

	Objectives	Rate your understanding of the objective				
Objective 1	Express an area under a function on the coordinate plane as an integral	1	2	3	4	5
Objective 2	Divide regions into ones that can be expressed in terms of functions	1	2	3	4	5
Objective 3	Use both functions in terms of both x and y	1	2	3	4	5

### Warm Up

Evaluate the following integrals. (By yourself)

1.  $\int \frac{1}{x^2} dx$

2.  $\int_0^5 3x^{2/3} + 6\sqrt{x} + 3 dx$

3.  $\int_{3\pi}^{6\pi} \cos(y)(\sin(y))^5 dy$

### Problems

These problems involve areas on the coordinate plane. You may reference Example 199 in your example packet. (In groups)

- Find the area that is both below  $y = \sqrt{x}$  and above  $y = x^2$  on the  $xy$ -plane. Graph the region, and then write the curves as functions, and then use the intersection points as the limits of integration.
- Find the area that is both below  $y = \sqrt{x}$  and above  $y = x^2$  on the  $xy$ -plane. (Note: this is the same area as above). Integrate with respect to  $dy$  instead of  $dx$ , as you did in problem #1.
- Find the area bounded by the line  $y = 2\pi$ , the  $y$  axis, the curve  $x = \sin(5y)$ , and the  $x$ -axis.
- Find the area of the region bounded by  $y = -x^3 + 4x$  and  $y = x^2 - 2x + 5$  from  $x = 0$  to  $x = 2$ .
- Find the area of the triangle formed by the points  $(1, 2)$ ,  $(5, 1)$ , and  $(3, 6)$ . Solve again by rewriting your integrands and limits to integrate with respect to the other variable.
- Find the area of the trapezoid formed by the points  $(0, 2)$ ,  $(2, 0)$ ,  $(2, 5)$ , and  $(0, 3)$ . Check that the formula for the area produces the same result.
- Solve the last problem using three integrals with respect to  $y$ .

### Self Quiz

(By yourself)

- Calculate the area bounded by the functions  $y = 2x^2$  and  $y = x^3$ .
- Solve the last problem using an integral with respect to  $y$ .

### Reflection

Objectives		Rate your understanding of the objective				
Objective 1	Express an area under a function on the coordinate plane as an integral	1	2	3	4	5
Objective 2	Divide regions into ones that can be expressed in terms of functions	1	2	3	4	5
Objective 3	Use both functions in terms of both x and y	1	2	3	4	5

#### Study Skills:

- Remember to read through examples from the book BEFORE your professor goes over the section in class.
- After class read through the examples in your notes from that day and try to do the problems yourself (without looking at your notes).
- After class read through the examples from the book in the section you JUST covered and make sure you understand them.