# Amplitude Modulation Simulation Software

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## 1 System Overview

The AM simulation software is a software written in Java with user interface (UI) built using Swing.

- **AMSignal**: Represents the AM signal with attributes for time, message, carrier, modulated, demodulated signals, and frequency spectra.
- **ControlPanel**: Provides a GUI for configuring signal parameters (e.g., frequency, amplitude, modulation index) and initiating actions like signal updates or data exports.
- **ModulationAndDemodulation**: Implements core signal processing for modulation, demodulation, noise addition, and spectrum computation.
- SignalPlotPanel: Visualizes time and frequency domain plots with zoom and pan capabilities.
- TimeDomainSimulationWindow: Supports real-time time-domain signal animation.
- SpectrumAnalysisFFT: Performs Fast Fourier Transform (FFT)-based spectrum analysis.
- **TotalHarmonicDistortion**: Analyzes Total Harmonic Distortion (THD) with harmonic visualization.
- SignalToNoiseRatio: Computes and displays Signal-to-Noise Ratio (SNR).
- DataExporter: Exports signal data to CSV files for external analysis.

The main application (Main.java) integrates these components into a tabbed interface, with each tab dedicated to a specific AM variant.

## 2 Functioning Logic

The software operates through a user-driven workflow:

- 1. **Parameter Configuration**: Users input signal parameters (e.g., carrier frequency  $f_c$ , message frequency  $f_m$ , modulation index m) via the ControlPanel.
- 2. Signal Generation: The AMSignal class generates the message and carrier signals based on user inputs. For a sinusoidal message signal  $m(t) = A_m \cos(2\pi f_m t)$  and carrier  $c(t) = A_c \cos(2\pi f_c t)$ , the modulated signal is computed according to the AM variant.
- 3. **Modulation**: The ModulationAndDemodulation class applies the appropriate modulation technique (e.g., DSB-AM:  $s(t) = A_c[1 + m \cdot m(t)]\cos(2\pi f_c t)$ ).
- 4. **Demodulation**: Demodulation is performed (e.g., envelope detection for DSB-AM) to recover the message signal.
- 5. **Visualization**: The SignalPlotPanel displays time-domain signals and frequency spectra, while SpectrumAnalysisFFT provides dynamic FFT analysis.
- 6. **Analysis**: THD and SNR are computed and visualized using dedicated modules.
- 7. **Export**: Users can export signal data to CSV files via DataExporter.

## 3 Simulation and Modeling

The simulation is based on discrete-time signal processing, with signals sampled at a rate  $f_s$  (default: 100 kHz) to ensure Nyquist compliance  $(f_s \ge 2 \cdot \max(f_c, f_m))$ . The AMSignal class models signals as arrays of doubles, representing sampled values over a time interval T.

#### 3.1 Time-Domain Simulation

The TimeDomainSimulationWindow animates signal propagation in real time, updating the display at a fixed frame rate (e.g., 60 FPS). The simulation loop:

- Generates signal samples for the current time window.
- Updates the modulated and demodulated signals.
- Renders the signals on a canvas using SignalPlotPanel.

#### 3.2 Frequency-Domain Modeling

Frequency-domain analysis is performed using FFT, implemented in SpectrumAnalysisFFT. The FFT transforms the time-domain signal x[n] into its frequency components X[k]:

$$X[k] = \sum_{n=0}^{N-1} x[n]e^{-j2\pi kn/N}, \quad k = 0, 1, \dots, N-1$$

where N is the number of samples. The resulting spectrum is visualized with amplitude (dB) versus frequency (Hz).

## 4 Utilization of Algorithms

The software employs several algorithms for signal processing and analysis:

#### 4.1 Fast Fourier Transform (FFT)

The FFT algorithm (Cooley-Tukey) is used for efficient spectrum computation. The SpectrumAnalysisFFT class:

- Samples the signal over a window of N points.
- Applies a Hamming window to reduce spectral leakage.
- Computes the FFT to obtain the frequency spectrum.
- Updates the spectrum display dynamically.

#### **4.2** Modulation Algorithms

The ModulationAndDemodulation class implements modulation for each AM variant:

- **DSB-AM**:  $s(t) = A_c[1 + m \cdot m(t)] \cos(2\pi f_c t)$ .
- **DSB-SC**:  $s(t) = A_c \cdot m(t) \cos(2\pi f_c t)$ .
- SSB: Filters one sideband using a Hilbert transform-based approach.
- VSB: Retains a vestige of one sideband using a bandpass filter.
- QAM: Combines two modulated signals in quadrature:  $s(t) = I(t)\cos(2\pi f_c t) + Q(t)\sin(2\pi f_c t)$ .

#### 4.3 Demodulation Algorithms

Demodulation techniques include:

- Envelope Detection (DSB-AM): Applies a rectifier and low-pass filter to extract m(t).
- **Coherent Detection** (DSB-SC, SSB): Multiplies the received signal by a synchronized carrier and filters the result.

• QAM Demodulation: Uses two coherent detectors for in-phase (I) and quadrature (Q) components.

#### 4.4 Noise Addition

Gaussian noise is added to simulate real-world conditions, with variance controlled by the SNR parameter. The noise is generated using a random number generator and added to the modulated signal.

## 5 Physics Models

The software is grounded in the physics of electromagnetic wave modulation:

#### 5.1 Signal Representation

Signals are modeled as continuous-time functions sampled discretely. The message signal m(t) is typically a low-frequency sinusoid, while the carrier c(t) is a high-frequency sinusoid. The modulated signal s(t) combines these according to the AM variant.

### 5.2 Frequency Spectrum

The frequency spectrum of an AM signal is derived from its Fourier transform. For DSB-AM, the spectrum includes:

$$S(f) = \frac{A_c}{2} \left[ \delta(f - f_c) + \delta(f + f_c) \right] + \frac{mA_c}{2} \left[ M(f - f_c) + M(f + f_c) \right]$$

where M(f) is the message spectrum, and  $\delta(f)$  represents the carrier impulses.

#### 5.3 Total Harmonic Distortion (THD)

THD is computed as the ratio of the power of harmonic components to the fundamental frequency:

$$\text{THD} = \sqrt{\frac{\sum_{n=2}^{\infty} P_n}{P_1}}$$

where  $P_n$  is the power of the n-th harmonic, extracted via FFT.

#### 5.4 Signal-to-Noise Ratio (SNR)

SNR is calculated as:

SNR (dB) = 
$$10 \log_{10} \left( \frac{P_{\text{signal}}}{P_{\text{noise}}} \right)$$

where  $P_{\text{signal}}$  and  $P_{\text{noise}}$  are the signal and noise powers, respectively, computed from the FFT spectrum.