

Piecewise Regression QPoisson Error on Real Data using STAN Directly

Michael Gilchrist

date: 2022-12-22

Goal

- Fit two piece quasipoisson to data

Recap

Set up

Install libraries

```
# install packages user might not have by replacing FALSE with TRUE

## load libraries
library(stats)
library(MASS) # provides negative binomial fitting: glm.nb
library(ggplot2)
library(ggpubr)
library(grid)
library(gridExtra)
library(GGally)
library(broom)
library(tidyverse)
library(viridisLite)
library(cmdstanr)
library(rstan)
options(mc.cores = (parallel::detectCores()-2))
rstan_options(auto_write = TRUE)
library(loo)

## options(ggplot2.continuous.colour="viridis",
##         ggplot2.discrete.colour="viridis",
##         ggplot2.scale_fill_discrete = scale_fill_viridis_d,
##         ggplot2.scale_fill_continuous = scale_fill_viridis_c)

library(reshape2)
```

```
library(lme4)
library(latex2exp)
```

Load Data

```
load(file.path("input", "data.processing_2022-12-15.Rda"),
      verbose = TRUE)
```

```
## Loading objects:
## motif_data
## motif_data_40C
## motif_stats
## motif_stats_40C
## bird_bill_data
```

```
motif_data
```

```
## # A tibble: 146 x 28
##   male round trial_round motif~1 motif~2 temp~3 humid~4 chamber date counter
##   <fct> <dbl>         <dbl>   <int>   <dbl>   <dbl>   <dbl> <fct>   <chr> <chr>
## 1 T229     1           1       0 0      45.8    NA 6     02/1~ KIM
## 2 T229     1           2      24 0.0131  42.3    NA 6     02/1~ KIM
## 3 T229     1           3     114 0.0622  40.7    NA 6     02/1~ KIM
## 4 T229     1           4     198 0.108   26.2    NA 6     02/1~ KIM
## 5 T229     1           5     315 0.172   34.9    NA 6     02/2~ KIM
## 6 T231     1           1      57 0.0431  42.8    NA 2     02/1~ RAS
## 7 T231     1           2       7 0.00529  45.0    NA 2     02/1~ RAS
## 8 T231     1           3      86 0.0650  41.1    NA 2     02/1~ KIM
## 9 T231     1           4      24 0.0181  27.2    NA 2     02/1~ RAS
## 10 T231    1           5     215 0.162   36.5    NA 2     02/2~ RAS
## # ... with 136 more rows, 18 more variables: test_order <int>,
## #   temp_target <dbl>, temp_median <dbl>, humidity_mean <dbl>, motif_rate <dbl>,
## #   mass <dbl>, n_obs_completed <lgl>, motif_count_plus_1 <int>,
## #   log_motif_count_plus_1 <dbl>, temp <dbl>, n_obs_round <int>, n_obs <int>,
## #   trial <int>, motif_prop_round <dbl>, weights <dbl>, svp <dbl>, vpd <dbl>,
## #   vpd_offset <dbl>, and abbreviated variable names 1: motif_count,
## #   2: motif_prop, 3: temp_mean, 4: humidity_mean
```

Examine Data

Create Working Dataset

```
filter_data <- TRUE

if(filter_data) {
  males_filtered_disp <- motif_stats_40C %>%
    filter(dispersion < 50) %>%
```

```

pull(male)

males_filtered_mean <- motif_stats %>%
  filter(mean > 10) %>% # changing from 10 to 40 removes previous male 7 (T258)
  pull(male)

male_vector <- intersect(males_filtered_mean, males_filtered_disp)
} else {
  male_vector <- motif_data %>% select(male) %>% distinct()
}

data_ind <- motif_data %>%
  filter(male %in% male_vector) %>%
  mutate(male = droplevels(male)) %>%
  mutate(index = as.integer(male)) %>%
  mutate(male = as.character(male)) %>%
  arrange(index) %>%
  select(male, index, motif_count, temp, round, trial_round, date, counter) %>%
  ## left_join(index_shape, by = "index") %>%
  mutate()

stats_ind <- motif_stats %>%
  filter(male %in% male_vector)

data_ind <- data_ind %>% filter(temp < 38) %>%
  group_by(male) %>% mutate(y0_simple.est = mean(motif_count), phi_ind = var(motif_count)/y0_simple.est)
  ungroup()

summary(data_ind)

```

```

##      male           index      motif_count      temp
## Length:38      Min.    : 1.000      Min.    : 0.0      Min.    :25.71
## Class :character 1st Qu.: 3.000      1st Qu.: 52.5      1st Qu.:29.51
## Mode  :character Median : 5.500      Median : 89.0      Median :33.52
##              Mean   : 5.579      Mean   :112.9      Mean   :31.88
##              3rd Qu.: 8.000      3rd Qu.:167.2      3rd Qu.:34.34
##              Max.    :11.000      Max.    :425.0      Max.    :37.64
##      round      trial_round      date      counter
## Min.    :1.000      Min.    :1.000      Length:38      Length:38
## 1st Qu.:1.000      1st Qu.:2.000      Class :character  Class :character
## Median :3.000      Median :3.000      Mode  :character  Mode  :character
## Mean   :2.211      Mean   :3.105
## 3rd Qu.:3.000      3rd Qu.:4.000
## Max.    :3.000      Max.    :6.000
## y0_simple.est      phi_ind
## Min.    : 24.00      Min.    : 0.142
## 1st Qu.: 64.33      1st Qu.: 6.955
## Median : 93.20      Median :12.986
## Mean   :112.89      Mean   :33.913
## 3rd Qu.:166.38      3rd Qu.:48.000
## Max.    :246.25      Max.    :128.361

```

```
summary_stats <- data_ind %>% ungroup() %>% summarize(y0_bar = mean(y0_simple.est), y0_sd = sd(y0_simple.est))

n_male <- length(unique(data_ind$male))
```

Set Up Data

```
data <- data_ind
motif_count <- data %>% pull(motif_count)
temp <- data %>% pull(temp)
N <- length(temp)
index <- data %>% pull(index)
## parameters to be printed

pars <- c("t0", "y0")
pars_full <- c(pars, "lp_")
```

Fit Models

QPoisson

```
iter <- 15000
tmax <- 46
t0max <- tmax - 0.5;
t0min <- 20;
## values to use for model predictions
tp = seq(25, tmax, length.out = 100)
n_cores <- 4
n_chains <- n_cores

##y0_grouping <- map_int(data$male, ~ if_else(. %in% y0_group[[1]], 1, 2))
model <- "qpoi"
stan_file <- "two.piece.qpoisson.2.0.stan"
## For debugging
## cmodel <- cmdstan_model(stan_file = stan_file)

stan_model(file = stan_file,
            verbose = TRUE)
```

```
##
## TRANSLATING MODEL '' FROM Stan CODE TO C++ CODE NOW.
```

```
## Define groups

flags <- c("separate", "grouping_1", "pooled")
flags_x <- flags
flags_y <- flags
fit_tbl <- crossing(model = model,
                    x0 = flags_x, y0 = flags_y,
```

```

        desc = "NA_character",
        y0_group_list = list(NA),
        x0_group_list = list(NA),
        fit = list(NA),
        llik = list(NA),
        r_eff = list(NA),
        loo = list(NA)
    )
}

for(x_flag in flags_x) {
  for(y_flag in flags_y) {

    desc <- paste0(model, ":", x_flag, ":", y_flag)
    curr_row <- which(fit_tbl$x0 == x_flag & fit_tbl$y0 == y_flag)

    fit_tbl[ curr_row, ]$desc <- desc
    print(desc)

    x0_group_list <- list()
    y0_group_list <- list()

    switch(x_flag,
      separate = {
        x0_group_list <- data$male %>% unique() %>% as.list()
      },
      grouping_1 = {
        ## set up groupings based on 2022-12-20 analysis
        ## Using male ID's instead index to make code more robust
        x0_group_list[[1]] <- c("T235", "T237", "T244", "T247", "T257", "T260")
        x0_group_list[[2]] <- c("T234", "T236", "T243", "T246", "T258")
      },
      pooled = {
        x0_group_list[[1]] <- data$male
      }
    )

    switch(y_flag,
      separate = {
        y0_group_list <- data$male %>% unique() %>% as.list()
      },
      grouping_1 = {
        ## set up groupings based on 2022-12-20 analysis
        ## Using male ID's instead index to make code more robust
        y0_group_list[[1]] <- c("T234", "T243", "T244", "T246", "T258", "T260")
        y0_group_list[[2]] <- c("T235", "T236", "T237", "T247", "T257")
      },
      pooled = {
        y0_group_list[[1]] <- data$male
      }
    )
  }
}

```

```

fit_tbl[ curr_row, ]$x0_group_list[[1]] <- x0_group_list

fit_tbl[ curr_row, ]$y0_group_list[[1]] <- y0_group_list

## Convert lists to a vector of concatenated strings
## This will simplify mapping male to an x0/y0 index
x0_group <-lapply(x0_group_list, paste, collapse = " ") %>% unlist()
y0_group <-lapply(y0_group_list, paste, collapse = " ") %>% unlist()

x0_index <- sapply(as.character(data$male), function(x) str_which(x0_group, x))
y0_index <- sapply(as.character(data$male), function(x) str_which(y0_group, x))

fit <- stan(file = stan_file,
            model_name = desc,
            data=list(x = temp,
                     y = motif_count,
                     N = N,
                     X = length(x0_group),
                     Y = length(y0_group),
                     NB = 1,
                     xx = x0_index,
                     yy = y0_index,
                     nbb = rep(1,N),
                     xmax = tmax,
                     x0_min = t0min,
                     x0_max = t0max,
                     y_xmax = 0,
                     y0_min = 10,
                     sd_y0_prior = 200,
                     alpha_theta_prior = 10,
                     ##tp = tp,
                     ## max threshold value.
                     ## having it too close to xmax *sometimes* leads to sampling
                     ## near xmax, but with lower lp and very high E13) b0 values
                     y_xmax = 0),
            cores = n_cores,
            chains = n_chains,
            iter = iter,
            warmup = floor(iter/2),
            verbose = TRUE)

fit_tbl[ curr_row, ]$fit <- list(fit)

}
}

```

```

## [1] "qpoi: separate, separate"
##
## TRANSLATING MODEL 'qpoi: separate, separate' FROM Stan CODE TO C++ CODE NOW.
##
## CHECKING DATA AND PREPROCESSING FOR MODEL 'anon_model' NOW.
##
## COMPILING MODEL 'anon_model' NOW.

```

```

##
## STARTING SAMPLER FOR MODEL 'anon_model' NOW.
## [1] "qpoi: separate, grouping_1"
##
## TRANSLATING MODEL 'qpoi: separate, grouping_1' FROM Stan CODE TO C++ CODE NOW.
##
## CHECKING DATA AND PREPROCESSING FOR MODEL 'anon_model' NOW.
##
## COMPILING MODEL 'anon_model' NOW.
##
## STARTING SAMPLER FOR MODEL 'anon_model' NOW.
## [1] "qpoi: separate, pooled"
##
## TRANSLATING MODEL 'qpoi: separate, pooled' FROM Stan CODE TO C++ CODE NOW.
##
## CHECKING DATA AND PREPROCESSING FOR MODEL 'anon_model' NOW.
##
## COMPILING MODEL 'anon_model' NOW.
##
## STARTING SAMPLER FOR MODEL 'anon_model' NOW.
## [1] "qpoi: grouping_1, separate"
##
## TRANSLATING MODEL 'qpoi: grouping_1, separate' FROM Stan CODE TO C++ CODE NOW.
##
## CHECKING DATA AND PREPROCESSING FOR MODEL 'anon_model' NOW.
##
## COMPILING MODEL 'anon_model' NOW.
##
## STARTING SAMPLER FOR MODEL 'anon_model' NOW.
## [1] "qpoi: grouping_1, grouping_1"
##
## TRANSLATING MODEL 'qpoi: grouping_1, grouping_1' FROM Stan CODE TO C++ CODE NOW.
##
## CHECKING DATA AND PREPROCESSING FOR MODEL 'anon_model' NOW.
##
## COMPILING MODEL 'anon_model' NOW.
##
## STARTING SAMPLER FOR MODEL 'anon_model' NOW.
## [1] "qpoi: grouping_1, pooled"
##
## TRANSLATING MODEL 'qpoi: grouping_1, pooled' FROM Stan CODE TO C++ CODE NOW.
##
## CHECKING DATA AND PREPROCESSING FOR MODEL 'anon_model' NOW.
##
## COMPILING MODEL 'anon_model' NOW.
##
## STARTING SAMPLER FOR MODEL 'anon_model' NOW.
## [1] "qpoi: pooled, separate"
##
## TRANSLATING MODEL 'qpoi: pooled, separate' FROM Stan CODE TO C++ CODE NOW.
##
## CHECKING DATA AND PREPROCESSING FOR MODEL 'anon_model' NOW.
##
## COMPILING MODEL 'anon_model' NOW.

```

```
##
## STARTING SAMPLER FOR MODEL 'anon_model' NOW.
## [1] "qpoi: pooled, grouping_1"
##
## TRANSLATING MODEL 'qpoi: pooled, grouping_1' FROM Stan CODE TO C++ CODE NOW.
##
## CHECKING DATA AND PREPROCESSING FOR MODEL 'anon_model' NOW.
##
## COMPILING MODEL 'anon_model' NOW.
##
## STARTING SAMPLER FOR MODEL 'anon_model' NOW.
## [1] "qpoi: pooled, pooled"
##
## TRANSLATING MODEL 'qpoi: pooled, pooled' FROM Stan CODE TO C++ CODE NOW.
##
## CHECKING DATA AND PREPROCESSING FOR MODEL 'anon_model' NOW.
##
## COMPILING MODEL 'anon_model' NOW.
##
## STARTING SAMPLER FOR MODEL 'anon_model' NOW.

## save(file = "fit_tbl.Rda", fit_tbl)
qpoisson_fit_tbl <- fit_tbl
```

- Models fit without any warnings.

Negative Binomial

```
iter <- 15000
tmax <- 46
t0max <- tmax - 0.5;
t0min <- 20;
## values to use for model predictions
tp = seq(25, tmax, length.out = 100)
n_cores <- 4
n_chains <- n_cores

##y0_grouping <- map_int(data$male, ~ if_else(. %in% y0_group[[1]], 1, 2))
model <- "nb"
stan_file <- "two.piece_nb_1.0.stan"
## For debugging
##cmodel <- cmdstan_model(stan_file = stan_file)

stan_model(file = stan_file,
           verbose = TRUE)

##
## TRANSLATING MODEL '' FROM Stan CODE TO C++ CODE NOW.
```



```

## Define groups

flags <- c("separate", "grouping_1", "pooled")
flags_x <- flags
flags_y <- flags
fit_tbl <- crossing(model = model,
                    x0 = flags_x, y0 = flags_y,
                    desc = "NA_character",
                    y0_group_list = list(NA),
                    x0_group_list = list(NA),
                    fit = list(NA),
                    llik = list(NA),
                    r_eff = list(NA),
                    loo = list(NA)
                    )

for(x_flag in flags_x) {
  for(y_flag in flags_y) {

    desc <- paste0(model, ":", x_flag, ":", y_flag)
    curr_row <- which(fit_tbl$x0 == x_flag & fit_tbl$y0 == y_flag)

    fit_tbl[ curr_row, ]$desc <- desc
    print(desc)

    x0_group_list <- list()
    y0_group_list <- list()

    switch(x_flag,
           separate = {
             x0_group_list <- data$male %>% unique() %>% as.list()
           },
           grouping_1 = {
             ## set up groupings based on 2022-12-20 analysis
             ## Using male ID's instead index to make code more robust
             x0_group_list[[1]] <- c("T235", "T237", "T244", "T247", "T257", "T260")
             x0_group_list[[2]] <- c("T234", "T236", "T243", "T246", "T258")
           },
           pooled = {
             x0_group_list[[1]] <- data$male
           }
    )

    switch(y_flag,
           separate = {
             y0_group_list <- data$male %>% unique() %>% as.list()
           },
           grouping_1 = {
             ## set up groupings based on 2022-12-20 analysis
             ## Using male ID's instead index to make code more robust
             y0_group_list[[1]] <- c("T234", "T243", "T244", "T246", "T258", "T260")
           }
    )
  }
}

```

```

        y0_group_list[[2]] <- c("T235", "T236", "T237", "T247", "T257")
      },
      pooled = {
        y0_group_list[[1]] <- data$male
      }
    )

    fit_tbl[ curr_row, ]$x0_group_list[[1]] <- x0_group_list

    fit_tbl[ curr_row, ]$y0_group_list[[1]] <- y0_group_list

    ## Convert lists to a vector of concatenated strings
    ## This will simplify mapping male to an x0/y0 index
    x0_group <- lapply(x0_group_list, paste, collapse = " ") %>% unlist()
    y0_group <- lapply(y0_group_list, paste, collapse = " ") %>% unlist()

    x0_index <- sapply(as.character(data$male), function(x) str_which(x0_group, x))
    y0_index <- sapply(as.character(data$male), function(x) str_which(y0_group, x))

    fit <- stan(file = stan_file,
               model_name = desc,
               data=list(x = temp,
                        y = motif_count,
                        N = N,
                        X = length(x0_group),
                        Y = length(y0_group),
                        NB = 1,
                        xx = x0_index,
                        yy = y0_index,
                        nbb = rep(1,N),
                        xmax = tmax,
                        x0_min = t0min,
                        x0_max = t0max,
                        y_xmax = 0,
                        y0_min = 10,
                        sd_y0_prior = 200,
                        alpha_theta_prior = 10,
                        alpha_phi_prior = 10,
                        ##tp = tp,
                        ## max threshold value.
                        ## having it too close to xmax *sometimes* leads to sampling
                        ## near xmax, but with lower lp and very high E13) b0 values
                        y_xmax = 0),
               cores = n_cores,
               chains = n_chains,
               iter = iter,
               warmup = floor(iter/2),
               verbose = FALSE)

    fit_tbl[ curr_row, ]$fit <- list(fit)
  }
}

```

```
## [1] "nb: separate, separate"
## [1] "nb: separate, grouping_1"
## [1] "nb: separate, pooled"
## [1] "nb: grouping_1, separate"
## [1] "nb: grouping_1, grouping_1"
## [1] "nb: grouping_1, pooled"
## [1] "nb: pooled, separate"
## [1] "nb: pooled, grouping_1"
## [1] "nb: pooled, pooled"
```

```
nb_fit_tbl <- fit_tbl

## save(file = "fit_tbl.Rda", fit_tbl)
```

Model Comparison

LOO Analysis

```
fit_tbl <- bind_rows(qpoisson_fit_tbl, nb_fit_tbl, .id = NULL)

for(curr_row in 1:length(fit_tbl$fit)) {

  desc <- fit_tbl[[curr_row, "desc"]]
  fit <- fit_tbl[[curr_row, "fit"]][[1]]
  print(paste0("Model ", curr_row, ": ", desc))

  # loo analysis based on: http://mc-stan.org/loo/articles/loo2-with-rstan.html
  #
  # Extract pointwise log-likelihood
  # using merge_chains=FALSE returns an array, which is easier to
  # use with relative_eff()
  llik <- extract_log_lik(fit, merge_chains = FALSE)
  fit_tbl[[curr_row, "llik"]] <- list(llik)

  # as of loo v2.0.0 we can optionally provide relative effective sample sizes
  # when calling loo, which allows for better estimates of the PSIS effective
  # sample sizes and Monte Carlo error
  r_eff <- relative_eff(exp(llik), cores = n_cores)
  fit_tbl[[curr_row, "r_eff"]] <- list(r_eff)

  # preferably use more than 2 cores (as many cores as possible)
  # will use value of 'mc.cores' option if cores is not specified
  loo <- loo(llik, r_eff = r_eff,
             cores = n_cores,
             save_psis = TRUE,
             moment_match = TRUE)
  fit_tbl[[curr_row, "loo"]] <- list(loo)
  print(loo)
}
```

```

## [1] "Model 1: qpoi: grouping_1, grouping_1"
##
## Computed from 30000 by 38 log-likelihood matrix
##
##           Estimate   SE
## elpd_loo  -276.8 34.9
## p_loo      21.6  7.6
## looic      553.5 69.8
## -----
## Monte Carlo SE of elpd_loo is NA.
##
## Pareto k diagnostic values:
##           Count Pct.    Min. n_eff
## (-Inf, 0.5] (good)    33   86.8%   2810
## (0.5, 0.7] (ok)       3    7.9%   292
## (0.7, 1] (bad)        2    5.3%    22
## (1, Inf) (very bad)  0    0.0%   <NA>
## See help('pareto-k-diagnostic') for details.
## [1] "Model 2: qpoi: grouping_1, pooled"
##
## Computed from 30000 by 38 log-likelihood matrix
##
##           Estimate   SE
## elpd_loo  -298.0 34.1
## p_loo      16.3  5.2
## looic      595.9 68.2
## -----
## Monte Carlo SE of elpd_loo is NA.
##
## Pareto k diagnostic values:
##           Count Pct.    Min. n_eff
## (-Inf, 0.5] (good)    35   92.1%   1109
## (0.5, 0.7] (ok)       1    2.6%  11233
## (0.7, 1] (bad)        1    2.6%   113
## (1, Inf) (very bad)  1    2.6%    22
## See help('pareto-k-diagnostic') for details.
## [1] "Model 3: qpoi: grouping_1, separate"
##
## Computed from 30000 by 38 log-likelihood matrix
##
##           Estimate   SE
## elpd_loo  -291.6 48.7
## p_loo      64.4 24.9
## looic      583.1 97.3
## -----
## Monte Carlo SE of elpd_loo is NA.
##
## Pareto k diagnostic values:
##           Count Pct.    Min. n_eff
## (-Inf, 0.5] (good)    22   57.9%  3189
## (0.5, 0.7] (ok)       8   21.1%   904
## (0.7, 1] (bad)        3    7.9%    35
## (1, Inf) (very bad)  5   13.2%     3
## See help('pareto-k-diagnostic') for details.

```

```

## [1] "Model 4: qpoi: pooled, grouping_1"
##
## Computed from 30000 by 38 log-likelihood matrix
##
##           Estimate   SE
## elpd_loo  -283.7 36.8
## p_loo      28.0  9.6
## looic      567.4 73.6
## -----
## Monte Carlo SE of elpd_loo is NA.
##
## Pareto k diagnostic values:
##           Count Pct.   Min. n_eff
## (-Inf, 0.5] (good)    33   86.8%   274
## (0.5, 0.7] (ok)       3    7.9%   160
## (0.7, 1] (bad)        1    2.6%    26
## (1, Inf) (very bad)   1    2.6%    59
## See help('pareto-k-diagnostic') for details.
## [1] "Model 5: qpoi: pooled, pooled"
##
## Computed from 30000 by 38 log-likelihood matrix
##
##           Estimate   SE
## elpd_loo  -305.5 36.0
## p_loo      20.3  6.4
## looic      611.0 72.0
## -----
## Monte Carlo SE of elpd_loo is NA.
##
## Pareto k diagnostic values:
##           Count Pct.   Min. n_eff
## (-Inf, 0.5] (good)    36   94.7%   717
## (0.5, 0.7] (ok)       1    2.6%   469
## (0.7, 1] (bad)        1    2.6%    30
## (1, Inf) (very bad)   0    0.0%   <NA>
## See help('pareto-k-diagnostic') for details.
## [1] "Model 6: qpoi: pooled, separate"
##
## Computed from 30000 by 38 log-likelihood matrix
##
##           Estimate   SE
## elpd_loo  -298.9 45.9
## p_loo      63.0 22.8
## looic      597.8 91.9
## -----
## Monte Carlo SE of elpd_loo is NA.
##
## Pareto k diagnostic values:
##           Count Pct.   Min. n_eff
## (-Inf, 0.5] (good)    25   65.8%   323
## (0.5, 0.7] (ok)       6   15.8%    48
## (0.7, 1] (bad)        4   10.5%    19
## (1, Inf) (very bad)   3    7.9%     1
## See help('pareto-k-diagnostic') for details.

```

```

## [1] "Model 7: qpoi: separate, grouping_1"
##
## Computed from 30000 by 38 log-likelihood matrix
##
##           Estimate   SE
## elpd_loo  -285.1 40.4
## p_loo      42.1 15.7
## looic      570.2 80.7
## -----
## Monte Carlo SE of elpd_loo is NA.
##
## Pareto k diagnostic values:
##           Count Pct.   Min. n_eff
## (-Inf, 0.5] (good)    31   81.6%  1885
## (0.5, 0.7] (ok)       3    7.9%   388
## (0.7, 1] (bad)        2    5.3%    52
## (1, Inf) (very bad)  2    5.3%    13
## See help('pareto-k-diagnostic') for details.
## [1] "Model 8: qpoi: separate, pooled"
##
## Computed from 30000 by 38 log-likelihood matrix
##
##           Estimate   SE
## elpd_loo  -302.0 39.0
## p_loo      32.4 10.2
## looic      604.1 78.0
## -----
## Monte Carlo SE of elpd_loo is NA.
##
## Pareto k diagnostic values:
##           Count Pct.   Min. n_eff
## (-Inf, 0.5] (good)    23   60.5%  1146
## (0.5, 0.7] (ok)       5   13.2%  3817
## (0.7, 1] (bad)        5   13.2%    67
## (1, Inf) (very bad)  5   13.2%     2
## See help('pareto-k-diagnostic') for details.
## [1] "Model 9: qpoi: separate, separate"
##
## Computed from 30000 by 38 log-likelihood matrix
##
##           Estimate   SE
## elpd_loo  -297.4 49.7
## p_loo      69.1 25.2
## looic      594.8 99.4
## -----
## Monte Carlo SE of elpd_loo is NA.
##
## Pareto k diagnostic values:
##           Count Pct.   Min. n_eff
## (-Inf, 0.5] (good)    20   52.6%  1626
## (0.5, 0.7] (ok)      10   26.3%   346
## (0.7, 1] (bad)       4   10.5%    32
## (1, Inf) (very bad)  4   10.5%     4
## See help('pareto-k-diagnostic') for details.

```

```

## [1] "Model 10: nb: grouping_1, grouping_1"
##
## Computed from 30000 by 38 log-likelihood matrix
##
##           Estimate  SE
## elpd_loo   -215.3 4.9
## p_loo       2.0 0.9
## looic       430.6 9.7
## -----
## Monte Carlo SE of elpd_loo is 0.0.
##
## All Pareto k estimates are good (k < 0.5).
## See help('pareto-k-diagnostic') for details.
## [1] "Model 11: nb: grouping_1, pooled"
##
## Computed from 30000 by 38 log-likelihood matrix
##
##           Estimate  SE
## elpd_loo   -219.0 4.7
## p_loo       1.7 0.5
## looic       438.1 9.5
## -----
## Monte Carlo SE of elpd_loo is 0.0.
##
## All Pareto k estimates are good (k < 0.5).
## See help('pareto-k-diagnostic') for details.
## [1] "Model 12: nb: grouping_1, separate"
##
## Computed from 30000 by 38 log-likelihood matrix
##
##           Estimate  SE
## elpd_loo   -219.1 4.0
## p_loo       4.3 1.1
## looic       438.2 8.0
## -----
## Monte Carlo SE of elpd_loo is NA.
##
## Pareto k diagnostic values:
##           Count Pct.   Min. n_eff
## (-Inf, 0.5] (good)   33   86.8%   7133
## (0.5, 0.7]  (ok)     4   10.5%   2175
## (0.7, 1]    (bad)     1    2.6%   2960
## (1, Inf)    (very bad) 0    0.0%   <NA>
## See help('pareto-k-diagnostic') for details.
## [1] "Model 13: nb: pooled, grouping_1"
##
## Computed from 30000 by 38 log-likelihood matrix
##
##           Estimate  SE
## elpd_loo   -215.5 5.1
## p_loo       1.9 0.9
## looic       430.9 10.1
## -----
## Monte Carlo SE of elpd_loo is 0.0.

```

```

##
## All Pareto k estimates are good (k < 0.5).
## See help('pareto-k-diagnostic') for details.
## [1] "Model 14: nb: pooled, pooled"
##
## Computed from 30000 by 38 log-likelihood matrix
##
##           Estimate SE
## elpd_loo   -218.7 4.7
## p_loo        1.3 0.4
## looic       437.4 9.4
## -----
## Monte Carlo SE of elpd_loo is 0.0.
##
## All Pareto k estimates are good (k < 0.5).
## See help('pareto-k-diagnostic') for details.
## [1] "Model 15: nb: pooled, separate"
##
## Computed from 30000 by 38 log-likelihood matrix
##
##           Estimate SE
## elpd_loo   -219.7 4.2
## p_loo        4.5 1.2
## looic       439.5 8.3
## -----
## Monte Carlo SE of elpd_loo is NA.
##
## Pareto k diagnostic values:
##           Count Pct.    Min. n_eff
## (-Inf, 0.5] (good)    34   89.5%   7574
## (0.5, 0.7]  (ok)      2    5.3%   3068
## (0.7, 1]    (bad)      2    5.3%    581
## (1, Inf)    (very bad) 0    0.0%    <NA>
## See help('pareto-k-diagnostic') for details.
## [1] "Model 16: nb: separate, grouping_1"
##
## Computed from 30000 by 38 log-likelihood matrix
##
##           Estimate SE
## elpd_loo   -215.6 4.8
## p_loo        2.3 1.0
## looic       431.1 9.6
## -----
## Monte Carlo SE of elpd_loo is NA.
##
## Pareto k diagnostic values:
##           Count Pct.    Min. n_eff
## (-Inf, 0.5] (good)    37   97.4%  17849
## (0.5, 0.7]  (ok)      0    0.0%    <NA>
## (0.7, 1]    (bad)      1    2.6%    915
## (1, Inf)    (very bad) 0    0.0%    <NA>
## See help('pareto-k-diagnostic') for details.
## [1] "Model 17: nb: separate, pooled"
##

```



```
## Computed from 30000 by 38 log-likelihood matrix
##
##           Estimate SE
## elpd_loo   -218.7 4.6
## p_loo       1.9 0.6
## looic       437.3 9.2
## -----
## Monte Carlo SE of elpd_loo is 0.0.
##
## All Pareto k estimates are good (k < 0.5).
## See help('pareto-k-diagnostic') for details.
## [1] "Model 18: nb: separate, separate"
##
## Computed from 30000 by 38 log-likelihood matrix
##
##           Estimate SE
## elpd_loo   -219.4 3.9
## p_loo       4.3 1.1
## looic       438.9 7.8
## -----
## Monte Carlo SE of elpd_loo is NA.
##
## Pareto k diagnostic values:
##           Count Pct.   Min. n_eff
## (-Inf, 0.5] (good)    33   86.8%   8535
## (0.5, 0.7]  (ok)      4   10.5%   3318
## (0.7, 1]    (bad)      1    2.6%   2695
## (1, Inf)    (very bad) 0    0.0%   <NA>
## See help('pareto-k-diagnostic') for details.
```

```
comp <- loo_compare(fit_tbl$loo)
index <- comp %>% rownames() %>% sub(pattern = "model", x= ., "") %>% as.integer()
desc <- fit_tbl$desc[index]
rownames(comp) <- desc

#loo_tbl<- bind_cols( desc = desc, index = index, comp) %>% tibble() %>% arrange(index)

print(comp)
```

```
##
##           elpd_diff se_diff
## nb: grouping_1, grouping_1    0.0    0.0
## nb: pooled, grouping_1      -0.2    0.4
## nb: separate, grouping_1     -0.3    0.2
## nb: separate, pooled        -3.4    1.6
## nb: pooled, pooled          -3.4    1.7
## nb: grouping_1, pooled       -3.7    1.6
## nb: grouping_1, separate     -3.8    1.2
## nb: separate, separate      -4.1    1.3
## nb: pooled, separate         -4.4    1.0
## qpoi: grouping_1, grouping_1 -61.4   33.5
## qpoi: pooled, grouping_1     -68.4   35.1
## qpoi: separate, grouping_1   -69.8   38.8
## qpoi: grouping_1, separate   -76.3   47.8
## qpoi: separate, separate     -82.1   48.7
```

```
## qpoi: grouping_1, pooled      -82.7      32.2
## qpoi: pooled, separate       -83.6      44.8
## qpoi: separate, pooled       -86.7      37.6
## qpoi: pooled, pooled         -90.2      34.4
```

Plot Results

```
for(curr_row in 1:length(fit_tbl$fit)) {

  desc <- fit_tbl[[curr_row, "desc"]]
  fit <- fit_tbl[[curr_row, "fit"]]

  x0_group_list <- fit_tbl[[curr_row, "x0_group_list"]][[1]]
  y0_group_list <- fit_tbl[[curr_row, "y0_group_list"]][[1]]

}

pars <- c("x0", "y0", "theta")
pars_full <- c(pars, "lp_")

print(desc)
print(fit, pars = pars)

#traceplot(model, pars = pars, inc_warmup = FALSE)
#plot(model, pars = pars) #, ggtitle(title))

pairs(model, pars = pars_full)

## Plot parameter estimate summaries
tmp_plot <- list()
for(par in pars) {
  tmp_plot[[par]] <- stan_plot(model, pars = par)
}
gt <- arrangeGrob(grobs = tmp_plot)
as_ggplot(gt)

}
```

```
## Error: <text>:32:5: unexpected '}'
## 31:
## 32:   }
##      ^
```