

# Boundary Layer Schemes

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## 1 Functionalities

The `BoundaryLayerSchemesWindow` class provides the following functionalities:

- **Initialization:** Sets up a window for boundary layer schemes analysis, integrating with the model to access ocean and atmosphere temperatures and coupling parameters.
- **Simulation Control:** Allows users to start and stop a simulation, updating parameters (drag coefficient, sensible heat coefficient, boundary layer depth, KPP mixing coefficient) and selecting between Bulk and KPP schemes.
- **Visualization:** Displays a heatmap of heat flux (Bulk scheme) or diffusivity (KPP scheme) with annotations and a scatter plot of flux/diffusivity versus temperature gradient, updated in real-time via animation.
- **Parameter Input:** Enables users to input simulation parameters and select schemes, with validation to ensure physical constraints.
- **Logging and Error Handling:** Logs initialization, simulation control, and plot updates using the logging module, with exception handling to display errors via message boxes.

## 2 Simulation Logic

The simulation logic in `BoundaryLayerSchemesWindow` centers around managing boundary layer schemes analysis and visualization.

### 2.1 Initialization

- **Purpose:** Initializes the analysis window with model integration and visualization setup.
- **Process:**

- Stores the model instance for access to ocean and atmosphere temperatures and coupling parameters.
- Sets up a window with a control panel for inputting drag coefficient, sensible heat coefficient, boundary layer depth, KPP mixing coefficient, and selecting Bulk/KPP schemes.
- Initializes a matplotlib figure with two subplots: one for a heatmap of heat flux or diffusivity with annotations, and one for a scatter plot of flux/diffusivity versus temperature gradient.
- Sets up a simulation grid ( $n_y \times n_x$ ) matching the model's ocean temperatures and initializes arrays for heat flux and diffusivity.
- Sets the time step  $\Delta t = 1800$  s to match the main simulation.
- Sets up a timer for animation updates every 100 ms and initializes the plot.
- Logs initialization details and handles exceptions, displaying errors via QMessageBox.

## 2.2 Simulation Control

- **Purpose:** Manages the start and stop of the boundary layer schemes simulation.
- **Process (Start):**
  - Validates inputs: drag coefficient ( $> 0$ ), sensible heat coefficient ( $\geq 0$ ), boundary layer depth ( $> 0$ ), KPP mixing coefficient ( $> 0$ ).
  - Updates model parameters (`model.coupling.drag_coeff`).
  - Resets simulation step, time steps, flux arrays, and diffusivity arrays.
  - Starts a timer to trigger animation updates every 100 ms.
  - Disables the start button and enables the stop button.
- **Process (Stop):**
  - Stops the timer and animation.
  - Enables the start button and disables the stop button.
  - Logs actions and handles exceptions, displaying errors via QMessageBox.

## 2.3 Plot Update

- **Purpose:** Updates the visualization of heat flux or diffusivity and their relationship with temperature gradients.
- **Process:**
  - Checks if the simulation should continue (current step < total\_time/ $\Delta t$ ).
  - Validates and updates parameters from user inputs and selected scheme.
  - Computes heat flux (Bulk scheme) or diffusivity and heat flux (KPP scheme) based on ocean and atmosphere temperatures and wind speed.
  - Stores flux and temperature gradient data for visualization.
  - Updates plots: a heatmap of heat flux or diffusivity with sparse annotations, and a scatter plot of flux/diffusivity versus temperature gradient colored by time.
  - Increments the simulation step and logs actions.

## 3 Physics and Mathematical Models

The `BoundaryLayerSchemesWindow` class implements models for boundary layer dynamics, comparing Bulk and KPP schemes.

### 3.1 Bulk Heat Flux (Bulk Scheme)

- **Purpose:** Computes sensible heat flux between ocean and atmosphere.
- **Equation:**

$$Q_b = \rho_{\text{air}} C_p^{\text{air}} C_h U (T_o - T_a),$$

where  $\rho_{\text{air}} = 1.225 \text{ kg/m}^3$ ,  $C_p^{\text{air}} = 1005 \text{ J/kg/K}$ ,  $C_h$  is the sensible heat coefficient ( $\text{W/m}^2/\text{K}$ ),  $U$  is wind speed ( $\text{m/s}$ ),  $T_o$  is ocean temperature ( $\text{K}$ ), and  $T_a$  is atmosphere temperature ( $\text{K}$ ).

- **Implementation:** `update_plot` computes  $Q_b$  using user-input  $C_h$  and model temperature fields.

### 3.2 KPP Scheme

- **Purpose:** Computes turbulent diffusivity and heat flux using the K-Profile Parameterization (KPP) scheme.

- **Equations:**

$$K(z) = k_m \left(1 - \frac{z}{h}\right)^2,$$

$$Q_{\text{KPP}} = -K(z) \frac{\partial T_o}{\partial y},$$

where  $k_m$  is the KPP mixing coefficient ( $\text{m}^2/\text{s}$ ),  $h$  is the boundary layer depth (m),  $z \in [0, h]$ , and  $\frac{\partial T_o}{\partial y} \approx \frac{T_{o,i+1,j} - T_{o,i-1,j}}{2\Delta y}$ .  $K(z)$  is clipped to  $[0, k_m]$ .

- **Implementation:** `update_plot` computes  $K(z)$  and  $Q_{\text{KPP}}$  using user-input  $k_m$  and  $h$ .

### 3.3 Temperature Gradient

- **Purpose:** Computes the temperature difference driving the heat flux.
- **Equation:**

$$\Delta T = T_o - T_a,$$

where  $\Delta T$  is the temperature gradient (K).

- **Implementation:** `update_plot` computes  $\Delta T$  for scatter plot visualization.

## 4 Algorithms

### 4.1 Initialization Algorithm

- **Input:** Model instance (`model`).
- **Steps:**
  1. Log initialization.
  2. Store `model` as an instance variable.
  3. Set window title to "Boundary Layer Schemes Analysis" and size to  $900 \times 600$ .
  4. Create a control panel with inputs for drag coefficient (`model.coupling.drag_coef`), sensible heat coefficient ( $10.0 \text{ W/m}^2/\text{K}$ ), boundary layer depth (50.0 m), KPP mixing coefficient ( $0.01 \text{ m}^2/\text{s}$ ), and a selector for Bulk/KPP schemes.
  5. Create start and stop buttons, with stop initially disabled.
  6. Initialize a matplotlib figure with two subplots: heatmap and scatter plot.

7. Set up simulation grid ( $n_y \times n_x$ ) from model's ocean temperatures and initialize arrays for heat flux and diffusivity.
8. Set  $\Delta t = 1800$  s.
9. Initialize empty lists for time steps, bulk fluxes, KPP fluxes, and temperature gradients.
10. Set up a timer for 100 ms updates and call `update_plot(0)`.
11. Log completion or errors, displaying critical errors via `QMessageBox`.

## 4.2 Start Simulation Algorithm (`start_simulation`)

- **Input:** None (uses input fields).
- **Steps:**
  1. Log start of simulation.
  2. Read and validate inputs: drag coefficient ( $> 0$ ), sensible heat coefficient ( $\geq 0$ ), boundary layer depth ( $> 0$ ), KPP mixing coefficient ( $> 0$ ).
  3. Update `model.coupling.drag_coeff`.
  4. Reset `current_step`, `time_steps`, `bulk_fluxes`, `kpp_fluxes`, `temp_gradients`, and heat flux/diffusivity arrays.
  5. Start timer (100 ms interval).
  6. Disable start button and enable stop button.
  7. Log completion or errors, displaying warnings or critical errors via `QMessageBox`.

## 4.3 Stop Simulation Algorithm (`stop_simulation`)

- **Input:** None.
- **Steps:**
  1. Log stop of simulation.
  2. Stop timer and animation (`anim.event_source.stop()`).
  3. Set `anim` to None.
  4. Enable start button and disable stop button.
  5. Log completion or errors, displaying critical errors via `QMessageBox`.

## 4.4 Plot Update Algorithm (update\_plot)

- **Input:** Frame number (unused directly, tracks via current\_step).
- **Steps:**
  1. Log start of update at current\_step.
  2. If  $\text{current\_step} \geq \text{total\_time}/\Delta t$  or model is invalid, call stop\_simulation.
  3. Validate and read inputs: drag coefficient, sensible heat coefficient, boundary layer depth, KPP mixing coefficient, and scheme.
  4. Compute Bulk heat flux:  $Q_b = \rho_{\text{air}} C_p^{\text{air}} C_h U (T_o - T_a)$ .
  5. Compute KPP diffusivity and flux:
    - $K(z) = k_m \left(1 - \frac{z}{h}\right)^2$ , clipped to  $[0, k_m]$ .
    - $Q_{\text{KPP}} = -K \frac{\partial T_o}{\partial y}$ , with  $\frac{\partial T_o}{\partial y} \approx \frac{T_{o,i+1,j} - T_{o,i-1,j}}{2\Delta y}$ .
  6. Update fields:  $Q_b$  for Bulk scheme,  $K(z)$  for KPP scheme.
  7. Store flattened  $Q_b$ ,  $Q_{\text{KPP}}$ , and  $\Delta T = T_o - T_a$  for scatter plot.
  8. Update plots:
    - Left: Heatmap of  $Q_b$  (Bulk, coolwarm) or  $K(z)$  (KPP, viridis) with annotations every  $\text{ny}/5 \times \text{nx}/5$ .
    - Right: Scatter plot of  $Q_b$  or  $K(z)$  vs.  $\Delta T$ , colored by time (plasma).
  9. Increment current\_step.
  10. Log completion or errors, displaying warnings or critical errors via QMessageBox.