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EE5609 Assignment 3

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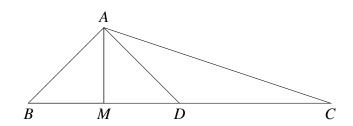
1 Problem

AD is the median of a $\triangle ABC$ and $AM \perp BC$. prove that

$$AB^2 = AD^2 - BC.DM + (\frac{BC}{2})^2$$

2 Solution

In a right angle triangle, square of the hypotenuse is equal to the sum of the squares of the other two sides. Also, a medain devides the sides into two equal halves.



from the above figure

$$||B - D|| = ||D - C|| \tag{2.0.1}$$

$$AM \perp BC$$
 (2.0.2)

then as per the pythagoras theorem

$$||A - B||^2 = ||B - M||^2 + ||A - M||^2$$
 (2.0.3)

$$= ||B - M||^2 + ||A - D||^2 - ||M - D||^2$$
 (2.0.4)

$$= (||B - D|| - ||M - D||)^2 + ||A - D||^2 - ||M - D||^2$$
(2.0.5)

$$= ||B - D||^2 + ||M - D||^2 - 2||B - D|| ||M - D|| + ||A - D||^2 - ||M - D||^2$$
(2.0.6)

$$= ||B - D||^2 - 2||B - D|| ||M - D|| + ||A - D||^2$$
(2.0.7)

$$= ||A - D||^2 + \left\| \frac{B - C}{2} \right\|^2 - 2||B - D|| ||M - D||$$
(2.0.8)

$$= ||A - D||^2 + \left\| \frac{B - C}{2} \right\|^2 - 2 \left\| \frac{B - C}{2} \right\| ||M - D||$$
(2.0.9)

$$= ||A - D||^2 + \left| \left| \frac{B - C}{2} \right| \right|^2 - ||B - C|| \, ||M - D||$$
(2.0.10)

Hence proved.