} \frac{x^2 - 1}{x - 1}$$

1.5 If DSP fails, try manipulating the expression, and try again.

If that fails, check for asymptotes.

Determine whether  $\lim = \infty$  or  $-\infty$ .

*This is the only time we are allowed to use a table or a sketch.*

Otherwise,  
limit DNE.

*$\lim_{x \rightarrow 5^+} \frac{1}{x-5}$ ? try  $\frac{1}{5.1-5}$ , get clues.*

Find a cubic function with  $\underline{f(5) = 60}$   
and  $\underline{f(-1) = f(0) = f(6) = 0}$   
 $\underline{=0 \quad =0 \quad =0}$

-1, 0, 6 are zeros of  $f(x)$ .

$f(x) = 2x^2 - 6x + 4 = 0$   
Find zeros.

$$x = -1 \quad x = 0 \quad x = 6$$
$$x + 1 = 0 \quad x = 0 \quad x - 6 = 0$$

$$(x+1) \times (x-6) = 0$$

$$f(x) = \boxed{n} x(x+1)(x-6) \quad f(5) = 60$$

$$f(5) = \boxed{n} 5(6)(-1)$$

$$2(x^2 - 3x + 2) = 0$$
$$2(x-1)(x-2) = 0$$

↙                      ↘

$$x-1=0 \quad x-2=0$$
$$x=1 \quad x=2$$

$$f(5) = -30n = 60$$

$n = -2$

$$\underline{f(x) = -2x(x+1)(x-6)}$$