

ASSIGNMENT 2

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1 PROBLEM

If A is a square matrix such that $A^2 = A$, then $(I + A)^3 - 7A$ is equal to

- (A) A
- (B) $I - A$
- (C) I
- (D) $3A$

2 SOLUTION

$$\begin{aligned}
 (I + A)^3 - 7A &= I^3 + A^3 + 3I^2A + 3IA^2 - 7A \\
 &= I + A^2A + 3IA + 3IA - 7A \\
 &= I + AA + 6IA - 7A \\
 &= I + A^2 + 6A - 7A \\
 &= I + A + 6A - 7A \\
 &= I + 7A - 7A \\
 &= I
 \end{aligned}$$

3 ANSWER

$(I + A)^3 = I$
 option C is the valid answer