

Assignment: Left Recursion & Left Factoring

1) Program \rightarrow program id (identifiers-list) : declarations
subprogram-declarations
Compound-statement.

Nothing to Remove

2) Identifiers-list \rightarrow id | identifiers-list, id

Removing Left Recursion

identifiers-list \rightarrow id identifiers-list'

identifiers-list' \rightarrow , id identifiers-list' | ϵ

3) declarations \rightarrow declarations var identifiers-list : type ;

Removing Left Recursion

declarations \rightarrow declarations'

declarations' \rightarrow var identifiers-list : type ; declarations' | ϵ

4) type \rightarrow standard-type | array [num....num] of standard-type

5) standard-type \rightarrow integer | real

6) subprogram-declarations \rightarrow subprogram-declarations subprogram-declaration ; | ϵ

Removing Left Recursion

subprogram-declarations \rightarrow subprogram-declarations' | ϵ

subprogram-declarations' \rightarrow subprogram-declaration ; subprogram-declarations' | ϵ

7) subprogram-declaration \rightarrow subprogram-head declarations compound-statement.

8) ~~subprogram-head \rightarrow function id arguments : standard-type ;~~
~~procedure id arguments ;~~

8) arguments \rightarrow (parameter-list) | ϵ

10) parameter-list \rightarrow identifiers-list : type | parameter-list ;
identifiers-list : type

Removing Left Recursion

parameter-list \rightarrow identifiers-list : parameter-list'

parameter-list' \rightarrow ; identifiers-list : type parameter-list' | ϵ

10) subprogram-head \rightarrow function id arguments : standard-types ;
procedure id arguments ;

~~Removing Left Factoring~~ Looking to Remove.

~~subprogram-head \rightarrow id arguments subprogram-head'~~
~~subprogram-head' \rightarrow function procedure : ; standard-type ;~~
 ~~ϵ~~

11) compound-statement \rightarrow begin optional-statement end

12) optional-statement \rightarrow statement-list $\mid \epsilon$

13) statement-list \rightarrow statement \mid statement-list ; statement

~~Removing Left Recursion~~

14) statement-list \rightarrow statement statement-list' ϵ
statement-list' \rightarrow ; statement statement-list' $\mid \epsilon$

14) statement \rightarrow variable assignop expression \mid procedure-statement
 \mid compound-statement \mid if expression then
statement else statement \mid while expression
do statement.

15) variable \rightarrow id \mid id (expression)

~~Removing Left Factoring~~

variable \rightarrow id variable'
variable' \rightarrow [expression] $\mid \epsilon$

16) expression-list \rightarrow expression \mid expression-list, expression

~~Removing Left Recursion~~

expression-list \rightarrow expression expression-list'

expression-list' \rightarrow , expression expression-list' $\mid \epsilon$

17) expression \rightarrow simple-expression / ^{simple-}expression ^{temp} simple-expression

~~Removing Left Factoring~~

expression \rightarrow simple-expression expression'

expression' \rightarrow temp simple-expression $\mid \epsilon$

18) $\text{simple-expression} \rightarrow \text{term} \mid \text{sign term} \mid \text{simple-expression}$
addop term

Removing Left Recursion

$\text{simple-expression} \rightarrow \text{term} \mid \text{sign term} \mid \text{simple-expression}'$
 $\text{simple-expression}' \rightarrow \text{addop term simple-expression}' \mid \epsilon$

19) $\text{term} \rightarrow \text{factor} \mid \text{term mulop factor}$

Removing Left Recursion

$\text{term} \rightarrow \text{factor term}'$
 $\text{term}' \rightarrow \text{mulop factor term}' \mid \epsilon$

20) $\text{factor} \rightarrow \text{id} \mid \text{id (expression-list)} \mid \text{num} \mid (\text{expression}) \mid$
not factor

Removing Left Recursion factoring

$\text{factor} \rightarrow \text{id factor}' \mid \text{num} \mid (\text{expression}) \mid \text{not factor}$
 $\text{factor}' \rightarrow (\text{expression-list}) \mid \epsilon$

21) $\text{sign} \rightarrow + \mid -$

Nothing to Remove

22) $\text{Procedure-statement} \rightarrow \text{id} \mid \text{id (expression-list)}$

Removing Left Factoring

$\text{Procedure-statement} \rightarrow \text{id Procedure-statement}'$
 $\text{Procedure-statement}' \rightarrow (\text{expression-list}) \mid \epsilon$