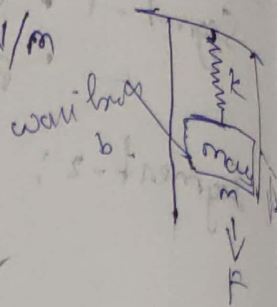


Assignment-1

Equation
where

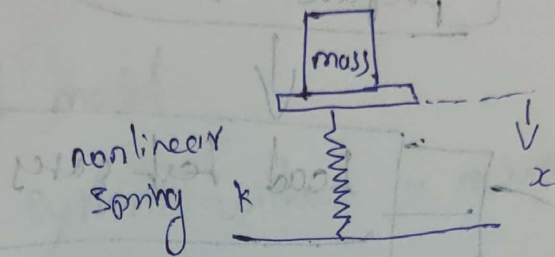
$$m \frac{d^2 x}{dt^2} + b \frac{dx}{dt} + kx = F$$

where
 $m = 10 \text{ kg}$, $b = 50 \text{ N-s/m}$, $k = 100 \text{ N/m}$



$$m \frac{d^2 x}{dt^2} = F - b \frac{dx}{dt} - kx$$

Assignment-2



initial condition

$$x(0) = 1$$

Equation

$$m \frac{d^2 x}{dt^2} + kx = F \Rightarrow m \frac{d^2 x}{dt^2} = F - kx$$

where

$m = 20 \text{ kg}$, $k = 10 \text{ N/m}$.

Assignment-3

$m = 10 \text{ kg}$, $k = 1 \text{ N/m}$, $b = 0.5 \text{ N-sec/m}$, outputs about 1.8

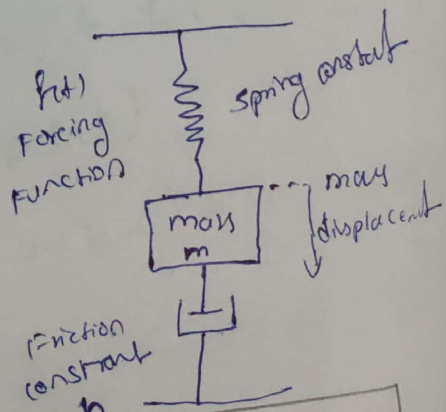
initial condition $y(0) = 1.8$.

equations

$$m \frac{d^2 y(t)}{dt^2} + b \frac{dy(t)}{dt} + ky(t) = f(t)$$

$$m \frac{d^2 y(t)}{dt^2} + b \frac{dy(t)}{dt} + ky(t) = f(t)$$

$$m \frac{d^2 y(t)}{dt^2} = f(t) - b \frac{dy(t)}{dt} - ky(t)$$



Assignment - 4

clock pendulum

$\frac{d\phi}{dt}$ in 2 seconds.

Assume small angles, ϕ , in the analysis so that $\sin \phi \approx \phi$ and $\cos \phi \approx 1$.

Equation

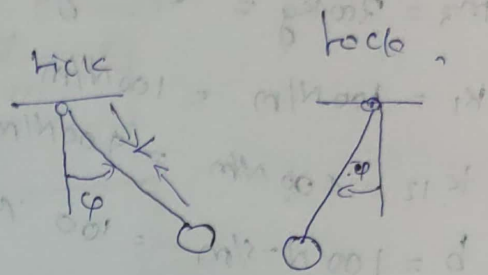
$$mL^2 \frac{d^2\phi}{dt^2} + mgL\phi = F$$

where

$$m = 1 \text{ kg}, L = 0.9939 \text{ m}, g = 9.81 \text{ m/s}^2$$

$$mL^2 \frac{d^2\phi}{dt^2} + mgL\phi = F$$

$$mL^2 \frac{d^2\phi}{dt^2} = F - mgL\phi$$



where

$$m = 1 \text{ kg}$$

$$L = 0.9939 \text{ m}$$

$$g = 9.8 \text{ m/s}^2$$

$$L^2 = 0.9878$$

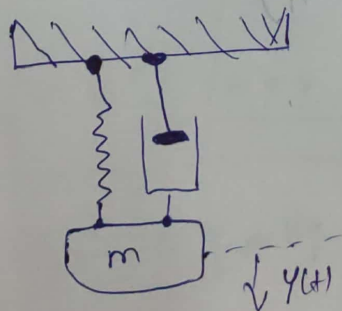
Assignment - 5

Critically Damped system

$$mgL\phi$$

mass $m = 80 \text{ kg}$ Spring constant $k = 1000 \text{ N/m}$

damping coefficient is $c = 178.89 \text{ N-s/m}$ initial displacement 2 m .



$$m \frac{d^2 y(t)}{dt^2} = 0 - y(t)k - c \frac{dy(t)}{dt}$$

Equation

$$m \frac{d^2 y(t)}{dt^2} + c \frac{dy(t)}{dt} + ky(t) = 0$$

Vibration Absorber

August - 6

where

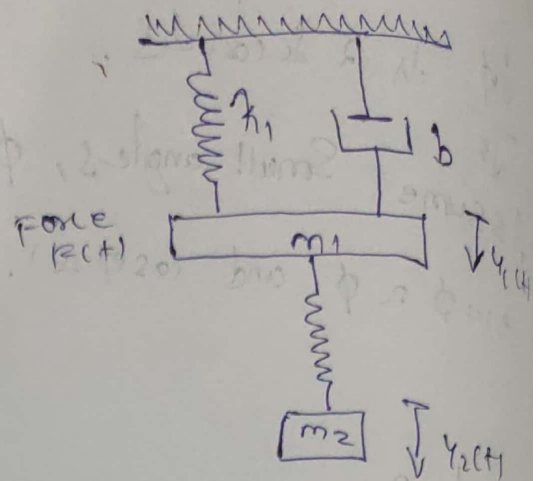
$$m_1 = 20 \text{ kg} = 20000 \text{ g}$$

$$m_2 = 200 \text{ kg} = 200000 \text{ g}$$

$$K_1 = 100 \text{ N/m} = 100 \text{ N/m}$$

$$K_{12} = 400 \text{ N/m} = 400 \text{ N/m}$$

$$b = 100 \text{ N-s/m} = 100 \text{ N-s/m}$$



equation 1

$$\rightarrow \textcircled{1} m_1 \frac{d^2 y_1}{dt^2} + K_{12} (y_1 - y_2) + b \frac{dy_1}{dt} + K_1 y_1 = F(t)$$

$$\rightarrow \textcircled{2} m_2 \frac{d^2 y_2}{dt^2} + K_{12} (y_2 - y_1) = 0$$

$\rightarrow \textcircled{1}$

$$m_1 \frac{d^2 y_1}{dt^2} = F(t) - K_{12} (y_1 - y_2) - b \frac{dy_1}{dt} - K_1 y_1$$

$\rightarrow \textcircled{2}$

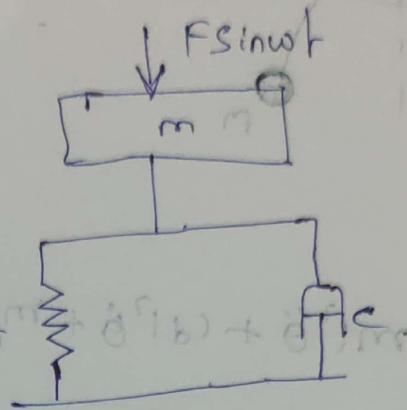
$$m_2 \frac{d^2 y_2}{dt^2} = -K_{12} (y_2 - y_1)$$

Assignment - 7

Forced SMD System

$$m = 1 \text{ kg}; k = 100 \text{ N/m}; c = 2 \text{ N-s/m}; x(0) = 2 \text{ cm};$$

$$r = \sin \omega t = 100 \sin(20t)$$



equation:-

$$m \frac{d^2 x(t)}{dt^2} + c \frac{dx(t)}{dt} + kx(t) = F \sin \omega t$$

$$m \frac{d^2 x(t)}{dt^2} + c \frac{dx(t)}{dt} = F \sin \omega t - kx(t)$$

$$\frac{m d^2 x(t)}{dt^2} \oplus = F \sin \omega t - kx(t) - c \frac{dx(t)}{dt}$$

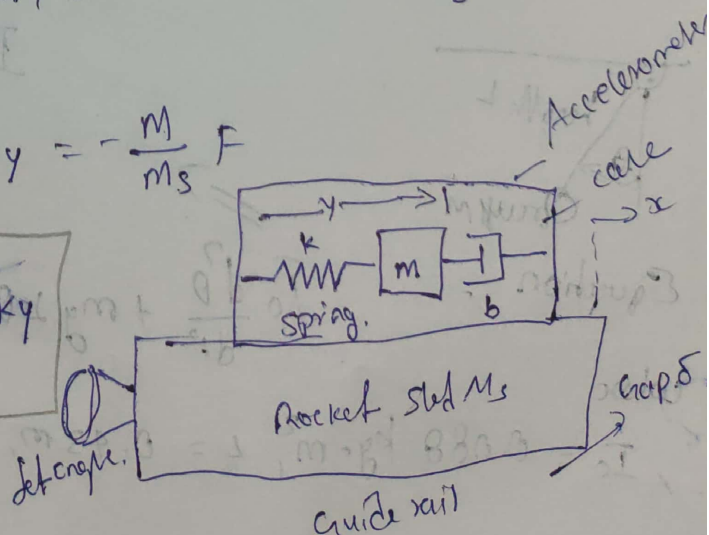
Assignment - 8

Mechanical Accelerometer

$$m = 10 \text{ kg}; k = 32 \text{ N/m}; b = 12 \text{ N}. m_s = 100 \text{ kg}$$

$$m \frac{d^2 y}{dt^2} + b \frac{dy}{dt} + ky = -\frac{m}{m_s} F$$

$$m \frac{d^2 y}{dt^2} = -\frac{m}{m_s} F - b \frac{dy}{dt} - ky$$



pendulum

Assignment 9
Viscous Damping

where

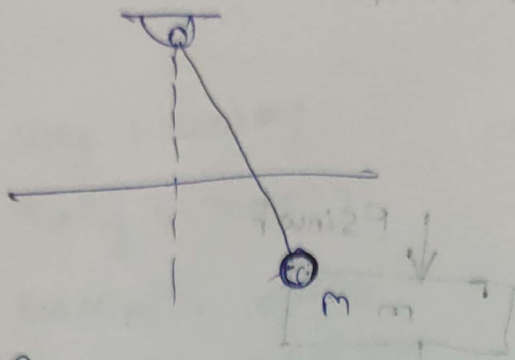
$$m = 10g$$

$$l = 5cm$$

$$c_d = 14 \frac{sec}{cm}$$

$$g = 981 \text{ cm/sec}^2$$

$$\theta(0) = 1.57, \dot{\theta}(0) = 0$$



equation -

$$m l^2 \ddot{\theta} + c_d l^2 \dot{\theta} + m g l \theta = 0$$

$\frac{3 \text{ sec}}{u}$

$$m l^2 \ddot{\theta} = -c_d l^2 \dot{\theta} - m g l \theta$$

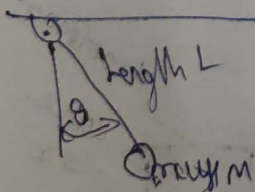
Assignment - 10

pendulum oscillator

Torque on the mass is $T = m g L \sin \theta$

where g is the gravitational constant. $\theta_0 = 0^\circ$

$$-\pi/4 < \theta < \pi/4$$



$$I_0 \frac{d^2 \theta}{dt^2} = -m g L \sin \theta + T_{in}$$

Equation

$$I_0 \frac{d^2 \theta}{dt^2} + m g L \theta = T_{in}$$

where

$$I_0 = 0.088 \text{ kg-m}^2, L = 0.43 \text{ m}, g = 9.81 \text{ m/s}^2$$