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Факультет «Информатика и системы управления»

Кафедра «Системы обработки информации и управления»

## ОТЧЁТ ПО Лабораторной работе №3

Выполнил:

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Подпись и дата:

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## **1) Описание задания:**

1. Выберите набор данных (датасет) для решения задачи классификации или регрессии.
2. В случае необходимости проведите удаление или заполнение пропусков и кодирование категориальных признаков.
3. С использованием метода `train_test_split` разделите выборку на обучающую и тестовую.
4. Обучите модель ближайших соседей для произвольно заданного гиперпараметра  $K$ . Оцените качество модели с помощью подходящих для задачи метрик.
5. Произведите подбор гиперпараметра  $K$  с использованием `GridSearchCV` и `RandomizedSearchCV` и кросс-валидации, оцените качество оптимальной модели. Используйте не менее двух стратегий кросс-валидации.
6. Сравните метрики качества исходной и оптимальной моделей.

## **2) Текст программы и итоги:**

```
!pip install scikit-learn
```

```
Requirement already satisfied: scikit-learn in c:\users\user\
anaconda3\lib\site-packages (1.2.2)
Requirement already satisfied: numpy>=1.17.3 in c:\users\user\
anaconda3\lib\site-packages (from scikit-learn) (1.26.4)
Requirement already satisfied: scipy>=1.3.2 in c:\users\user\
anaconda3\lib\site-packages (from scikit-learn) (1.11.4)
Requirement already satisfied: joblib>=1.1.1 in c:\users\user\
anaconda3\lib\site-packages (from scikit-learn) (1.2.0)
Requirement already satisfied: threadpoolctl>=2.0.0 in c:\users\user\
anaconda3\lib\site-packages (from scikit-learn) (2.2.0)
```

```
import numpy as np
import pandas as pd
import sklearn
from typing import Dict, Tuple
from scipy import stats
from sklearn import datasets
from sklearn import model_selection
from sklearn.model_selection import train_test_split
from sklearn.neighbors import KNeighborsRegressor,
KNeighborsClassifier
from sklearn.metrics import accuracy_score, balanced_accuracy_score
from sklearn import metrics
from sklearn.metrics import precision_score, recall_score, f1_score,
classification_report
from sklearn.metrics import confusion_matrix
from sklearn.metrics import mean_absolute_error, mean_squared_error,
mean_squared_log_error, median_absolute_error, r2_score
from sklearn.metrics import roc_curve, roc_auc_score
import seaborn as sns
import matplotlib.pyplot as plt
%matplotlib inline
sns.set(style="ticks")
```

## Загрузка и первичный анализ данных

```
data = pd.read_csv('data/onlinefoods.csv', sep=",")
```

```
# размер набора данных
```

```
data.shape
```

```
(388, 13)
```

```
# типы колонок
```

```
data.dtypes
```

Age	int64
Gender	object

```

Marital Status      object
Occupation          object
Monthly Income      object
Educational Qualifications  object
Family size         int64
latitude            float64
longitude           float64
Pin code            int64
Output              object
Feedback            object
Unnamed: 12         object
dtype: object

```

```

# проверим есть ли пропущенные значения
data.isnull().sum()

```

```

Age                0
Gender             0
Marital Status     0
Occupation         0
Monthly Income     0
Educational Qualifications  0
Family size        0
latitude           0
longitude          0
Pin code           0
Output             0
Feedback           0
Unnamed: 12        0
dtype: int64

```

```

# Первые 5 строк датасета
data.head()

```

	Age	Gender	Marital Status	Occupation	Monthly Income \
0	20	Female	Single	Student	No Income
1	24	Female	Single	Student	Below Rs.10000
2	22	Male	Single	Student	Below Rs.10000
3	22	Female	Single	Student	No Income
4	22	Male	Single	Student	Below Rs.10000

	Educational Qualifications	Family size	latitude	longitude	Pin code \
0	Post Graduate	4	12.9766	77.5993	560001
1	Graduate	3	12.9770	77.5773	560009
2	Post Graduate	3	12.9551	77.6593	560017
3	Graduate	6	12.9473	77.5616	

```
560019
4          Post Graduate          4    12.9850    77.5533
560010
```

```
Output Feedback Unnamed: 12
0    Yes    Positive      Yes
1    Yes    Positive      Yes
2    Yes    Negative      Yes
3    Yes    Positive      Yes
4    Yes    Positive      Yes
```

```
total_count = data.shape[0]
print('Всего строк: {}'.format(total_count))
```

```
Всего строк: 388
```

Так как пропусков нет, то этап заполнения пропусков можно пропустить.

## Кодирование категориальных признаков

```
from sklearn.preprocessing import OrdinalEncoder
```

```
data_oe = data[['Family size', 'Feedback']]
```

```
oe = OrdinalEncoder()
```

```
cat_enc_oe = oe.fit_transform(data_oe)
```

```
cat_enc_oe
```

```
array([[3., 1.],
       [2., 1.],
       [2., 0.],
       [5., 1.],
       [3., 1.],
       [1., 1.],
       [2., 1.],
       [2., 1.],
       [1., 1.],
       [3., 1.],
       [4., 1.],
       [1., 0.],
       [4., 1.],
       [3., 1.],
       [4., 1.],
       [5., 1.],
       [1., 1.],
       [2., 0.],
       [3., 0.],
       [0., 1.],
       [2., 1.],
       [3., 1.]])
```

```
[3., 1.],
[3., 1.],
[2., 1.],
[2., 1.],
[4., 1.],
[2., 1.],
[2., 1.],
[3., 1.],
[4., 1.],
[3., 1.],
[3., 1.],
[4., 1.],
[1., 1.],
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[4., 1.],
[4., 0.],
[2., 1.],
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[1., 1.],
[0., 1.],
[2., 1.],
[4., 1.],
[3., 1.],
[4., 1.],
[2., 1.],
[0., 1.],
[3., 1.],
[1., 1.],
[5., 1.],
[3., 1.],
[3., 1.],
[3., 1.],
[3., 1.],
[3., 1.],
```

```
[2., 1.],
[2., 1.],
[1., 1.],
[3., 1.],
[2., 1.],
[3., 1.],
[3., 1.],
[2., 1.],
[4., 1.],
[3., 1.],
[2., 1.],
[2., 1.],
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[3., 1.],
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[0., 1.],
[4., 1.],
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[0., 1.],
[1., 1.],
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[0., 1.],
[1., 1.],
[4., 1.],
[1., 1.],
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[4., 1.],
[1., 1.],
[4., 1.],
[2., 1.],
```

```
[4., 1.],
[2., 1.],
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[4., 0.],
[5., 0.],
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[2., 1.],
[3., 1.],
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[3., 1.],
[2., 1.],
[2., 1.],
[4., 0.],
[1., 1.],
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[2., 0.],
[3., 1.],
[2., 1.],
[2., 1.],
[3., 1.],
[4., 0.],
[4., 1.],
[1., 1.],
```



```
[1., 0.],
[0., 1.],
[2., 1.],
[0., 1.],
[2., 1.],
[1., 1.],
[5., 1.],
[1., 1.],
[2., 0.],
[0., 0.],
[2., 1.],
[2., 1.],
[2., 0.],
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[5., 1.],
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[1., 1.],
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[1., 1.],
[4., 1.],
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[1., 1.],
[3., 0.],
[0., 1.],
[1., 1.],
[3., 0.],
[5., 0.],
[2., 1.],
[1., 0.],
[2., 1.],
[3., 1.],
[2., 0.],
[4., 1.],
[1., 0.],
```

```
[4., 1.],
[2., 1.],
[0., 1.],
[1., 1.],
[3., 1.],
[4., 1.],
[1., 1.],
[1., 1.],
[2., 1.],
[1., 1.],
[4., 0.],
[2., 1.],
[5., 1.],
[4., 1.],
[2., 0.],
[1., 1.],
[2., 1.],
[2., 0.],
[2., 1.],
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[1., 1.],
[2., 1.],
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[2., 1.],
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[2., 1.],
[5., 0.],
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[1., 1.],
[2., 1.],
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[2., 1.],
[1., 1.],
[5., 1.],
[2., 1.],
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[5., 0.],
[2., 1.],
[5., 0.],
[5., 1.],
[1., 0.],
[1., 0.],
[2., 0.],
[3., 1.],
[1., 1.],
[2., 0.],
```

```
[1., 1.],
[2., 1.],
[1., 1.],
[1., 1.],
[1., 0.],
[2., 1.],
[1., 1.],
[1., 1.],
[3., 1.],
[2., 1.],
[1., 1.],
[4., 0.],
[3., 1.],
[5., 1.],
[1., 1.],
[3., 1.],
[2., 1.],
[1., 1.],
[1., 1.],
[1., 1.],
[4., 0.],
[2., 1.],
[1., 1.],
[5., 1.],
[2., 1.],
[4., 0.],
[0., 0.],
[2., 0.],
[4., 1.],
[2., 1.],
[0., 1.],
[1., 0.],
[5., 0.],
[2., 0.],
[5., 1.],
[3., 1.],
[1., 1.],
[2., 1.],
[2., 1.],
[1., 1.],
[3., 1.],
[4., 1.],
[1., 0.],
[4., 1.],
[1., 1.],
[1., 1.],
[2., 1.],
[1., 1.],
[4., 0.],
```

```
[2., 1.],  
[5., 1.],  
[4., 1.],  
[2., 0.],  
[1., 1.],  
[2., 1.],  
[2., 0.],  
[2., 1.],  
[1., 1.],  
[1., 1.],  
[2., 1.],  
[5., 1.],  
[1., 1.],  
[3., 1.],  
[3., 1.],  
[2., 1.],  
[1., 1.],  
[3., 0.],  
[0., 1.],  
[1., 1.],  
[3., 0.],  
[5., 1.],  
[2., 1.],  
[1., 0.],  
[2., 1.],  
[3., 1.],  
[2., 0.],  
[4., 1.],  
[1., 0.],  
[3., 1.],  
[3., 1.],  
[2., 1.],  
[1., 1.],  
[3., 0.],  
[0., 1.],  
[1., 1.],  
[3., 1.],  
[5., 1.],  
[2., 1.],  
[1., 1.],  
[1., 1.],  
[4., 0.],  
[2., 1.],  
[5., 1.],  
[4., 1.],  
[2., 0.],  
[1., 1.],  
[2., 1.],  
[2., 0.],
```

```
[2., 1.],  
[1., 1.],  
[1., 1.],  
[2., 1.],  
[5., 1.],  
[1., 1.],  
[2., 1.],  
[1., 1.],  
[0., 0.],  
[2., 0.],  
[5., 0.],  
[2., 1.],  
[0., 0.],  
[1., 1.],  
[3., 1.],  
[1., 1.],  
[2., 1.],  
[2., 1.],  
[1., 1.],  
[3., 1.],  
[4., 1.],  
[1., 1.],  
[4., 1.]])
```

```
# Уникальные значения 1 признака  
np.unique(cat_enc_oe[:, 0])
```

```
array([0., 1., 2., 3., 4., 5.])
```

```
# Уникальные значения 2 признака  
np.unique(cat_enc_oe[:, 1])
```

```
array([0., 1.])
```

## Разделение выборки на обучающую и тестовую

```
data= np.c_[cat_enc_oe[:, 0], cat_enc_oe[:, 1]]
```

```
data_x_train, data_x_test, data_y_train, data_y_test =  
train_test_split(data, cat_enc_oe[:, 1], test_size=0.2,  
random_state=1)
```

```
# Размер обучающей выборки  
data_x_train.shape, data_y_train.shape
```

```
((310, 2), (310,))
```

```
# Размер тестовой выборки  
data_x_test.shape, data_y_test.shape
```

```
((78, 2), (78,))
```

```

np.unique(data_y_train)
array([0., 1.])
np.unique(data_y_test)
array([0., 1.])

def class_proportions(array: np.ndarray) -> Dict[int, Tuple[int, float]]:
    """
    Вычисляет пропорции классов
    array - массив, содержащий метки классов
    """
    # Получение меток классов и количества меток каждого класса
    labels, counts = np.unique(array, return_counts=True)
    # Превращаем количество меток в процент их встречаемости
    # делим количество меток каждого класса на общее количество меток
    counts_perc = counts/array.size
    # Теперь sum(counts_perc)==1.0
    # Создаем результирующий словарь,
    # ключом словаря является метка класса,
    # а значением словаря процент встречаемости метки
    res = dict()
    for label, count2 in zip(labels, zip(counts, counts_perc)):
        res[label] = count2
    return res

def print_class_proportions(array: np.ndarray):
    """
    Вывод пропорций классов
    """
    proportions = class_proportions(array)
    if len(proportions)>0:
        print('Метка \t Количество \t Процент встречаемости')
        for i in proportions:
            val, val_perc = proportions[i]
            val_perc_100 = round(val_perc * 100, 2)
            print('{} \t {} \t \t {}'.format(i, val, val_perc_100))

# В исходной выборке нет явного дисбаланса классов для целевого признака
print_class_proportions(cat_enc_oe[:, 1])

Метка      Количество      Процент встречаемости
0.0      71      18.3%
1.0     317      81.7%

# Для обучающей выборки
print_class_proportions(data_y_train)

```

Метка	Количество	Процент встречаемости
0.0	58	18.71%
1.0	252	81.29%

*# Для тестовой выборки*

```
print_class_proportions(data_y_test)
```

Метка	Количество	Процент встречаемости
0.0	13	16.67%
1.0	65	83.33%

Модель ближайших соседей для произвольно заданного гиперпараметра K. Оценка качества модели с помощью подходящих для задачи метрик.

*# 27 ближайших соседей*

```
cl1_1 = KNeighborsClassifier(n_neighbors=27)
cl1_1.fit(data_x_train, data_y_train)
```

```
KNeighborsClassifier(n_neighbors=27)
```

```
target1_1 = cl1_1.predict(data_x_test)
```

```
len(target1_1), target1_1
```

```
(78,
 array([1., 1., 1., 1., 1., 1., 1., 1., 1., 1., 1., 1., 1., 1., 1.,
        1., 1.,
        1., 1., 1., 1., 1., 1., 1., 0., 0., 1., 1., 1., 1., 1., 1.,
        1., 1.,
        1., 0., 1., 1., 1., 1., 1., 1., 1., 1., 0., 0., 0., 1., 1.,
        1., 1.,
        1., 1., 1., 1., 0., 1., 1., 1., 1., 1., 1., 0., 1., 1.,
        1., 1.,
        1., 1., 1., 1., 1., 1., 1., 1., 1., 0.])))
```

Так как класс не сбалансирован, то будем использовать метрику Precision, recall и F-мера для оценки качества модели.

```
precision_score(data_y_test, target1_1), recall_score(data_y_test,
target1_1)
```

```
(0.9420289855072463, 1.0)
```

*# Параметры TP, TN, FP, FN считаются отдельно для каждого класса  
# и берется средневзвешенное значение, дисбаланс классов учитывается  
# в виде веса классов (вес - количество истинных значений каждого  
класса).*

```
precision_score(data_y_test, target1_1, average='weighted')
```

```
0.9516908212560387
```

```
f1_score(data_y_test, target1_1, average='weighted')  
0.9448213478064225
```

Вывод: качество модели высокое.

## Подбор гиперпараметра K

```
from sklearn.model_selection import GridSearchCV, RandomizedSearchCV  
from sklearn.neighbors import KNeighborsRegressor,  
KNeighborsClassifier  
from sklearn.model_selection import cross_val_score, cross_validate  
from sklearn.model_selection import KFold, RepeatedKFold, LeaveOneOut,  
LeavePOut, ShuffleSplit, StratifiedKFold  
from sklearn.metrics import accuracy_score, balanced_accuracy_score  
from sklearn.metrics import precision_score, recall_score, f1_score,  
classification_report  
from sklearn.metrics import confusion_matrix  
from sklearn.metrics import mean_absolute_error, mean_squared_error,  
mean_squared_log_error, median_absolute_error, r2_score  
from sklearn.metrics import roc_curve, roc_auc_score  
from sklearn.model_selection import GridSearchCV, RandomizedSearchCV  
from sklearn.model_selection import learning_curve, validation_curve  
  
n_range = np.array([1, 2, 3, 4, 5, 1, 2, 3, 4, 5, 1, 2, 3, 4, 5, 1, 2,  
3, 4, 5, 1, 2, 3, 4, 5])  
tuned_parameters = [{'n_neighbors': n_range}]  
tuned_parameters  
  
[{'n_neighbors': array([1, 2, 3, 4, 5, 1, 2, 3, 4, 5, 1, 2, 3, 4, 5,  
1, 2, 3, 4, 5, 1, 2,  
3, 4, 5])}]  
  
%%time  
clf_gs = GridSearchCV(KNeighborsClassifier(), tuned_parameters, cv=7,  
scoring='accuracy')  
clf_gs.fit(data_x_train, data_y_train)  
  
CPU times: total: 812 ms  
Wall time: 821 ms  
  
GridSearchCV(cv=7, estimator=KNeighborsClassifier(),  
param_grid=[{'n_neighbors': array([1, 2, 3, 4, 5, 1, 2,  
3, 4, 5, 1, 2, 3, 4, 5, 1, 2, 3, 4, 5, 1, 2,  
3, 4, 5])}],  
scoring='accuracy')  
  
clf_gs.cv_results_  
  
{'mean_fit_time': array([0.0008488 , 0.00089312, 0.00068358,  
0.00074404, 0.00071229,
```



```

0.00057013, 0.00085493, 0.00073515, 0.00057002, 0.00057002,
0.00056992, 0.00085514, 0.00056999, 0.00057002, 0.00085507,
0.00056996, 0.00049189, 0.00056747, 0.00042759, 0.00083453,
0.00071955, 0.00085674, 0.00068392, 0.00056423, 0.00099812]),
'std_fit_time': array([6.35850677e-04, 3.76105894e-04, 4.34903542e-
04, 4.25540645e-04,
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04,
4.93655942e-04, 4.93655958e-04, 4.93567458e-04, 3.49109231e-
04,
4.93626451e-04, 4.93655942e-04, 3.49081483e-04, 4.93596973e-
04,
4.62120587e-04, 4.91477308e-04, 4.93734605e-04, 3.42394830e-
04,
4.40180252e-04, 3.49793101e-04, 4.14029063e-04, 4.88814405e-
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'mean_score_time': array([0.00512651, 0.00429327, 0.00359055,
0.00353037, 0.00370448,
0.00359283, 0.00327703, 0.00396664, 0.00354471, 0.0035617 ,
0.00342911, 0.0034194 , 0.00341896, 0.00356184, 0.00356177,
0.00369467, 0.00352308, 0.00371984, 0.00370414, 0.00386732,
0.00370472, 0.00327754, 0.00379617, 0.00328251, 0.00299113]),
'std_score_time': array([1.11419154e-03, 4.74665409e-04, 5.20446350e-
04, 4.68985091e-04,
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04,
4.80579977e-04, 4.93518288e-04, 4.85528930e-04, 4.94030056e-
04,
4.93793919e-04, 4.93774340e-04, 4.93577273e-04, 6.94577911e-
04,
4.93088974e-04, 4.32091327e-04, 4.50601144e-04, 6.42459295e-
04,
6.34471289e-04, 4.55333762e-04, 6.69032923e-04, 4.44720808e-
04,
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'param_n_neighbors': masked_array(data=[1, 2, 3, 4, 5, 1, 2, 3, 4, 5,
1, 2, 3, 4, 5, 1, 2, 3,
4, 5, 1, 2, 3, 4, 5],
mask=[False, False, False, False, False, False, False, False,
False,
False, False, False, False, False, False, False, False,
False,
False, False, False, False, False, False, False,
False,
False],
fill_value='?',
dtype=object),
'params': [{'n_neighbors': 1},

```

```

{'n_neighbors': 2},
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'split0_test_score': array([1., 1., 1., 1., 1., 1., 1., 1., 1., 1.,
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    1., 1., 1., 1., 1., 1., 1.]),
'split1_test_score': array([1., 1., 1., 1., 1., 1., 1., 1., 1., 1.,
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    1., 1., 1., 1., 1., 1., 1.]),
'split2_test_score': array([1., 1., 1., 1., 1., 1., 1., 1., 1., 1.,
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'split3_test_score': array([1., 1., 1., 1., 1., 1., 1., 1., 1., 1.,
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    1., 1., 1., 1., 1., 1., 1.]),
'split4_test_score': array([1., 1., 1., 1., 1., 1., 1., 1., 1., 1.,
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    1., 1., 1., 1., 1., 1., 1.]),
'split5_test_score': array([1., 1., 1., 1., 1., 1., 1., 1., 1., 1.,
1., 1., 1., 1., 1., 1., 1.,
    1., 1., 1., 1., 1., 1., 1.]),
'split6_test_score': array([1., 1., 1., 1., 1., 1., 1., 1., 1., 1.,
1., 1., 1., 1., 1., 1., 1.,
    1., 1., 1., 1., 1., 1., 1.]),
'mean_test_score': array([1., 1., 1., 1., 1., 1., 1., 1., 1., 1.,
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    1., 1., 1., 1., 1., 1., 1.]),
'std_test_score': array([0., 0., 0., 0., 0., 0., 0., 0., 0., 0.,
0., 0., 0., 0., 0., 0., 0.,
    0., 0., 0., 0., 0., 0., 0.])

```

```

0., 0., 0., 0., 0., 0.,
    0., 0., 0., 0., 0., 0., 0., 0.]),
'rank_test_score': array([1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
1, 1, 1, 1, 1, 1, 1,
    1, 1, 1])})

# Лучшая модель
clf_gs.best_estimator_

KNeighborsClassifier(n_neighbors=1)

# Лучшее значение метрики
clf_gs.best_score_

1.0

# Лучшее значение параметров
clf_gs.best_params_

{'n_neighbors': 1}

```

Делаем то же самое, только с помощью Randomized Search:

```

%%time
clf_rs = RandomizedSearchCV(KNeighborsClassifier(), tuned_parameters,
cv=7, scoring='accuracy')
clf_rs.fit(data_x_train, data_y_train)

CPU times: total: 344 ms
Wall time: 344 ms

RandomizedSearchCV(cv=7, estimator=KNeighborsClassifier(),
    param_distributions=[{'n_neighbors': array([1, 2,
3, 4, 5, 1, 2, 3, 4, 5, 1, 2, 3, 4, 5, 1, 2, 3, 4, 5, 1, 2,
    3, 4, 5])}],
    scoring='accuracy')

clf_rs.best_score_, clf_rs.best_params_
(1.0, {'n_neighbors': 5})

clf_gs.best_score_, clf_gs.best_params_
(1.0, {'n_neighbors': 1})

```

Используем стратегии StratifiedKFold и StratifiedShuffleSplit кросс-валидации:

```

X = cat_enc_oe[:, 0]
y = cat_enc_oe[:, 1]
skf = StratifiedKFold(n_splits=3)

```

```

for train, test in skf.split(X, y):
    print("%s %s" % (train, test))

[116 117 118 119 120 121 122 125 126 127 128 129 130 131 132 134 135
136
138 139 140 142 143 145 146 147 148 149 150 151 152 153 154 155 156
157
159 160 162 163 164 165 167 168 170 171 172 173 174 175 176 179 180
182
183 184 185 186 187 189 190 191 192 193 194 195 196 197 198 199 200
201
202 203 204 205 206 207 208 209 210 211 212 213 214 215 216 217 218
219
220 221 222 223 224 225 226 227 228 229 230 231 232 233 234 235 236
237
238 239 240 241 242 243 244 245 246 247 248 249 250 251 252 253 254
255
256 257 258 259 260 261 262 263 264 265 266 267 268 269 270 271 272
273
274 275 276 277 278 279 280 281 282 283 284 285 286 287 288 289 290
291
292 293 294 295 296 297 298 299 300 301 302 303 304 305 306 307 308
309
310 311 312 313 314 315 316 317 318 319 320 321 322 323 324 325 326
327
328 329 330 331 332 333 334 335 336 337 338 339 340 341 342 343 344
345
346 347 348 349 350 351 352 353 354 355 356 357 358 359 360 361 362
363
364 365 366 367 368 369 370 371 372 373 374 375 376 377 378 379 380
381
382 383 384 385 386 387] [ 0  1  2  3  4  5  6  7  8  9 10
11 12 13 14 15 16 17
18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34
35
36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52
53
54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70
71
72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88
89
90 91 92 93 94 95 96 97 98 99 100 101 102 103 104 105 106
107
108 109 110 111 112 113 114 115 123 124 133 137 141 144 158 161 166
169
177 178 181 188]
[ 0  1  2  3  4  5  6  7  8  9 10 11 12 13 14 15 16
17
18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34
35

```

53	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52
71	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70
89	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88
107	90	91	92	93	94	95	96	97	98	99	100	101	102	103	104	105	106
169	108	109	110	111	112	113	114	115	123	124	133	137	141	144	158	161	166
270	177	178	181	188	250	251	252	253	254	255	258	260	264	265	267	268	269
290	272	273	274	275	276	277	279	280	281	282	283	284	285	286	287	288	289
308	291	292	293	294	295	296	297	298	299	300	301	302	303	304	305	306	307
326	309	310	311	312	313	314	315	316	317	318	319	320	321	322	323	324	325
344	327	328	329	330	331	332	333	334	335	336	337	338	339	340	341	342	343
362	345	346	347	348	349	350	351	352	353	354	355	356	357	358	359	360	361
380	363	364	365	366	367	368	369	370	371	372	373	374	375	376	377	378	379
128	381	382	383	384	385	386	387]	[116	117	118	119	120	121	122	125	126	127
157	138	139	140	142	143	145	146	147	148	149	150	151	152	153	154	155	156
182	159	160	162	163	164	165	167	168	170	171	172	173	174	175	176	179	180
201	183	184	185	186	187	189	190	191	192	193	194	195	196	197	198	199	200
219	202	203	204	205	206	207	208	209	210	211	212	213	214	215	216	217	218
237	220	221	222	223	224	225	226	227	228	229	230	231	232	233	234	235	236
263	238	239	240	241	242	243	244	245	246	247	248	249	256	257	259	261	262
17	266	271	278]														
35	[ 0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
53	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34
71	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52
89	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70
	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88

```

90 91 92 93 94 95 96 97 98 99 100 101 102 103 104 105 106
107
108 109 110 111 112 113 114 115 116 117 118 119 120 121 122 123 124
125
126 127 128 129 130 131 132 133 134 135 136 137 138 139 140 141 142
143
144 145 146 147 148 149 150 151 152 153 154 155 156 157 158 159 160
161
162 163 164 165 166 167 168 169 170 171 172 173 174 175 176 177 178
179
180 181 182 183 184 185 186 187 188 189 190 191 192 193 194 195 196
197
198 199 200 201 202 203 204 205 206 207 208 209 210 211 212 213 214
215
216 217 218 219 220 221 222 223 224 225 226 227 228 229 230 231 232
233
234 235 236 237 238 239 240 241 242 243 244 245 246 247 248 249 256
257
259 261 262 263 266 271 278] [250 251 252 253 254 255 258 260 264 265
267 268 269 270 272 273 274 275
276 277 279 280 281 282 283 284 285 286 287 288 289 290 291 292 293
294
295 296 297 298 299 300 301 302 303 304 305 306 307 308 309 310 311
312
313 314 315 316 317 318 319 320 321 322 323 324 325 326 327 328 329
330
331 332 333 334 335 336 337 338 339 340 341 342 343 344 345 346 347
348
349 350 351 352 353 354 355 356 357 358 359 360 361 362 363 364 365
366
367 368 369 370 371 372 373 374 375 376 377 378 379 380 381 382 383
384
385 386 387]

```

```

from sklearn.model_selection import StratifiedShuffleSplit
X = cat_enc_oe
y = y = cat_enc_oe[:, 1]
sss = StratifiedShuffleSplit(n_splits=5, random_state=0)
for i, (train_index, test_index) in enumerate(sss.split(X, y)):
    print(f"Fold {i}:")
    print(f"  Train: {train_index}")
    print(f"  Test:  {test_index}")

```

```

Fold 0:
  Train: [170 375 168 256 196  83 117 370 166  1 173 223 262  28 232
295 257 385
 355 235  67 254  64 222 224  43  59 341  95 210 300 332 237  45 133
209
 298 275 259 272 285 193 100 105  2 169 342  3 334  77 163 270  63
4

```

197 226 271 10 31 94 183 371 16 37 158 155 255 70 164 174 343  
 87  
 335 132 248 128 228 36 244 205 314 319 247 292 377 291 6 34 233  
 176  
 73 144 265 200 276 85 25 157 47 156 88 211 199 337 46 120 212  
 125  
 137 281 221 358 263 145 75 316 127 324 339 69 326 23 250 320 15  
 153  
 331 347 351 288 165 106 202 253 44 333 367 9 220 344 191 96 112  
 79  
 35 11 179 33 296 177 323 48 171 304 139 297 130 284 24 225 245  
 198  
 294 18 307 374 369 308 91 109 86 20 325 338 234 29 327 301 239  
 359  
 123 74 313 380 353 39 252 283 141 329 149 8 366 32 214 378 119  
 352  
 98 217 185 13 121 274 302 360 136 286 182 19 162 189 143 172 269  
 184  
 278 218 241 315 41 381 89 90 159 216 365 84 65 345 104 21 190  
 140  
 57 80 161 111 7 321 303 17 148 5 110 93 72 208 78 61 116  
 97  
 290 229 310 267 268 56 328 126 249 150 348 26 192 81 322 152 379  
 363  
 68 317 180 299 356 206 364 138 306 42 12 135 51 264 372 251 30  
 38  
 280 384 154 386 52 282 62 195 387 231 260 309 243 289 122 181 71  
 354  
 383 124 240 346 201 312 118 53 258 175 305 22 188 40 146 114 277  
 82  
 361 131 227 213 101 151 187 14 368 66 336 382 362 261 203 113 330  
 349  
 293 376 350 215 129 279 58]  
 Test: [ 27 115 194 92 204 178 236 103 50 373 238 99 107 142 76  
 160 266 207  
 230 60 340 242 273 357 287 186 55 219 167 246 147 49 0 134 102  
 318  
 54 108 311]  
 Fold 1:  
 Train: [ 11 74 62 30 242 6 335 230 97 9 152 130 199 103 325  
 31 237 196  
 315 75 68 96 357 356 253 372 100 297 89 262 71 265 44 157 260  
 247  
 175 250 257 203 351 238 27 21 82 219 38 201 102 41 368 159 222  
 106  
 284 155 333 124 228 264 174 136 282 37 123 172 51 113 42 186 328  
 227  
 92 316 5 119 132 134 332 353 323 59 163 302 45 236 366 46 350  
 279

349 168 23 26 320 381 187 365 273 307 327 339 24 217 188 329 167  
189  
361 61 224 169 209 183 343 12 212 164 334 165 296 290 346 133 58  
33  
360 114 178 118 65 383 220 221 143 69 20 4 141 81 53 17 135  
60  
48 375 64 166 140 144 278 99 266 142 289 29 77 313 314 252 40  
281  
239 272 151 258 259 49 86 245 180 204 379 117 342 149 14 207 251  
127  
39 93 301 354 263 231 202 275 193 173 283 223 261 300 16 148 277  
269  
116 138 153 19 267 177 43 274 78 184 88 235 176 154 7 312 35  
385  
359 248 214 308 126 306 80 28 200 194 170 101 162 299 213 63 246  
305  
128 386 36 52 370 108 226 374 156 304 91 249 18 270 285 145 362  
10  
303 197 98 76 47 271 295 171 218 70 104 66 34 287 364 122 373  
348  
121 382 198 384 298 195 225 336 378 54 318 293 160 129 57 191 215  
87  
369 79 326 15 111 112 90 341 311 376 280 276 206 73 32 25 288  
208  
67 190 241 347 107 125 232 147 371 83 146 240 158 185 243 137 331  
268  
205 229 256 2 216 294 310 139 8 244 94 0 355 210 337 1 309  
291  
22 181 352 85 182 56 84]  
Test: [380 255 50 150 317 387 120 254 95 131 324 233 344 3 358  
367 211 330  
377 292 363 319 345 179 161 338 340 109 234 192 110 105 286 322 72  
115  
55 13 321]  
Fold 2:  
Train: [318 253 174 19 56 69 128 242 15 116 216 331 76 204 366  
200 371 104  
66 98 244 148 218 224 28 156 51 208 123 6 107 356 319 122 351  
330  
338 166 105 339 149 277 316 364 160 34 154 213 102 147 369 233 377  
101  
301 22 378 275 4 281 315 173 299 266 219 214 5 192 383 78 10  
343  
259 381 114 385 187 133 265 267 115 239 46 380 44 188 90 229 284  
73  
18 12 263 113 195 361 308 370 183 13 269 386 276 294 335 202 283  
118  
137 300 176 282 292 60 62 305 363 217 241 142 136 179 120 75 285  
59



67 121 296 85 279 141 211 111 324 252 298 210 365 61 1 270 209  
 43  
 250 86 307 157 323 49 139 337 0 185 91 199 236 83 189 190 54  
 238  
 329 288 119 373 367 345 326 274 138 286 254 140 163 237 177 240 382  
 23  
 387 99 248 359 71 320 168 321 180 347 354 374 108 334 221 249 222  
 310  
 212 196 360 64 235 289 95 303 197 26 124 38 161 340 309 31 150  
 96  
 82 306 178 35 198 186 9 349 293 97 117 341 336 205 287 37 20  
 181  
 290 272 146 313 130 145 89 194 84 30 17 93 295 379 328 151 7  
 230  
 291 246 297 80 3 103 110 143 260 350 368 39 127 94 175 191 232  
 106  
 182 226 58 203 247 251 65 258 264 215 317 162 201 357 21 372 271  
 311  
 220 126 327 243 255 77 55 353 256 332 88 131 81 262 167 206 155  
 74  
 280 109 384 32 355 2 333 207 125 36 72 132 257 152 52 184 47  
 223  
 362 11 346 302 24 87 144 231 63 153 228 342 312 135 234 27 48  
 376  
 92 50 314 170 45 348 278]  
 Test: [134 261 268 304 129 100 70 29 227 40 68 245 171 14 42  
 358 325 193  
 41 159 375 53 16 158 33 165 322 79 352 25 172 225 57 344 169  
 164  
 8 273 112]  
 Fold 3:  
 Train: [247 111 1 303 279 152 145 86 49 286 299 261 284 89 324  
 98 78 150  
 137 100 80 231 24 327 88 384 330 318 113 162 267 340 28 123 151  
 82  
 357 268 141 169 172 34 229 50 271 353 56 134 346 99 127 226 36  
 201  
 214 341 195 235 115 158 207 280 95 239 22 251 120 217 143 27 379  
 139  
 65 104 227 91 289 66 257 249 140 48 164 177 218 193 276 352 310  
 347  
 5 148 375 67 326 262 336 185 209 339 133 147 60 386 160 11 248  
 183  
 33 266 190 273 308 4 293 90 126 62 360 132 69 12 377 301 254  
 97  
 205 294 188 328 283 309 182 252 25 105 385 297 165 211 75 20 8  
 156  
 61 16 18 298 149 269 237 168 125 378 37 323 202 128 170 292 366  
 74

258 203 204 243 312 245 371 295 259 225 215 191 192 43 77 186 334  
373  
109 87 30 197 118 343 219 167 381 354 63 96 103 144 21 241 287  
117  
224 344 116 76 210 10 355 382 42 52 321 129 189 364 9 223 122  
359  
367 342 338 350 250 345 6 29 329 228 314 107 35 365 136 59 300  
3  
376 44 101 51 138 72 270 244 55 199 306 263 315 81 374 368 277  
176  
53 212 130 121 372 19 114 155 157 274 351 264 17 184 194 79 331  
40  
380 216 304 370 302 46 73 320 54 337 108 7 369 265 163 363 39  
317  
291 362 232 57 171 221 208 272 110 38 383 0 187 322 23 45 260  
175  
230 26 166 307 319 335 313 124 41 161 238 255 64 174 142 173 135  
240  
311 181 356 256 68 325 196 47 93 333 305 233 13 222 112 281 71  
296  
102 213 32 348 159 94 92]  
Test: [ 2 288 178 387 275 200 180 198 84 153 234 70 290 206 179  
83 85 14  
246 154 285 131 316 146 236 253 282 58 361 15 31 119 332 106 278  
358  
220 242 349]  
Fold 4:  
Train: [ 89 334 236 359 114 39 53 271 302 189 379 36 173 251 71  
184 197 175  
108 382 15 352 348 61 84 217 191 98 11 202 69 315 215 377 190  
322  
269 239 355 341 142 375 87 125 201 343 311 314 232 56 35 228 122  
242  
206 57 291 324 25 237 156 52 252 371 353 216 310 360 279 192 327  
210  
200 118 362 218 212 273 133 146 47 34 121 58 250 308 54 135 51  
50  
19 214 178 231 101 18 226 62 120 88 6 79 372 44 112 154 317  
91  
139 277 256 333 198 185 127 339 92 80 37 77 4 31 213 30 366  
336  
261 179 386 329 342 280 95 188 68 13 307 113 93 361 132 43 193  
124  
115 266 225 319 155 340 323 219 292 253 131 170 24 148 196 338 259  
17  
276 205 110 176 387 378 109 262 67 45 358 186 152 325 243 144 157  
281  
229 14 289 344 370 150 49 270 159 264 21 106 78 221 180 64 20  
240

```

26 23 5 312 241 141 299 103 128 283 0 158 76 29 227 55 364
74
288 86 3 373 345 194 166 268 321 301 137 320 300 168 247 274 278
163
224 182 174 107 265 41 290 297 38 129 368 296 96 81 234 161 1
33
153 245 365 83 172 305 134 272 222 66 235 298 99 149 211 16 383
187
316 46 171 208 326 357 248 335 85 376 294 22 136 164 104 384 332
9
363 167 145 117 254 169 244 177 162 183 94 138 140 100 203 123 147
223
10 8 40 160 119 105 328 287 385 195 346 267 48 102 249 381 60
233
275 230 337 207 374 82 285 97 209 143 65 331 165 130 181 369 151
246
90 63 282 116 111 12 304]
Test: [220 263 42 255 126 318 238 380 356 293 72 258 303 73 309
367 286 350
199 27 28 313 70 2 257 59 330 349 284 32 204 306 7 347 351
354
260 295 75]

```

Оцениваем качество оптимальной модели:

```

from sklearn.preprocessing import StandardScaler
X = cat_enc_oe[:, 0]
y = cat_enc_oe[:, 1]

scoring = {'precision': 'precision_weighted',
           'recall': 'recall_weighted',
           'f1': 'f1_weighted'}

X1 = X.reshape(-1, 1)
scaler = StandardScaler()
X_scaled = scaler.fit_transform(X1)
knn = KNeighborsClassifier(n_neighbors=5)
skf = StratifiedKFold(n_splits=3, shuffle=True, random_state=1)
cv_scores = cross_validate(KNeighborsClassifier(n_neighbors=2),
                           X_scaled, y, scoring=scoring,
                           cv=3, return_train_score=True)

cv_scores
{'fit_time': array([0.0016253, 0.0010519, 0.0009973]),
 'score_time': array([0.01635671, 0.01194477, 0.00997305]),
 'test_precision': array([0.6775641, 0.69149464, 0.70741403]),
 'train_precision': array([0.74211644, 0.70994257, 0.70186859]),
 'test_recall': array([0.75384615, 0.60465116, 0.63565891]),
 'train_recall': array([0.80232558, 0.64092664, 0.62548263]),

```

```
'test_f1': array([0.71079165, 0.64075872, 0.66501973]),  
'train_f1': array([0.75602468, 0.6693309 , 0.65715174])}
```

**Вывод:** так как для обучающей выборки и тестовой результаты довольно близкие друг к другу, то можно сказать, что данная модель не недообучена и не переобучена. Параметр ближайших соседей, равный 5, является оптимальным.

## Построение кривых обучения и валидации

```
def plot_learning_curve(estimator, title, X, y, ylim=None, cv=None,  
                        n_jobs=None, train_sizes=np.linspace(.1, 1.0,  
5), scoring='f1_weighted'):  
    """  
    Generate a simple plot of the test and training learning curve.  
  
    Parameters  
    -----  
    estimator : object type that implements the "fit" and "predict"  
methods  
        An object of that type which is cloned for each validation.  
  
    title : string  
        Title for the chart.  
  
    X : array-like, shape (n_samples, n_features)  
        Training vector, where n_samples is the number of samples and  
        n_features is the number of features.  
  
    y : array-like, shape (n_samples) or (n_samples, n_features),  
optional  
        Target relative to X for classification or regression;  
        None for unsupervised learning.  
  
    ylim : tuple, shape (ymin, ymax), optional  
        Defines minimum and maximum yvalues plotted.  
  
    cv : int, cross-validation generator or an iterable, optional  
        Determines the cross-validation splitting strategy.  
        Possible inputs for cv are:  
        - None, to use the default 3-fold cross-validation,  
        - integer, to specify the number of folds.  
        - :term:`CV splitter`,  
        - An iterable yielding (train, test) splits as arrays of  
indices.  
  
        For integer/None inputs, if ``y`` is binary or multiclass,  
        :class:`StratifiedKFold` used. If the estimator is not a  
classifier  
        or if ``y`` is neither binary nor multiclass, :class:`KFold`  
is used.
```

Refer :ref:`User Guide <cross\_validation>` for the various cross-validators that can be used here.

```
n_jobs : int or None, optional (default=None)
    Number of jobs to run in parallel.
    ``None`` means 1 unless in a :obj:`joblib.parallel_backend`
context.
    ``-1`` means using all processors. See :term:`Glossary
<n_jobs>`
    for more details.

train_sizes : array-like, shape (n_ticks,), dtype float or int
    Relative or absolute numbers of training examples that will be
used to
    generate the learning curve. If the dtype is float, it is
regarded as a
    fraction of the maximum size of the training set (that is
determined
    by the selected validation method), i.e. it has to be within
(0, 1].
    Otherwise it is interpreted as absolute sizes of the training
sets.
    Note that for classification the number of samples usually
have to
    be big enough to contain at least one sample from each class.
    (default: np.linspace(0.1, 1.0, 5))
"""
plt.figure()
plt.title(title)
if ylim is not None:
    plt.ylim(*ylim)
plt.xlabel("Training examples")
plt.ylabel(scoring)
train_sizes, train_scores, test_scores = learning_curve(
    estimator, X, y, cv=cv, scoring=scoring, n_jobs=n_jobs,
train_sizes=train_sizes)
train_scores_mean = np.mean(train_scores, axis=1)
train_scores_std = np.std(train_scores, axis=1)
test_scores_mean = np.mean(test_scores, axis=1)
test_scores_std = np.std(test_scores, axis=1)
plt.grid()

plt.fill_between(train_sizes, train_scores_mean -
train_scores_std,
                 train_scores_mean + train_scores_std, alpha=0.3,
                 color="r")
plt.fill_between(train_sizes, test_scores_mean - test_scores_std,
                 test_scores_mean + test_scores_std, alpha=0.1,
color="g")
```

```

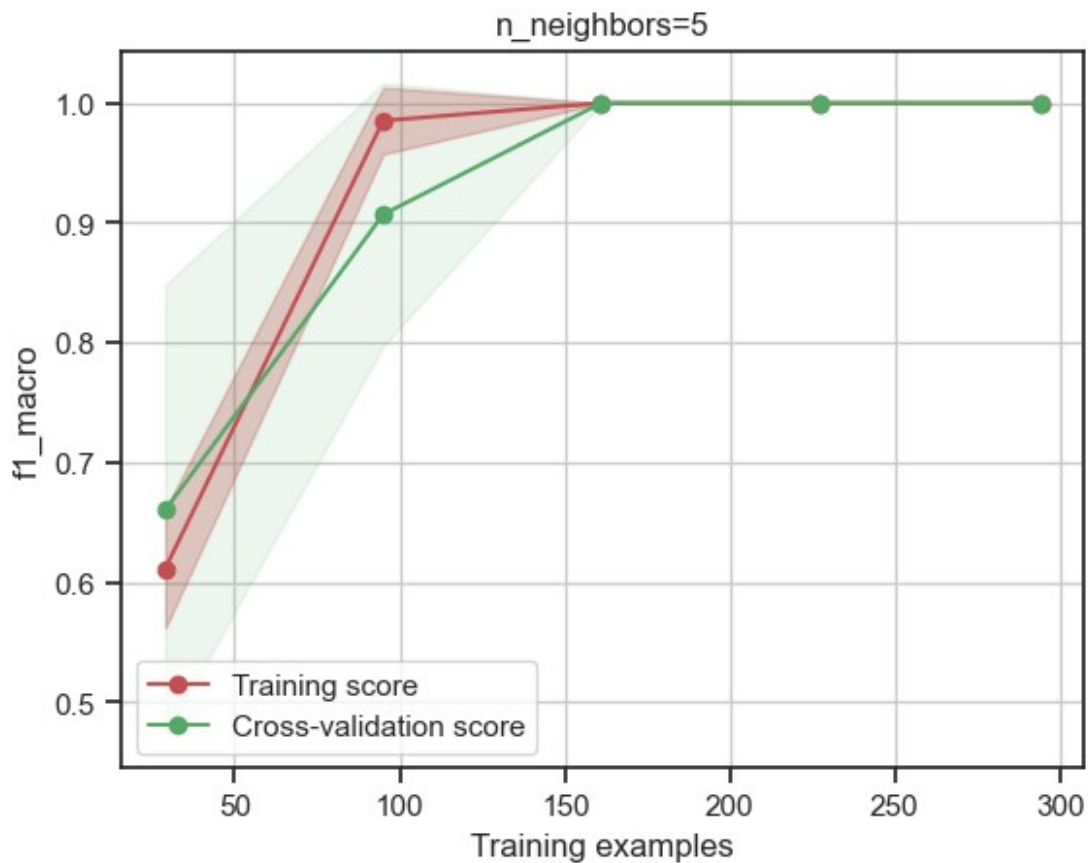
plt.plot(train_sizes, train_scores_mean, 'o-', color="r",
         label="Training score")
plt.plot(train_sizes, test_scores_mean, 'o-', color="g",
         label="Cross-validation score")

plt.legend(loc="best")
return plt

plot_learning_curve(KNeighborsClassifier(n_neighbors=5),
'n_neighbors=5',
                    data_x_train, data_y_train, cv=20,
                    scoring='f1_macro')

<module 'matplotlib.pyplot' from 'C:\\Users\\user\\anaconda3\\Lib\\
site-packages\\matplotlib\\pyplot.py'>

```



```

import matplotlib.pyplot as plt
import numpy as np
from sklearn.datasets import load_digits
from sklearn.neighbors import KNeighborsClassifier
from sklearn.model_selection import validation_curve

```

```

data = np.c_[cat_enc_oe[:, 0], cat_enc_oe[:, 1]]
X, y = data, cat_enc_oe[:, 1]

# Define the range for the parameter (e.g., number of neighbors)
parameter_range = np.arange(1, 20, 1)

# Calculate accuracy on training and test set using the parameter with
cross-validation
train_score, test_score = validation_curve(
    KNeighborsClassifier(), X, y,
    param_name="n_neighbors",
    param_range=parameter_range,
    cv=15, scoring="f1_macro"
)

# Calculate mean and standard deviation of training and testing scores
mean_train_score = np.mean(train_score, axis=1)
std_train_score = np.std(train_score, axis=1)
mean_test_score = np.mean(test_score, axis=1)
std_test_score = np.std(test_score, axis=1)

# Plot mean accuracy scores for training and testing scores
plt.plot(parameter_range, mean_train_score, label="Training Score",
color='b')
plt.plot(parameter_range, mean_test_score, label="Cross Validation
Score", color='g')

# Create the plot
plt.title("Validation Curve with KNN Classifier")
plt.xlabel("Number of Neighbours")
plt.ylabel("F1_macro")
plt.tight_layout()
plt.legend(loc='best')
plt.show()

```

