

KOALA: Estimating coalition probabilities in multi-party electoral systems

Alexander Bauer¹, Andreas Bender¹, André Klima¹, Helmut Küchenhoff¹

¹ Statistical Consulting Unit StaBLab, Department of Statistics, LMU Munich, Germany

Alexander.Bauer@stat.uni-muenchen.de

Motivation Election poll-based reporting What's the status quo? What do we propose? Typical election poll reporting: Good reporting: is based on observed mean voter shares should impart findings in an easily graspable way sets the focus on individual party achievements should prevent potential misunderstandings imparts sample uncertainty only insufficiently should focus on the most relevant topics We aim at **shifting the focus** from Example Incomprehensive Uncertainty-based Reporting on Union and FDP to jointly obtain a majority before the German federal election 2013 observed party shares event probabilities Last pre-election opinion poll: Source: Forsa, 20.09.2013 Flaws of this type of reporting: Foundations of KOALA-based reporting: Misleading conclusions are drawn • Use event **probabilities** instead of voter shares Union SPD Greens FDP The Left AfD Others A mean share of 50% only means that it's slightly Probabilities comprise sample uncertainty in a natural way **40%** 26% 10% **5%** 9% 4% 6% more probable that a majority is missed and are less at risk to be misinterpreted Sample uncertainty is ignored Use event probabilities instead of voter shares After redistribution of party votes <5% E.g., with a mean voter share of 5%, FDP will only Focusing on the main events allows the reader to easily (i.e. the minimum hurdle to pass into German parliament) enter the parliament with $\sim 50\%$ grasp the big picture Union-FDP jointly obtain exactly 50%. Redistribution of votes is ignored FAZ.net bases the conclusion on the observed voter KOALA headline: Media headline: share and not on the redistributed 50% share "Union-FDP gains seat majority with 26%, "Union-FDP loses its majority" FDP passes into parliament with 51%*" Source: FAZ.net (2017). Umfrage zur Bundestagswahl: Schwarz-Gelb verliert die Mehrheit.http://archive.is/SuXVt. Accessed 26 April 2018. * If the election was held today

1 Event probability estimation

We use a Multinomial-Dirichlet model for the true party shares θ_j (Gelman et al., 2013):

$$(\theta_1,\ldots,\theta_k)^T \sim Dirichlet(\alpha_1,\ldots,\alpha_k), \text{ with } \alpha_1=\ldots=\alpha_k=\frac{1}{2}$$

Given one survey, the posterior also is a Dirichlet distribution with $\alpha_j = x_j + \frac{1}{2}$ for each party j and its observed vote counts x_j .

Using Monte Carlo simulations of election outcomes, we obtain obtain specific event probabilities by taking their relative frequency of occurence.

Pooling is used to summarize multiple polls to reduce sample uncertainty:

- We pool the most recent survey per polling agency within the past 14 days
- The summed number of votes per party are also multinomially distributed
- But: Polls from different polling agencies are correlated

Hence: We adjust the distribution by using an effective sample size (Hanley et al., 2003): Party-specific correlations were estimated based on 20 surveys of polling agencies Emnid and Forsa, using

$$Cov(X_{Aj}, X_{Bj}) = \frac{1}{2} \cdot \left(Var(X_{Aj}) + Var(X_{Bj}) - Var(X_{Aj} - X_{Bj})\right),$$

with

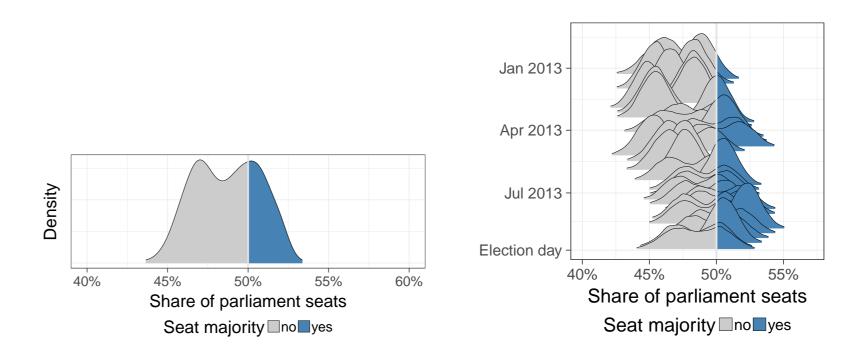
- $Var(X_{Ai})$, $Var(X_{Bi})$ the theoretical variances of binomial distributions,
- $Var(X_{Aj} X_{Bj})$ estimated from the party share differences.

For simplicity, we set the correlation to a fixed value of 0.5. The effective sample size n_{eff} is then defined as the ratio between the estimated variance for the pooled sample and the theoretical variance for a sample of size one:

$$n_{\rm eff} = \frac{Var(\text{pooled})}{Var(\text{sample of size one})}$$

2 Visualization

To visualize the development of such probabilities together with the underlying uncertainty for a specific coalition we use **ridgeline plots** (Wilke, 2017) for the simulated seat distributions:



Looking at the probabilities based on the last opinion poll before the German election 2013, the posterior distribution is bimodal, based on the distinction whether FDP and/or AfD pass the 5% hurdle. The resulting probability for a Union-FDP majority is 27.2%, based on 10,000 simulations.

3 Implementation and results communication

Results for selected elections are presented on koala.stat.uni-muenchen.de

The implementation is based on several points:

- Our approach is implemented in the R package coalitions
- The website is shiny-based
- The website update approach is automated
- Automatic tweets are sent in the case of new results
- For sharing our results we automatically export them to Google Sheets



Shiny







References

Bender, A. and Bauer, A. (2018). coalitions: Coalition probabilities in multi-party democracies. *Journal of Open Source Software*, **3(23)**, 606, https://doi.org/10.21105/joss.00606. Unser AStA-Paper no ois Technical Report?

Gelman, A. et al. (2013). Bayesian Data Analysis, 3rd edition. Boca Raton, FL: CRC press.

Hanley, J. A. et al. (2003). Statistical analysis of correlated data using gen- eralized estimating equations: an orientation. *American journal of epidemiology*, **157(4)**, 364–375.

Wilke C.O. (2017). ggridges: Ridgeline Plots in 'ggplot2'. R package version 0.4.1. URL https://CRAN.R-project.org/package=ggridges