

We investigate the immunization level required to halt the propagation of an online meme whose basic reproduction number is 4. The mitigation of contagion processes on networks has been studied extensively over the last two decades. We derive closed-form threshold conditions for (a) purely random vaccination and (b) vaccination restricted to degree k . Methodology Network construction To satisfy $z = 3$ and $q = 4$ simultaneously in the absence of degree correlations, a degree distribution is chosen as a Poisson distribution. [b] Generation of synthetic contact network [1] Set population size $N = 10^4$. Draw $N(1 - \phi)$ degrees from a Poisson distribution. Epidemic model A standard SIR process with per-contact infection rate β and recovery rate $\gamma = 1$ was implemented with a time step of 1 day. Vaccination scenarios and initial conditions **Scenario A:** random vaccination. A fraction f of nodes is switched to state I at $t = 0$. Simulation settings For each scenario three stochastic realisations were run up to $t = 100$ time units. Compartment counts and final epidemic sizes are shown in Table 1. Analytical Results Random vaccination threshold Random removal of a fraction f of nodes scales the mean excess degree $\langle k \rangle$ as $\langle k \rangle \propto f^{-1}$.

Thus 75% random coverage is required.

Vaccination confined to degree $k = 10$ nodes Let P_{10} be the proportion of degree-10 vertices in the untreated graph. Results

leading to $R_0(\alpha) = \beta q(\alpha)$. Substituting the Poisson backbone with $z = 3$ gives $P_{10} \approx 8.1 \times 10^{-4}$. Even for $\alpha = 1$ we obtain a value of $R_0 > 1$.

Simulation Results Key outcome metrics are summarised in Table 2. Vaccinating 75% of the population at random still

Scenario	Peak I/N	Final R/N
[h] Outcome metrics from FastGEMF simulations	1.02×10^{-2}	7.66×10^{-1}
All degree-10 vaccinated	1.06×10^{-2}	1.42×10^{-1}

[http://www.santafe.edu/~wbarthelme/meme/epidemic/epidemic.html] Epidemic trajectories for (left) 75% random vaccination and (right) targeted vaccination at $k = 10$.

Discussion The analytical percolation framework predicts that random vaccination at $f_c = 0.75$ should suffice. Our numerical simulations confirm this result.

Conversely, degree-targeted vaccination restricted to $k = 10$ nodes provides limited leverage despite its conceptual appeal.

Conclusion Random immunisation demands a theoretical 75% coverage to halt a meme with $R_0 = 4$ on the studied network.

*References 9

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