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Aim: to find Fourier series of the given function in an interval $[a, b]$ and visualize it using MATLAB.

Fourier series of the function $f(x)$ on the interval $[-L, L]$

is given by

$$f(x) = \frac{a_0}{2} + \sum_{n=1}^{\infty} a_n \cos\left(\frac{n\pi x}{L}\right) + b_n \sin\left(\frac{n\pi x}{L}\right)$$

where

$$a_0 = \frac{1}{L} \int_{-L}^L f(x) dx, \quad a_n = \frac{1}{L} \int_{-L}^L f(x) \cos\left(\frac{n\pi x}{L}\right) dx, \quad b_n = \frac{1}{L} \int_{-L}^L f(x) \sin\left(\frac{n\pi x}{L}\right) dx$$

Exercise:

Find the Fourier series of the function

$$f(x) = |x|, -2 < x < 2$$

and visualize it.

```

clc
clear all
syms x
L=input('the value of L');
f=input('Enter the function of x');
n=input('Enter the number of terms of series');
d=(1/(2*L))*int(f,x,-L,L);
For j=1:n
    for k=1:1i
        a(k)=(1/L)*int(f*cos((k*pi*x)/L),x,-L,L);
        c(k,1)=cos((k*pi*x)/L);
        b(k)=(1/L)*int(f*sin((k*pi*x)/L),x,-L,L);
        s(k,1)=sin((k*pi*x)/L);
    end
    f_r(1i)=d+a*c+b*s;
    h1=ezplot(f_r(j));
    hold all
hold on
    h2=ezplot(f);

```

```
hold off
set(h1,'color','g','linestyle','-')
legend('1st','2nd','3rd','4th','5th','f')
```

OUTPUT:

the value of L

2

Enter the function of x

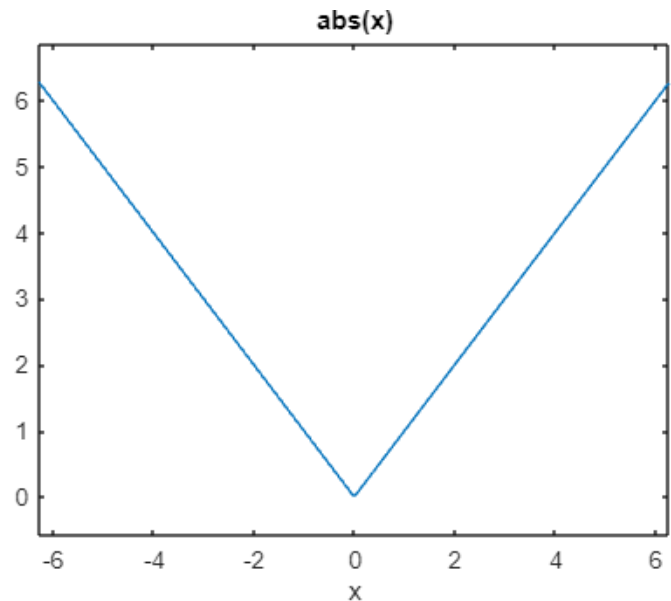
abs(x)

Enter the number of terms of series

n=5

$d = (1/(2*L)) * \int_{-L}^L f(x) dx$

d = 1

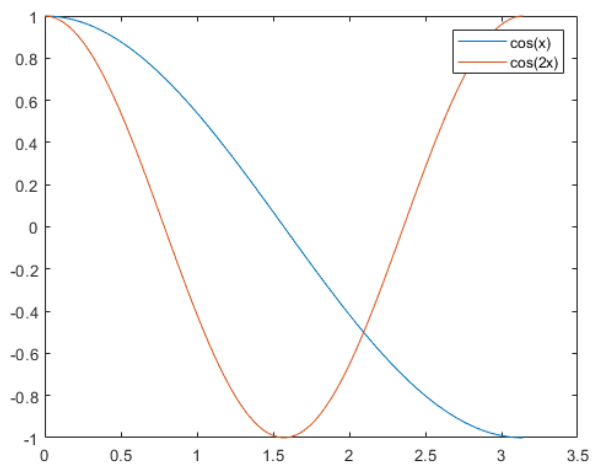


```
x = linspace(0,pi);
y1 = cos(x);
plot(x,y1)
```

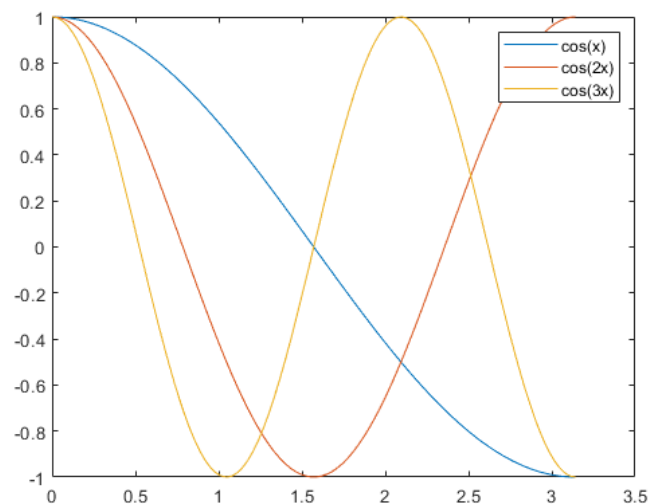
hold on

```
y2 = cos(2*x);
plot(x,y2)
```

```
legend('cos(x)', 'cos(2x)')
```



```
y3 = cos(3*x);
plot(x,y3, 'DisplayName', 'cos(3x)')
hold off
```

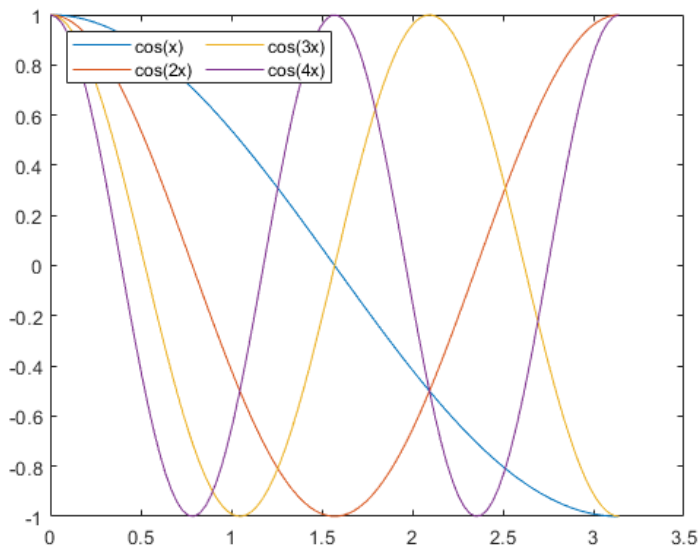


```
x = linspace(0,pi);
y1 = cos(x);
plot(x,y1)
```

```
hold on
y2 = cos(2*x);
plot(x,y2)
```

```
y3 = cos(3*x);
plot(x,y3)
```

```
y4 = cos(4*x);
plot(x,y4)
hold off
```



```
legend({'cos(x)', 'cos(2x)', 'cos(3x)', 'cos(4x)'}, 'Location', 'northwest', 'NumColumns', 2)
```

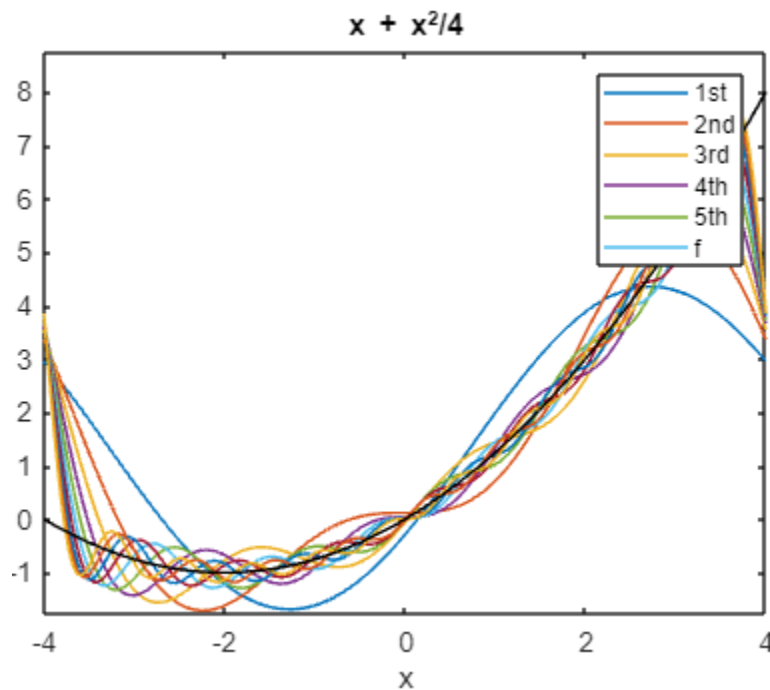
Exercise:

Find the Fourier series of the function $f(x) = x + x^2 / 4$ and visualize it.

MATLAB Code:

```
clc
clear all
syms x
L=input('the value of L');
f=input('Enter the function of x');
n=input('Enter the number of terms of series');
d=(1/(2*L))*int(f,x,-L,L);
For j=1:n
    for k=1:1i
        a(k)=(1/L)*int(f*cos((k*pi*x)/L),x,-L,L);
        c(k,1)=cos((k*pi*x)/L);
        b(k)=(1/L)*int(f*sin((k*pi*x)/L),x,-L,L);
        s(k,1)=sin((k*pi*x)/L);
    end
    f_r(1i)=d+a*c+b*s;
    h1=ezplot(f_r(j));
    hold all
    hold on
    h2=ezplot(f);
    hold off
    set(h1,'color','g','linestyle','-')
    legend('1st','2nd','3rd','4th','5th','f')
```

OUTPUT:



Exercise:

Find the Fourier series of the function

$$f(x) = |x|, -2 < x < 2$$

and visualize it.

MATLAB Code:

```
clc
clear all
syms x
L=input('the value of L');
f=input('Enter the function of x');
n=input('Enter the number of terms of series');
d=(1/(2*L))*int(f,x,-L,L);
for j=1:n
    for k=1:j
        a(k)=(1/L)*int(f*cos((k*pi*x)/L),x,-L,L);
        c(k,1)=cos((k*pi*x)/L);
        b(k)=(1/L)*int(f*sin((k*pi*x)/L),x,-L,L);
        s(k,1)=sin((k*pi*x)/L);
    end
    f_r(j)=d+a*c+b*s;
    h1=ezplot(f_r(j));
hold all
```

```

end
hold on
h2=ezplot(f,[-L L]);
hold off

```

MATLAB Output:

the value of L

2

Enter the function of x

abs(x)

Enter the number of terms of series

n=5

$d = (1/(2*L)) * \text{int}(f, x, -L, L)$

d = 1

