

Q.1 Find all the 1<sup>st</sup> order partial derivatives of the following: (3 x 2 = 6 points)

a.  $F(x, y, z) = 4x^3y^2 - e^zy^4 + z^3 + 4y - x^{16}$

A)  $F(x, y, z) = 4x^3y^2 - e^zy^4 + z^3 + 4y - x^{16}$   
(With respect to  $x$ ):  $\frac{\partial}{\partial x}(F(x, y, z)) = \frac{\partial}{\partial x}(4x^3y^2) + \frac{\partial}{\partial x}(-e^zy^4) + \frac{\partial}{\partial x}(z^3) + \frac{\partial}{\partial x}(4y) + \frac{\partial}{\partial x}(-x^{16})$   
 $= \frac{\partial}{\partial x}(4x^3y^2) + \frac{\partial}{\partial x}(-e^zy^4) + \frac{\partial}{\partial x}(z^3) + \frac{\partial}{\partial x}(4y) + \frac{\partial}{\partial x}(-x^{16})$   
 $= (3x^2)(4y^2) + 0 + 0 + 0 - 16x^{15}$   
 $= 12x^2y^2 - 16x^{15}$

(With respect to  $y$ ):  $\frac{\partial}{\partial y}(F(x, y, z))$   
 $= \frac{\partial}{\partial y}(4x^3y^2) + \frac{\partial}{\partial y}(-e^zy^4) + \frac{\partial}{\partial y}(z^3) + \frac{\partial}{\partial y}(4y) + \frac{\partial}{\partial y}(-x^{16})$   
 $= (2y)(4x^3) + (-e^z)(4y^3) + 0 + 4 + 0$   
 $= 8x^3y - 4e^zy^3 + 4$

(With respect to  $z$ ):  $\frac{\partial}{\partial z}(F(x, y, z))$   
 $= \frac{\partial}{\partial z}(4x^3y^2) + \frac{\partial}{\partial z}(-e^zy^4) + \frac{\partial}{\partial z}(z^3) + \frac{\partial}{\partial z}(4y) + \frac{\partial}{\partial z}(-x^{16})$   
 $= 0 + (e^z)(-y^4) + 3z^2 + 0 + 0$   
 $= -e^zy^4 + 3z^2$

b.  $W(a, b, c, d) = a^2 + b^3 - c^2d^4 - 5a^3c$

$$B) W(a, b, c, d) = a^2 + b^3 - c^2 d^4 - 5a^3 c$$

$$\begin{aligned} & \text{(With respect to } a): \frac{\partial}{\partial a}(W(a, b, c, d)) \\ &= \frac{\partial}{\partial a}(a^2) + \frac{\partial}{\partial a}(b^3) + \frac{\partial}{\partial a}(-c^2 d^4) + \frac{\partial}{\partial a}(-5a^3 c) \\ &= 2a + 0 + 0 - 15a^2 c \\ &= 2a - 15a^2 c \end{aligned}$$

$$\begin{aligned} & \text{(With respect to } b): \frac{\partial}{\partial b}(W(a, b, c, d)) \\ &= \frac{\partial}{\partial b}(a^2) + \frac{\partial}{\partial b}(b^3) + \frac{\partial}{\partial b}(-c^2 d^4) + \frac{\partial}{\partial b}(-5a^3 c) \\ &= 0 + 3b^2 + 0 + 0 \\ &= 3b^2 \end{aligned}$$

$$\begin{aligned} & \text{(With respect to } c): \frac{\partial}{\partial c}(W(a, b, c, d)) \\ &= \frac{\partial}{\partial c}(a^2) + \frac{\partial}{\partial c}(b^3) + \frac{\partial}{\partial c}(-c^2 d^4) + \frac{\partial}{\partial c}(-5a^3 c) \\ &= 0 + 0 + (-2c)(d^4) + (-5a^3)(1) \\ &= -2cd^4 - 5a^3 \end{aligned}$$

$$\begin{aligned} & \text{(With respect to } d): \frac{\partial}{\partial d}(W(a, b, c, d)) \\ &= \frac{\partial}{\partial d}(a^2) + \frac{\partial}{\partial d}(b^3) + \frac{\partial}{\partial d}(-c^2 d^4) + \frac{\partial}{\partial d}(-5a^3 c) \\ &= 0 + 0 + (-4d^3)(c^2) + 0 \\ &= -4c^2 d^3 \end{aligned}$$

Q. 2 For this question, you need to implement a python code to compute the partial derivatives of the following:

a.  $F(x, y, z) = 2x^3y^2 - ezy^4z + z^4 + 3yz$

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PS G:\Other computers\Desktop\@College\SCSU Spring 2025\Deep Learning\Assignme
1DerivativeCalc.py
Welcome to the Python partial derivative tool! Press CTRL+C anytime to quit.

====Function #1====

How many variables should the program have?
3

❖Function variables generated! Their names are as follows:
x1
x2
x3

Would you like to rename the variables? (y/n)
y

Please enter the new name for variable x1:
x
Please enter the new name for variable x2:
y
Please enter the new name for variable x3:
z

Function variables renamed! Their new names are as follows:
x
y
z

Please enter the expression for the function you'd like to differentiate.
Note that multiplication MUST be explicit (enter 2*x*y instead of 2xy).
Enter your expression below:
2*x^3*y^2-e^z*y^4*z+z^4+3*y*z

Your final function is: f(x, y, z) = -e^z*y^4*z + 2*x^3*y^2 + 3*y*z + z^4

Partial Derivatives:
With respect to x: 6*x^2*y^2
With respect to y: -4*e^z*y^3*z + 4*x^3*y + 3*z
With respect to z: -e^z*y^4*log(e) - e^z*y^4 + 3*y + 4*z^3

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b.  $W(a, b, c, d) = 2a^2b + b^3 - 3c^2d^4 - 5a^3c$

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=====Function #2=====
How many variables should the program have?
4

Function variables generated! Their names are as follows:
x1
x2
x3
x4

Would you like to rename the variables? (y/n)
y

Please enter the new name for variable x1:
a
Please enter the new name for variable x2:
b
Please enter the new name for variable x3:
c
Please enter the new name for variable x4:
d

Function variables renamed! Their new names are as follows:
a
b
c
d

Please enter the expression for the function you'd like to differentiate.
Note that multiplication MUST be explicit (enter 2*x*y instead of 2xy).
Enter your expression below:
2*a^2*b+b^3-3*c^2*d^4-5*a^3*c

Your final function is: f(a, b, c, d) = -5*a^3*c + 2*a^2*b + b^3 - 3*c^2*d^4

Partial Derivatives:
With respect to a: -15*a^2*c + 4*a*b
With respect to b: 2*a^2 + 3*b^2
With respect to c: -5*a^3 - 6*c*d^4
With respect to d: -12*c^2*d^3

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Your program should perform the following tasks:

- It should ask the user to input the number of variables/symbols to be used for an expression, e.g., for the first expression, your program should take a value of 3. **(2 points for each expression = 4 points)**
- Next, your program should ask the user to enter the expression that you want to compute the partial derivative of. You need to make sure the expressions are entered in a right format. For more information, check the python documentation. **(2 points for each expression = 4 points)**
- You need to attach three snapshots of your python run as following:
  - Snapshot of program asking the user to enter the number of variables for both expressions. **(1 point for each expression = 2 points)**
  - Snapshot of program asking user to enter the mathematical expression (for

each expression). **(1 point for each expression = 2 points)**

iii. Actual computed partial derivatives of both expressions. **(1 point for each expression = 2 points)**

d. Submit your python code file or notebook file to the drop box. **(If python file is missing, a 10 points penalty will be imposed)**