

# Wave Current Interaction

## Core Components and Initialization

The `WaveCurrentInteraction` class, implemented in C#, models the interaction between waves and currents in an estuarine environment using linear wave theory and simplified wave-enhanced friction. The class is initialized with the following parameters:

- Wave height:  $H_w$  (m)
- Wave direction:  $\theta_w$  (degrees, aligned with wind)
- Wave period:  $T_w$  (s)
- Water depth:  $h$  (m)
- Gravitational acceleration:  $g = 9.81 \text{ m/s}^2$

The constructor sets these parameters, and the `UpdateParameters` method allows dynamic updates during simulation.

## Functioning Logic

The class provides two primary methods to account for wave-current interactions:

1. `ComputeStokesDrift`: Calculates Stokes drift velocities ( $u_s, v_s$ ) based on linear wave theory, representing the net mass transport induced by waves.
2. `ComputeWaveEnhancedFriction`: Computes a wave-enhanced bottom friction coefficient using a simplified Grant-Madsen approach, accounting for increased turbulence due to wave orbital velocities.

## Stokes Drift Computation

The `ComputeStokesDrift` method calculates Stokes drift velocities using linear wave theory for shallow water:

- **Wave characteristics:**
  - Approximate wavelength:  $\lambda = \sqrt{gh}T_w$
  - Wave number:  $k = 2\pi/\lambda$
  - Angular frequency:  $\omega = 2\pi/T_w$
  - Wave amplitude:  $a = H_w/2$
- **Stokes drift magnitude:** Near the surface ( $z \approx 0$ ):

$$u_s = \frac{a^2 \omega k \cosh(2kz)}{2 \sinh^2(kh)} \approx \frac{a^2 \omega k}{2 \sinh^2(kh)} \quad (1)$$

- **Directional components:**

$$u_s = u_{s,\text{mag}} \cos(\theta_w \pi / 180) \quad (2)$$

$$v_s = u_{s,\text{mag}} \sin(\theta_w \pi / 180) \quad (3)$$

If  $H_w \leq 0$  or  $T_w \leq 0$ , the method returns  $(u_s, v_s) = (0, 0)$ . NaN or Infinity values are clamped to zero to ensure numerical stability.

## Wave-Enhanced Friction

The `ComputeWaveEnhancedFriction` method calculates an enhanced bottom friction coefficient:

- **Wave orbital velocity** at the bottom:

$$u_b = \frac{a\omega}{\sinh(kh)} \quad (4)$$

where  $a = H_w/2$ ,  $\omega = 2\pi/T_w$ ,  $k = 2\pi/\sqrt{gh}T_w$ .

- **Enhanced friction coefficient:**

$$C_d = C_{d0}(1 + \beta|u_b|) \quad (5)$$

where  $C_{d0}$  is the base friction coefficient, and  $\beta = 0.2$  is an empirical factor.

- **Constraints:** The result is clamped between  $C_{d0}$  and 0.01 to prevent numerical instability.

If  $H_w \leq 0$  or  $T_w \leq 0$ , the base friction coefficient is returned unchanged.

## Physical and Mathematical Models

The `WaveCurrentInteraction` class employs the following models:

- **Stokes Drift:**

$$\lambda = \sqrt{gh}T_w \quad (6)$$

$$k = \frac{2\pi}{\lambda}, \quad \omega = \frac{2\pi}{T_w}, \quad a = \frac{H_w}{2} \quad (7)$$

$$u_{s,\text{mag}} = \frac{a^2\omega k}{2\sinh^2(kh)} \cosh(2k \cdot 0) \quad (8)$$

$$u_s = u_{s,\text{mag}} \cos\left(\theta_w \frac{\pi}{180}\right), \quad v_s = u_{s,\text{mag}} \sin\left(\theta_w \frac{\pi}{180}\right) \quad (9)$$

- **Wave-Enhanced Friction:**

$$u_b = \frac{a\omega}{\sinh(kh)} \quad (10)$$

$$C_d = C_{d0}(1 + 0.2|u_b|), \quad C_d \in [C_{d0}, 0.01] \quad (11)$$

These models capture wave-induced transport and turbulence effects, integrating with estuarine circulation models to enhance realism in velocity and friction calculations.