

$$\lim_{n \rightarrow \infty} \frac{\sum_{i=1}^n i^2}{n^3} = \lim_{n \rightarrow \infty} \frac{\sum_{i=1}^n i^2 - \sum_{i=1}^{n-1} i^2}{n^3 - (n-1)^3} = \lim_{n \rightarrow \infty} \frac{n^2}{n^3 - (n^3 - 3n^2 + 3n - 1)} = \lim_{n \rightarrow \infty} \frac{n^2}{3n^2 - 3n + 1} = \frac{1}{3}$$

$$\text{故 } f(n) = \sum_{i=1}^n i^2 \text{ 是 } \Theta(n^3)$$