

NAME : KRUNAL RANK

Roll No: U18C0081

CLASS: B TECH 3<sup>RD</sup> YEAR,

COMPUTER ENGINEERING.

AIML  
Tutorial 11

Ans 1:

1.  $\{p(f(a), g(y)) \text{ and } p(x, x)\}$

$$\psi_1 = p(f(a), g(y))$$

$$\psi_2 = p(x, x)$$

$$\theta = \{f(a) / x\}$$

$$S1 \Rightarrow \psi_1 = p(f(a), g(y))$$

$$\psi_2 = p(f(a), f(a))$$

$$\theta = \{f(a) / g(y)\}, \text{Unification failed}$$

2:  $\psi_1 = p(b, x, f(g(z)))$

$$\psi_2 = p(z, f(y), f(y))$$

$$\theta = \{b / z\}$$

$$S1 \Rightarrow \psi_1 = p(b, x, f(g(z))) \quad \psi_2 = p(b, f(y), f(y))$$

$$\theta = \{f(y) / z\}, \{f(y) / x\}$$

$$S2 \Rightarrow \psi_1 = p(b, f(y), f(g(z))) \quad \psi_2 = p(b, f(y), f(y))$$

$$\theta = \{g(b) / y\}$$

$$S3 \Rightarrow p(b, f(g(b)), f(g(b))) ; p(b, f(g(b)), f(g(b)))$$

$$\text{Unifier} = \{b / z, f(y) / x, g(b) / y\}$$



$$3. \{p(x, x), p(z, f(z))\}$$

$$\theta = \{x/z\}$$

$$S_1 \Rightarrow \{p(z, z), p(z, f(z))\}$$

$$\theta = \{f(z)/z\}, \text{Unification failed.}$$

$$4. S_0 = p_1(\text{prime}(11)), p_2(\text{prime}(4))$$

$$\theta = \{11/y\}$$

$$S_1 = p_1(\text{prime}(11)), p_2(\text{prime}(11))$$

$$\text{Hence, Unifier} = \{11/y\}$$

$$5. S_0 = p(a, g(x, y), f(y))$$

$$p(a, g(f(b), a), x)$$

$$\theta = \{f(b)/x\}$$

$$S_1 = \{g(a, g(f(b), a), f(y)), g(a, g(f(b), a), f(b))\}$$

$$\theta =$$

$$\theta = \{b/y\}$$

$$S_2 = \{g(a, g(f(b), a), f(b)), g(a, g(f(b), a), f(b))\}$$

$$\text{Hence, Unifier} = \{f(b)/x, b/y, a/a\}$$

$$6. S_0 = \{\text{knows}(\text{Richard}, x), \text{knows}(\text{Richard}, \text{John})\}$$

$$\theta = \{\text{John}/x\}$$

$$S_1 = \{\text{knows}(\text{Richard}, \text{John}), \text{knows}(\text{Richard}, \text{John})\}$$

$$\text{Hence, unifier} = \{\text{John}/x\}$$



Ans 2:

a) John likes all kinds of food.

i)  $\forall x: \text{food}(x) \rightarrow \text{likes}(\text{John}, x)$

ii)  $\forall x \rightarrow \text{food}(x) \vee \text{likes}(\text{John}, x)$

iii)

a) John likes all kinds of food

b) Apple and vegetable are food

c) Anything anyone eats and not killed is food.

d) Anil eats peanut and is alive.

e) Harry eats everything that Anil eats

Prove that:-

f) John likes peanuts.

Step 1:-

a)  $\forall x: \text{food}(x) \rightarrow \text{likes}(\text{John}, x)$

b)  $\text{food}(\text{Apple}) \wedge \text{food}(\text{Vegetable})$

c)  $\forall x \forall y: \text{eats}(x, y) \wedge \sim \text{killed}(x) \rightarrow \text{food}(y)$

d)  $\text{eats}(\text{Anil}, \text{Peanuts}) \rightarrow \text{alive}(\text{Anil})$

e)  $\forall x: \text{Anil eats}(x) \rightarrow \text{eats}(\text{Harry}, x)$

f)  $\forall x: \sim \text{killed}(x) \rightarrow \text{alive}(x)$

g)  $\forall x: \text{alive}(x) \rightarrow \sim(\text{killed}(x))$

} added predicates

h)  $\text{likes}(\text{John}, \text{peanuts})$



Step 2:-

Remove Implications:-

- $\rightarrow \forall x \text{ food}(x) \vee \text{likes}(\text{John}, x)$
- $\text{food}(\text{Apple}) \wedge \text{food}(\text{Vegetable})$
- $\forall x, y \rightarrow [\text{eats}(x, y) \wedge \sim \text{killed}(x)] \vee \text{food}(y)$
- $\text{eats}(\text{Anil}, \text{Peanuts}) \wedge \text{Alive}(\text{Anil})$
- $\forall x \rightarrow \forall x \text{ eats}(\text{Anil}, x) \vee \text{eats}(\text{Harry}, x)$
- $\forall x \sim (\sim \text{killed}(x)) \vee \text{alive}(x)$
- $\forall x \sim \text{alive}(x) \vee \sim (\text{killed}(x))$
- $\text{likes}(\text{John}, \text{peanuts})$

Move negation inwards:-

- $\forall x \sim \text{food}(x) \vee \text{likes}(\text{John}, x)$
- $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetables})$
- $\forall x, y \sim \text{eats}(x, y) \vee \text{killed}(x) \vee \text{food}(y)$
- $\text{eats}(\text{Anil}, \text{Peanuts}) \wedge \text{Alive}(\text{Anil})$
- $\forall w \text{ eats}(\text{Anil}, w) \vee \text{eats}(\text{Harry}, w)$
- $\forall g \sim \text{killed}(g) \vee \text{alive}(g)$
- $\forall k \sim \text{alive}(k) \vee \sim (\text{killed}(k))$
- $\text{likes}(\text{John}, \text{Peanuts})$

Drop universal quantifiers:-

- $\sim \text{food}(x) \vee \text{likes}(\text{John}, x)$
- $\text{food}(\text{Apple})$
- $\text{food}(\text{vegetable})$
- $\sim \text{eats}(y, z) \vee \text{killed}(y) \vee \text{food}(z)$
- $\text{eats}(\text{Anil}, \text{peanuts})$
- $\text{alive}(\text{Anil})$
- $\text{eats}(\text{Anil}, w) \vee \text{eats}(\text{Harry}, w)$
- $\text{killed}(g) \vee \text{alive}(g)$
- $\sim \text{alive}(k) \vee \sim \text{killed}(k)$
- $\text{likes}(\text{John}, \text{peanuts})$



Step 3: Negate the ~~prove~~ statement to be proved.  
Hence,  
g)  $\neg \text{likes}(\text{John}, \text{peanuts})$

Step 5: Draw Resolution Graph

