

# Crystal Structures, Dimorphism and Lithium Mobility of $\text{Li}_7\text{MO}_6$ ( $\text{M} = \text{Bi}, \text{Ru}, \text{Os}$ )

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**Abstract.**  $\text{Li}_7\text{MO}_6$  ( $\text{M} = \text{Bi}, \text{Ru}, \text{Os}$ ) have been synthesized by solid state reaction of  $\text{Li}_2\text{O}$  with  $\text{Bi}_2\text{O}_3$ , or  $\text{MO}_2$  ( $\text{M} = \text{Ru}, \text{Os}$ ) and characterized using powder X-ray diffraction, differential scanning calorimetry, magnetic susceptibility (for  $\text{M} = \text{Ru}, \text{Os}$ ), ionic conductivity and  ${}^6\text{Li}$  solid state NMR (for  $\text{M} = \text{Bi}$ ) measurements. All three compounds exhibit a temperature induced triclinic – rhombohedral phase transition. Structures of the new low temperature triclinic phases have been refined by the Rietveld method from powder X-ray data using atomic parameters of  $\text{Li}_7\text{TaO}_6$  as a starting model. ( $\text{Li}_7\text{BiO}_6$ : triclinic,  $P\bar{1}$ ,  $a = 5.5071(1)$ ,  $b = 6.0425(1)$ ,  $c = 5.5231(1)$  Å,  $\alpha = 116.912(1)$ ,  $\beta = 120.867(1)$ ,  $\gamma = 62.234(1)$ °,  $V = 133.96(1)$  Å<sup>3</sup>,  $Z = 1$ ,  $T = 230$  K;  $\text{Li}_7\text{RuO}_6$ : triclinic,  $P\bar{1}$ ,  $a = 5.3654(1)$ ,  $b = 5.8584(1)$ ,  $c = 5.3496(1)$  Å,  $\alpha = 117.182(1)$ ,  $\beta = 119.117(1)$ ,  $\gamma = 62.632(1)$ °,  $V = 124.43(1)$  Å<sup>3</sup>,  $Z = 1$ ,  $T = 295$  K;  $\text{Li}_7\text{OsO}_6$ : triclinic,  $P\bar{1}$ ,  $a = 5.3786(1)$ ,  $b = 5.8725(1)$ ,  $c =$

5.3591(1) Å,  $\alpha = 117.193(1)$ ,  $\beta = 119.277(1)$ ,  $\gamma = 62.700(1)$ °,  $V = 125.15(1)$  Å<sup>3</sup>,  $Z = 1$ ,  $T = 295$  K). Upon cooling,  $\text{Li}_7\text{RuO}_6$  and  $\text{Li}_7\text{OsO}_6$  undergo a magnetic transition at 12 and 13 K, respectively, from the paramagnetic to the antiferromagnetic state. The higher ionic conductivity of  $\text{Li}_7\text{BiO}_6$  at  $T < 300$  °C, as compared to  $\text{Li}_7\text{RuO}_6$  and  $\text{Li}_7\text{OsO}_6$ , can be ascribed to the undergoing of the triclinic – rhombohedral transition at a much lower temperature. At  $T > 300$  °C, the ionic conductivity of all three compounds increases sharply due to the melting of the lithium sublattice; for  $\text{Li}_7\text{RuO}_6$  and  $\text{Li}_7\text{OsO}_6$  the latter effect is superimposed by the phase transitions to the rhombohedral modifications.

**Keywords:** Crystal structure; Ionic conductivity; Lithiumhexaoxometallate; Rietveld refinement; X-ray powder diffraction

## Introduction

There exists an extended family of lithium hexaoxometallates that show quite similar structural characteristics, despite of their different general compositions  $\text{Li}_6\text{MO}_6$ ,  $\text{Li}_7\text{MO}_6$  and  $\text{Li}_8\text{MO}_6$ . Basic features are triple slabs of composition  $[\text{Li}_2\text{MO}_6]$  with the cations occupying the octahedral voids of two close packed oxygen layers. These slabs are stacked in a way that an approximate hexagonal close packing of oxygen atoms results. Depending on the formula type, the tetrahedral interstices resulting between each two slabs  $[\text{Li}_2\text{MO}_6]$  are fully ( $\text{Li}_8\text{MO}_6$ ), or partly ( $\text{Li}_7\text{MO}_6$  and  $\text{Li}_6\text{MO}_6$ ), occupied. This class of compounds has attracted renewed attention since the defective character of the lithium partial structures offers promising prospects with respect to ionic conductivity and might lay a basis for intercalation and deintercalation experiments. A comprehensive compilation of all representatives is given at [1]. More recent works [2, 3] are focusing on lithium ionic conductivity. To all representatives of formula types  $\text{Li}_7\text{MO}_6$  and  $\text{Li}_8\text{MO}_6$  trigonal symmetry with space groups  $R\bar{3}$ , or  $R\bar{3}$  was assigned, previously. However, during our reinvestigation on  $\text{Li}_7\text{MO}_6$  ( $\text{M} = \text{Nb}, \text{Ta}, \text{Sb}$ ) [4] we noticed slight splittings of powder X-ray diffraction peaks, reducing the symmetry to triclinic ( $P\bar{1}$ ).

Here we report on three further examples of the triclinic – rhombohedral dimorphism in lithiumhexaoxometallates, observed for  $\text{Li}_7\text{BiO}_6$ ,  $\text{Li}_7\text{RuO}_6$  and  $\text{Li}_7\text{OsO}_6$ . The temperatures of the phase transitions have been determined using differential scanning calorimetry (DSC) and temperature dependent X-ray diffractometry. The structures of the low temperature triclinic modifications have been refined by the Rietveld method from laboratory X-ray diffraction data. Li mobility has been studied by impedance and  ${}^6\text{Li}$  solid state nuclear magnetic resonance (NMR) spectroscopy.

## Results and Discussion

### Syntheses

Starting from binary components,  $\text{Li}_7\text{BiO}_6$  and  $\text{Li}_7\text{RuO}_6$  have been synthesized through solid state reaction in a flow of oxygen. For  $\text{Li}_7\text{RuO}_6$  [5] an excess of  $\text{LiOH}$  has been used. Nevertheless we got always obtained samples containing small amounts of  $\text{Li}_3\text{RuO}_4$  [6] and of a second, unknown phase [7] together with some  $\text{Li}_2\text{O}$ . Attempts to synthesize  $\text{Li}_7\text{OsO}_6$  at the same conditions as  $\text{Li}_7\text{BiO}_6$  and  $\text{Li}_7\text{RuO}_6$  led to oxidation of osmium to +7 with the formation of known  $\text{Li}_5\text{OsO}_6$  [8]. In order to stabilize osmium in a lower oxidation state,  $\text{OsO}_2$  and  $\text{Li}_2\text{O}$  have been allowed to react under Ar in a closed capsule giving  $\text{Li}_7\text{OsO}_6$ , small quantities of  $\text{Li}_2\text{O}$  and metallic Os, as admixtures. By repeated grinding and annealing the formation of impurity phases could be reduced, but not fully suppressed. The compounds are colourless ( $\text{Li}_7\text{BiO}_6$ ), brown ( $\text{Li}_7\text{RuO}_6$ ) and black ( $\text{Li}_7\text{OsO}_6$ ). If exposed to air, they slowly absorb car-

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**Table 1** Temperatures of the phase transition triclinic – rhombohedral for  $\text{Li}_7\text{MO}_6$ , ( $\text{M} = \text{Bi}, \text{Ru}, \text{Os}$ ).

	X-ray powder diffraction data (3 °C/min)	DSC, onset of peaks (10 °C/min)
$\text{Li}_7\text{BiO}_6$	–	7 °C
$\text{Li}_7\text{RuO}_6$	460–480 °C	450 °C
$\text{Li}_7\text{OsO}_6$	350–370 °C	365 °C

bon dioxide and water which is becoming detectable after a few days by DTA. These compounds evolve oxygen at  $T \approx 1000$  °C.

### DSC Analysis and Temperature-Dependent X-ray Powder Diffractometry

All three compounds were checked for possible phase transitions by DSC measurements and temperature dependent X-ray diffractometry. By means of DSC, upon cooling, an endothermal effect at  $T = 7$  °C was observed for  $\text{Li}_7\text{BiO}_6$ . The corresponding low temperature X-ray diffractogram, recorded at  $T = -43$  °C (230 K), allows to connect this peak with a transition of the well known rhombohedral modification of  $\text{Li}_7\text{BiO}_6$ , stable at room temperature [9], to a triclinic one. High temperature X-ray powder diffraction patterns of triclinic  $\text{Li}_7\text{RuO}_6$  and  $\text{Li}_7\text{OsO}_6$  show a phase transition to the rhombohedral form in a range of  $T = 460$ –480 °C and  $T = 350$ –370 °C, correspondingly. The associated peaks in the DSC are observed at  $T = 450$  °C and  $T = 365$  °C (see Table 1). Hence, all three lithiumoxometalates obtained follow to the same transition scheme from triclinic (LT) to rhombohedral (HT) as reported previously for  $\text{Li}_7\text{MO}_6$  ( $\text{M} = \text{Nb}, \text{Ta}, \text{Sb}$ ) [4].

### Crystal Structures of Triclinic Modifications of $\text{Li}_7\text{MO}_6$ ( $\text{M} = \text{Bi}, \text{Ru}, \text{Os}$ )

Using high resolution synchrotron powder data, we have determined and refined the crystal structure of  $\text{Li}_7\text{TaO}_6$  at room temperature by Fourier techniques and Rietveld refinement, respectively [4]. This first example of a triclinic modification of the lithium-rich hexaoxometallates was refined assuming equal partial occupations for all four different lithium positions. Following this model we have refined the new structures by the Rietveld method from powder XRD patterns in the space group  $P\bar{1}$ , fixing the occupation factors of lithium atoms at 0.875. The details of the refinement and structural parameters are listed in Tables 2 and 3. The refinement has led to a good coincidence of the calculated intensities to the measured XRD patterns (Fig. 1–3).

The characteristic feature of the structure is a slightly distorted hexagonal closed packing of oxygen atoms (Fig. 4). The heavy metal atoms Bi, Ru and Os are placed at the origin of the unit cell and surrounded by six oxygen atoms in shape of virtually ideal octahedra (Table 4). The averaged M–O distances ( $\bar{d}(\text{Bi}–\text{O}) = 2.145$  Å,  $\bar{d}(\text{Ru}–\text{O}) = 1.980$  Å,  $\bar{d}(\text{Os}–\text{O}) = 1.998$  Å) agree well with distances found in analogous compounds of pentavalent metals in octahedral coordination, or with the sum of crystal radii reported for oxides for coordination numbers CN = VI [10] ( $\bar{d}(\text{Bi}^{5+}–\text{O}) = 2.13$  Å for  $\text{Na}_3\text{BiO}_4$  [11], or 2.16 Å [10],  $\bar{d}(\text{Ru}^{5+}–\text{O}) = 1.986$  Å in  $\text{Sr}_3\text{LiRuO}_6$  [12] or 1.965 Å [10],  $\bar{d}(\text{Os}^{5+}–\text{O}) = 1.97$  Å [10]). The O–M–O angles diverge but insignificantly from 90°. The  $\text{MO}_6$  octahedra are connected to each other via strongly distorted octahedra of  $\text{Li}(4)\text{O}_6$ . Half of the tetrahedral interstices between resulting slabs  $[\text{Li}(4)\text{MO}_2]$  are filled with  $\text{Li}_1\text{–Li}_3$  atoms building a double layer of edge-shared  $(\text{Li}(1\text{–}3)\text{O}_4)$  tetra-

**Table 2** Crystallographic data and details on refinement for triclinic modifications of  $\text{Li}_7\text{MO}_6$ ,  $\text{M} = (\text{Bi}, \text{Ru}, \text{Os})$ .

	$\text{Li}_7\text{BiO}_6$	$\text{Li}_7\text{RuO}_6$	$\text{Li}_7\text{OsO}_6$
space group	$P\bar{1}$	$P\bar{1}$	$P\bar{1}$
$a$ /Å	5.5071(1)	5.3654(1)	5.3786(1)
$b$ /Å	6.0425(1)	5.8584(1)	5.8725(1)
$c$ /Å	5.5231(1)	5.3496(1)	5.3591(1)
$\alpha$ /°	116.912(1)	117.182(1)	117.193(1)
$\beta$ /°	120.867(1)	119.117(1)	119.277(1)
$\gamma$ /°	62.234(1)	62.632(1)	62.700(1)
$V$ /Å <sup>3</sup>	133.96(1)	124.43(1)	125.15(1)
$Z$	1	1	1
$T$ /K	230	295	295
formula weight /g·mol <sup>-1</sup>	353.56	245.65	334.78
$\rho_{\text{calc}}$ /g·cm <sup>-3</sup>	4.383	3.365	4.436
radiation source, monochromator	Cu-K <sub>α1</sub> , germanium	Cu-K <sub>α1</sub> , germanium	Cu-K <sub>α1</sub> , germanium
capillary diameter	0.3	0.3	0.3
2 $\theta$ range, step width /°	12 to 105, 0.01	5 to 105, 0.01	5 to 110, 0.01
No. of refined parameters	39	39	39
$R_p$ /% a)	6.35	5.44	5.21
$R_{\text{wp}}$ /% a)	8.23	7.45	6.92
$R_F$ /% a)	2.47	3.92	2.39
$\chi^2$ a)	1.92	1.39	1.61

a)  $R_p$ ,  $R_{\text{wp}}$ ,  $R_F$  and  $\chi^2$  as defined in FullProf

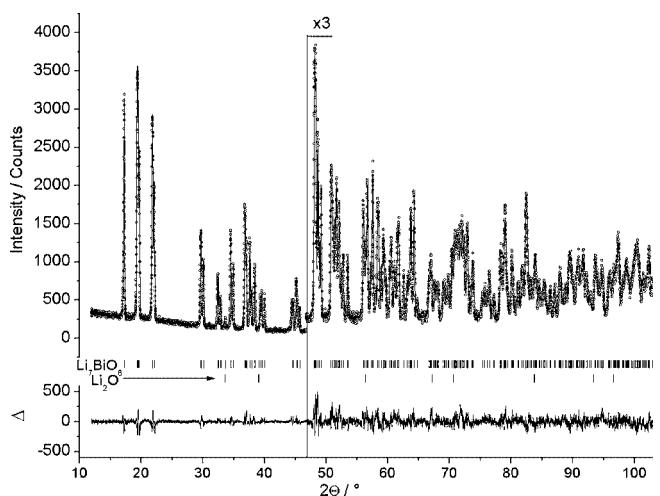
hedra. The eight lithium positions within the unit cell build a distorted cube with a mean Li–Li distance of 2.39(5) Å for  $\text{Li}_7\text{BiO}_6$ , 2.41(3) Å for  $\text{Li}_7\text{RuO}_6$  and 2.40(4) Å for  $\text{Li}_7\text{OsO}_6$  (Table 3, Fig. 5), excellently agreeing with the value found for  $\text{Li}_7\text{TaO}_6$  (2.41 Å) [4].

### Magnetic Properties

Magnetization of the samples has been measured at three different magnetic fields of 1, 3 and 5 T. A small field dependence of the samples susceptibilities has been corrected

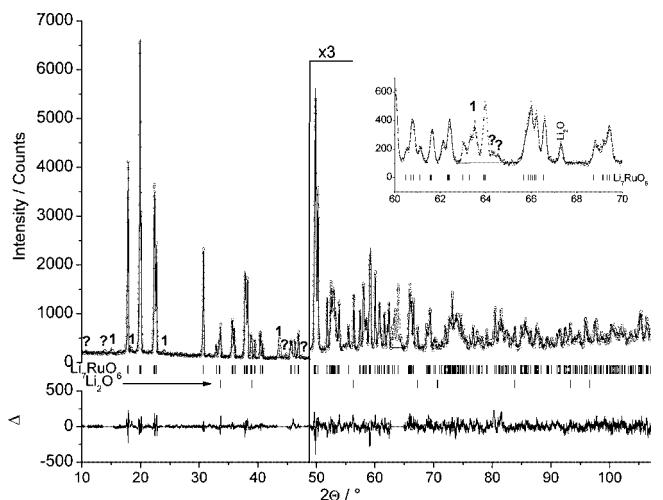
**Table 3** Atomic parameters and isotropic thermal displacement parameters for triclinic modifications of  $\text{Li}_7\text{MO}_6$ ,  $\text{M} = (\text{Bi}, \text{Ru}, \text{Os})$ .

Atom	occupancy	x	y	z	$B_{eq} / \text{\AA}^2$
Bi					1.43(1)
Ru	1	0	0	0	1.51(1)
Os					1.57(1)
O1	1	0.911(2)	0.244(1)	0.393(2)	2.41(8)
		0.8996(9)	0.2362(9)	0.3695(8)	2.00(6)
		0.912(1)	0.235(1)	0.379(1)	2.13(8)
		0.253(1)	0.237(1)	0.085(2)	2.41(8)
O2	1	0.225(1)	0.2311(9)	0.081(1)	2.00(6)
		0.217(2)	0.243(2)	0.081(2)	2.13(8)
		0.386(1)	0.751(1)	0.230(2)	2.41(8)
O3	1	0.3700(9)	0.7835(8)	0.2372(9)	2.00(6)
		0.374(1)	0.780(1)	0.232(1)	2.13(8)
		0.489(5)	0.368(4)	0.070(6)	3.1(2)
Li1	0.875	0.498(3)	0.378(3)	0.105(3)	3.9(2)
		0.501(5)	0.399(5)	0.097(5)	2.9(2)
		0.123(5)	0.622(5)	0.190(5)	3.1(2)
Li2	0.875	0.101(3)	0.649(4)	0.219(3)	3.9(2)
		0.109(5)	0.686(5)	0.252(6)	2.9(2)
		0.742(5)	0.635(5)	0.536(5)	3.1(2)
Li3	0.875	0.782(3)	0.655(3)	0.528(3)	3.9(2)
		0.764(5)	0.642(5)	0.501(4)	2.9(2)
		0.657(5)	0.032(4)	0.359(5)	3.1(2)
Li4	0.875	0.637(4)	0.013(2)	0.312(4)	3.9(2)
		0.651(5)	0.019(3)	0.315(6)	2.9(2)

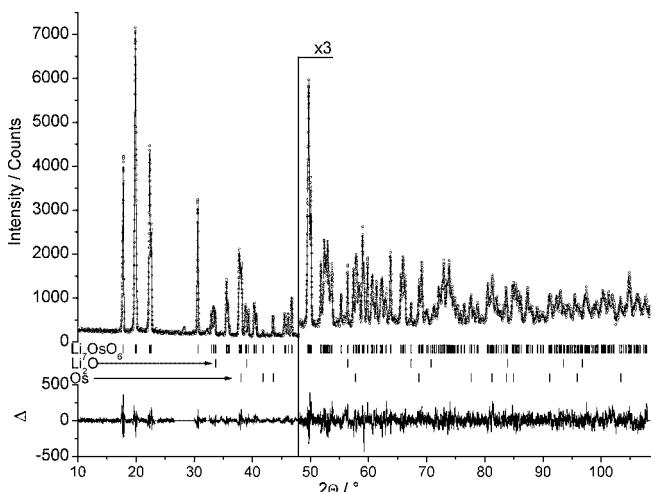


**Fig. 1** Observed and calculated powder X-ray diffraction patterns for  $\text{Li}_7\text{BiO}_6$  at 230 K. Shown are the observed (circles) and calculated (solid line) data and the enlarged difference curve between observed and calculated profiles (below in an additional window). Vertical lines indicate the Bragg reflection positions for  $\text{Li}_7\text{BiO}_6$  (top) and  $\text{Li}_2\text{O}$  (bottom). The high angle part is enlarged for clarity.

by extrapolation of the measured values to  $1/H \rightarrow 0$ . Fig. 6 and 7 (squares) show the temperature dependencies of the magnetic susceptibilities for  $\text{Li}_7\text{RuO}_6$  and  $\text{Li}_7\text{OsO}_6$  after correction for the weights of the samples due to small quantities of diamagnetic impurities of  $\text{Li}_2\text{O}$  and others and, finally, for the core diamagnetism ( $-113 \cdot 10^{-11} \text{ m}^3 \cdot \text{mol}^{-1}$  for  $\text{Li}_7\text{RuO}_6$  and  $-125 \cdot 10^{-11} \text{ m}^3 \cdot \text{mol}^{-1}$  for  $\text{Li}_7\text{OsO}_6$  [13], p. 426). Upon cooling the compounds undergo a transition

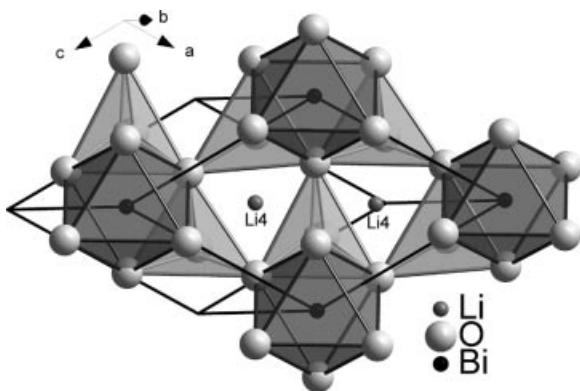


**Fig. 2** Observed and calculated powder X-ray diffraction patterns for  $\text{Li}_7\text{RuO}_6$  at room temperature. Shown are the observed (circles) and calculated (solid line) data and the enlarged difference curve between observed and calculated profiles (below in an additional window). Vertical lines indicate the Bragg reflection positions for  $\text{Li}_7\text{RuO}_6$  (top) and  $\text{Li}_2\text{O}$  (bottom). Peaks of the  $\text{Li}_3\text{RuO}_4$  admixture are indicated by “1” and of an unknown phase by “?”. The high angle part is enlarged for clarity. The excluded region at  $2\theta$  from 62.8 to 64.9 degrees is shown in an enlarged scale.



**Fig. 3** Observed and calculated powder X-ray diffraction patterns for  $\text{Li}_7\text{OsO}_6$  at room temperature. Shown are the observed (circles) and calculated (solid line) data and the enlarged difference curve between observed and calculated profiles (below in an additional window). Vertical lines indicate the Bragg reflection positions for  $\text{Li}_7\text{OsO}_6$  (top) and  $\text{Li}_2\text{O}$  (middle) and Os (bottom). The high angle part is enlarged for clarity.

from the paramagnetic to the antiferromagnetic state at very close Néel temperatures  $T_N$  of 12 K for  $\text{Li}_7\text{RuO}_6$ , and 13 K for  $\text{Li}_7\text{OsO}_6$ . These temperatures are similar to other known compounds containing isolated  $\text{RuO}_6^{7-}$  or  $\text{OsO}_6^{7-}$  octahedra ( $T_N = 18$  K in  $\text{La}_3\text{RuO}_7$  [14],  $T_N = 14$  K in  $\text{La}_7\text{Ru}_3\text{O}_{18}$  [15], or  $T_N = 17$  K in  $\text{La}_2\text{NaOsO}_6$  [16]).

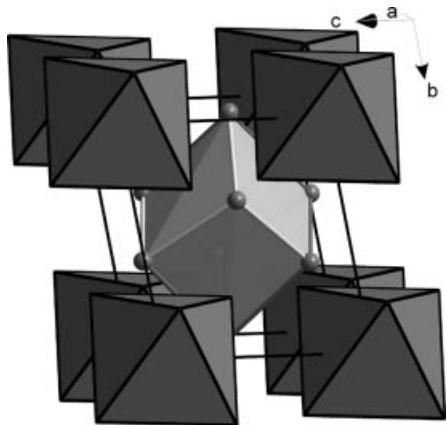


**Fig. 4** A schematic representation of the crystal structure of the LT modification of  $\text{Li}_7\text{BiO}_6$ . In front: dark-grey  $\text{BiO}_6$  octahedra and  $\text{Li}4$  atoms building monolayer of  $[\text{Li}(4)_{1.75}\text{BiO}_2]$ . In background: one layer of light-grey  $\text{Li}(1-3)\text{O}_4$  tetrahedra. Big light-grey spheres exhibiting oxygen atoms build a slightly distorted hcp packing.

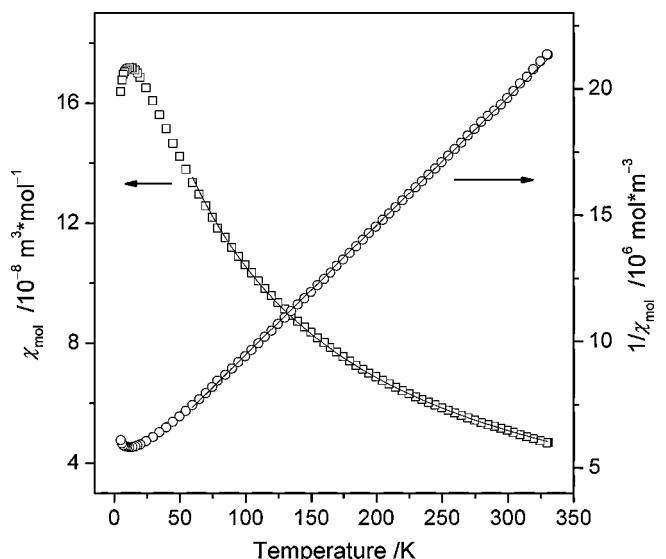
**Table 4** Distances and angles for triclinic modifications  $\text{Li}_7\text{MO}_6$ , M = (Bi, Ru, Os).

distances /Å angles /°	$\text{Li}_7\text{BiO}_6$	$\text{Li}_7\text{RuO}_6$	$\text{Li}_7\text{OsO}_6$
M–O(1)	2.155(8) x 2	1.991(4) x 2	2.008(6) x 2
M–O(2)		1.984(6) x 2	2.011(9) x 2
M–O(3)	2.19(1) x 2 2.093(7) x 2	1.966(5) x 2	1.975(7) x 2
O–M–O	88.4(3) – 91.6(3) 180.0(3)	89.1(3) – 90.9(4) 180.0(4)	89.0(6) – 91.0(6) 180.0(6)
Li(1)–O(1)	2.11(2)	1.95(2)	2.05(3)
Li(1)–O(2)	1.86(4)	1.94(2)	2.07(3)
Li(1)–O(3)	1.83(4)	1.95(2)	1.86(3)
Li(1)–O(4)	1.97(2)	2.01(2)	1.90(3)
O–Li(1)–O	97(1) – 126(2)	92(1) – 116(1)	93(1) – 120(1)
Li(2)–O(1)	2.15(3)	1.99(2)	1.86(3)
Li(2)–O(2)	1.90(2)	1.81(2)	1.84(3)
Li(2)–O(3)	1.98(3)	2.08(2)	2.21(3)
Li(2)–O(4)	1.82(4)	1.88(2)	1.81(3)
O–Li(2)–O	105(1) – 113(1)	99(1) – 122(1)	97(1) – 127(1)
Li(3)–O(1)	2.02(3)	1.84(2)	1.90(3)
Li(3)–O(2)	2.15(4)	2.08(2)	2.03(3)
Li(3)–O(3)	1.86(3)	1.90(2)	1.98(2)
Li(3)–O(4)	1.89(2)	2.02(2)	1.92(3)
O–Li(3)–O	100(1) – 119(1)	98(1) – 124(1)	94(1) – 122(1)
Li(4)–O(1)	2.19(4)	2.17(2)	2.11(3)
Li(4)–O(2)	2.32(2)	2.45(2)	2.39(2)
Li(4)–O(3)	2.11(2)	2.06(2)	2.14(2)
Li(4)–O(4)	2.41(3)	2.20(2)	2.21(3)
Li(4)–O(5)	2.12(3)	2.15(2)	2.20(3)
Li(4)–O(6)	2.41(3)	2.17(2)	2.26(2)
O–Li(4)–O	83(1) – 100(1) 169(1) – 175(1)	74(1) – 100(1) 164(1) – 178(1)	76(1) – 99(1) 166(1) – 178(1)
Li(1)–Li(2)	2.10(4)	2.16(3)	2.27(4)
Li(1)–Li(3)	2.41(3)	2.37(2)	2.18(3)
Li(1)–Li(4)	2.68(5)	2.51(2)	2.61(3)
Li(2)–Li(3)	2.27(5)	2.39(3)	2.49(4)
Li(2)–Li(4)	2.57(3)	2.61(2)	2.34(4)
Li(3)–Li(4)	2.31(3)	2.43(3)	2.49(4)
Li–Li–Li	75(1) – 102(1)	78(1) – 100(1)	78(2) – 97(2)

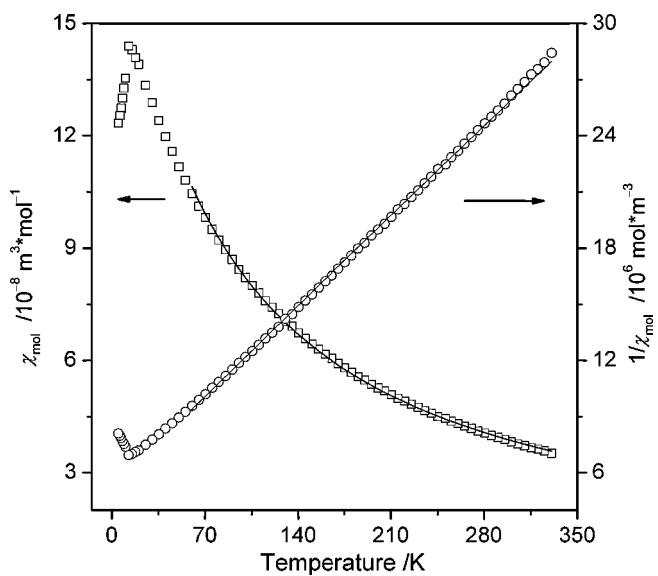
The high temperature paramagnetic regions of the magnetic curves (60 – 330 K) have been fitted with the program CONDON [17], accounting for the interelectronic repulsion (Racah-Parameters  $B$  and  $C$ ), ligand-field splitting, spin-orbit coupling (spin-orbit coupling constant  $\zeta$ ), and cooperative interactions in the molecular field approximation. The program is based on the quantum-chemical equations taken from the works of Condon and Shortley [18], and Griffith [19] and has been already successfully applied to the discussion of the magnetic properties of such 5d ions like  $\text{Re}^{3+}$  [20],  $\text{Os}^{4+}$  [21], or  $\text{Os}^{5+}$  [22]. The values of spin-orbit coupling constants for  $\text{Ru}^{5+}$  ( $\zeta = 1500 \text{ cm}^{-1}$ ) and  $\text{Os}^{5+}$  ( $\zeta = 4500 \text{ cm}^{-1}$ ) have been taken from [23]. The Racah-parameters  $B = 693 \text{ cm}^{-1}$  and  $C = 2952 \text{ cm}^{-1}$  for  $\text{Os}^{5+}$  have been taken from [13], p. 253. Exact values of Racah-parameters



**Fig. 5** Perspective view of the crystal structure of the LT modification of  $\text{Li}_7\text{BiO}_6$ . The regular  $\text{BiO}_6$ -octahedra and the lithium metal positions marking the corners of a distorted cube (lithium sub-lattice) are drawn.



**Fig. 6** Temperature dependence of magnetic susceptibility (open squares) and inverse magnetic susceptibility (open circles) of  $\text{Li}_7\text{RuO}_6$  extrapolated to  $1/H \rightarrow 0$ . The solid line shows a fit using parameters as described in the text.

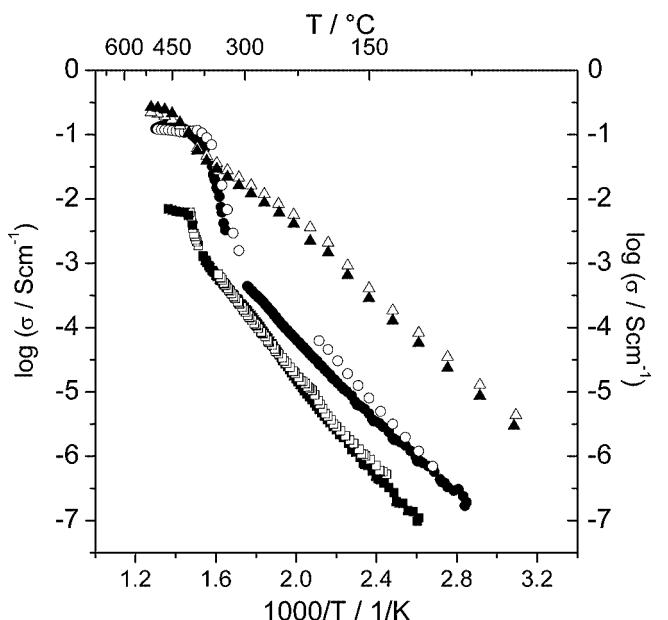


**Fig. 7** Temperature dependence of magnetic susceptibility (open squares) and inverse magnetic susceptibility (open circles) of  $\text{Li}_7\text{OsO}_6$  extrapolated to  $1/H \rightarrow 0$ . The solid line shows a fit using parameters as described in the text.

for  $\text{Ru}^{5+}$  are not known yet, thus they have been obtained by extrapolation of the Racah-parameters for  $\text{Ru}^{3+}$  ( $B = 464 \text{ cm}^{-1}$ ,  $C = 1875 \text{ cm}^{-1}$  [13], p. 252) using common trends of their change with an increasing charge of an ion ( $B = 500 \text{ cm}^{-1}$ ,  $C = 2000 \text{ cm}^{-1}$ ). For both compounds two parameters have been refined – the ligand-field parameter  $B_0^4$ , and the molecular field parameter  $\lambda_{\text{MF}}$ . The refinements converged at  $B_0^4 = 51185 \text{ cm}^{-1}$ ,  $B_4^4 = \sqrt{5/14} B_0^4$ ,  $\lambda_{\text{MF}} = -4.30 \times 10^6 \text{ mol} \cdot \text{m}^{-3}$  for  $\text{Li}_7\text{RuO}_6$ , and  $B_0^4 = 84960 \text{ cm}^{-1}$ ,  $B_4^4 = \sqrt{5/14} B_0^4$ ,  $\lambda_{\text{MF}} = -5.17 \times 10^6 \text{ mol} \cdot \text{m}^{-3}$  for  $\text{Li}_7\text{OsO}_6$ . The calculated fits agree well with the measured susceptibilities (solid lines in Figs. 6, 7;  $\text{SQ}^{(1)} = 0.5\%$  for  $\text{Li}_7\text{RuO}_6$ ,  $\text{SQ} = 0.7\%$  for  $\text{Li}_7\text{OsO}_6$ ). The resulted ligand-field parameters  $D_q = B_0^4 / 21$  for cubic symmetry ( $2437 \text{ cm}^{-1}$  for  $\text{Li}_7\text{RuO}_6$ , and  $4046 \text{ cm}^{-1}$  for  $\text{Li}_7\text{OsO}_6$ ) are in the expected region (compare with  $D_q = 2510 \text{ cm}^{-1}$  for  $4d^3 \text{ Mo}^{3+}$ ,  $D_q = 2860 \text{ cm}^{-1}$  for  $4d^5 \text{ Ru}^{3+}$ , and  $D_q = 3710 \text{ cm}^{-1}$  for  $5d^3 \text{ Os}^{5+}$ , all in the octahedral  $\text{H}_2\text{O}$ -ligand field [13], p. 253).

### Ionic Conductivity

The Arrhenius plots of the temperature-dependent ionic conductivity for  $\text{Li}_7\text{MO}_6$  ( $\text{M} = \text{Bi}$  [4],  $\text{Ru}$ ,  $\text{Os}$ ) are displayed in Fig. 8. The corresponding activation energies ( $E_a$ ) as derived from the slopes of the conductivity curves using the



**Fig. 8** Temperature dependence of ionic conductivity for  $\text{Li}_7\text{MO}_6$  ( $\text{M} = \text{Ru}$  (squares),  $\text{Os}$  (circles), and  $\text{Bi}$  (triangles)). Filled symbols represent heating, open symbols – cooling.

Arrhenius equation and the conductivities at selected temperatures are listed in Table 5.

When comparing conductivity in the low temperature region ( $T < 300 \text{ }^\circ\text{C}$ ), the previously measured rhombohedral bismuthate [2, 4] has a by two orders of magnitude higher ionic conductivity. Nomura and Greenblatt [2] have ascribed this fact to a reduction of the ion jumps energy barrier in bismuthate due to an optimized size of the lithium-oxygen channel for passage of lithium atoms through it. However our analysis of Li–Li interatomic distances does not reveal any significant distinctions for all  $\text{Li}_7\text{MO}_6$ . The higher conductivity of bismuthate seems more probably caused by the transition from the triclinic modification to the rhombohedral at a much lower temperature ( $7 \text{ }^\circ\text{C}$  for  $\text{Li}_7\text{BiO}_6$ ) as compared to other  $\text{Li}_7\text{MO}_6$  (see Table 1). This assumption is supported by NMR investigations on  $\text{Li}_7\text{BiO}_6$  (see below)

**Table 5** Ionic Conductivity ( $\sigma$ ) and the Activation Energies ( $E_a$ ) for  $\text{Li}_7\text{MO}_6$  ( $\text{M} = \text{Bi}, \text{Ru}, \text{Os}$ ).

	$\sigma / \text{S} \cdot \text{cm}^{-1}$	$E_a / \text{eV}$
$\text{Li}_7\text{BiO}_6$ a)	$110 \text{ }^\circ\text{C}: 8.24 \times 10^{-5}$	$50-200 \text{ }^\circ\text{C}: 0.58$
	$150 \text{ }^\circ\text{C}: 4.06 \times 10^{-4}$	$200-400 \text{ }^\circ\text{C}: 0.48$
	$300 \text{ }^\circ\text{C}: 1.86 \times 10^{-2}$	$400-700 \text{ }^\circ\text{C}: 0.27$
	$450 \text{ }^\circ\text{C}: 0.1718$	
$\text{Li}_7\text{RuO}_6$	$110 \text{ }^\circ\text{C}: 1.10 \times 10^{-7}$	$110-390 \text{ }^\circ\text{C}: 0.81$
	$150 \text{ }^\circ\text{C}: 7.18 \times 10^{-7}$	$420-460 \text{ }^\circ\text{C}: 0.19$
	$300 \text{ }^\circ\text{C}: 2.08 \times 10^{-4}$	
	$450 \text{ }^\circ\text{C}: 6.69 \times 10^{-3}$	
$\text{Li}_7\text{OsO}_6$	$110 \text{ }^\circ\text{C}: 8.39 \times 10^{-7}$	$110-300 \text{ }^\circ\text{C}: 0.66$
	$150 \text{ }^\circ\text{C}: 4.58 \times 10^{-6}$	$420-490 \text{ }^\circ\text{C}: 0.13$
	$300 \text{ }^\circ\text{C}: 4.40 \times 10^{-4}$	
	$450 \text{ }^\circ\text{C}: 0.1155$	

a) Data taken from [4]

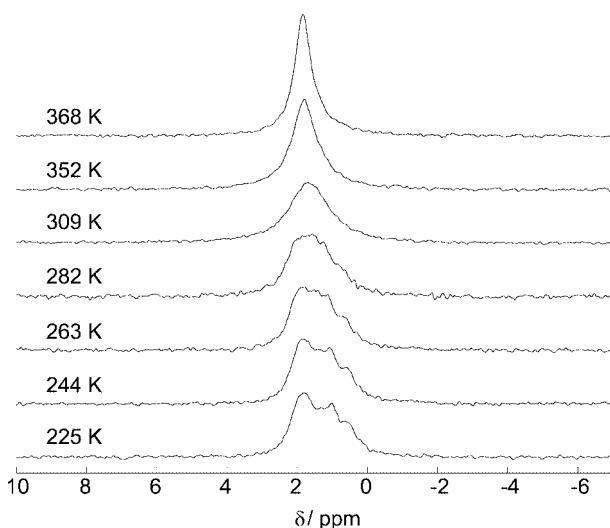
<sup>1)</sup>  $\text{SQ} = (\text{FQ}/n)^{1/2} \cdot 100\%$ , with  $\text{FQ} = \sum_{i=1}^n \{[\chi_{\text{obs}}(i) - \chi_{\text{cal}}(i)] / \chi_{\text{obs}}(i)\}^2$

showing a much higher mobility of lithium ions in the rhombohedral phase as compared to the triclinic one.

On heating, at  $390 < T < 420$  °C for  $\text{Li}_7\text{RuO}_6$  and  $300 < T < 380$  °C for  $\text{Li}_7\text{OsO}_6$  the conductivity increases sharply due to the phase transition to the HT modifications, superimposed with the melting of the lithium sublattice. At higher temperatures the conductivity achieves plateaus. The corresponding low activation energies for conduction in this region indicate almost free motion of  $\text{Li}^+$  ions through the structure. The conductivity of the HT forms of  $\text{Li}_7\text{RuO}_6$  and  $\text{Li}_7\text{OsO}_6$  is several orders of magnitude higher than the values of the room temperature modifications.

## ***6*Li NMR**

NMR is widely applied to study the dynamics of chemical processes [24].  ${}^6\text{Li}$  solid-state MAS NMR measurements were performed to study the mobility of the lithium ions in  $\text{Li}_7\text{BiO}_6$ . The lithium-6 nucleus has only a very small electrical quadrupole moment and therefore yields sharp lines under fast magic-angle spinning. If the cation hopping rate is in the same order of magnitude as the separation of the peaks in the NMR spectrum one can study the dynamics by varying the temperature and observing the influence of the motion on the NMR spectrum. The NMR spectra of  $\text{Li}_7\text{BiO}_6$  at different temperatures are given in Fig. 9. At 225 K we see a superposition of multiple non-resolved peaks. Deconvolution was attempted but unsuccessful, possibly because the chemical shift of a lithium cation depends on both its crystallographic position and on the occupancy of the neighbouring lithium cation sites, which leads to a large number of resonances with slightly different chemical shifts. When we raise the temperature, the lithium cations become more mobile and the different resonances reach coalescence at about 282 K. Further heating sharpens the spectrum, indicating that all lithium sites are exchanging.



**Fig. 9**  ${}^6\text{Li}$  MAS NMR spectra of  $\text{Li}_7\text{BiO}_6$  at different temperatures.  $\omega_r/(2\pi) = 14$  kHz.

## **Experimental Section**

**Syntheses.** The lithium hexaoxometalates have been synthesized by solid-state reaction of mixtures of the respective metal oxides with an excessive amount of lithium hydroxide in a stream of dry oxygen or with a stoichiometric amount of lithium oxide under dry argon.  $\text{Li}_2\text{O}$  was prepared by dehydrating  $\text{LiOH}\cdot\text{H}_2\text{O}$  (Fluka, 99+ %) in vacuum at  $T = 800$  °C [25].

**$\text{Li}_7\text{BiO}_6$ :** Mixtures of  $\text{Bi}_2\text{O}_3$  (Merck, 99.9 %) and  $\text{LiOH}\cdot\text{H}_2\text{O}$  in a ratio  $\text{Li}/\text{Bi} = 7.35$  were heated in a nickel boat, placed in a quartz tube, in a flow of dry oxygen at  $T = 700$  °C for one day.

**$\text{Li}_7\text{RuO}_6$ :** Mixtures of  $\text{RuO}_2$  (Alfa-Aesar, 99.95 %) and  $\text{LiOH}\cdot\text{H}_2\text{O}$  in a ratio  $\text{Li}/\text{Ru} = 7.5$  were pressed to a pellet and heated in a gold boat, placed in a quartz tube, in a flow of dry oxygen at  $T = 950$  °C for two days.

**$\text{Li}_7\text{OsO}_6$ :** Mixtures of  $\text{OsO}_2$  (Alfa-Aesar, 99.99 %) and  $\text{Li}_2\text{O}$  in a ratio  $\text{Li}/\text{Os} = 8.1$  were heated in a silver crucible sealed in a quartz ampoule under dry argon atmosphere at  $T = 700$  °C for two days.

**Characterization.** X-ray powder diffraction data of  $\text{Li}_7\text{RuO}_6$ ,  $\text{Li}_7\text{OsO}_6$  at room temperature, and of  $\text{Li}_7\text{BiO}_6$  at  $T = 230$  K, were collected with a Stoe Stadi-P transmission laboratory diffractometer (primary beam Johansson-type Ge-monochromator for  $\text{Cu}-\text{K}_{\alpha 1}$ -radiation, linear PSD) in steps of  $0.01^\circ$  in  $2\theta$  over different ranges of  $2\theta$  for approximately 24 hours each, with the samples sealed in glass capillaries of 0.3 mm diameter (Hilgenberg, glass No. 50). From visual inspection, it was concluded that  $\text{Li}_7\text{RuO}_6$ ,  $\text{Li}_7\text{OsO}_6$  at room temperature and  $\text{Li}_7\text{BiO}_6$  at  $T = 230$  K are isostructural to triclinic  $\text{Li}_7\text{TaO}_6$  [4]. The crystal structures of the compounds were refined by the Rietveld method [26] using the FullProf program package [27] and the atomic parameters of  $\text{Li}_7\text{TaO}_6$  as a starting model. While the lattice constants of  $\text{Li}_7\text{RuO}_6$  and  $\text{Li}_7\text{OsO}_6$  differed not very much from those of  $\text{Li}_7\text{TaO}_6$  and thus were directly refined, for  $\text{Li}_7\text{BiO}_6$ , due to the large difference in volumes, the unit cell was re-indexed by CRYSFIRE [28] using LZON algorithm [29], leading to a successful Rietveld refinement. Small amounts of additional phases ( $\text{Li}_2\text{O}$  in all compounds and Os in the osmonate) noticeable in the XRD patterns were included in the Rietveld refinement with their scale factors, lattice constants, half-widths and peak shapes profile parameters varied. The temperature factors of crystallographically different positions of the same element were constrained.

Temperature dependent Guinier recordings (Enraf-Nonius FR 553,  $\text{CuK}_{\alpha 1}$ , Johansson monochromator) were conducted in a temperature range from room temperature to  $T = 500$  °C with a heating rate of 3 K/min.

Differential Scanning Calorimetry (DSC) data were recorded on a calorimeter (model 404, Netzsch, Germany) by heating and cooling the sample in an aluminium crucible with 10 K/min from room temperature to  $T = 600$  °C.

Magnetization was measured on powder samples of  $\text{Li}_7\text{RuO}_6$  (57.6 mg) and  $\text{Li}_7\text{OsO}_6$  (29.2 mg) using a SQUID magnetometer (MPMS-XL7, Quantum Design, USA) in the temperature range 5 – 330 K at fields of 1, 3 and 5 T.

The ionic conductivity was measured using compact polycrystalline powder samples (diameter 6 mm, thicknesses 0.85 mm, pressed with 350 MPa) in an ion-blocking cell Ag/sample/Ag. During the measurement, the samples were placed into a quartz glass cell [30] under dry argon. The temperature dependent ac impedance spectra were measured with a Novocontrol Alpha-A 4.2 Analyzer combined with the impedance interface ZG4 in a 2-wire arrangement

in the frequency range of  $\nu = 0.5$  Hz to  $\nu = 20$  MHz. Measurements and data recording were performed with the WinDeta program [31]. The bulk conductivity was determined by non linear mean square deviation curve fitting of the impedance spectrum using the WinFit program [32].

All NMR experiments were performed using a Bruker DSX-400 spectrometer operating at 9.4 T with a resonance frequency of 58.8 MHz for <sup>6</sup>Li. Chemical shifts were referenced to 1 M aqueous LiCl. The sample was sealed in a Pyrex tube fitting exactly into the MAS rotor. <sup>6</sup>Li MAS NMR experiments were performed in the temperature range of 225 K to 368 K using a Bruker 4 mm triple resonance probe at magic-angle spinning frequency of 14 kHz. The temperature was calibrated using the temperature-dependent <sup>207</sup>Pb chemical shift of PbNO<sub>3</sub> [33].

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## References

- [1] J. Hauck, *Z. Naturforsch.* **1969**, *24b*, 1067.
- [2] E. Nomura, M. Greenblatt, *J. Solid State Chem.* **1984**, *52*, 91.
- [3] E. Nomura, M. Greenblatt, *Solid State Ionics* **1984**, *13*, 249.
- [4] C. Mühle, R. E. Dinnebier, L. van Wüllen, G. Schwering, M. Jansen, *Inorg. Chem.* **2004**, *43*, 874.
- [5] R. Scholderer, H. Gläser, *Z. Anorg. Allg. Chem.* **1964**, *327*, 15.
- [6] a) T. S. Bush, C. R. A. Catlow, P. D. Battle, *J. Mater. Chem.* **1995**, *5*, 1269; b) A. Alexander, P. D. Battle, J. C. Burley, D. J. Gallon, C. P. Grey, S. H. Kim, *J. Mater. Chem.* **2003**, *13*, 2612.
- [7] I. S. Shaplygin, M. I. Gadzhiev, V. B. Lazarev, *Russ. J. Inorg. Chem.* **1987**, *32*, 418.
- [8] T. Betz, R. Hoppe, *Z. Anorg. Allg. Chem.* **1985**, *524*, 17.
- [9] R. Scholderer, *Angew. Chem.* **1958**, *70*, 583.
- [10] R. D. Shannon, *Acta Crystallogr.* **1976**, *A32*, 751.
- [11] B. Schwedes, R. Hoppe, *Z. Anorg. Allg. Chem.* **1972**, *393*, 136.
- [12] J. Darriet, F. Grasset, P. D. Battle, *Mat. Res. Bull.* **1997**, *32*, 139.
- [13] H. Lueken, *Magnetochemie*, Teubner, Stuttgart, Leipzig 1999.
- [14] P. Khalifah, D. M. Ho, Q. Huang, R. J. Cava, *J. Solid State Chem.* **2002**, *165*, 359.
- [15] P. Khalifah, Q. Huang, D. M. Ho, H. W. Zandbergen, R. J. Cava, *J. Solid State Chem.* **2000**, *155*, 189.
- [16] W. R. Gemmill, M. D. Smith, R. Prozorov, H.-C. zur Loye, *Inorg. Chem.* **2005**, *44*, 2639.
- [17] H. Schilder, H. Lueken, *J. Magn. Magn. Mater.* **2004**, *281*, 17.
- [18] E. U. Condon, G. H. Shortley, *The Theory of Atomic Spectra*, Cambridge University Press 1977.
- [19] J. S. Griffith, *The Theory of Transition Metal Ions*, Cambridge University Press 1977.
- [20] W. Bronger, G. Auffermann, H. Schilder, *Z. Anorg. Allg. Chem.* **1998**, *624*, 497.
- [21] W. Bronger, T. Sommer, G. Auffermann, P. Müller, H. Schilder, *Z. Anorg. Allg. Chem.* **2001**, *627*, 426.
- [22] G. Auffermann, W. Bronger, P. Müller, G. Roth, H. Schilder, T. Sommer, *Z. Anorg. Allg. Chem.* **2005**, *631*, 1060.
- [23] W. Haberditzl, *Quantenchemie*, Vol. 4, Dr. Alfred Hüthig Verlag, Heidelberg 1979, p. 109.
- [24] R. R. Ernst, G. Bodenhausen, A. Wokaun, *Principles of Nuclear Magnetic Resonance in One and Two Dimensions*, Clarendon Press, Oxford 1987.
- [25] G. Brauer, *Handbuch der Präparativen Anorganischen Chemie*, 3rd. ed., Vol. 2, F. Enke, Stuttgart 1978, p. 950.
- [26] a) H. M. Rietveld, *Acta Crystallogr.* **1967**, *22*, 151; b) H. M. Rietveld, *J. Appl. Crystallogr.* **1969**, *2*, 65.
- [27] J. Rodriguez-Carvajal, FULLPROF Version Juli 2001, CEA/Saclay, France, 2001.
- [28] R. Shirley, The Crysfire 2002 System for Automatic Powder Indexing: User's Manual, The Lattice Press, 41 Guildford Park Avenue, Guildford, Surrey GU2 7NL, England, 2002.
- [29] R. Shirley, D. Louer, *Acta Crystallogr.* **1978**, *A34*, S382.
- [30] U. Köhler, *Dissertation*, Univ. Hannover 1987.
- [31] Novocontrol GmbH, WinDeta V 4.5, Hundsangen, Germany, 1995–2003.
- [32] Novocontrol GmbH, WinFit V 2.9, Hundsangen, Germany, 1996.
- [33] A. Bielecki, D. P. Burum, *J. Magn. Reson. A* **1995**, *116*, 215.