

Assignment 14: Due Mon Nov 13th

Suppose

$$\log_5(a) + \log_5(b^2) = -91$$

$$\log_5(b) + \log_5(a^2) = 103$$

$$A = \log_5(a)$$

$$B = \log_5(b)$$

Find ab.

$$\log_5(a) + 2 \cdot \log_5(b) = -91$$

$$\log_5(b) + 2 \cdot \log_5(a) = 103$$

$$A + 2B = -91$$

$$B + 2A = 103$$

$$B = 103 - 2A$$

$$A + 2(103 - 2A) = -91$$

$$A + 206 - 4A = -91$$

$$-3A + 206 = -91$$

$$-3A = -297$$

$$A = 99$$

$$\log_5 a = 99$$

$$a = 5^{99}$$

$$B + 2(99) = 103$$

$$B + 198 = 103$$

$$B = -95$$

$$\log_5 b = -95$$

$$b = 5^{-95}$$

$$(5^{99})(5^{-95})$$

$$5^4 = 625$$