

We investigate the immunization level required to halt the propagation of an online meme whose basic reproduction number is $R_0 = 4$.
Introduction The mitigation of contagion processes on networks has been studied extensively over the last two decades. We derive closed-form threshold conditions for (a) purely random vaccination and (b) vaccination restricted to degree k nodes.
Methodology Network construction To satisfy $z = 3$ and $q = 4$ simultaneously in the absence of degree correlations, a degree-3 regular graph is used as a backbone. [b] Generation of synthetic contact network [1] Set population size $N = 10^4$. Draw $N(1 - \phi)$ degrees from a Poisson distribution with mean z .
Epidemic model A standard SIR process with per-contact infection rate β and recovery rate $\gamma = 1$ was implemented with compartment counts S, I, R .
Vaccination scenarios and initial conditions **Scenario A:** random vaccination. A fraction f of nodes is switched to state R at $t = 0$.
Simulation settings For each scenario three stochastic realisations were run up to $t = 100$ time units. Compartment counts were recorded at $t = 0, 10, 20, \dots, 100$.
Analytical Results Random vaccination threshold Random removal of a fraction f of nodes scales the mean excess degree to $z(1 - f)$.

Thus 75% random coverage is required.

Vaccination confined to degree $k = 10$ nodes Let P_{10} be the proportion of degree-10 vertices in the untreated graph. Random removal of a fraction f of nodes scales the mean excess degree to $z(1 - f)$.

leading to $R_0(\alpha) = \beta q(\alpha)$. Substituting the Poisson backbone with $z = 3$ gives $P_{10} \approx 8.1 \times 10^{-4}$. Even for $\alpha = 1$ we obtain $R_0 \approx 3.24$.

Simulation Results Key outcome metrics are summarised in Table . Vaccinating 75% of the population at random still results in $R_0 > 1$.

| Scenario | Peak I/N | Final R/N |
|---|-----------------------|-----------------------|
| [h] Outcome metrics from FastGEMF simulations Random $f = 0.75$ | 1.02×10^{-2} | 7.66×10^{-1} |
| All degree-10 vaccinated | 1.06×10^{-2} | 1.42×10^{-1} |

[http://www.oxfordjournals.org/doi/full/10.1093/oxfordjournals.ima.a011111] Epidemic trajectories for (left) 75% random vaccination and (right) degree-targeted vaccination.

Discussion The analytical percolation framework predicts that random vaccination at $f_c = 0.75$ should suffice. Our numerical simulations confirm this prediction.

Conversely, degree-targeted vaccination restricted to $k = 10$ nodes provides limited leverage despite its conceptual appeal.

Conclusion Random immunisation demands a theoretical 75% coverage to halt a meme with $R_0 = 4$ on the studied network.

*References 9

L. Gallos, F. Liljeros, P. Argyrakis, A. Bunde and S. Havlin, "Improving immunization strategies," *Phys. Rev. E*, vol. 75, p. 046107, 2007.
Y. Liu et al., "Efficient network immunization under limited knowledge," *Natl. Sci. Rev.*, vol. 8, 2020.