Today

- Sequence modelling
- 2 Recurrent neural network
 - Definition
 - Training
 - Gated architectures
- RNN generators
- 4 Convolutional LM
- The Transformer
- 6 seq2seq
- Take-home message
- 8 Bonus: Recursive NN



2 / 54

Sequential data

- Time series
 - Financial data analysis: stock market, commodities, Forex
 - Healthcare: pulse rate, sugar level (from medical equipment and wearables)
- Text and speech: speech understanding, text generation
- Spatiotemporal data
 - Self-driving and object tracking
 - Plate tectonic activity
- Physics: jet identification
- etc.

Sequence modelling I

Sequence classification

- **1** $x = x_1, x_2, \dots, x_n, x_i \in V$ objects
- ② $y \in \{1, ..., L\}$ labels
- $\{(x^{(1)},y_1),(x^{(2)},y_2),\ldots,(x^{(m)},y_m)\}$ training data

Classification problem: $\gamma: \mathbf{x} \to \mathbf{y}$

- Activity recognition: x pulse rate, y activity (walking, running, peace)
- ② Opinion mining: x sentence, y sentiment (positive, negative)
- 3 Trading: x stock market, y action (sell, buy, do nothing)

Sequence modelling II

Sequence labelling

- **1** $x = x_1, x_2, ..., x_n, x_i \in V$ objects
- ② $y = y_1, y_2, \dots, y_n, y_i \in \{1, \dots, L\}$ labels
- $\{(\pmb{x}^{(1)}, \pmb{y}^{(1)}), (\pmb{x}^{(2)}, \pmb{y}^{(2)}), \dots, (\pmb{x}^{(m)}, \pmb{y}^{(m)})\}$ training data
- **4** exponential number of possible solutions : if length(x) = n, there are L^n possible solutions

Classification problem: $\gamma: \mathbf{x} \to \mathbf{y}$

- Part of speech tagging: x word, y part of speech (verb, noun, etc.)
- ② Genome annotation: x DNA, y genes
- **1** HEP tracking: x a set of hits with backgrounds, y hit classification

Sequence labelling tasks

POS tagging and Named Entity Recognition

X (words)	the	cat	sat	on	а	mat
Y (tags)	DET	NOUN	VERB	PREP	DET	NOUN

Table: POS tagging

Alex	is	going	to	Los	Angeles
B-PER	0	0	0	B-LOC	I-LOC

Table: NER (IOB2)

Alex	travels	with	Marty	A.	Rick	to	NY	city
S-PER	0	0	B-PER	I-PER	E-PER	0	B-LOC	E-LOC

Table: NER (IOBES)

Sequence modelling III

Sequence transduction / transformation

- \bullet $\mathbf{x} = x_1, x_2, \dots, x_n, x_i \in V_{source}$ objects
- $\mathbf{v} = y_1, y_2, \dots, y_n, y_i \in V_{target}$ objects
- $\{(x^{(1)},y^{(1)}),(x^{(2)},y^{(2)}),\ldots,(x^{(m)},y^{(m)})\}$ training data
- $\mathbf{v}^{(1)}$, $\mathbf{v}^{(1)}$ are of different length

Transduction problem: $x_{source} \rightarrow y_{target}$

- **1** Machine translation: x sentence in German, y sentence in English
- ② Speech recognition: x spoken language, y text
- **3** Chat bots: x question, y answer

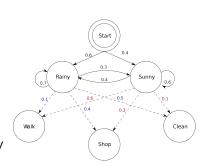


Traditional ML approaches to sequence modeling

- Hidden Markov Models (HMM)
- Conditional Random Fields (CRF)
- Local classifier: for each x define features, based on x_{-1} , x_{+1} , etc, and perform classification n times

Problems:

- Markov assumption: fixed length history
- Computation complexity

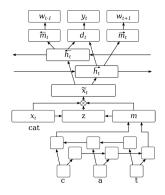


DL approaches to sequence modeling

- Neural networks
- Recurrent neural network and its modifications: LSTM, GRU, Highway
- 2D Convolutional Neural Network
- Transformer
- Pointer network

Problems:

- Training time
- 2 Amount of training data



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Neural language model [1]

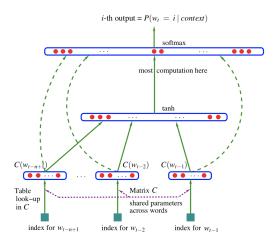
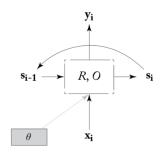


Figure: Neural language model

Recurrent neural network

- Input: sequence of vectors
- $x_{1:n} = x_1, x_2, \ldots, x_n, x_i \in \mathbb{R}^{d_{in}}$
- Output: a single vector $y_n = RNN(x_{1:n}), y_n \in \mathbb{R}^{d_{out}}$
- For each prefix x_{i:j} define an output vector y_i:
 y_i = RNN(x_{1:i})
- RNN^* is a function returning this sequence for input sequence $x_{1:n}$: $y_{1:n} = RNN^*(x_{1:n}), y_i \in \mathbb{R}^{d_{out}}$



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Sequence modelling with RNN

Sequence classification Put a dense layer on top of RNN to predict the desired class of the sequence after the whole sequence is processed

$$p(I_j|\mathbf{x}_{1:n}) = \operatorname{softmax}(RNN(\mathbf{x}_{1:n}) \times W + b)_{[j]}$$

② Sequence labelling Produce an output y_i for each input RNN reads in. Put a dense layer on top of each output to predict the desired class of the input

$$p(l_j|\mathbf{x}_j) = \mathtt{softmax}(RNN(\mathbf{x}_{1:j}) \times W + b)_{[j]}$$



More details on RNN

- $RNN^*(x_{1:n}, s_0) = y_{1:n}$
- $y_i = O(s_i)$ simple activation function
- $s_i = R(s_{i-1}, x_i)$, where R is a recursive function, s_i is a state vector
- s₀ is initialized randomly or is a zero vector
- ullet $x_i \in \mathbb{R}^{d_{in}}$, $y_i \in \mathbb{R}^{d_{out}}$, $s_i \in \mathbb{R}^{f(d_{out})}$
- θ shared weights

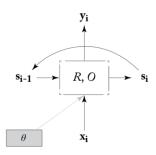


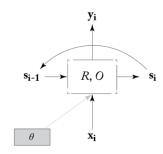
Figure: Goldberg, Yoav. Neural network methods for natural language processing 🔞 🗆 🔻 🎒 🔻 🧵 🔻 💈 💉 🤰

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More details on RNN

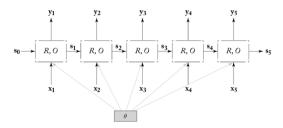
•
$$s_i = R(x_i, s_{i-1}) = g(s_{i-1}W^s + x_iW^x + b)$$

- $y_i = O(s_i) = s_i$
- ullet $y_i, s_i, b \in \mathbb{R}^{d_{out}}, x_i \in \mathbb{R}^{d_{in}}$
- ullet $W^{ imes} \in \mathbb{R}^{d_{in} imes d_{out}}$ $W^{s} \in \mathbb{R}^{d_{out} imes d_{out}}$



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RNN unrolled



$$s_4 = R(s_3, x_4) = R(R(s_2, x_3), x_4) = R(R(R(s_1, x_2), x_3), x_4) =$$

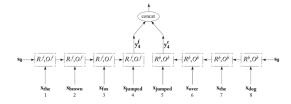
$$= R(R(R(R(s_0, x_1), x_2), x_3), x_4)$$

Figure: Goldberg, Yoav. Neural network methods for natural language processing 🔞 🗆 🖟 👩 🖟 🔞 👂 🔞 💆 💉 💆 💉 🔻

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Bidirectional RNN (Bi-RNN)

The input sequence can be read from left to right and from right to left. Which direction is better?

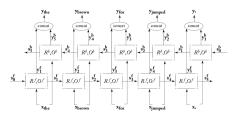


$$biRNN(x_{1:n}, i) = y_i = [RNN^f(x_{1:i}); RNN^r(x_{n:i})]$$

Figure: Goldberg, Yoav. Neural network methods for natural language processing 🔞 🗆 🔻 🎒 🔻 🧵 🔻 💈 💉 🤰

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Bi-RNN

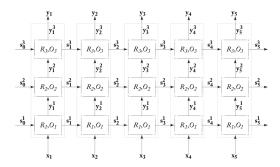


$$biRNN^*(x_{1:n}, i) = y_{1:n} = biRNN(x_{1:n}, 1) \dots biRNN(x_{1:n}, n)$$

Figure: Goldberg, Yoav. Neural network methods for natural language processing () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () + () +

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Multilayer RNN



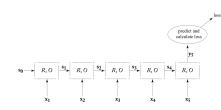
Connections between different layers are possible too: $y_1^2 = \mathtt{concat}(x_1, y_1^1)$

Figure: Goldberg, Yoav. Neural network methods for natural language processing 🔞 🗆 🤊 📲 👂 🔞 📳 👢 🥏 🔊 🔾

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Sequence classification

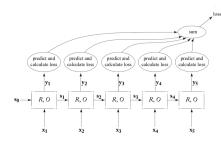
- $\hat{y_n} = O(s_n)$
- prediction = $MLP(\hat{y_n})$
- Loss: $L(\hat{y_n}, y_n)$
- L can take any form: cross entropy, hinge, margin, etc.



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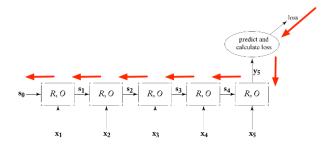
Sequence labelling

- Output \hat{t}_i for each input $x_{1,i}$
- Local loss: $L_{local}(\hat{t}_i, t_i)$
- Global loss: $L(\hat{t}_n, t_n) = \sum_i L_{local}(\hat{t}_i, t_i)$
- L can take any form: cross entropy, hinge, margin, etc.



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Backpropogation through time



$$\begin{split} s_i &= R(x_i, s_{i-1}) = g(s_{i-1}W^s + x_iW^x + b) \\ \text{Chain rule: } &\frac{\partial L}{\partial w} = \frac{\partial L}{\partial p(\hat{y}_5)} \frac{\partial p(\hat{y}_5)}{\partial s_4} (\frac{\partial s_4}{\partial w} + \frac{\partial s_4}{\partial s_3} \frac{\partial s_3}{\partial w} + \frac{\partial s_4}{\partial s_3} \frac{\partial s_3}{\partial s_2} \frac{\partial s_2}{\partial s_w} + \ldots) \end{split}$$

Figure: Goldberg, Yoav. Neural network methods for natural language processing 🔞 🗆 🔻 🎒 🔻 🧵 🔻 💈 💉 🤰

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Vanishing gradient problem

Chain rule:
$$\frac{\partial L}{\partial w} = \frac{\partial L}{\partial p(\hat{y}_5)} \frac{\partial p(\hat{y}_5)}{\partial s_4} (\frac{\partial s_4}{\partial w} + \frac{\partial s_4}{\partial s_3} \frac{\partial s_3}{\partial w} + \frac{\partial s_4}{\partial s_3} \frac{\partial s_3}{\partial s_2} \frac{\partial s_2}{\partial s_w} + \ldots)$$
 $g - \text{sigmoid}$

- 1 Many sigmoids near 0 and 1
 - Gradients \rightarrow 0
 - Not training for long term dependencies
- Many sigmoids > 1
 - Gradients \rightarrow + inf
 - Not training again

Solution: gated architectures (LSTM and GRU)



Controlled memory access

- Entire memory vector is changed: $s_{i+1} = R(x_i, s_i)$
- Controlled memory access: $s_{i+1} = g \odot R(x_i, s_i) + (1 g)s_i$ $g \in [0, 1]^d, s, x \in \mathbb{R}^d$
- Differential gates: $\sigma(g), g' \in \mathbb{R}^d$
- This controllable gating mechanism is the basis of the LSTM and the GRU architectures

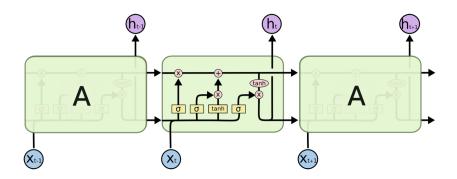
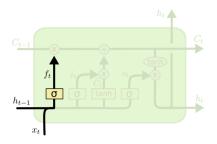
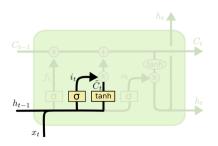


Figure: colahbloghttp://colah.github.io/posts/2015-08-Understanding-LSTMs/

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$$f_t = \sigma\left(W_f \cdot [h_{t-1}, x_t] + b_f\right)$$

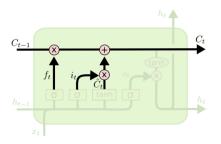


$$i_t = \sigma \left(W_i \cdot [h_{t-1}, x_t] + b_i \right)$$

$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$

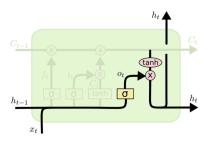
Figure: colahbloghttp://colah.github.io/posts/2015-08-Understanding-LSTMs/ $_4$ $_{\square}$ $_{\square}$

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$$C_t = f_t * C_{t-1} + i_t * \tilde{C}_t$$

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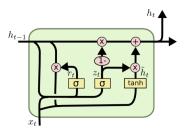


$$o_t = \sigma (W_o [h_{t-1}, x_t] + b_o)$$

$$h_t = o_t * \tanh (C_t)$$

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Gated recurrent unit



$$z_{t} = \sigma (W_{z} \cdot [h_{t-1}, x_{t}])$$

$$r_{t} = \sigma (W_{r} \cdot [h_{t-1}, x_{t}])$$

$$\tilde{h}_{t} = \tanh (W \cdot [r_{t} * h_{t-1}, x_{t}])$$

$$h_{t} = (1 - z_{t}) * h_{t-1} + z_{t} * \tilde{h}_{t}$$

Figure: colahbloghttp://colah.github.io/posts/2015-08-Understanding-LSTMs/

Katya Artemova (HSE) Sequence modelling September 25, 2019 30 / 54

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Language model

Compute the probability of a sequence of words:

$$P(w_1, w_2, \ldots, w_n)$$

Predict next word:

$$P(w_n|w_1,w_2,\ldots,w_{n-1})$$

Perplexity

$$2^{H(p)} = 2^{\frac{1}{|V|} - \sum_{x} \log_2 p(x)}$$



Sequence generation

Teacher forcing: $x := \langle s \rangle x, y := x \langle /s \rangle$

$$x : \langle s \rangle x_1 x_2 \dots x_n$$

$$y: x_1x_2...x_n < /s >$$

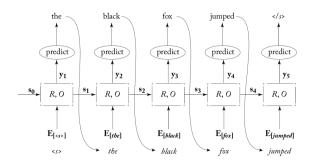


Figure: Goldberg, Yoav. Neural network methods for natural language processing 🔞 🗇 🥫 👂 🔞 💆 🥏 🔊 🧸 🔊

33 / 54

Sequence generation

- Examples of generated texts:
 http://karpathy.github.io/2015/05/21/rnn-effectiveness/
- Examples of generated MIDI music: https://towardsdatascience.com/how-to-generate-music-using-a-lstm-neural-network-in-keras-68786834d4c5

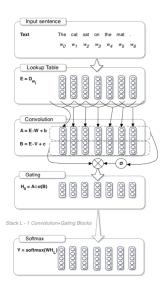
Pros and cons of RNNs

- Advantages:
 - ► RNNs are popular and successful for variable-length sequences
 - ► The gating models such as LSTM are suited for long-range error propagation
- Problems:
 - ► The sequentiality prohibits parallelization within instances
 - Long-range dependencies still tricky, despite gating

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Language Modeling with Gated Convolutional Networks



- Embeddings $\in D^{|V| \times e}$
- Input: $w_0, ..., w_n \to E = [D_{w_0}, ..., D_{w_n}]$
- Hidden layers: h_0, \ldots, h_n :

$$h_l(X) = (X \times W + b) \circ \sigma(X \times V + c)$$

- Gated linear unit: $X \circ \sigma(X)$
- **Output**: $Y = \operatorname{softmax}(WH_L)$

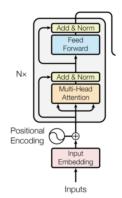
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- 2 Recurrent neural network
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The Transformer

An alternative architecture to RNN which allows of parallel and faster training

- Several layers of identical modules
- Each module consists of Multi-Head Attention and Feed Forward layers
- Input: embeddings. To get embeddings for numerical input, apply any dense layer
- Positional embeddings to make use of the order of the sequence



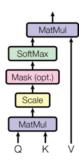
Katya Artemova (HSE) Sequence modelling September 25, 2019 39 / 54

Scaled Dot-Product Attention

An attention function can be described as mapping a query and a set of key-value pairs to an output, where the query, keys, values, and output are all vectors:

$$Attention(Q, K, V) = softmax(\frac{QK^{T}}{\sqrt{d_k}})V,$$

where the input consists of queries Q and keys K of dimension d_k and values V of dimension d_V



Multi-head Attention

Multi-head attention allows the model to jointly attend to information from different representation subspaces at different positions

Concat

Scaled Dot-Product
Attention

Linear Linear Linear

$$MultiHead(Q, K, V) = concat(head_1, ..., head_h)W^O,$$

where

 $head_i = Attention(QW_i^Q, KW_i^K, VW_i^V)$ and W are projection matrices.



The Transformer

Bringing it all together:

- LayerNorm: $\frac{x-\mu}{\sigma}$
- Residual connection:LayerNorm(x+Sublayer(x))
- Position-wise Feed-Forward Networks: $FFN(x) = \max(0, xW_1 + b_1)W_2 + b_2$

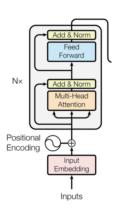


Figure: Vaswani, Ashish, et al. "Attention is all you need." Advances in neural information processing systems 2017.

Positional Encoding

We need to inject some information about the relative or absolute position of x_{pos} in the sequence:

$$PE_{(pos,2i)} = \sin(pos/10000^{2i/d_{model}})$$

$$PE_{(pos,2i+1)} = \cos(pos/10000^{2i/d_{model}})$$

Positional encoding: x = x + PE(x)



Figure: Vaswani, Ashish, et al. "Attention is all you need." Advances in neural information processing systems 2017.

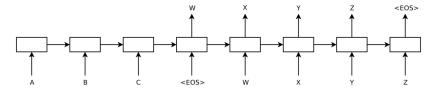
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Sequence 2 sequence learning

Encoder-decoder model for:

- Machine translation
- Chit-chat bots



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Take-home message

- There is a lot of sequential data around us
- Before DL: HMM, MEMM
- Mid 2010 DL: RNN, LSTM, etc
- Late 2010 DL: the Transformer
- 2020: stack more transformer blocks (Trasformer XL)

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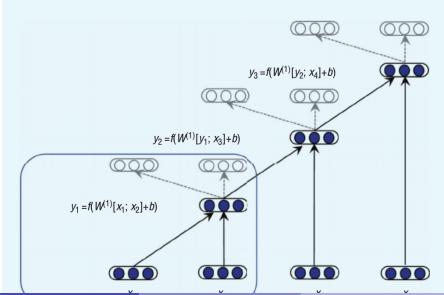
Modeling trees with Recursive NN

- Input: $x_1, x_2, ..., x_n$
- A binary tree T can be represented as a unique set of triplets (i, k, j), s.t. i < k < j, $x_{i:j}$ is parent of $x_{i:k}$, $i_{k+1,j}$
- RecNN takes as an input a binary tree and returns as output a corresponding set of inside state vectors $s_{i:i}^{A} \in \mathbb{R}^{d}$
- Each state vector $s_{i:j}^{A}$ represents the corresponding tree node $q_{i:j}^{A}$ and encodes the entire structure rooted at that node

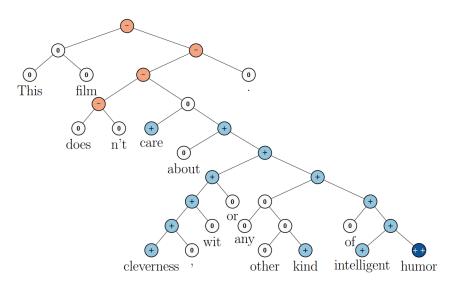
RecNN

- Input: x_1, x_2, \dots, x_n and a binary tree T
- $RecNN(x_1, x_2, \dots, x_n, T) = \{s_{i:j}^A \in \mathbb{R}^d | q_{i:j}^A \in T\}$
- $s_{i:i}^{\mathbf{A}} = v(x_i)$
- $s_{i:j}^{A} = R(A, B, C, s_{i:k}^{B}, s_{k+1:j}^{C}), q_{i:k}^{B} \in T, q_{k+1:j}^{C} \in T$
- $R(A, B, C, s_{i:k}^B, s_{k+1:i}^C) = g([s_{i:k}^B, s_{k+1:i}^C]W)$

RecNN



RecNN [2]



Reference I



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Reading

- Neural Networks for NLP. Joav Goldberg, Ch. 14-16
- Stuart Russell, Peter Norvig. Artificial Intelligence: A Modern Approach, Ch. 15
- Oan Jurafsky, James H. Martin. Speech and Language Processing, Ch. 3, Ch. 8