

Blade Element Momentum Theory

Exercise 02 : BEM code for the NREL 5MW Wind Turbine

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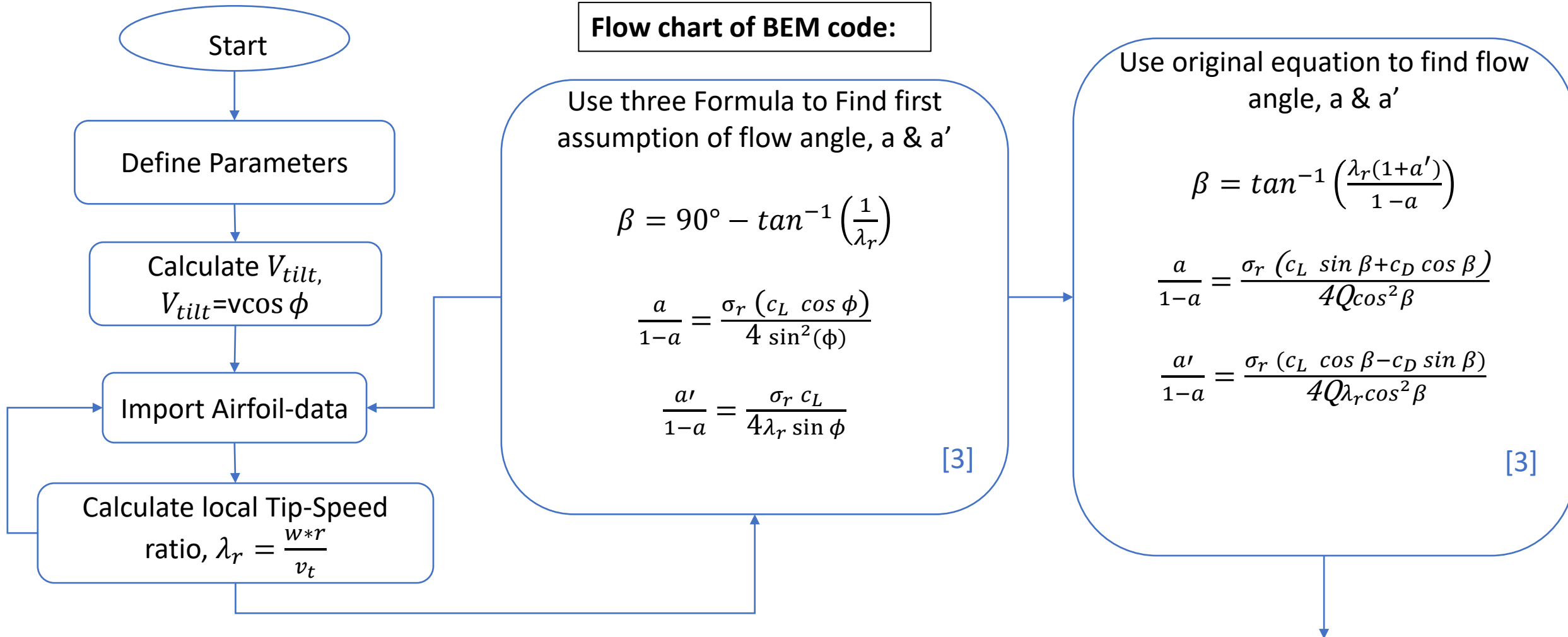
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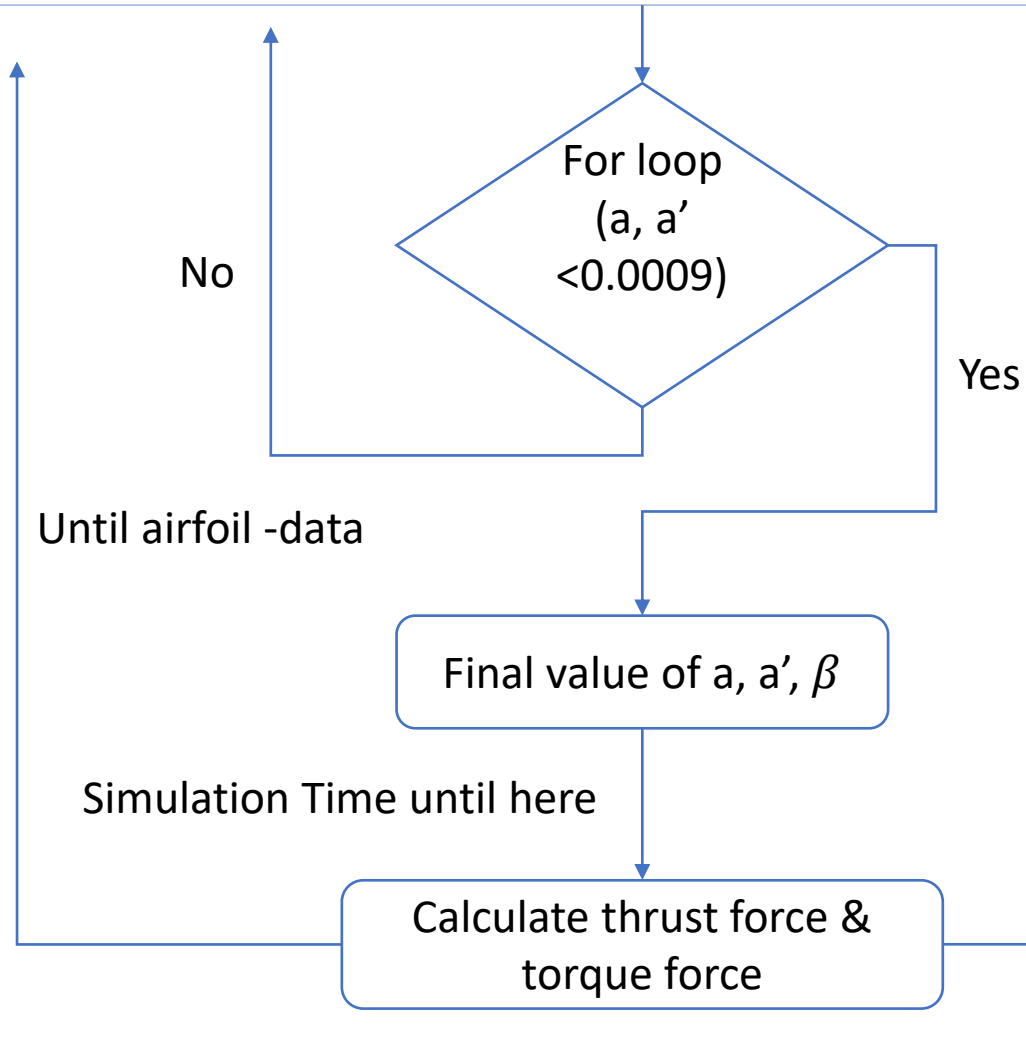


1. Flow Chart

Flow chart of BEM code:



1. Flow Chart



Equation of Thrust and Torque Force:

$$dT = \sigma_r \pi \rho \frac{v_1^2 (1 - a)^2}{\sin^2 \beta} (c_L \cos \beta + c_D \sin \beta) r dr$$

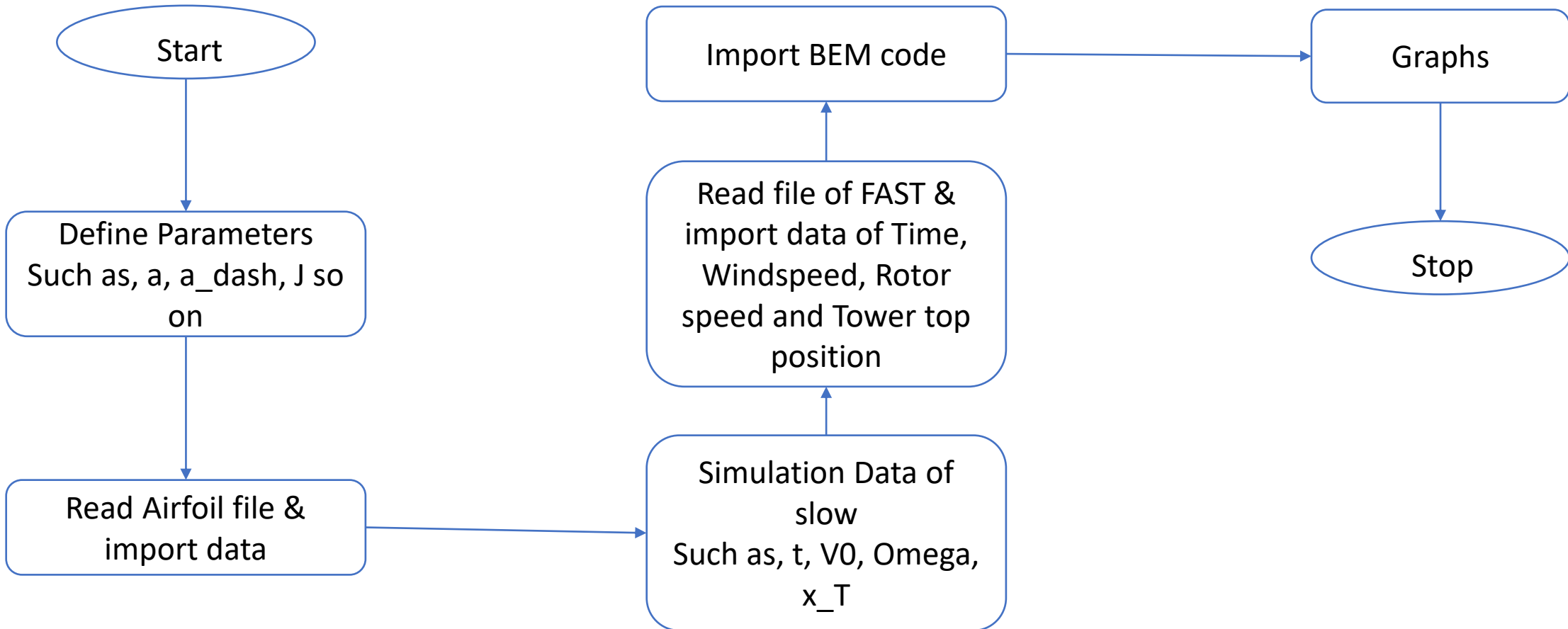
$$dM = \sigma_r \pi \rho \frac{v_1^2 (1 - a)^2}{\sin^2 \beta} (c_L \sin \beta - c_D \cos \beta) r dr$$

[3]



1. Flow Chart

Flow chart of Simulation and comparison of FAST and SLOW code:



2. Highlight of the Code

```
% Iterate to find axial and tangential induction factors
for iter = 1:30
    phi = atan((1 - a) * v_0 / ((1 + ap) * Omega * r)); % Angle of relative flow
    AOA = phi * 180 / pi - TA; % Angle of Attack
    N_airfoil = BEM.NFoil(i); % Number of Airfoils
    L_airfoil = BEM.DRNodes(i); % length of airfoil for each node

    % Compute Cl and Cd directly from the BEM
    Cl = interp1(BEM.AoA{N_airfoil}, BEM.Cl{N_airfoil}, AOA, 'linear', 'extrap');
    Cd = interp1(BEM.AoA{N_airfoil}, BEM.Cd{N_airfoil}, AOA, 'linear', 'extrap');

    % Calculation of axial and tangential induction factor
    Sigma_i = Sigma(i);
    lambda_r_i = lambda_r(i);

    eq1 = @(a_new) a_new / (1 - a_new) - (Sigma_i * Cl * cos(phi)) / (4 * sin(phi)^2);

    eq2 = @(ap_new, a_new) ap_new / (1 - a_new) - (Sigma_i * Cl) / (4 * lambda_r_i * sin(phi));

    a_new = fzero(eq1, a);
    ap_new = fzero(@(ap_new) eq2(ap_new, a_new), ap);
```

MATLAB
a & a'

2. Highlight of the Code

```
106. # Function to calculate the new flow angle (new_beta)
107. def new_Beta(local_tsr, a, a_dash):
108. return math.degrees(math.atan((local_tsr * (1 + a_dash)) / (1 - a)))
109. # Function to calculate the axial induction factor (a)
110. def axial_induction_factor(B, c, r, new_beta, Cl):
111. Q = ((2 / math.pi) * math.acos(math.exp(-((B / 2) * (1 - r / R)) / (r / R *
    math.cos(math.radians(new_beta))))))
112. Solidity = (B * c / (2 * math.pi * r))
113. numerator = Solidity * Cl * math.sin(math.radians(new_beta))
114. denominator = 4 * Q * (math.cos(math.radians(new_beta))**2) + Solidity * Cl *
    math.sin(math.radians(new_beta))
115. return numerator / denominator
116. # Function to calculate the tangential induction factor (a_dash)
117. def tangential_induction_factor(B, c, r, new_beta, a, Cl, Cd):
118. Q = ((2 / math.pi) * math.acos(math.exp(-((B / 2) * (1 - r / R)) / (r / R *
    math.cos(math.radians(new_beta))))))
119. Solidity = (B * c / (2 * math.pi * r))
120. numerator = Solidity * (1 - a) * Cl
121. denominator = 4 * Q * ((2 * math.pi * blade_rotational_speed * r) / (Vt * 60)) *
    (math.cos(math.radians(new_beta)))
122. return numerator / denominator
```

PYTHON
a & a'

Q = Tip loss correction factor

Cl & Cd

Vt = Tilt Velocity

2. Highlight of the Code

MATLAB Thrust & Torque

% Thrust force and moment calculation for each airfoil

```
Thrust_in_points(i) = Sigma_i * pi * rho * v_0^2 * (1 - a)^2 * (Cl * cos(phi) + Cd * sin(phi)) * r * L_airfoil / sin(phi)^2;  
Moment_in_points(i) = Sigma_i * pi * rho * v_0^2 * (1 - a)^2 * (Cl * sin(phi) - Cd * cos(phi)) * r^2 * L_airfoil / sin(phi)^2;  
end
```

% Total of Thrust force and moment

```
F_a = sum(Thrust_in_points);  
M_a = sum(Moment_in_points);  
end
```


2. Highlight of the Code

PYTHON Thrust & Torque

```
190. # Function to calculate aerodynamic thrust force for each section
191. def aerodynamic_thrust_force(B, Beta, a, Density, Vt, r):
192. Solidity = (B * c / (2 * math.pi * r))
193. thrust = (Solidity * math.pi * Density * Vt**2 * (1 - a)**2 * (Cl * math.sin(math.radians(Beta)) + Cd * math.cos(math.radians(Beta))) * r * DRNodes) /
           math.cos(math.radians(Beta))**2
194. return thrust
195. # Function to calculate aerodynamic torque force for each section
196. def aerodynamic_torque(B, R, Beta, a, a_dash, Density, Vt, r, blade_rotational_speed):
197. Solidity = (B * c / (2 * math.pi * r))
198. torque = (Solidity * math.pi * Density * Vt**2 * (1 - a)**2 * (Cl * math.cos(math.radians(Beta)) - Cd * math.cos(math.radians(Beta))) * r**2 * DRNodes) /
           math.cos(math.radians(Beta))**2
199. return torque
```

2. Highlight of the Code

MATLAB
RK4

```
% simulation using Runge kutta 4
```

```
Tic
```

```
for k = 1:n-1
```

```
k1 = dt * SLOW(x(k,:), v_0(k), Parameter);
```

```
k2 = dt * SLOW(x(k,:) + 0.5 * k1, v_0(k) + 0.5 * dt, Parameter);
```

```
k3 = dt * SLOW(x(k,:) + 0.5 * k2, v_0(k) + 0.5 * dt, Parameter);
```

```
k4 = dt * SLOW(x(k,:) + k3, v_0(k) + dt, Parameter); x(k+1,:) = x(k,:) + (1/6) * (k1 + 2*k2 + 2*k3 + k4);
```

```
End
```

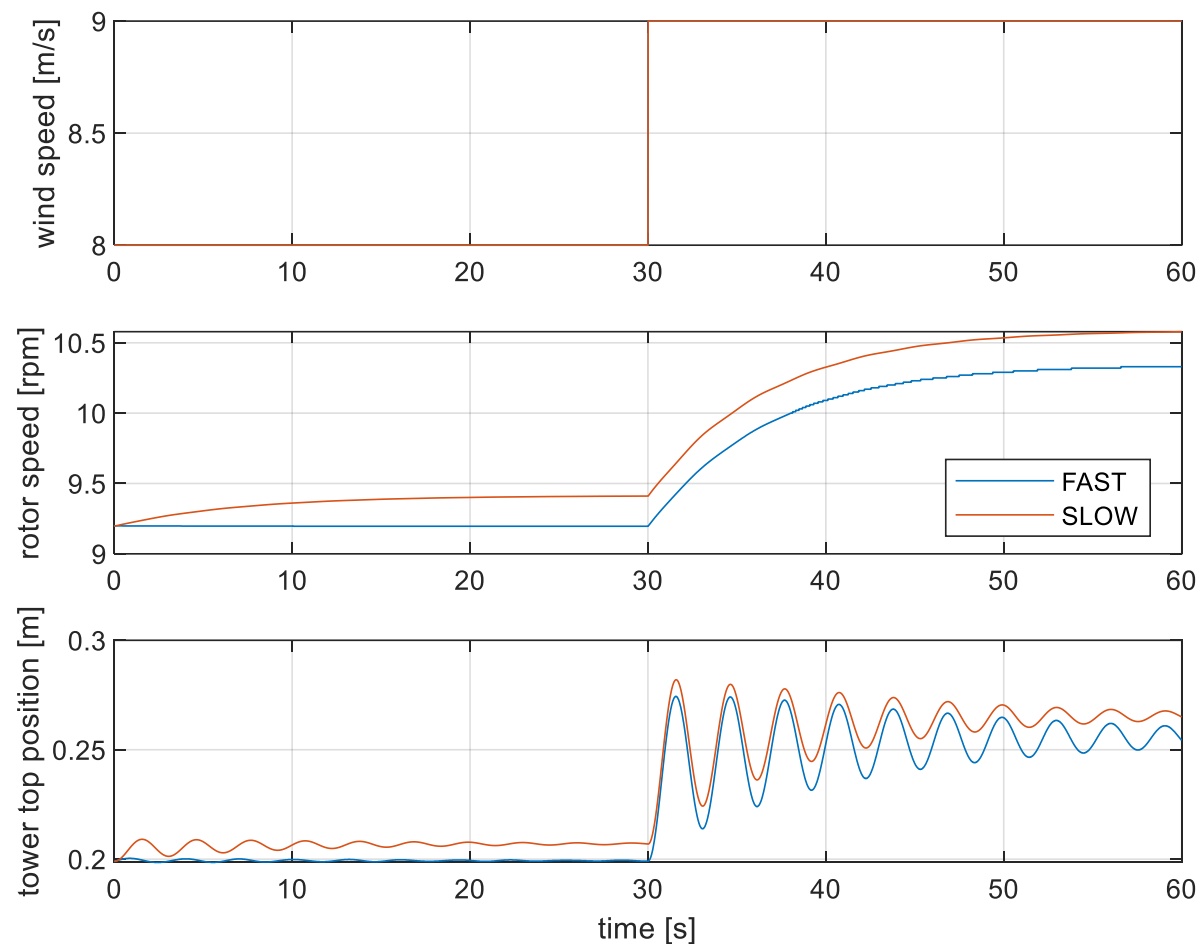
```
TimeRatio = TMax/toc;
```

2. Highlight of the Code

Python
RK4

```
189. # Simulation using Runge Kutta 4
190. start_time = time.time()
191. for k in range(n - 1):
192. k1 = dt * self.slow(x[k, :], v_0[k], parameters)
193. k2 = dt * self.slow(x[k, :] + 0.5 * k1, v_0[k] + 0.5 * dt, parameters)
194. k3 = dt * self.slow(x[k, :] + 0.5 * k2, v_0[k] + 0.5 * dt, parameters)
195. k4 = dt * self.slow(x[k, :] + k3, v_0[k] + dt, parameters)
196. x[k + 1, :] = x[k, :] + (1 / 6) * (k1 + 2 * k2 + 2 * k3 + k4)
197. end_time = time.time()
198. TimeRatio = TMax / (end_time - start_time)
199. print(f"Time Ratio (Sim/CPU): = {TimeRatio:.4f} MN")
```

3. Results



Graphs &
Compare with FAST

Time Ratio SLOW (Sim/CPU): 0.998007

4. Problems and Solutions

1. Calculation of thrust force and torque for each blade section as we were taking fixed wind speed instead of Wind vector.
2. No supporting files for python as provided in MATLAB, so implementation of supporting files in main code were main issue.
3. Facing problems in generating graph in python.

5. Summary

We implemented the BEM code using both Python and MATLAB.

Python Implementation:

In our Python implementation, we followed the formula provided by G. Ingram [\[3\]](#). However, due to time constraints and difficulties in converting all supporting files from MATLAB to Python, we were unable to create graphs. Although we started, but it is not yet complete.

MATLAB Implementation:

In MATLAB, we followed to the notes from Professor's Lecture 02 [\[7\]](#). Using MATLAB, we were able to obtain results and compare them with OPENFAST.

6. Contribution

Topic	Contribution person name
Aerodynamic concepts	Karan Soni , Rahul Patil, Mostafa Mozafary
BEM code in python	Karan Soni, Rahul Patil
BEM code in MATLAB	Mostafa Mozafary, Rahul Patil
Presentation	Manthan Patel, Hassan Pour Saeid
Review and changes in Presentation	Karan Soni , Rahul Patil, Mostafa Mozafary

References

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2. J. Jonkman and M. L. Buhl. FAST User's Guide. Tech. rep. EL-500-38230. NREL, 2005. URL: <https://www.nrel.gov/docs/fy06osti/38230.pdf>.
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5. Python Software Foundation. The Python Standard Library. From <https://docs.python.org> .
6. Prof. Ragunathan Rengasamy. " Python for Data science, IIT Madras " [Online Lecture]. <https://nptel.ac.in>.
7. Prof. Dr.-Ing. David Schlipf. "Lecture #1 Introduction to Wind Turbine Aerodynamics" [Lecture notes]. 25.03.2024.