

# KOALA: Estimating coalition probabilities in multi-party electoral systems

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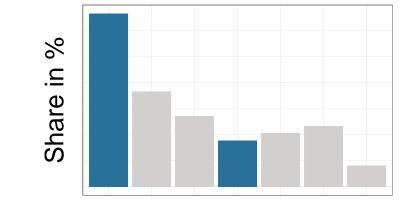
What do we propose?

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# Election poll-based reporting What's the status quo? Proposed type of reporting:

#### Typical election poll reporting:



- is based on observed mean voter shares
- sets the focus on individual party achievements
- imparts sample uncertainty only insufficiently

Typical headline:

Motivation

"The two parties jointly obtain 48% of all votes."

#### Real-world Example

Reporting on Union and FDP to jointly obtain a majority before the German federal election 2013

Last pre-election opinion poll: Source: Forsa, 20.09.2013

Union SPD Greens FDP The Left AfD Others **40%** 26% 10% **5%** 

After redistribution of party votes <5% (i.e. the minimum hurdle to pass into German parliament) Union-FDP jointly obtain exactly 50%.

Media headline:

"Union-FDP loses its majority"

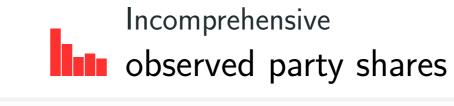
Source: FAZ.net (2017). Umfrage zur Bundestagswahl: Schwarz-Gelb verliert die Mehrheit.http://archive.is/SuXVt. Accessed 26 April 2018

- focuses on specific events (e.g. potential majorities)
- naturally imparts sample uncertainty using probabilities
- prevents misunderstandings by using this holistic approach

Proposed headline:

"The two parties have a probability of 32% to jointly obtain a majority."

#### We aim at **shifting the focus** from





Uncertainty-based event probabilities

Flaws of this type of reporting:

- Misleading conclusions are drawn A mean share of 50% only means that it's slightly more probable that a majority is missed
- Sample uncertainty is ignored E.g., with a mean voter share of 5%, FDP will only enter the parliament with  $\sim 50\%$
- Redistribution of votes is ignored FAZ.net bases the conclusion on the observed voter share and not on the redistributed 50% share

### Foundations of KOALA-based reporting:

- Use event **probabilities** instead of voter shares Probabilities comprise sample uncertainty in a natural way and are less at risk to be misinterpreted
- Use event probabilities instead of voter shares Focusing on the main events allows the reader to easily grasp the big picture

KOALA headline:

"Union-FDP gains seat majority with 26%, FDP passes into parliament with 51%\*" If the election was held today

## **Event probability estimation**

# **Estimating event probabilities**

**Multinomial-Dirichlet model** for the true party shares  $\theta_j$  (Gelman et al., 2013):

$$(\theta_1,\ldots,\theta_k)^T \sim Dirichlet(\alpha_1,\ldots,\alpha_k), \text{ with } \alpha_1=\ldots=\alpha_k=\frac{1}{2}$$

- Given one survey, we obtain a **Dirichlet posterior** with  $\alpha_j = x_j + \frac{1}{2}$  for each party jand its observed vote counts  $x_i$ .
- Using Monte Carlo simulations of election outcomes, we obtain obtain specific event probabilities by taking their relative frequency of occurence.

#### **Pooling multiple surveys**

We pool the most recent survey per pollilng agency within the past 14 days to reduce sample uncertainty. We adjust the uncertainty of the multinomially distributed summed number of votes per party by using an effective sample size (Hanley et al., 2003).

As polls from different polling agencies are correlated, party-specific correlations were estimated based on 20 surveys of polling agencies Emnid and Forsa, using

$$Cov(X_{Aj}, X_{Bj}) = \frac{1}{2} \cdot \left(Var(X_{Aj}) + Var(X_{Bj}) - Var(X_{Aj} - X_{Bj})\right),$$

with

- $X_{S_i}$  the observed voter number of party j in survey S,
- $Var(X_{Aj})$ ,  $Var(X_{Bj})$  the theoretical variances of binomial distributions,
- $Var(X_{Aj} X_{Bj})$  estimated from the party share differences.

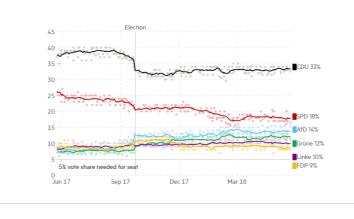
For simplicity, we set the correlation to a fixed value of 0.5.

The effective sample size  $n_{\rm eff}$  is then defined as the ratio between the estimated variance for the pooled sample and the theoretical variance for a sample of size one:

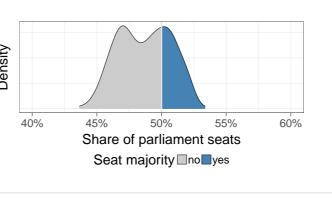
$$n_{\rm eff} = \frac{Var(\text{pooled})}{Var(\text{sample of size one})}$$

## **Visualization & Implementation**

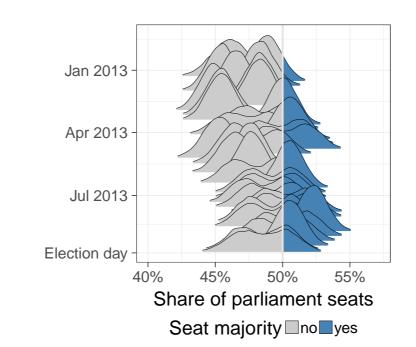
#### **Selected visualizations**



Adjusted line plots are used to visualize the pooled voter shares are visualized, showing both the mean share and the corresponding uncertainty



**Density plots** are used to depict one simulated seat distribution



Ridgeline plots (Wilke, 2017) are used to depict the simulated seat distribution development over time

## **Implementation**





### Major building blocks

- The accompanying R package coalitions
- An automated fetch-and-update process for the website
- An automated bot tweeting new results

#### References

Bender, A. and Bauer, A. (2018). coalitions: Coalition probabilities in multi-party democracies. Journal of Open Source Software, 3(23), 606, https://doi.org/10.21105/joss.00606. Unser AStA-Paper no ois Technical Report?

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