## Simulation data

reference doubleml.datasets.make\_irm\_data
https://docs.doubleml.org/stable/api/generated/doubleml.datasets.make\_irm\_data.html#d
oubleml-datasets-make-irm-data

### setting

```
library(mvtnorm)
#sample size, number of covariates, parameters setting
n=7500
p=10
tim=c(0,1,2,3,4)
beta=c(0.5,0.5,1,1/4,1/9,0,0,0,0,0)
G=matrix(0,(p-2),(p-2))
diag(G)=0.09
theta=0
logisticf=function(x){\exp(x)/(1+\exp(x))}
cd=sqrt(logisticf(tim*0)^2*(pi^2/3)/((1-logisticf(tim*0)^2)*sum(beta*beta)))
cy=sqrt((logisticf((tim*0+1.3)))^2/((1-(logisticf((tim*0+1.3)))^2)*sum(beta*beta)))
#functions and matrices(save value)
X1=matrix(0,n,(p-2))
vaso=matrix(0,n,1)
water=matrix(0,n,1)
Death=matrix(0,n,1)
treat=matrix(0,n,1)
data=matrix(0,n*length(tim),19)
data D=matrix(0,n,length(tim))
deathp=0
```

# generating

```
set.seed(1219)
v=matrix(c(rnorm(n*(p-2),0,1)),n,(p-2))
X2=matrix(c(rbinom(n,1,0.5),rnorm(n,0,1)),n,2)
set.seed(61916)
for(j in c(1:(length(tim)))){
 X1=rmvnorm(n,rep(0,(p-2)),G)+v-matrix(theta,n,p-2)
 X=cbind(X2,X1)
 term=c(X%*%matrix(beta,p,1)*cd[j])
  g=logisticf(term)
 treat=matrix(rbinom(n,1,g),n,1)
 water=matrix(rgamma(n,exp(term)/2,2),n,1)*5
 water[water<0.01]=0
 vaso=matrix(rgamma(n,exp(term)/2,2),n,1)/50
 vaso[vaso<0.001]=0
 theta=(water+vaso)/(1+water+vaso)
 y=-0.6+0.5*X[,2]+0.5*exp(c(X%*%matrix(beta,p,1)*cy[j]))*(1-c(treat))
  deathp=tanh(y)/2+0.5
```

```
data_D[,j]=c(rbinom(n,1,deathp))
 Death=data_D[,j]
 Score=c(rexp(n,(1-deathp/1.285)))
 Dsofa=(Score-1)
 Dsofamean=(1-deathp/1.285)^-1
 y0=-0.6+0.5*X[,2]
 y0=tanh(y0)/2+0.5
 y1=-0.6+0.5*X[,2]+0.5*exp(c(X%*%matrix(beta,p,1)*cy[j]))
 y1=tanh(y1)/2+0.5
 #store
 data[c((n*tim[j]+1):(n*tim[j]+n)),1]=c(1:n)
  data[c((n*tim[j]+1):(n*tim[j]+n)),2]=rep(tim[j],n)
  data[c((n*tim[j]+1):(n*tim[j]+n)),3]=y1-y0
 data[c((n*tim[j]+1):(n*tim[j]+n)),4]=Death
 data[c((n*tim[j]+1):(n*tim[j]+n)),5]=(1-y1/1.285)^{(-1)}-(1-y0/1.285)^{(-1)}
 data[c((n*tim[j]+1):(n*tim[j]+n)),6]=Dsofa
  data[c((n*tim[j]+1):(n*tim[j]+n)),7]=c(treat)
 data[c((n*tim[j]+1):(n*tim[j]+n)),18]=vaso
 data[c((n*tim[j]+1):(n*tim[j]+n)),19]=water
 data[c((n*tim[j]+1):(n*tim[j]+n)),8:17]=X
}
colnames(data)=c("id","bloc","true ite.(Death)","Death","true ite(Dsofa)","Dsofa",
"Treat", "gender", "age", "X1", "X2", "X3", "X4", "X5", "X6", "X7", "X8", "vaso", "water")
data=as.data.frame(data)
data bloc1=data[data$bloc==0,]
data_bloc1$Death=data_D[,1]
data bloc1$Treat=1-data bloc1$Treat
#mark NA at Death=1
for(j in c(1:(length(tim)-1))){
  count=c(1:n)
 deathid=count[c(count*data D[,j])!=0]
 for(i in c(1:length(deathid))){
    data[(data$id==deathid[i] & data$bloc>=j),c(-1,-2)]=NA
  }
}
data=na.omit(data)
colnames(data bloc1)=c("id","bloc","true ite.(Death)","Death","true ite(Dsofa)",
"Dsofa", "Treat", "X1", "X2", "X3", "X4", "X5", "X6", "X7", "X8", "X9", "X10", "vaso", "water")
```

#### export

```
data_class=data_bloc1[,c(-5,-6,-18,-19)]
data_cont=data_bloc1[,c(-3,-4,-18,-19)]
write.csv(data_class,"C:/Users/ASUS/Desktop/cg working/CausalML/simulation
data_DTR/for plan/simulation data(binary).csv",row.names = F)
write.csv(data_cont,"C:/Users/ASUS/Desktop/cg working/CausalML/simulation
data_DTR/for plan/simulation data(cont.).csv",row.names = F)
write.csv(data,"C:/Users/ASUS/Desktop/cg working/CausalML/simulation data_DTR/for
plan/simulation data.csv",row.names = F)
```

```
#------binary case------
#data view
options(digits=4)
table view=as.data.frame(matrix(c(dim(data class),sum(data class$Death),
sum(data_class$Treat)),1,4))
colnames(table_view)=c("columns","rows","death","treatments")
head(data_class,10)
##
     id bloc true_ite.(Death) Death Treat X1
                                          X2
                                                   Х3
                                                          Х4
## 1
                                       0.6530 -0.004351 0.5868 -2.81646
                   0.43496
                             0
                                  1 1
## 2
     2
          0
                   0.13469
                             0
                                  1 1 -0.3354 -0.689923 0.3452 -0.18485
## 3
          0
     3
                             1
                                  1 1 0.6364 -0.764598 0.3414 0.11179
                   0.28341
## 4
     4
          0
                   0.58682
                             0
                                  0 0 -0.6669 0.507079 2.6162 1.75030
## 5
                   0.50444
     5
          0
                             1
                                  1 0 -0.2783 0.747434 0.4201 0.90179
## 6
     6
          0
                   0.04035
                             0
                                  0 1 -0.5594 -1.434221 0.3674 -0.86756
                                  0 1 -0.1179 -0.499280 -2.0258 1.00651
## 7
     7
                             0
          0
                   0.12383
## 8
     8
          0
                   0.37268
                             0
                                  1 1 -1.8862 1.478520 -0.1303 -0.03908
## 9
     9
          0
                   0.15913
                             1
                                  0 0 1.1972 -1.326675 1.5558 -0.65288
                                  1 0 -0.8247 -1.066176 -1.5254 -0.03394
## 10 10
          0
                   0.01654
                             0
##
                X7
                              Х9
          X6
                       X8
                                    X10
## 1
     0.76661 -1.3398 1.0175 0.8941 0.4022
## 2 -1.28426 -0.2198 0.2567 0.4932 -0.5382
## 3 -1.05009 0.9096 0.4286 -0.6812 -1.5088
## 4
     0.31831 -1.0196 -0.4373   0.8833   0.5784
     0.68670 -1.4643 2.1852 -0.1837 0.2503
## 5
## 6 -1.01713 0.3859 0.2017 -1.3333 -0.5931
## 7 -0.47259 1.0194 1.7846 -1.3659
                                 0.2302
## 8 -0.33175 0.4671 -0.5443 2.4378 0.1546
## 9
     0.19008 -1.4914 -0.3171 -2.2652 2.2846
## 10 0.01192 -1.5894 1.9007 1.6740 -0.8389
table_view
    columns rows death treatments
## 1 7500
           15 2751
                         3448
```

#### **ATE**

```
#calculating ATE
n=2000000
p=10
tim=c(0,1,2,3,4)
beta=c(0.5,0.5,1,1/4,1/9,0,0,0,0)
G=matrix(0,(p-2),(p-2))
diag(G)=0.09
theta=0

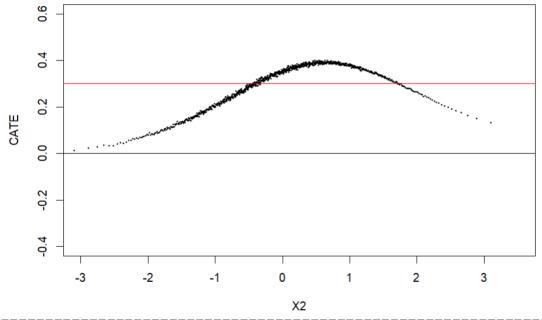
X1=matrix(0,n,(p-2))
vaso=matrix(0,n,1)
water=matrix(0,n,1)
Death=matrix(0,n,1)
```

```
treat=matrix(0,n,1)
logisticf=function(x){exp(x)/(1+exp(x))}
cd=sqrt(logisticf(tim*0)^2*(pi^2/3)/((1-logisticf(tim*0)^2)*sum(beta*beta)))
 cy = sqrt((logisticf((tim*0+1.3)))^2/((1-(logisticf((tim*0+1.3)))^2)*sum(beta*beta))) 
set.seed(1219)
v=matrix(c(rnorm(n*(p-2),0,1)),n,(p-2))
X2=matrix(c(rbinom(n,1,0.5),rnorm(n,0,1)),n,2)
#generating
j=1
set.seed(61916)
X1=rmvnorm(n,rep(0,(p-2)),G)+v-matrix(theta,n,p-2)
X=cbind(X2,X1)
term=c(X%*%matrix(beta,p,1)*cd[j])
g=logisticf(term)
y=-0.6+0.5*X[,2]+0.5*exp(c(X%*%matrix(beta,p,1)*cy[j]))*(1-c(treat))
deathp=tanh(y)/2+0.5
y0=-0.6+0.5*X[,2]
y0=tanh(y0)/2+0.5
y1=-0.6+0.5*X[,2]+0.5*exp(c(X%*%matrix(beta,p,1)*cy[j]))
y1=tanh(y1)/2+0.5
ATE=mean(y1-y0)
#ATE
ATE
## [1] 0.3016
```

## CATE(X2)

```
#calculating CATE(X2)
ft=2

XX=sort(X[,ft])
ITE=c(y1-y0)
ITE=ITE[order(X[,ft])]
qXX=quantile(XX,c(1:1000)/1000)
CATE=rep(0,1000)
CATE[1]=mean(ITE[XX<=qXX[1]])
for(i in c(2:1000)){
    temp=ITE[XX<=qXX[i] & XX>qXX[i-1]]
    CATE[i]=mean(temp)
}
plot(qXX,CATE,pch=20,cex=0.5,xlim=c(-3,3.5),ylim=c(-0.4,0.6),xlab="X2")
abline(ATE,0,col="red")
abline(0,0)
```



#-----continuous case------#

```
#data view
options(digits=4)
table_view=as.data.frame(matrix(c(dim(data_cont),mean(data_cont$Dsofa),sum(data_cont$
Treat)),1,4))
colnames(table_view)=c("columns", "rows", "mean(Dsofa)", "treatments")
head(data_cont,10)
##
      id bloc true ite(Dsofa)
                                  Dsofa Treat X1
                                                      X2
                                                                         X4
                                                                                  X5
                                                                Х3
## 1
       1
                      1.25872 3.49119
                                                  0.6530 -0.004351
                                                                     0.5868 -2.81646
            0
                                            1
                                              1
## 2
            0
       2
                      0.16055 -0.32401
                                            1
                                               1 -0.3354 -0.689923
                                                                     0.3452 -0.18485
                                                                     0.3414
## 3
       3
            0
                      0.61809 -0.17642
                                            1
                                                  0.6364 -0.764598
                                                                             0.11179
## 4
       4
            0
                      1.16091
                              1.19845
                                            0
                                               0 -0.6669
                                                          0.507079
                                                                     2.6162
                                                                             1.75030
## 5
       5
            0
                      0.99122
                               0.06078
                                            1
                                               0 -0.2783
                                                          0.747434
                                                                     0.4201
                                                                             0.90179
## 6
       6
            0
                      0.04150 -0.27655
                                            0
                                               1 -0.5594 -1.434221
                                                                    0.3674 -0.86756
## 7
       7
            0
                                               1 -0.1179 -0.499280 -2.0258
                      0.15597 -0.08961
## 8
       8
            0
                      0.44414 -0.44984
                                            1
                                               1 -1.8862 1.478520 -0.1303 -0.03908
## 9
       9
            0
                      0.41538
                               0.70374
                                            0
                                               0
                                                  1.1972 -1.326675
                                                                   1.5558 -0.65288
## 10 10
            0
                      0.01579 -0.81310
                                            1
                                               0 -0.8247 -1.066176 -1.5254 -0.03394
##
                                            X10
            Х6
                    X7
                            X8
                                     Х9
## 1
       0.76661 -1.3398
                        1.0175
                                0.8941
                                         0.4022
## 2
      -1.28426 -0.2198
                        0.2567
                                0.4932 -0.5382
## 3
      -1.05009
               0.9096
                        0.4286 -0.6812 -1.5088
## 4
       0.31831 -1.0196 -0.4373
                                0.8833
                                        0.5784
## 5
       0.68670 -1.4643 2.1852 -0.1837
                                        0.2503
## 6
      -1.01713 0.3859
                        0.2017 -1.3333 -0.5931
## 7
      -0.47259
                1.0194 1.7846 -1.3659
                                         0.2302
                                2.4378
## 8
      -0.33175
                0.4671 -0.5443
                                         0.1546
## 9
       0.19008 -1.4914 -0.3171 -2.2652
                                        2.2846
## 10 0.01192 -1.5894 1.9007 1.6740 -0.8389
```

```
table_view

## columns rows mean(Dsofa) treatments
## 1 7500 15 0.5941 3448
```

#### **ATE**

```
#calculating ATE
n=2000000
p = 10
tim=c(0,1,2,3,4)
beta=c(0.5,0.5,1,1/4,1/9,0,0,0,0,0)
G=matrix(0,(p-2),(p-2))
diag(G)=0.09
theta=0
X1=matrix(0,n,(p-2))
vaso=matrix(0,n,1)
water=matrix(0,n,1)
Death=matrix(0,n,1)
treat=matrix(0,n,1)
logisticf=function(x){exp(x)/(1+exp(x))}
cd=sqrt(logisticf(tim*0)^2*(pi^2/3)/((1-logisticf(tim*0)^2)*sum(beta*beta)))
cy=sqrt((logisticf((tim*0+1.3)))^2/((1-(logisticf((tim*0+1.3)))^2)*sum(beta*beta)))
set.seed(1219)
v=matrix(c(rnorm(n*(p-2),0,1)),n,(p-2))
X2=matrix(c(rbinom(n,1,0.5),rnorm(n,0,1)),n,2)
#generating
j=1
set.seed(61916)
X1=rmvnorm(n,rep(0,(p-2)),G)+v-matrix(theta,n,p-2)
X=cbind(X2,X1)
term=c(X%*%matrix(beta,p,1)*cd[j])
g=logisticf(term)
y=-0.6+0.5*X[,2]+0.5*exp(c(X%*%matrix(beta,p,1)*cy[j]))*(1-c(treat))
deathp=tanh(y)/2+0.5
y0=-0.6+0.5*X[,2]
y0=(1-(tanh(y0)/2+0.5)/1.285)^{(-1)}
y1=-0.6+0.5*X[,2]+0.5*exp(c(X%*%matrix(beta,p,1)*cy[j]))
y1=(1-(tanh(y1)/2+0.5)/1.285)^{(-1)}
ATE=mean(y1-y0)
#ATE
options(digits = 5)
ATE
## [1] 1.0015
```

# CATE(X2)

```
##calculating CATE(X2)
ft=2
XX=sort(X[,ft])
ITE=c(y1-y0)
ITE=ITE[order(X[,ft])]
qXX=quantile(XX,c(1:1000)/1000)
CATE=rep(0,1000)
CATE[1]=mean(ITE[XX<=qXX[1]])
for(i in c(2:1000)){
    temp=ITE[XX<=qXX[i] & XX>qXX[i-1]]
    CATE[i]=mean(temp)
}
plot(qXX,CATE,pch=20,cex=0.5,xlim=c(-3,3.5))
abline(ATE,0,col="red")
abline(0,0)
```

