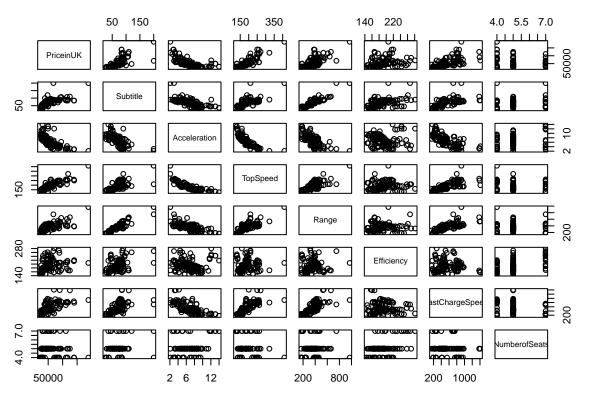
pdf_draft Kaleb Cervantes 4/20/2022

Model Selection

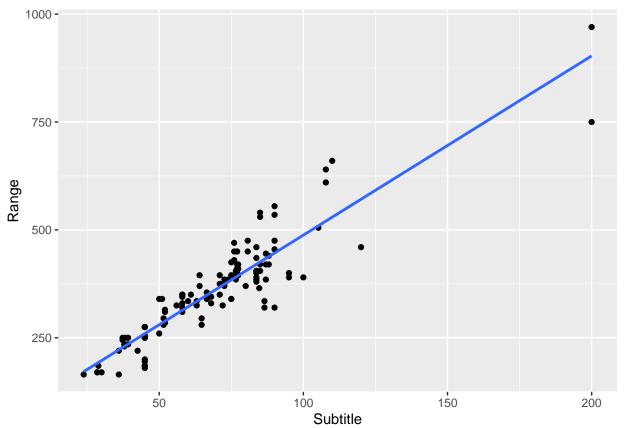
Variable Selection

The first thing was to check the correlations between some of the variables and visualize the data.

##		Subtitle Acceleration TopSpeed Range Efficiency	
##	Subtitle	1.00000000 -0.65205890 0.68551542 0.91104205 0.42266885	
##	Acceleration	-0.65205890 1.00000000 -0.83536291 -0.70220767 -0.03009386	
##	TopSpeed	0.68551542 -0.83536291 1.00000000 0.74349641 0.07810845	
##	Range	0.91104205 -0.70220767 0.74349641 1.00000000 0.04496225	
##	Efficiency	0.42266885 -0.03009386 0.07810845 0.04496225 1.00000000	
##	${\tt FastChargeSpeed}$	0.60230194 -0.71134894 0.73572843 0.72271112 -0.02642250	
##	NumberofSeats	0.08103089	
##	PriceinUK	0.70390802 -0.70863967 0.86502374 0.68439993 0.30531728	
##		FastChargeSpeed NumberofSeats PriceinUK	
##	Subtitle	0.6023019	
##	Acceleration	-0.7113489 0.30861901 -0.7086397	
##	TopSpeed	0.7357284 -0.21958021 0.8650237	
##	Range	0.7227111 -0.06531154 0.6843999	
##	T.C.C	-0.0264225 0.44090323 0.3053173	
	Efficiency	-0.0204223	
	FastChargeSpeed	***************************************	
	•	***************************************	



The most highly correlated variables are Subtitle and Range. These have a correlation of 0.91104205 and seem to have similar plots in the scatter plot matrix. A zoomed in scatter plot is included below.



When zoomed in, the two variables seem to have a linear relationship with each other. This indicates that

one of these may be dropped. Subtitle and Range have respective correlations 0.7039080 and 0.6843999 with the response. Since Subtitle has a stronger correlation with the response, that will be the predictor that is kept.

Transformations

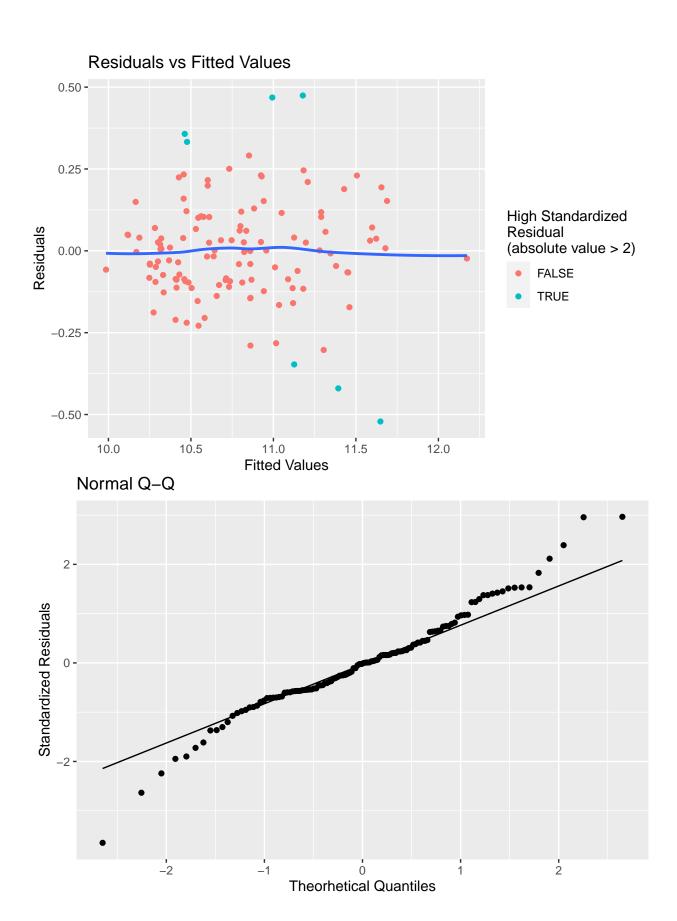
In the first row of the scatter plot matrix, TopSpeed and Acceleration appear to form a parabola when next to each other. As such, a quadratic transformation will be applied to those two variables.

Number of Seats also appears to behave as a factor in the scatter plot matrix. As such, it will be transformed into one.

In order to handle non-constant variance, logarithmic transformations will be applied to the other predictors and response variables.

Full Model

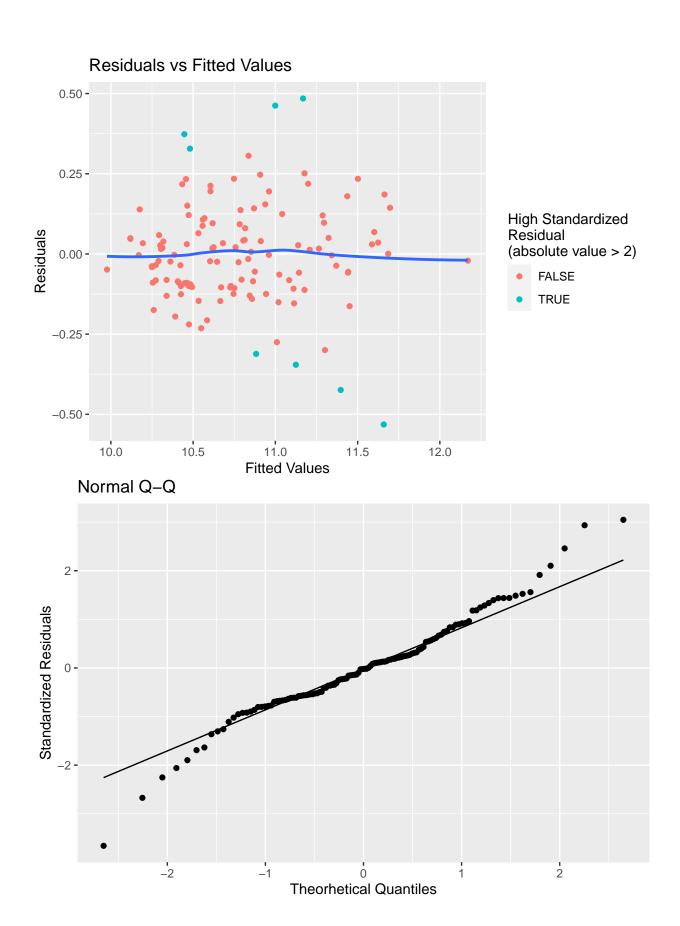
```
##
## Call:
## lm(formula = ., data = data)
## Residuals:
##
                 1Q
                      Median
                                   30
## -0.52123 -0.09026 -0.00196 0.08179
##
## Coefficients:
##
                                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                   5.237e+00 9.592e-01
                                                          5.460 2.90e-07 ***
## log(Subtitle)
                                   4.012e-01 9.933e-02
                                                          4.039 9.86e-05 ***
## poly(Acceleration, 2, raw = T)1 -2.076e-01 5.572e-02 -3.726 0.000307 ***
## poly(Acceleration, 2, raw = T)2 1.387e-02
                                              3.076e-03
                                                          4.510 1.61e-05 ***
## poly(TopSpeed, 2, raw = T)1
                                                          4.159 6.30e-05 ***
                                   1.321e-02
                                              3.176e-03
## poly(TopSpeed, 2, raw = T)2
                                  -1.910e-05 5.803e-06
                                                         -3.291 0.001334 **
## log(Efficiency)
                                   5.679e-01 1.738e-01
                                                          3.267 0.001443 **
## log(FastChargeSpeed)
                                  -6.657e-03 6.781e-02
                                                         -0.098 0.921973
## DriveFront Wheel Drive
                                  -2.338e-02 6.980e-02
                                                         -0.335 0.738269
## DriveRear Wheel Drive
                                  -3.726e-02 5.891e-02
                                                         -0.632 0.528352
## factor(NumberofSeats)5
                                  -1.268e-01 4.791e-02 -2.646 0.009308 **
## factor(NumberofSeats)7
                                  -2.770e-01 7.294e-02 -3.798 0.000238 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1665 on 112 degrees of freedom
## Multiple R-squared: 0.8815, Adjusted R-squared: 0.8698
## F-statistic: 75.71 on 11 and 112 DF, p-value: < 2.2e-16
## `geom_smooth()` using method = 'loess' and formula 'y ~ x'
```



Reduced Model

This full model seems to have met the assumptions for linear regression. However, it still contains predictors that are not significant. In order to reduce the model, a step-wise process will be used with BIC as the metric.

```
##
## Call:
## lm(formula = log(PriceinUK) ~ log(Subtitle) + poly(Acceleration,
##
       2, raw = T) + poly(TopSpeed, 2, raw = T) + log(Efficiency) +
       factor(NumberofSeats), data = data)
##
##
## Residuals:
##
       Min
                 1Q
                      Median
                                   30
## -0.53164 -0.09592 -0.00326 0.08894 0.48461
## Coefficients:
##
                                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                   5.139e+00 8.158e-01
                                                          6.299 5.67e-09 ***
## log(Subtitle)
                                   3.836e-01 8.049e-02
                                                          4.766 5.55e-06 ***
## poly(Acceleration, 2, raw = T)1 -2.248e-01
                                              4.879e-02
                                                         -4.608 1.06e-05 ***
## poly(Acceleration, 2, raw = T)2 1.456e-02 2.845e-03
                                                          5.117 1.26e-06 ***
## poly(TopSpeed, 2, raw = T)1
                                   1.280e-02
                                              2.711e-03
                                                          4.722 6.66e-06 ***
## poly(TopSpeed, 2, raw = T)2
                                                         -3.695 0.000338 ***
                                  -1.852e-05 5.013e-06
## log(Efficiency)
                                   6.144e-01
                                              1.454e-01
                                                          4.225 4.81e-05 ***
## factor(NumberofSeats)5
                                  -1.197e-01 4.577e-02
                                                         -2.615 0.010118 *
## factor(NumberofSeats)7
                                  -2.726e-01 7.175e-02 -3.799 0.000234 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1646 on 115 degrees of freedom
## Multiple R-squared: 0.881, Adjusted R-squared: 0.8727
## F-statistic: 106.4 on 8 and 115 DF, p-value: < 2.2e-16
## `geom_smooth()` using method = 'loess' and formula 'y ~ x'
```



This process removed log(FastChargeSpeed) and Drive from the model. The assumptions still appear to be met. In order to ensure no significant predictors were removed, a partial F-Test will be conducted between the two models.

```
## Analysis of Variance Table
##
## Model 1: log(PriceinUK) ~ log(Subtitle) + poly(Acceleration, 2, raw = T) +
      poly(TopSpeed, 2, raw = T) + log(Efficiency) + factor(NumberofSeats)
## Model 2: log(PriceinUK) ~ log(Subtitle) + poly(Acceleration, 2, raw = T) +
      poly(TopSpeed, 2, raw = T) + log(Efficiency) + log(FastChargeSpeed) +
##
      Drive + factor(NumberofSeats)
##
              RSS Df Sum of Sq
##
    Res.Df
                                    F Pr(>F)
## 1
        115 3.1166
## 2
        112 3.1036 3 0.012972 0.156 0.9256
```

Since the p-value is high, we lack statistically significant evidence that any significant predictors were dropped.

This leaves us with the formula:

```
\begin{split} \ln \text{PriceinUK} &= \beta_0 \\ &+ \beta_1 \ln \text{Subtitle} \\ &+ \beta_2 \text{Acceleration} + \beta_3 \text{Acceleration}^2 \\ &+ \beta_4 \text{TopSpeed} + \beta_5 \text{TopSpeed}^2 \\ &+ \beta_6 \ln \text{Efficiency} \\ &+ \beta_7 \left( \text{NumberofSeats} == 5 \right) + \beta_8 \left( \text{NumberofSeats} == 7 \right) \\ &+ \epsilon \end{split}
```