



# Bayesian Machine Learning for Business Analytics

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MGTA 495, Spring 2022

# What have we done so far...

- Trained some model

$$y = f(x, \theta)$$

where x are features and  $\theta$  are weights/biases.

- Performed various unsupervised learning tasks such as clustering, data reduction etc.
- This is all good – and is sometimes all we need – but sometimes we require **more**

# Getting richer insights

- How do we account for uncertainty? We usually just train the model by searching for the “best” architecture and weights  $\hat{f}(x, \hat{\theta})$
- Then we plug in some  $x^*$  to get a single prediction:

$$y^* = \hat{f}(x^*, \hat{\theta})$$

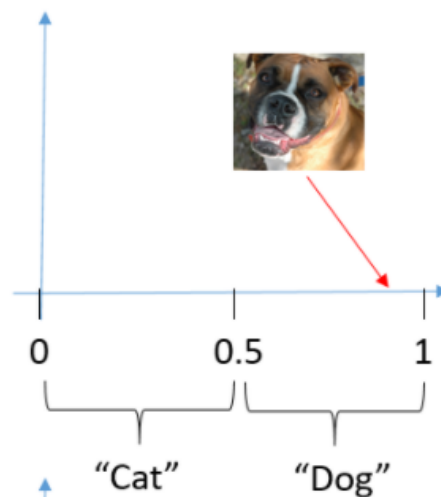
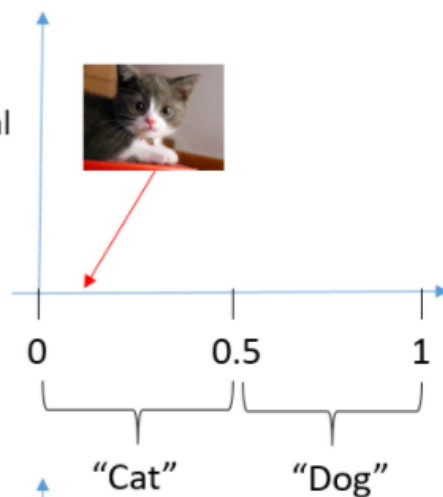
- Here  $y^*$  is a single number – but how sure is the model/machine of this prediction?
- Answering this question requires that the model also outputs some measure of uncertainty

# Getting richer insights

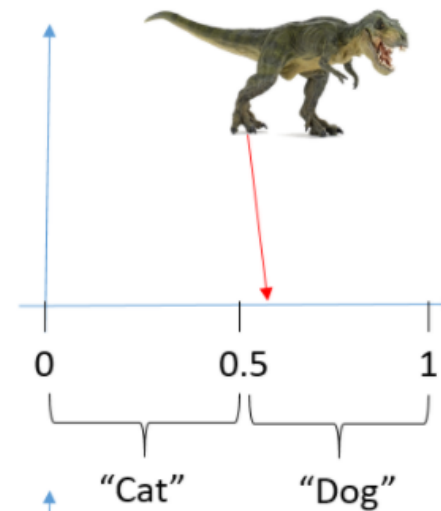
- If we are to use our model outputs for decision making, it is crucial that we characterize the associated uncertainty of the outputs
- How can we get a model to tell us "I don't know!" ? <sup>How ?</sup>
- How can we get a model to tell us "I'm really sure of this!" ?
- How can we add information we may already have to get better outputs?

# Example

Traditional  
NN

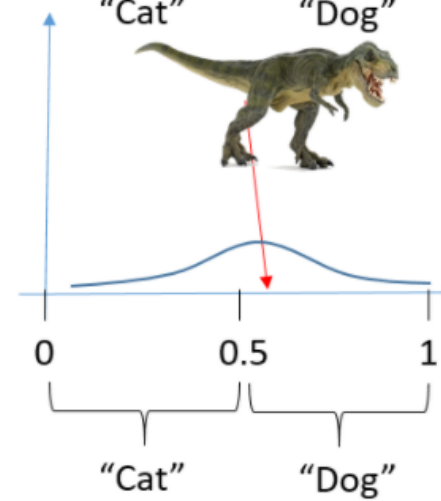
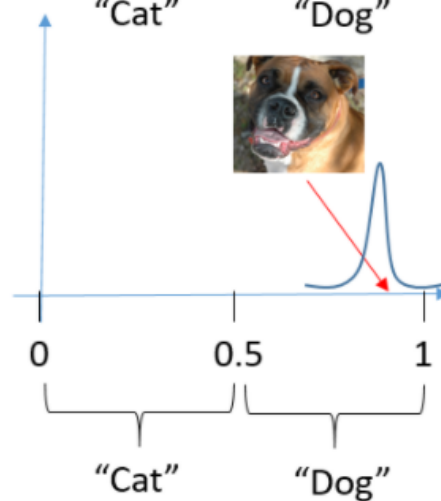
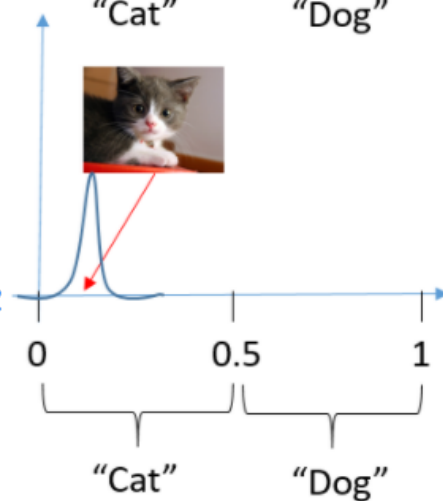


*show sth out of the class*



Probabilistic

*can tell  
because not sure*



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# What Uncertainties Do We Need in Bayesian Deep Learning for Computer Vision?

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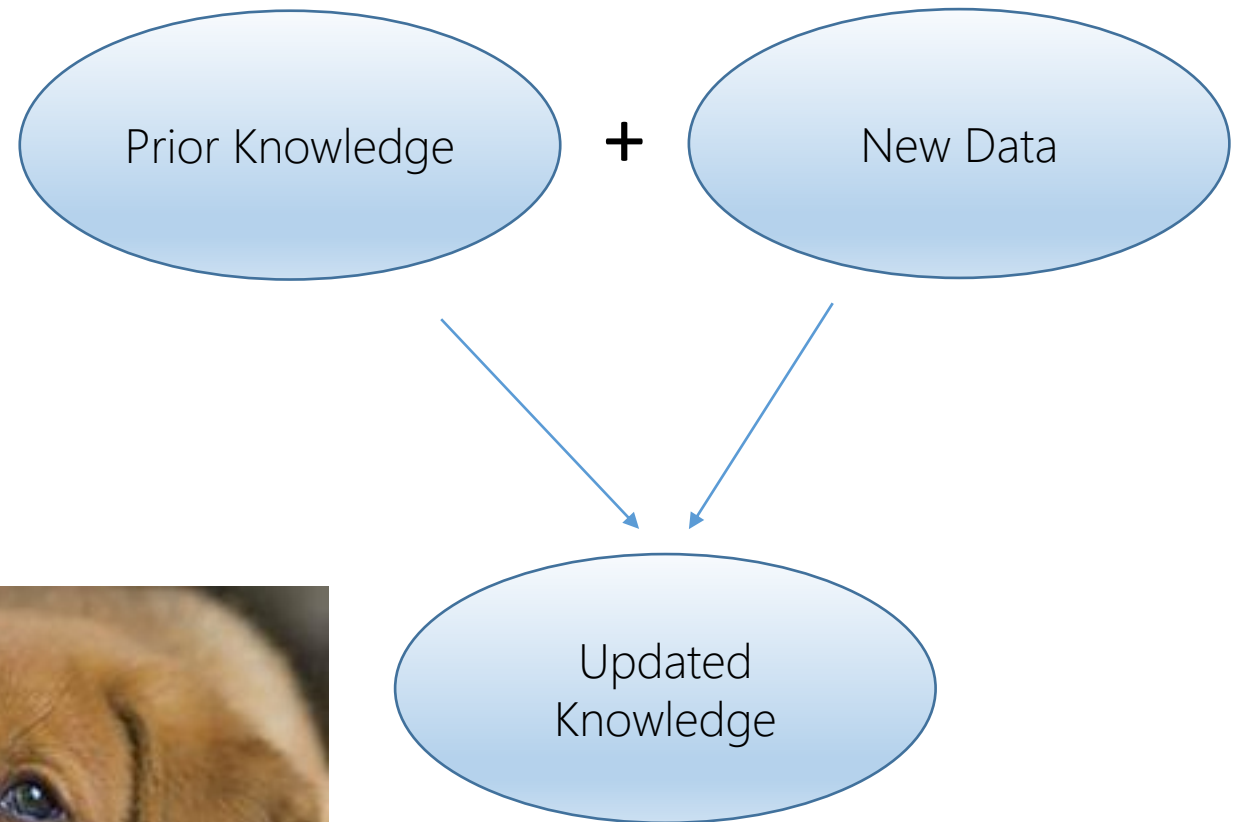
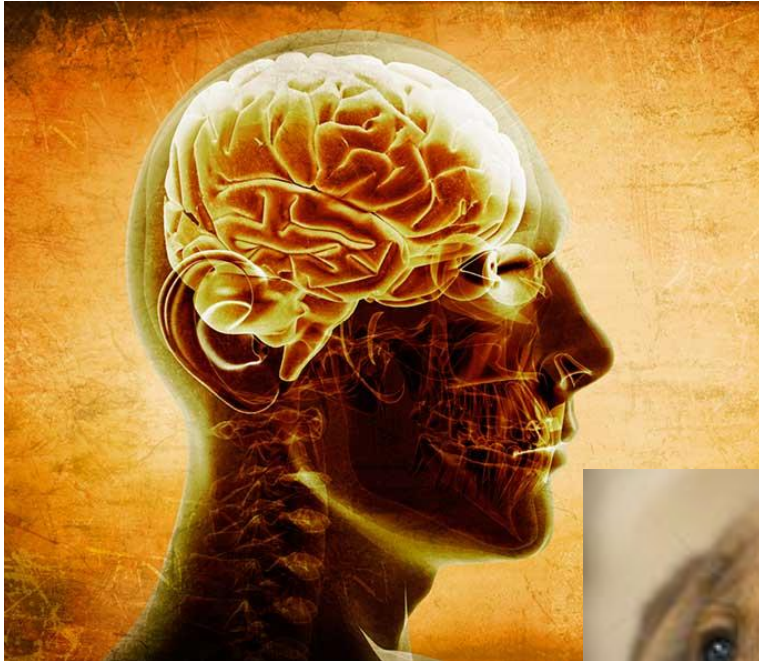
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Understanding what a model does not know is a critical part of many machine learning systems. Today, deep learning algorithms are able to learn powerful representations which can map high dimensional data to an array of outputs. However these mappings are often taken blindly and assumed to be accurate, which is not always the case. In two recent examples this has had disastrous consequences. In May 2016 there was the first fatality from an assisted driving system, caused by the perception system confusing the white side of a trailer for bright sky [1]. In a second recent example, an image classification system erroneously identified two African Americans as gorillas [2], raising concerns of racial discrimination. If both these algorithms were able to assign a high level of uncertainty to their erroneous predictions, then the system may have been able to make better decisions and likely avoid disaster.



# Reasoning



How do we formalize  
this process?

# Artificial Intelligence



If we want to design complex artificial systems, we need these systems to be able to (1) **form beliefs about the real world** and (2) **express the strength of these beliefs**

- "There is a car approaching"
- "This email is spam"
- "That person is lying"



# Probabilistic Reasoning

- How can we formalize this process?
- If we are to teach a machine how to do this, we need a specific set of rules that we can give to the machine
- Consider an event  $E$  about which there is uncertainty
  - How do we encode this uncertainty mathematically?
  - Suppose the machine currently have information  $I_1$  related to  $E$ , and then learn some new information  $I_2$ . How should we instruct the machine to update beliefs about  $E$ ?



# (Very) Simple Example

- Reasoning about a coin
- Initially, suppose you are pretty sure that it is a fair coin but you are not fully confident in this
  - How to express this precisely?
- You see one result of a coin toss. It is "Tails" – should you update? How?
- Suppose the next is also "Tails". What now?



Probabilistic Reasoning = Bayesian Reasoning

# Bayesian Reasoning

- Provides a specific set of instructions on how to reason with incomplete information
- Compare to deductive reasoning: If A then B
- Bayesian Reasoning: If A then B becomes more plausible
- Bayesian reasoning = using the laws of probability to drive our thinking
- This requires a **complete probabilistic model**

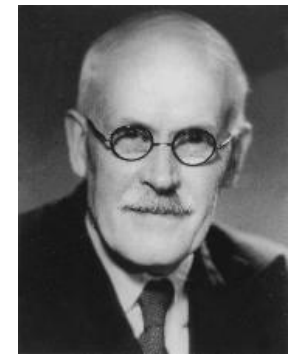
*models are pretty large, never very far  
when 1980s, computer cheap*



Thomas Bayes, 1701-1761



Pierre-Simon Laplace  
(1749-1827)

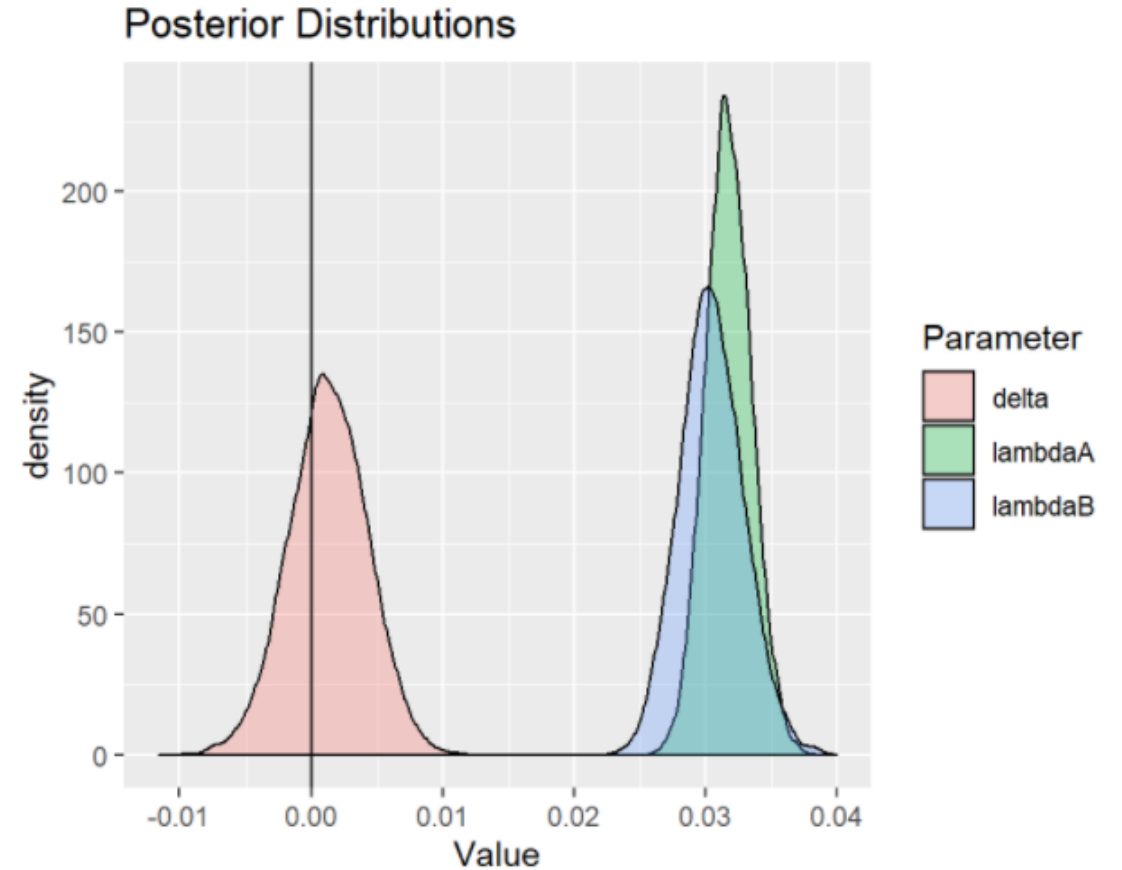


Harold Jeffreys (1891-  
1989)

*parallel*

# Week 1

- Introduction to Bayesian Thinking
  - How to encode knowledge as probabilities?
  - How to update knowledge when new information arrives?
- Simple Examples
  - How to update knowledge analytically?





# Week 2

- Hierarchical (or Multilevel) Models
- Shrinkage
- How to compare many individual estimates?
- Example:
  - Player 1 has played 6 matches and won 3
  - Player 2 has played 300 matches and won 150
  - Who is the better player?
- Bayesian Decision Theory

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# TrueSkill™ Ranking System

Established: November 18, 2005

Overview Publications Groups



The TrueSkill ranking system is a skill based ranking system for [Xbox Live](#) developed at [Microsoft Research](#). The purpose of a ranking system is to both identify and track the skills of gamers in a game (mode) in order to be able to match them into competitive matches. TrueSkill has been used to rank and match players in many different games, from Halo 3 to [Forza Motorsport 7](#).

An improved version of the TrueSkill ranking system, named [TrueSkill 2](#), launched with [Gears of War 4](#) and was later incorporated into [Halo 5](#).

# Week 3

## Project Meetings!

NO EXAMS

Done week 10

May 31st is final day

~~Don't~~ 20 min per team

little bit more technical  
use prob models for sth  
formly start in week 3  
main workload

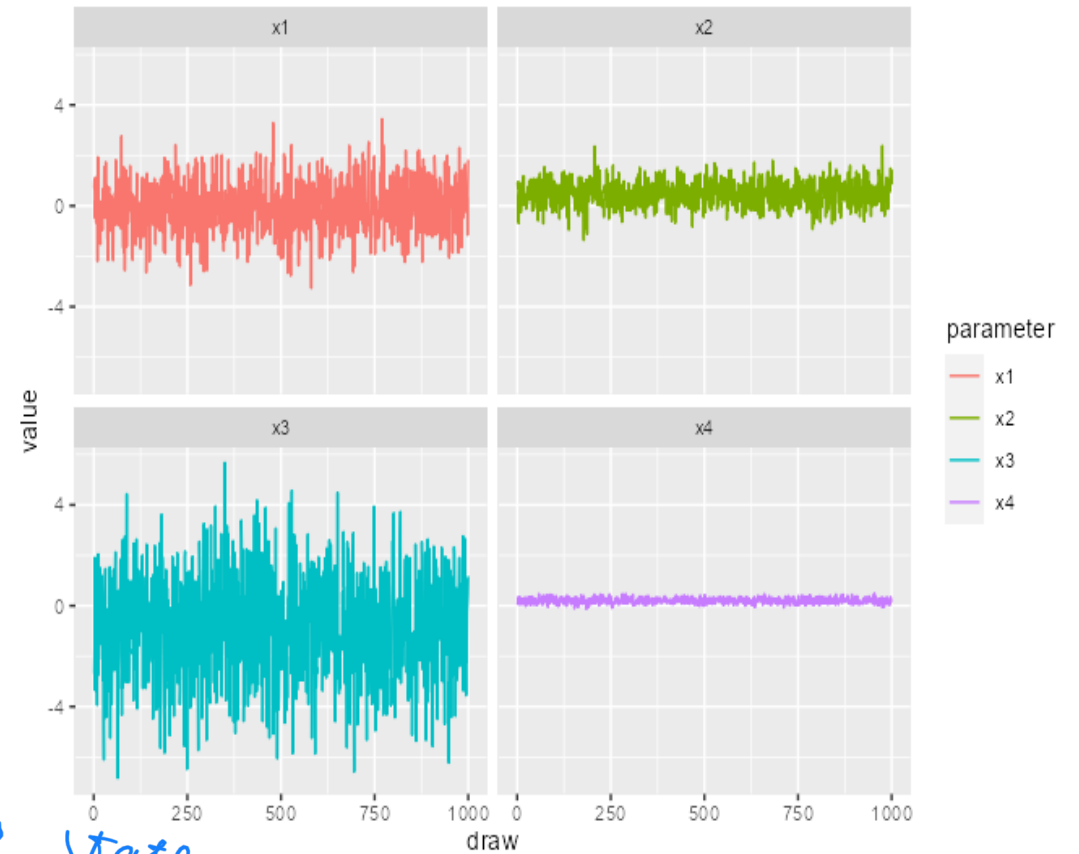
# Week 4

- Algorithms for probabilistic/Bayesian models
- Deterministic vs Probabilistic Algorithms
- Probabilistic programming
- Probabilistic algorithms are based on generating a stream of pseudo random numbers
- Markov Chain Monte Carlo
- Hybrid Monte Carlo

*Discrete time*

*continuous*

*state*

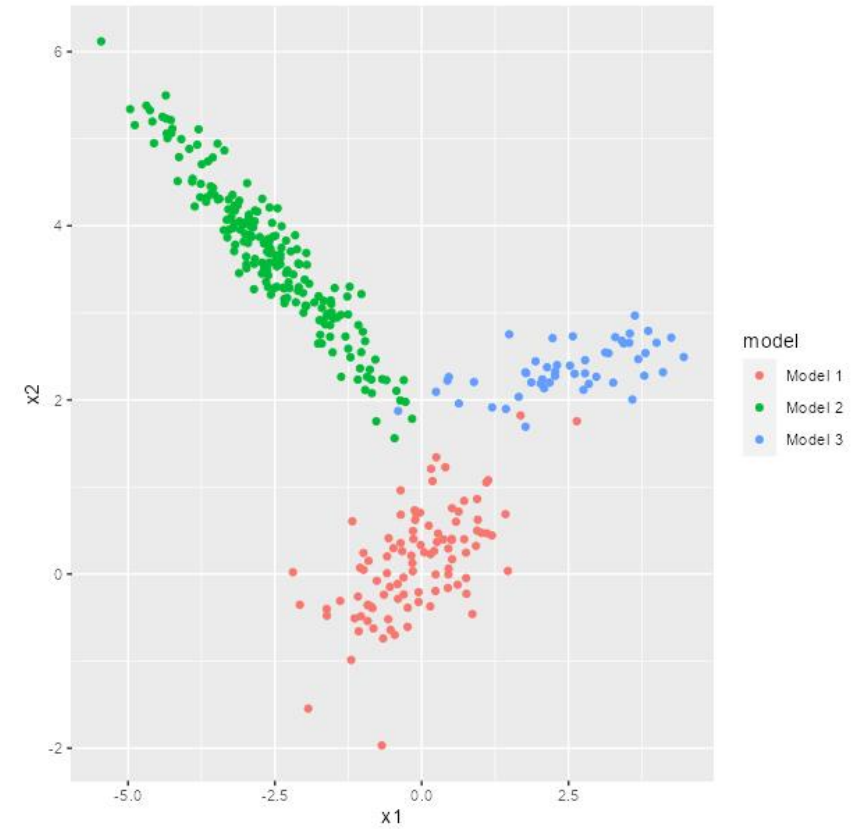


# Week 5

- Bayesian Classification
  - Logit Models
  - Multinomial Logit Models
  - Hierarchical Classification
- Naïve Bayes

# Week 6

- Mixture Models
- Bayesian Clustering



$$p(y|\theta) = \sum_{j=1}^K \lambda_j f(y|\gamma_j)$$



Week 7

Project Meetings 2

# Week 8,9

- Probabilistic Matrix Factorization
- Applications
  - Topic Models
  - Recommender Systems
  - Clustering of non-negative data

ReviewID 309501149

i	checked	in	on	labor	day	monday	when	most	guests
were	checking	out	so	i	asked	what	deals	on	room
upgrades	were	available	i	was	offered	a	corner	suite	for
75	extra	per	night	so	i	went	for	it	so
glad	i	did	the	bathroom	was	one	of	the	best
i've	ever	had	with	corner	panoramic	views	of	the	strip
from	the	separate	soaking	tub	similar	view	from	the	bedroom
aria	is	very	user	friendly	with	dining	options	from	casual
and	quick	to	high	end	experience	dining	i	recommend	the
caf	bardot	brasserie	and	jean	georges	steak	one	night	i
sat	at	the	bar	at	five50	pizza	for	a	quick
dinner	they	have	a	great	selection	of	beers	and	large
slices	of	wood	fire	oven	pizza	for	only	5.50	the
pizza	is	very	good	you	can	also	order	pizza	to
go	to	bring	to	your	room	the	pools	are	beautiful
with	an	outdoor	bar	serving	fun	frozen	cocktails	the	spa
is	a	not	to	be	missed	experience	for	35	a
guest	can	have	an	all	day	pass	to	enjoy	hot
stone	beds	a	salt	meditation	room	hot	and	cold	plunge
pools	and	a	coed	outdoor	infinity	edge	therapy	pool	that
is	stunning	after	dark	i	will	stay	at	aria	again
there	is	lots	to	like					

Topic  
a 1  
a 16  
a 19  
a NA

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Bayesian Nonparametric Poisson Factorization  
for Recommendation Systems

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Prem Gopalan  
Princeton University

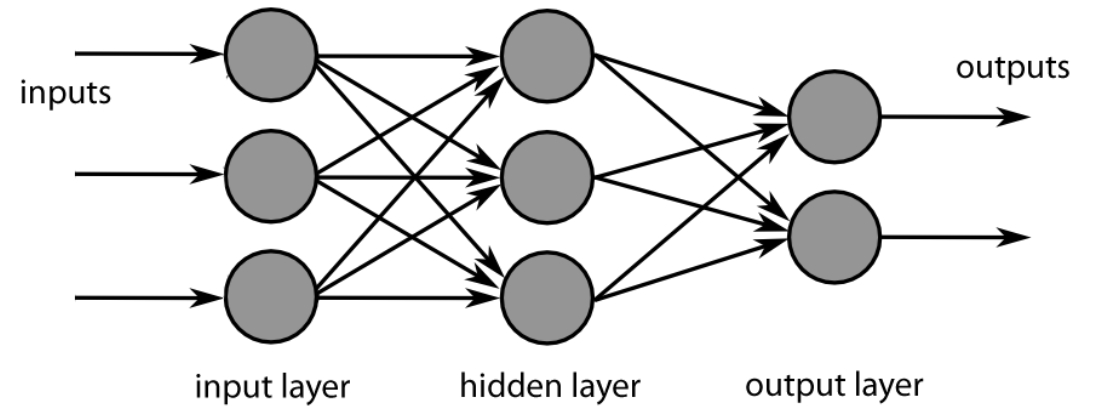
Francisco J. R. Ruiz  
University Carlos III in Madrid

Rajesh Ranganath  
Princeton University

David M. Blei  
Princeton University

# Other Topics....

- Bayesian Deep Learning
- Neural Nets with uncertainty
- Hard but promising area...



- Variational Autoencoders
- Generative Models
- Representing high dimensional data in smaller dimensions

Track: User Modeling, Interaction and Experience on the Web

WWW 2018, April 23-27, 2018, Lyon, France

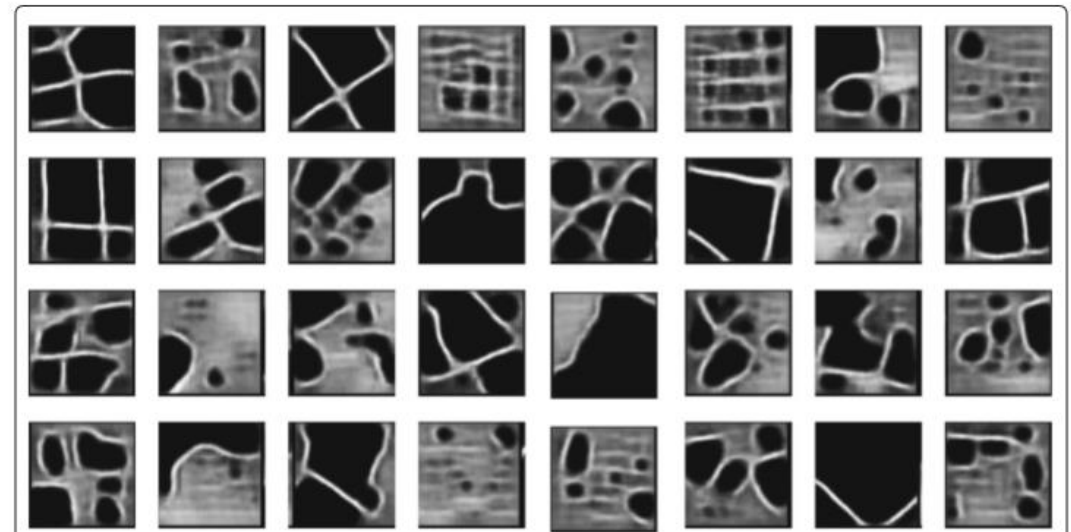
### Variational Autoencoders for Collaborative Filtering

Dawen Liang  
Netflix  
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Matthew D. Hoffman  
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Tony Jebara  
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Los Gatos, CA  
tjebara@netflix.com



**Fig. 8** Examples of synthetic urban street forms generated by passing a randomly sampled latent code  $z$  through the decoder network

Kempinska and Murcio *Applied Network Science* (2019) 4:114  
<https://doi.org/10.1007/s41109-019-0234-0>

Applied Network Science

RESEARCH

Open Access

### Modelling urban networks using Variational Autoencoders

Kira Kempinska<sup>1,2\*</sup> and Roberto Murcio<sup>1</sup>



### Learning Latent Representations of Bank Customers With The Variational Autoencoder

Rogelio A. Mancisidor<sup>a,b,\*</sup>, Michael Kampffmeyer<sup>a</sup>, Kjersti Aas<sup>c</sup>, Robert Jenssen<sup>a</sup>

# Logistics

- Regular class hours: Tuesdays, 9:00am-11:50am PST
- I am available on Discord for text/chat sessions
- No exams!
- 3 to 4 individual assignments
- Team project – to be presented on May 31 (week 10)
- Class materials: Slides, code, text book, articles



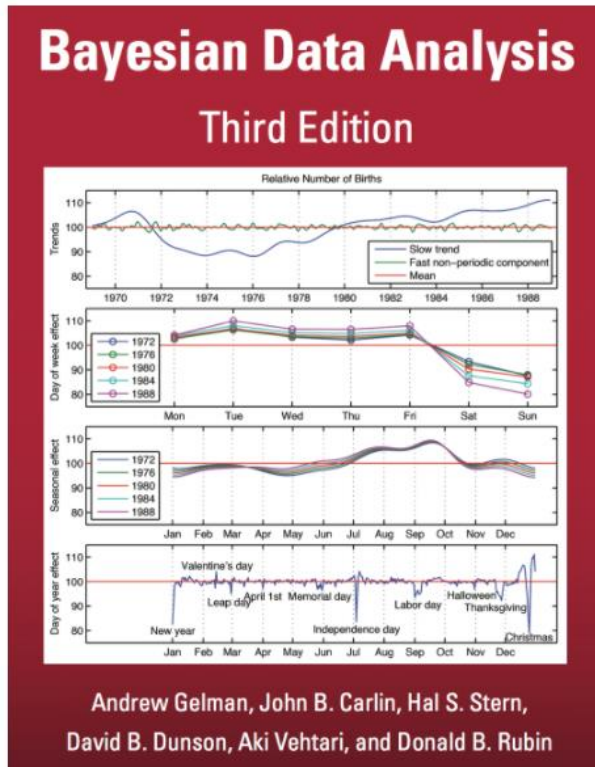
# Team Project

- Try to implement a Bayesian model using real data
- You should either code up your own algorithm OR at least make sure you understand the code if you use existing code
- I will serve as your consultant on the project
- Week 3: Project meeting 1
- Teams: self selected
- Output: Presentation in week 10

# Project Ideas

- Hierarchical/Multilevel Models for tabular data
  - Regression
  - Classification
  - Ranking project (sports, gaming etc)
- Document classification using topic models
- Project on Decision Theory
- Probabilistic Non-Negative Matrix Factorization
  - Recommendation systems
  - Count data
- Variational Autoencoders for generative tasks
- Bayesian Neural Nets

# Materials



+ articles + slides + code