## Variable Resolution

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### 1 Functionalities

The VariableResolutionGrid class provides the following functionalities:

- **Grid Initialization**: Creates a 2D grid of size  $N \times N$  with spatially variable resolution, adjusting  $\Delta x$  and  $\Delta y$  based on a coastal factor to refine resolution near coasts.
- **Spatial Step Retrieval**: Provides access to the spatial step arrays  $(\Delta x, \Delta y)$  for use in numerical computations in Model.py.
- Coastal Refinement: Simulates coastal regions by reducing spatial steps in a designated coastal zone, enhancing resolution where ocean-atmosphere interactions are more complex.
- **Logging and Error Handling**: Logs initialization and retrieval operations using the logging module, with exception handling to catch and log errors.

## 2 Simulation Logic

The simulation logic in VariableResolution.py centers around the VariableResolution class, which sets up and manages a variable resolution grid for the simulator.

#### 2.1 Initialization

- **Purpose**: Initializes a 2D grid with spatially variable resolution, refining spatial steps near coastal regions.
- Process:
  - Initializes parameters: grid\_size (N) and coast\_factor, which determines the degree of refinement near coasts.
  - Creates 2D arrays  $\Delta x$  and  $\Delta y$ , initially set to 1.0 across the  $N \times N$  grid.

- Defines a coastal region as the first N/4 grid points in both x and y directions.
- Reduces  $\Delta x$  and  $\Delta y$  by dividing by coast\_factor in the coastal region to achieve finer resolution.
- Logs initialization details and handles exceptions.

#### 2.2 Spatial Step Retrieval

- **Purpose**: Provides access to the spatial step arrays  $(\Delta x, \Delta y)$  for use in numerical computations.
- Process:
  - Returns the  $\Delta x$  and  $\Delta y$  arrays as a tuple.
  - Logs the retrieval operation and handles exceptions.

## 3 Algorithms

#### 3.1 Initialization Algorithm

- **Input**: grid\_size (N), coast\_factor.
- Steps:
  - 1. Log initialization parameters: grid\_size, coast\_factor.
  - 2. Store grid\_size and coast\_factor as instance variables.
  - 3. Initialize  $\Delta x$  and  $\Delta y$  as  $N \times N$  arrays filled with 1.0.
  - 4. Compute coastal width: coast\_width =  $\lfloor N/4 \rfloor$ .
  - 5. For each grid point (i, j):
    - If  $i < \text{coast\_width}$  or  $j < \text{coast\_width}$ :
      - \* Set  $\Delta x_{i,j} = \Delta x_{i,j} / \text{coast\_factor.}$
      - \* Set  $\Delta y_{i,j} = \Delta y_{i,j} / \text{coast\_factor.}$
  - 6. Log completion of initialization.
  - 7. Handle exceptions and log errors if initialization fails.

# 3.2 Spatial Step Retrieval Algorithm (get\_spatial\_steps)

• Input: None.

- Steps:
  - 1. Log start of spatial step retrieval.
  - 2. Return the tuple  $(\Delta x, \Delta y)$ .
  - 3. Log errors if retrieval fails.