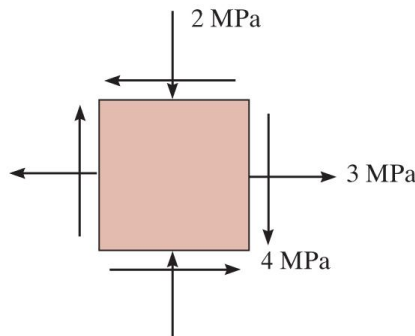
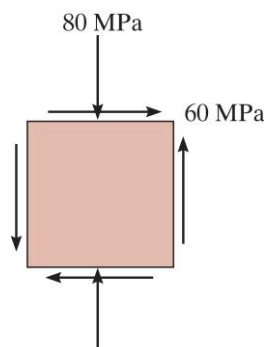


1. Determine the equivalent state of stress if an element is oriented  $20^\circ$  clockwise from the element shown. Show the result on the element. [15%] Ans: 47.5, 202, -15.8 MPa

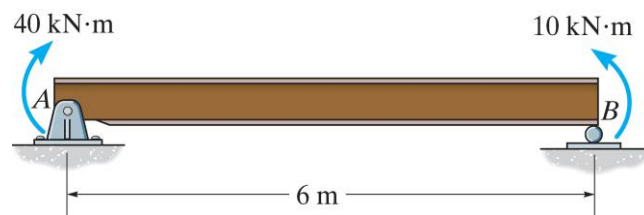


2. The state of stress at a point is shown on the element. (a) Determine the principal stresses and the corresponding orientation of the element. (b) Determine the maximum in-plane shear stress and average normal stress at the point, and specify the orientation of the element. You must use Mohr's circle to solve this problem. [20%] Ans: (a) 32.1, -112 MPa,  $28.15^\circ$  (b) 72.1, -40 MPa,  $-16.8^\circ$

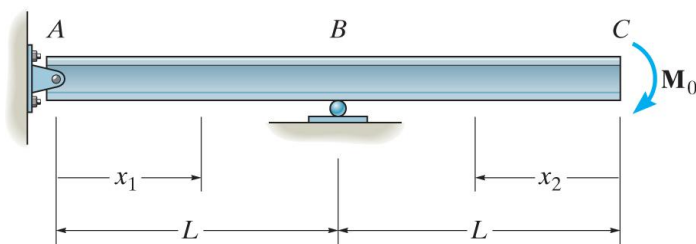


3. The state of plane strain at a point has components  $\epsilon_x = 250(10^{-6})$ ,  $\epsilon_y = 300(10^{-6})$ , and  $\gamma_{xy} = -180(10^{-6})$ . (a) Determine the in-plane principal strains. (b) Determine the maximum in-plane shear strain and average normal strain. You must use Mohr's circle to solve this problem. [15%] Ans: (a) 368, 182 ( $10^{-6}$ ) (b) 187, 275 ( $10^{-6}$ )
4. The state of plane strain at a point is represented on an element having components  $\epsilon_x = 200(10^{-6})$ ,  $\epsilon_y = 180(10^{-6})$ , and  $\gamma_{xy} = -300(10^{-6})$ . Determine the state of strain on an element oriented  $60^\circ$  counterclockwise from the reported position. [15%] Ans: 55.1, 325, 133 ( $10^{-6}$ )

5. Determine the maximum deflection of the simply supported beam. The Young's modulus  $E=200 \text{ GPa}$  and  $I=39.9(10^{-6}) \text{ m}^4$ . [15%] Ans:-14.2 mm



6. Determine the equation of the elastic curve for the beam using the coordinates  $x_1$  and  $x_2$ , and specify the deflection and slope at C.  $EI$  is constant. [20%]



$$\theta_C = \left. \frac{dv_2}{dx_2} \right|_{x_2=0} = -\frac{4M_0L}{3EI}$$

Ans.

The elastic Curves:

$$v_1 = \frac{M_0}{6EIL} [-x_1^3 + L^2x_1]$$

Ans.

$$v_2 = \frac{M_0}{6EIL} [-3Lx_2^3 + 8L^2x_2 - 5L^3]$$

Ans.

$$v_C = v_2|_{x_2=0} = -\frac{5M_0L^2}{6EI}$$

Ans.

The negative sign indicates downward deflection.