

Decision Tree:

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$x_1, x_2, \dots, x_n$

$y$

Node: features

leaf:  $y$

ALGO'S:

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ID3:

(iterative dichotomiser3)

Entropy & Information Gain functions

CART:

(classification and regression tree)

Gini function

steps in ID3:

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1. calculate entropy of dataset(target)
2. calculate entropy of each feature
3. calculate information gain of each feature
4. highest gain feature becomes root node.
5. repeat same steps to build complete tree.

1.

find out classes in dataset.

prob of class yes:

frequency of yes/no of samples

9/14

.642

prob of class no:

frequency of yes/no of samples

5/14

.358

$p(\text{yes}) * \log_2(p(\text{yes})) = .642 * (-0.63935479754) = -0.409152$

$p(\text{no}) * \log_2(p(\text{no})) = .358 * (-1.4819685074) = -0.530544$

$\text{entropy}(t) = -[p(\text{yes}) * \log_2(p(\text{yes})) + p(\text{no}) * \log_2(p(\text{no}))]$

=0.94

$H(T) = -\text{Sum}[p(c_i) * \log_2(p(c_i))]$

2.

2.1 Outlook:

find out unique values:

rainy

overcast

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sunny

entropy of rainy:
-[3/5*log2(3/5)+2/5*log2(2/5)]
=.971
entropy of overcast:
-[4/4*log2(4/4)]
=0
entropy of sunny:
-[3/5*log2(3/5)+2/5*log2(2/5)]
=.971

average entropy of outlook:
e(rainy)*p(r)+e(o)*p(o)+e(s)*p(s)
(.971*5/14)+0+. (971*5/14)
=.69

```

## 2.2 Temperature:

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find out unique values:
hot
cool
mild

entropy of hot:
-[2/4*log2(2/4)+2/4*log2(2/4)]
=1
entropy of cool:
-[3/4*log2(3/4)+1/4*log2(1/4)]
=0.811
entropy of mild:
-[4/6*log2(4/6)+2/6*log2(2/6)]
=0.918

average entropy of temperature:
e(hot)*p(hot)+e(cool)*p(cool)+e(mild)*p(mild)
(1*4/14)+(.811*4/14)+. (918*6/14)
=.92

```

## 2.3 Humidity:

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find out unique values:
high
normal

entropy of high:
-[3/7*log2(3/7)+4/7*log2(4/7)]
=.985
entropy of normal:
-[6/7*log2(6/7)+1/7*log2(1/7)]
=.591

average entropy of :
e(high)*p(high)+e(normal)*p(normal)
(.98*7/14)+(.591*7/14)
=.79

```

## 2.3 Windy:

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find out unique values:

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        true
        false

entropy of true:
    -[3/6*log2(3/6)+3/6*log2(3/6)]
    =1
entropy of false:
    -[6/8*log2(6/8)+2/8*log2(2/8)]
    =.811

average entropy of :
e(true)*p(true)+e(false)*p(false)
(1*6/14)+(.811*8/14)
=.892

```

3.

```

Information Gain of Outlook:
H(t)-H(Outlook)
=.94-.69
=.25

```

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Information Gain of Temperature:
H(t)-H(temperature)
=.94-.92
=.02

```

```

Information Gain of Humidity:
H(t)-H(Humidity)
=.94-.79
=.15

```

```

Information Gain of Windy:
H(t)-H(Windy)
=.94-.892
=.048

```

Now outlook is root node:  
 overcast is always yes  
 rainy,sunny need further splitting.

Rainy:

Outlook	Temp	Humidity	Windy	Play
Rainy	Hot	High	FALSE	No
Rainy	Hot	High	TRUE	No
Rainy	Mild	High	FALSE	No
Rainy	Cool	Normal	FALSE	Yes
Rainy	Mild	Normal	TRUE	Yes

repeat untill we get leaf....