

Segmentation

簡韶逸 Shao-Yi Chien

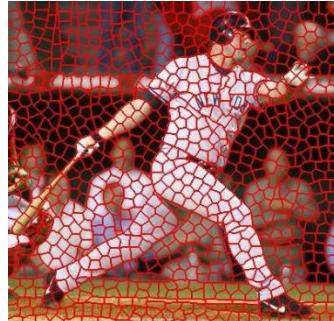
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National Taiwan University

Outline

- Segmentation
- Image segmentation
 - Object selection with interactive segmentation
 - Super-pixel methods
 - Semantic segmentation
- Video segmentation
 - Segmentation in motion field
 - Change detection method

Segmentation

- Group pixels that share similar attributes in perception into regions
 - Over-segmentation v.s. under-segmentation

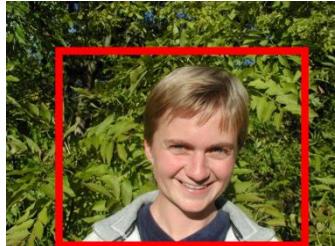


- Used as pre-processing or post-processing
- Select region-of-interest (ROI) in an image/video with/without users' inputs (ex. stroke)

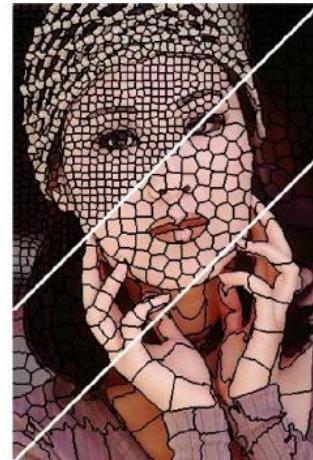
What We Will Introduce Today

Image Segmentation

Object Selection



Super-pixel



Semantic Segmentation



Video Segmentation

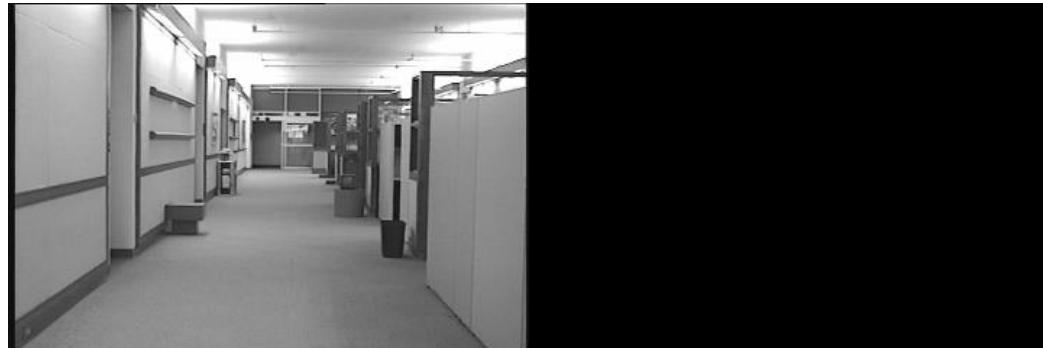


Image Segmentation: Object Selection with Interactive Segmentation

- Select region-of-interest (ROI) in an image/video with users' help
- Active contour
- Graphcut/Grabcut
- Deep interactive object selection



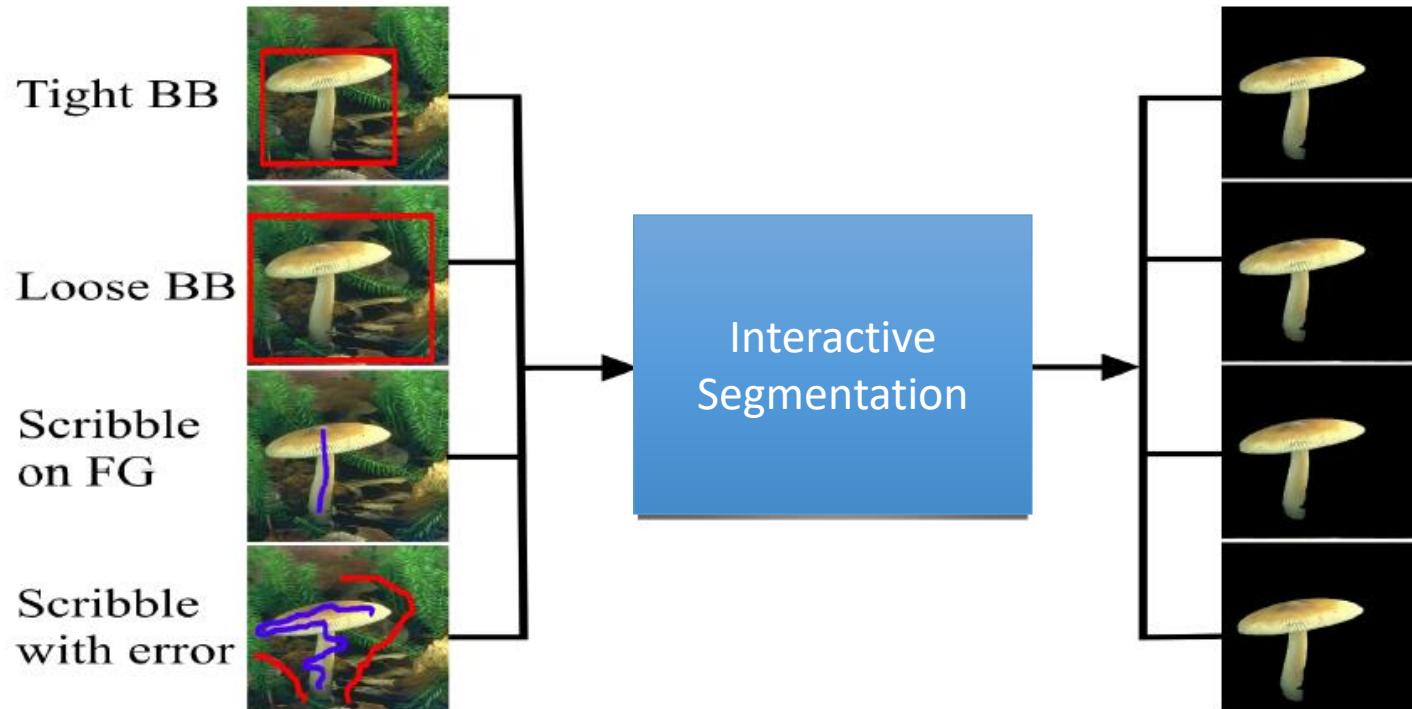
Where is the Foreground?

- Determining foreground objects is subjective
 - All people and horses, or...
 - The person in the middle



The Form of User Input

- Some examples



The Form of User Input

- Clicks



Active Contour

- To minimize the total energy of an active contour

$$\mathcal{E}_{int} + \mathcal{E}_{ext}$$

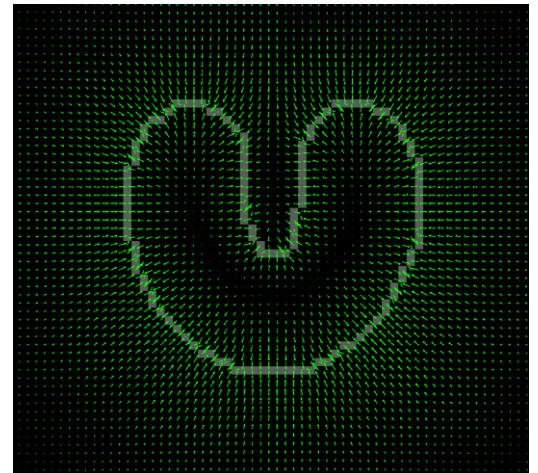
$$\mathcal{E}_{int} = \int \alpha(s) \|\mathbf{f}_s(s)\|^2 + \beta(s) \|\mathbf{f}_{ss}(s)\|^2 ds$$

$$\begin{aligned} E_{int} &= \sum_i \alpha(i) \|f(i+1) - f(i)\|^2 / h^2 \\ &\quad + \beta(i) \|f(i+1) - 2f(i) + f(i-1)\|^2 / h^4 \end{aligned}$$

$$\mathcal{E}_{image} = w_{line} \mathcal{E}_{line} + w_{edge} \mathcal{E}_{edge} + w_{term} \mathcal{E}_{term}$$

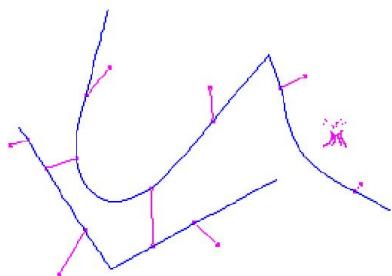
$$E_{edge} = \sum_i -\|\nabla I(\mathbf{f}(i))\|^2$$

$$E_{spring} = k_i \|\mathbf{f}(i) - \mathbf{d}(i)\|^2$$



Active Contour

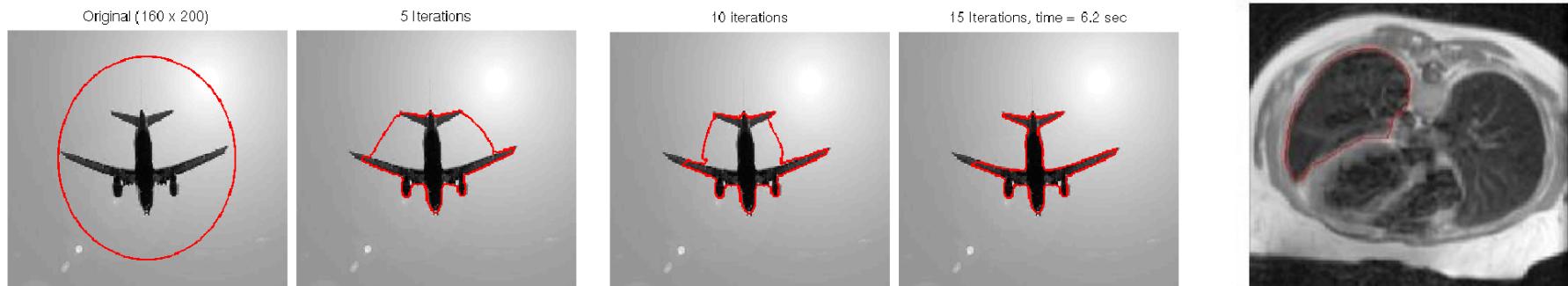
- To minimize the total energy of an active contour



(a)

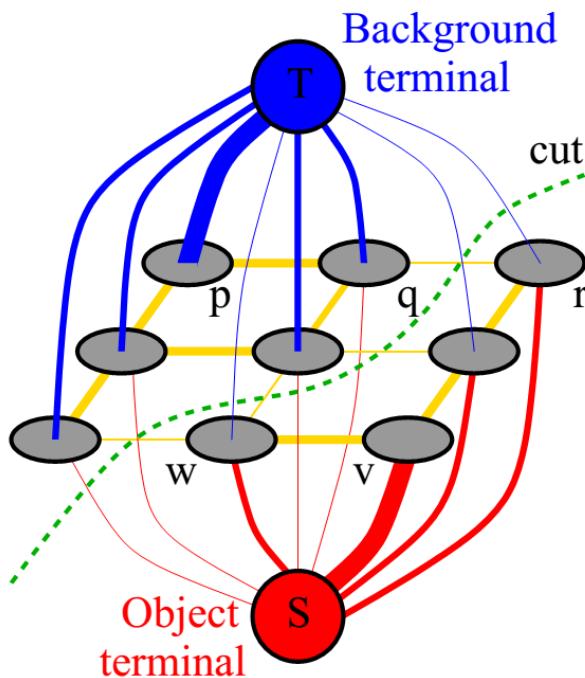


(b)



Graphcut

- Formulate the problem as a Markov-Random-Field (MRF)



$$E(A) = \lambda \cdot R(A) + B(A)$$

Region Properties
Term (Data Term)
Boundary
Properties Term
(Smooth Term)

$$R(A) = \sum_{p \in \mathcal{P}} R_p(A_p)$$

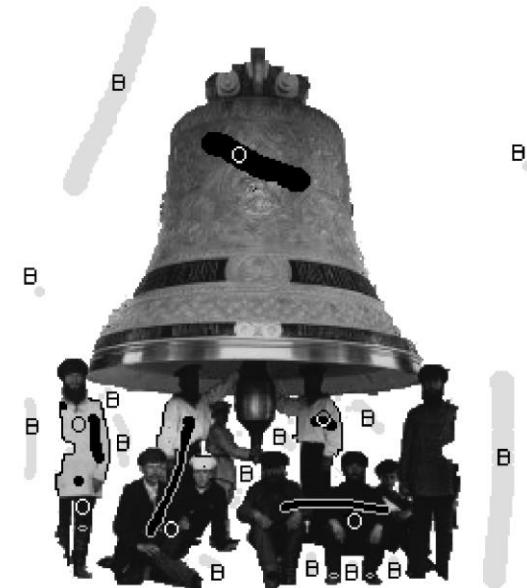
$$B(A) = \sum_{\{p,q\} \in \mathcal{N}} B_{\{p,q\}} \cdot \delta(A_p, A_q)$$

$$\delta(A_p, A_q) = \begin{cases} 1 & \text{if } A_p \neq A_q \\ 0 & \text{otherwise.} \end{cases}$$

[Boykov and Jolly ICCV 2001]

Graphcut

- An example



$$R_p(\text{"obj"}) = -\ln \Pr(I_p | \mathcal{O})$$

Can be modeled by histogram

$$R_p(\text{"bkg"}) = -\ln \Pr(I_p | \mathcal{B})$$

$$B_{\{p,q\}} \propto \exp\left(-\frac{(I_p - I_q)^2}{2\sigma^2}\right) \cdot \frac{1}{dist(p, q)}$$

[Boykov and Jolly ICCV 2001]

GrabCut

[Rother, Kolmogorov, Blake SIGGRAPH 2004]

1. Define graph

- usually 4-connected or 8-connected
 - Divide diagonal potentials by $\sqrt{2}$

2. Define unary potentials

- Color histogram or mixture of Gaussians for background and foreground

$$\text{unary_potential}(x) = -\log \left(\frac{P(c(x); \theta_{foreground})}{P(c(x); \theta_{background})} \right)$$

3. Define pairwise potentials

$$\text{edge_potential}(x, y) = k_1 + k_2 \exp \left\{ \frac{-\|c(x) - c(y)\|^2}{2\sigma^2} \right\}$$

4. Apply graph cuts

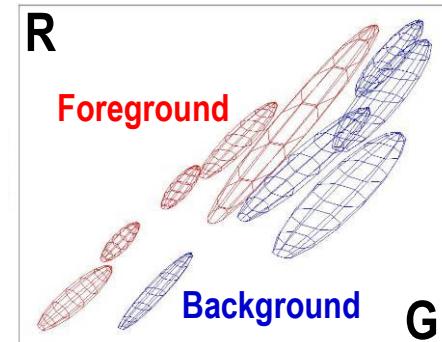
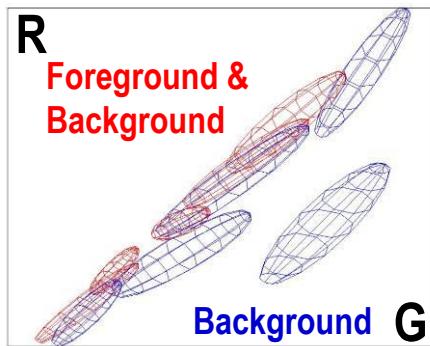
5. Return to 2, using current labels to compute foreground, background models

GrabCut

- Color model



Iterated
graph cut



Gaussian Mixture Model (typically 5-8 components)

GrabCut

- Easier examples



GrabCut

- More difficult examples

Initial
Rectangle



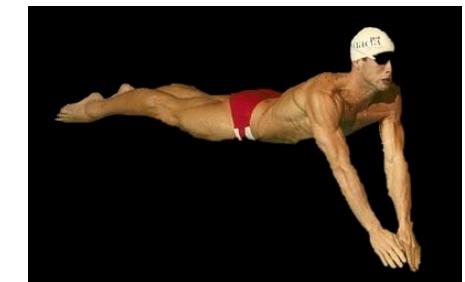
Fine structure



Harder Case

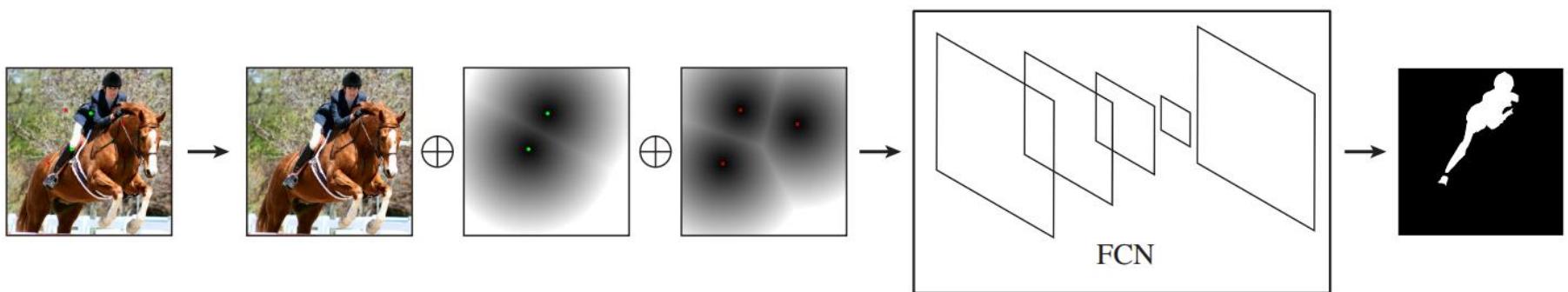


Initial
Result



Deep Interactive Segmentation

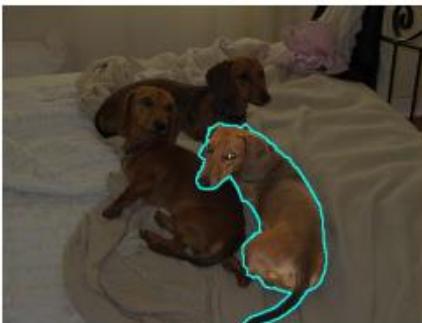
- FCN model
- User clicks are transformed into distance maps
- Input color image and the user clicks are cascaded as 5D input features



Ref: Ning Xu, Brian Price, Scott Cohen, Jimei Yang, Thomas Huang. Deep Interactive Object Selection. In *CVPR 2016*

Deep Interactive Segmentation

- Select different instances
- Select different parts



Ref: Ning Xu, Brian Price, Scott Cohen, Jimei Yang, Thomas Huang. Deep Interactive Object Selection. In *CVPR 2016*

Deep Interactive Segmentation

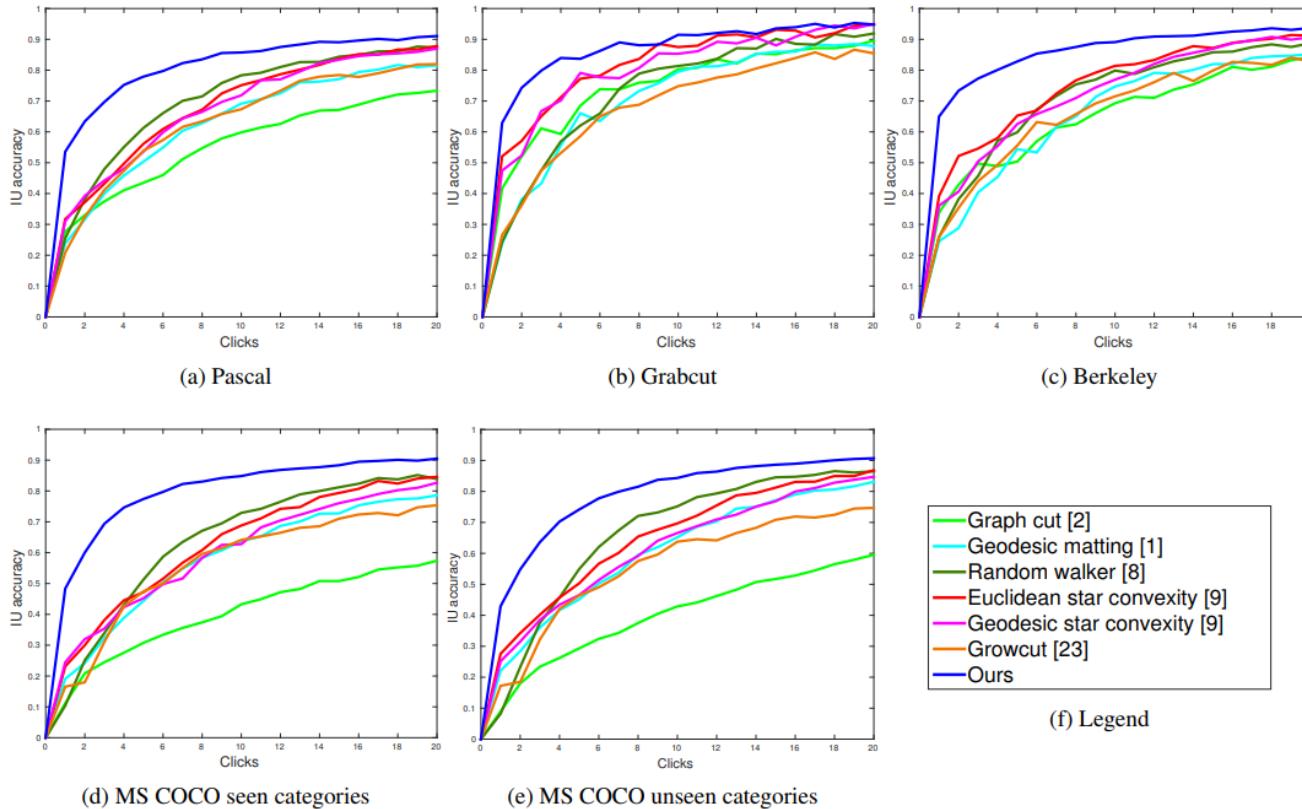
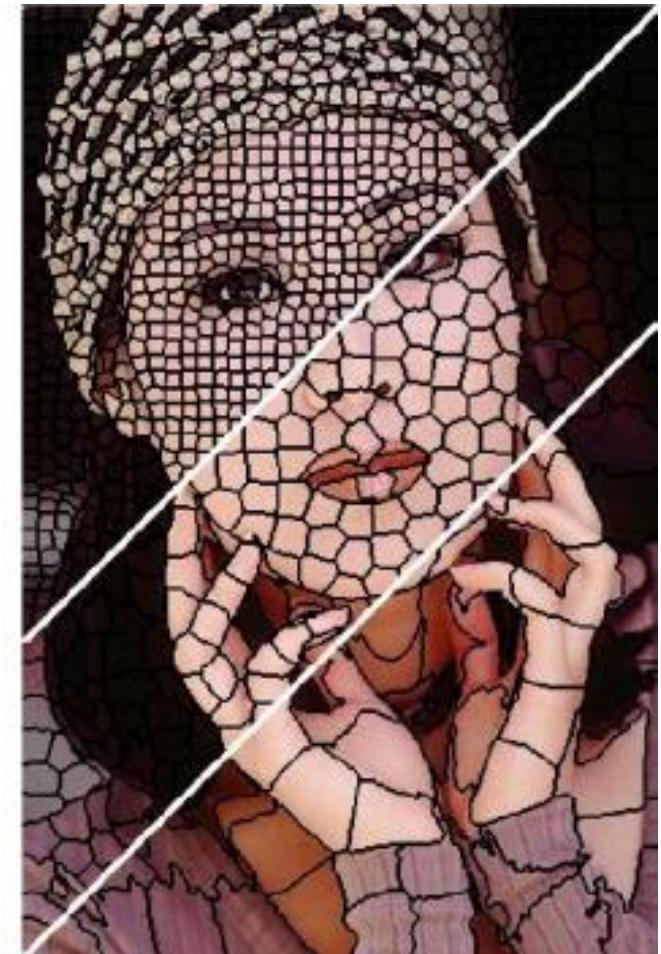
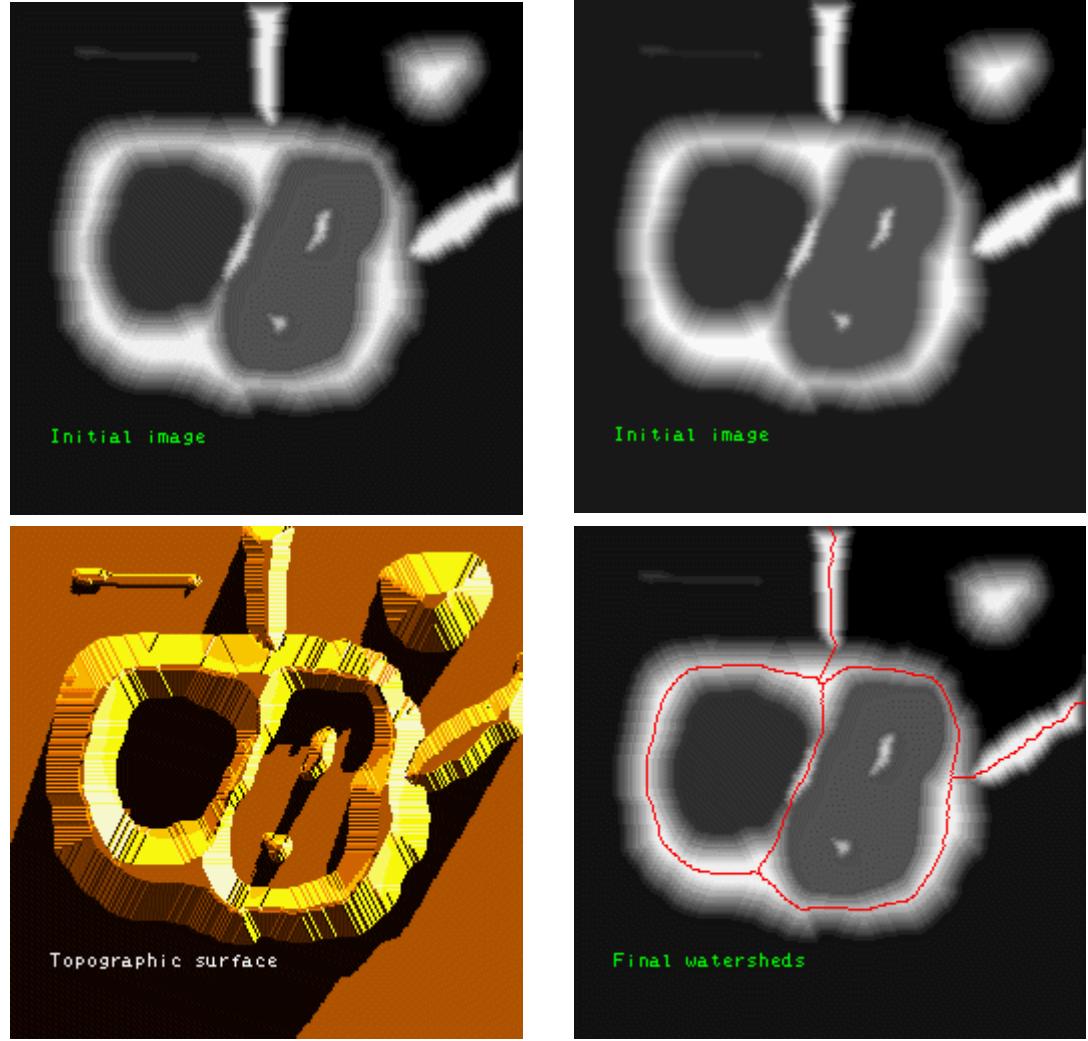
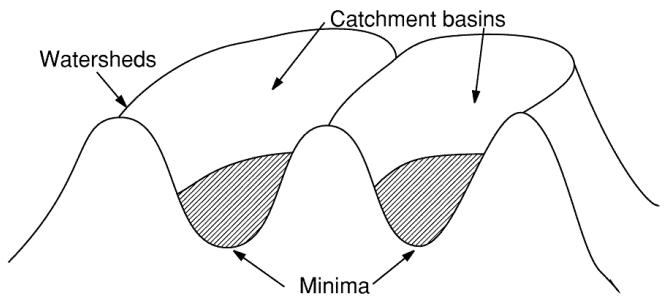


Image Segmentation: Superpixel

- Superpixels are grouping of pixels (over-segmentation)
- Watershed
- K-means
- Mean-shift
- Modern superpixel

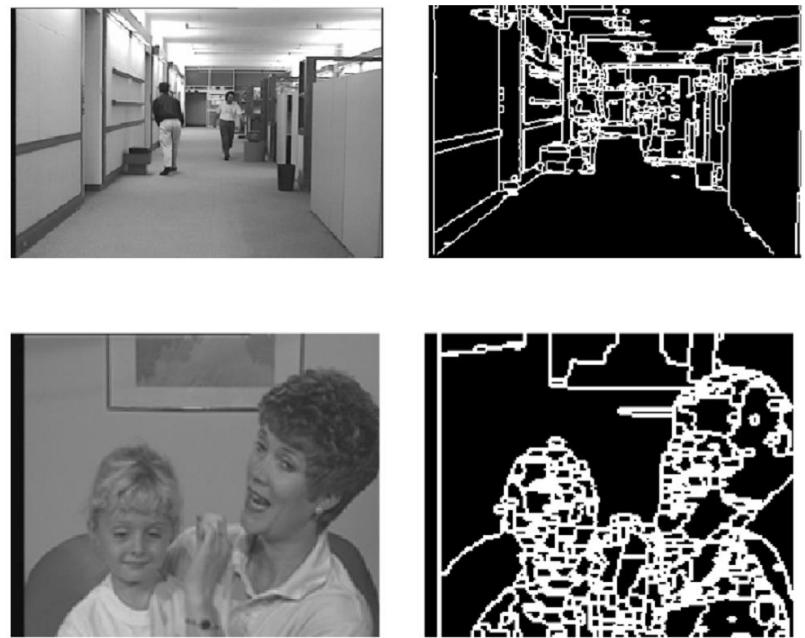
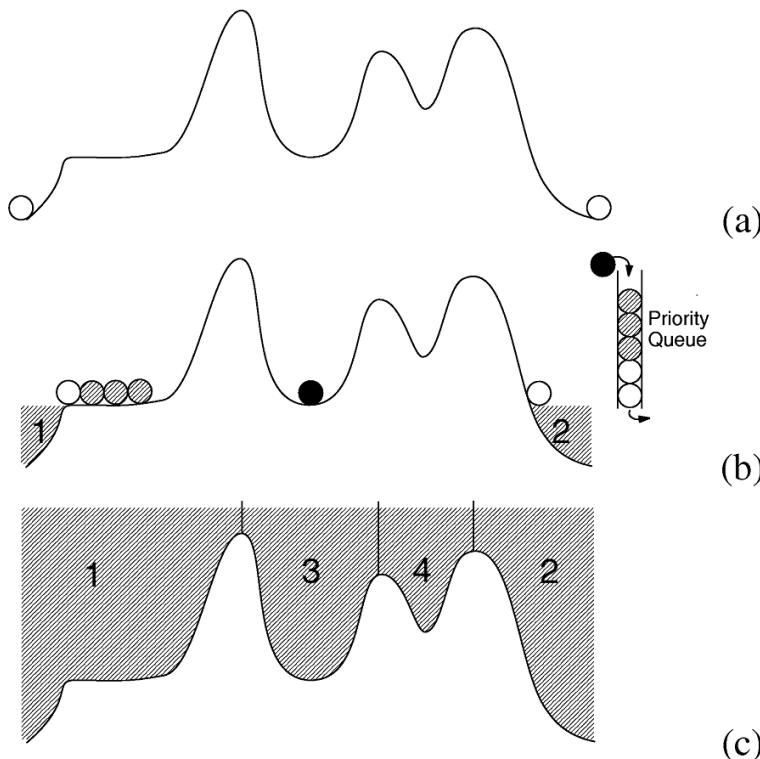


Watershed



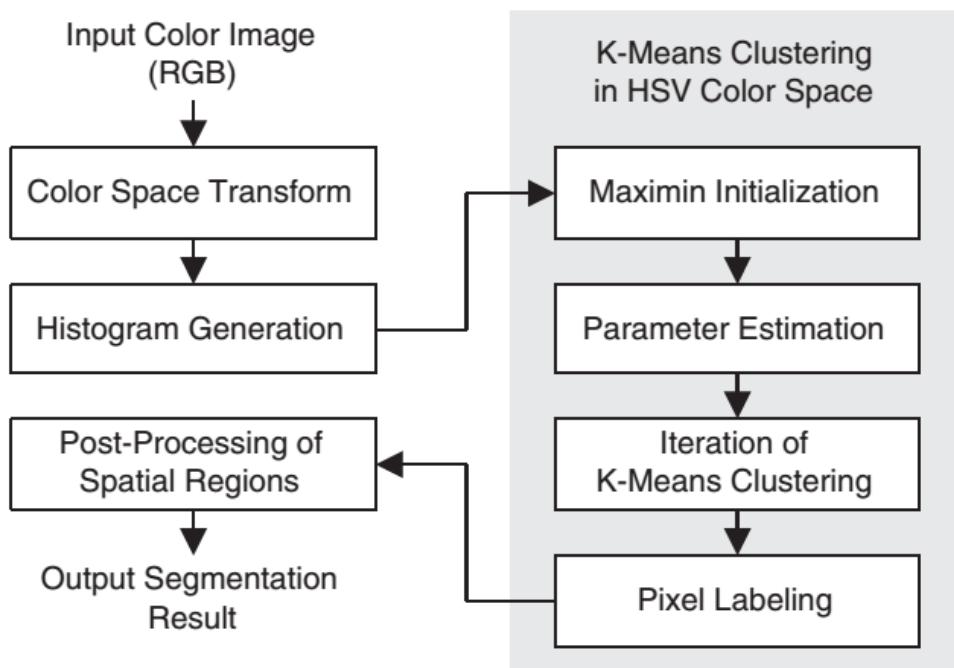
Watershed

- Can be implemented efficiently



Ref: S.-Y. Chien, Y.-W. Huang, and L.-G. Chen, "Predictive Watershed: A Fast Watershed Algorithm for Video Segmentation," *IEEE T. Circuits and Systems for Video Technology*, 2003.

K-means



- K-means in HSV color space
- The H term should be handled carefully

$$D^2(\mathbf{B}_i, \mathbf{C}_j^{(t)}) = D_h^2(h_i, h_j^{(t)}) + (s_i - s_j^{(t)})^2 + (v_i - v_j^{(t)})^2,$$

where

$$D_h^2(h_i, h_j^{(t)}) = \begin{cases} (\frac{360^\circ}{h_Q} - |h_i - h_j^{(t)}|)^2, & \text{if } |h_i - h_j^{(t)}| > \frac{180^\circ}{h_Q} \\ (h_i - h_j^{(t)})^2, & \text{otherwise.} \end{cases}$$

K-means



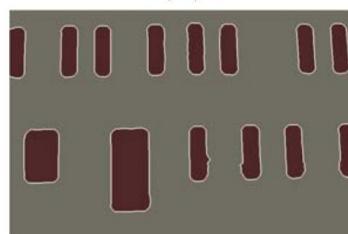
(a)



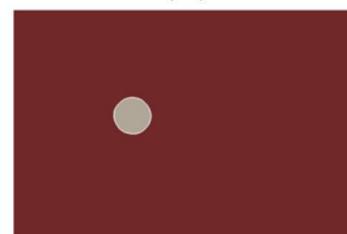
(b)



(c)



(d)



(e)



(f)



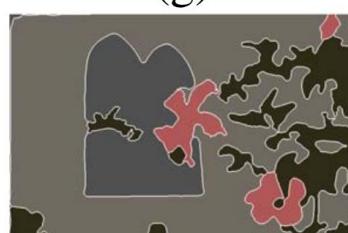
(g)



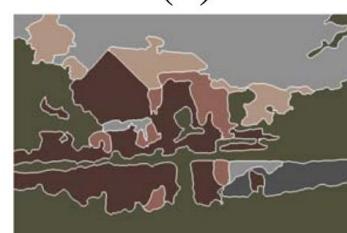
(h)



(i)



(j)



(k)

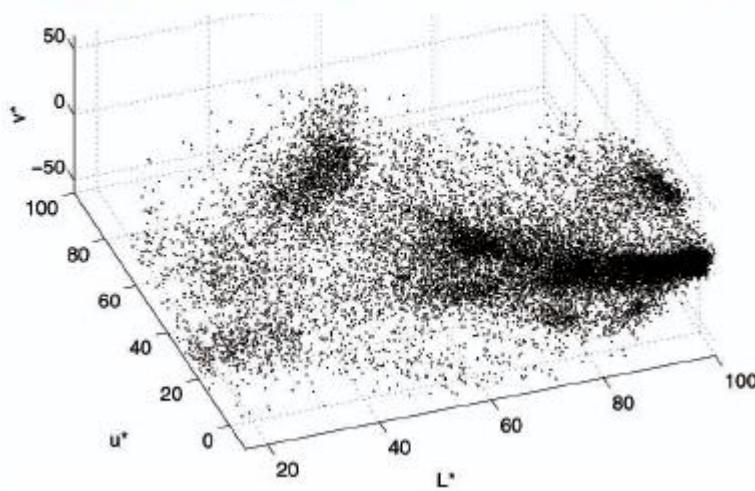
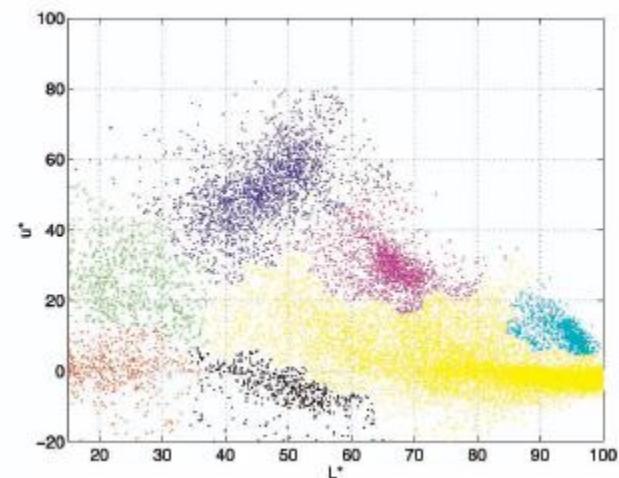
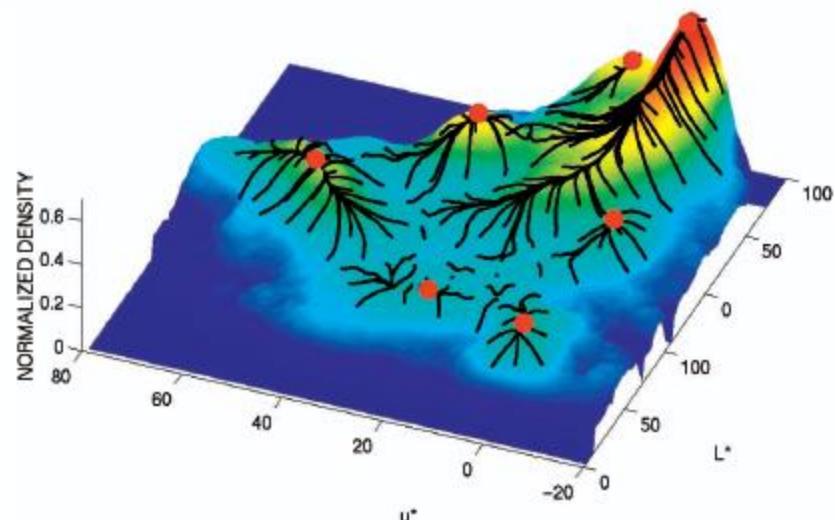


(l)

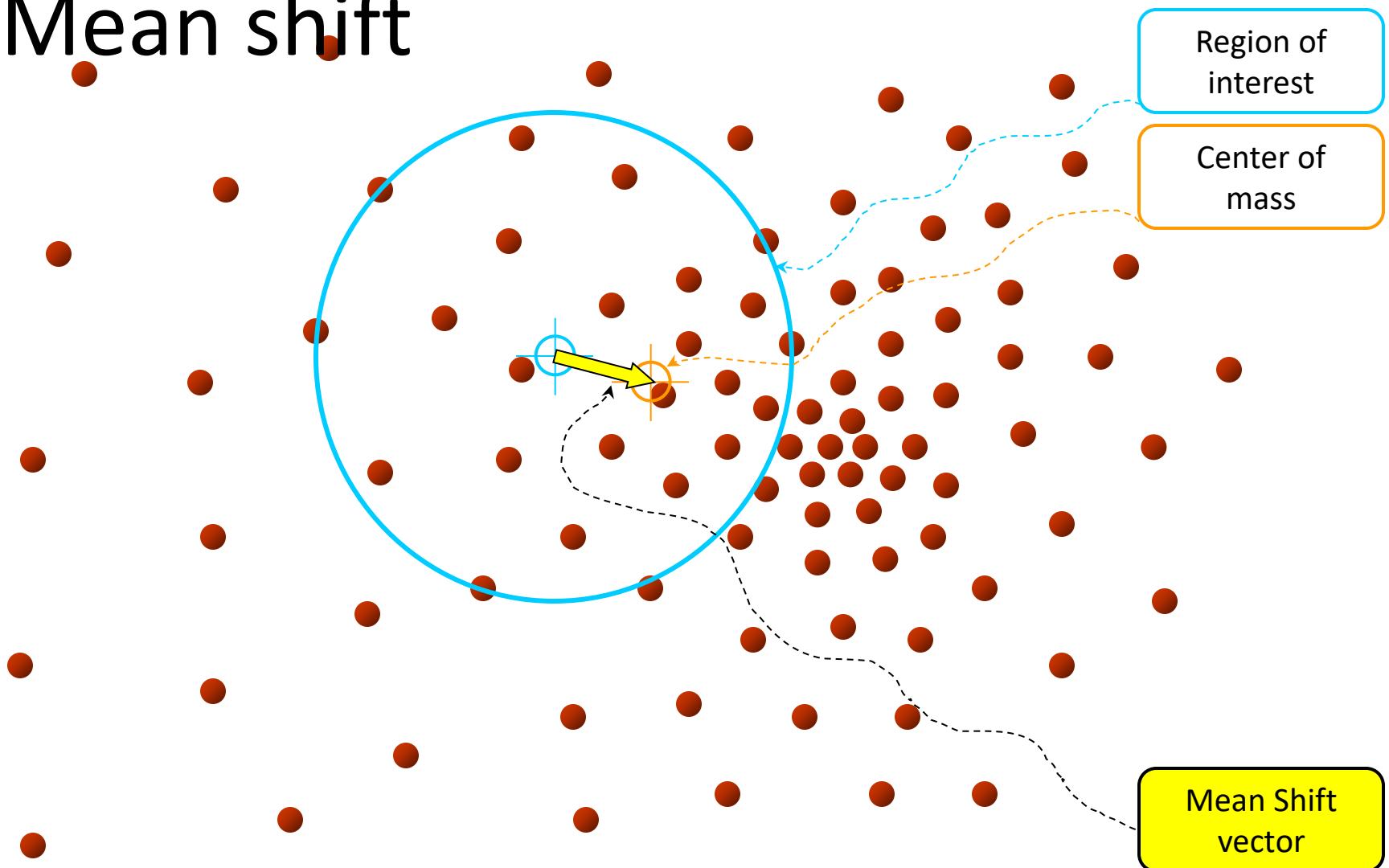
Ref: T.-W. Chen, Y.-L. Chen, and S.-Y. Chien, “Fast Image Segmentation Based on K-Means Clustering with Histograms in HSV Color Space,” MMSP2008.

Mean-shift Algorithm

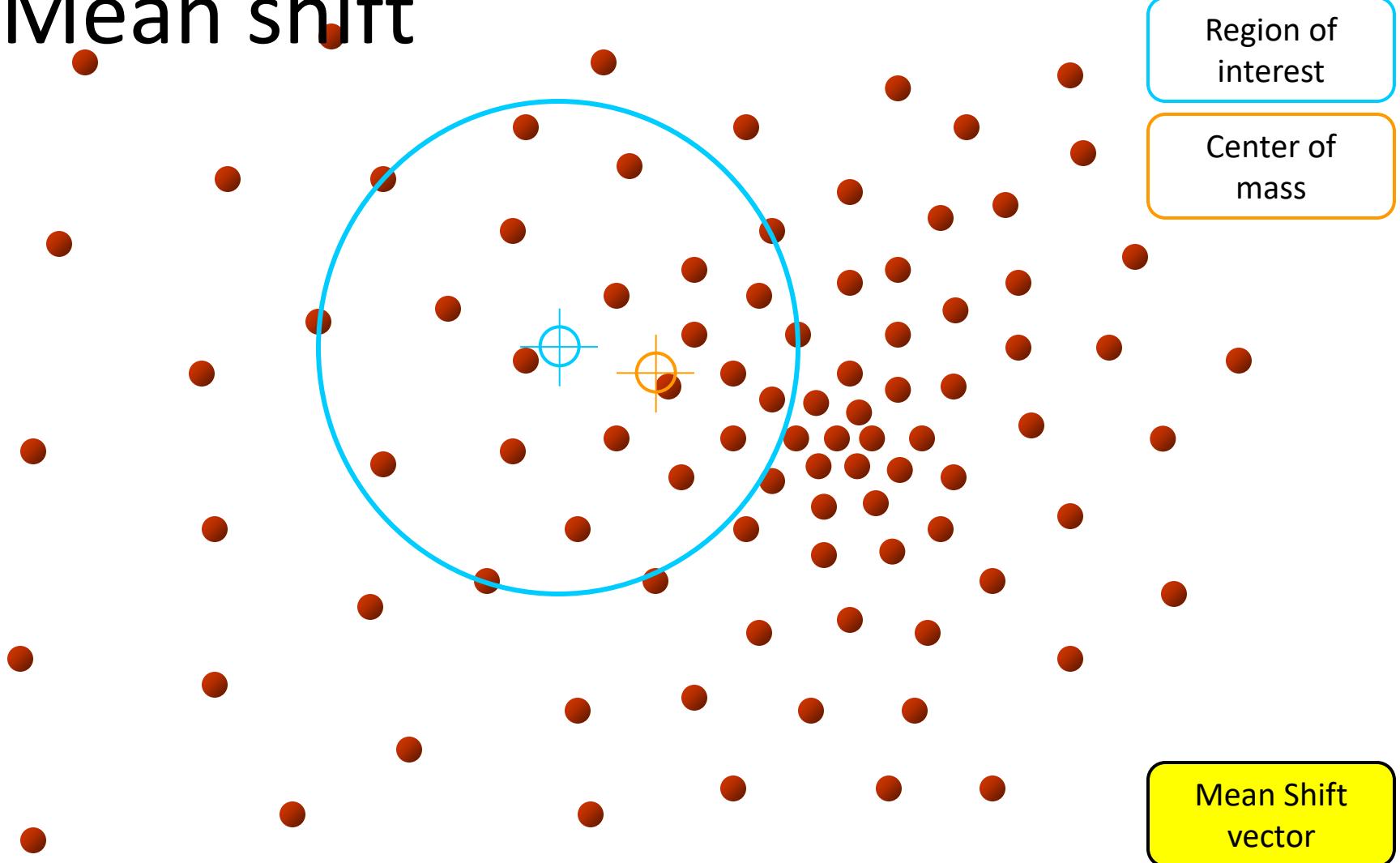
- Try to find *modes* of this non-parametric density



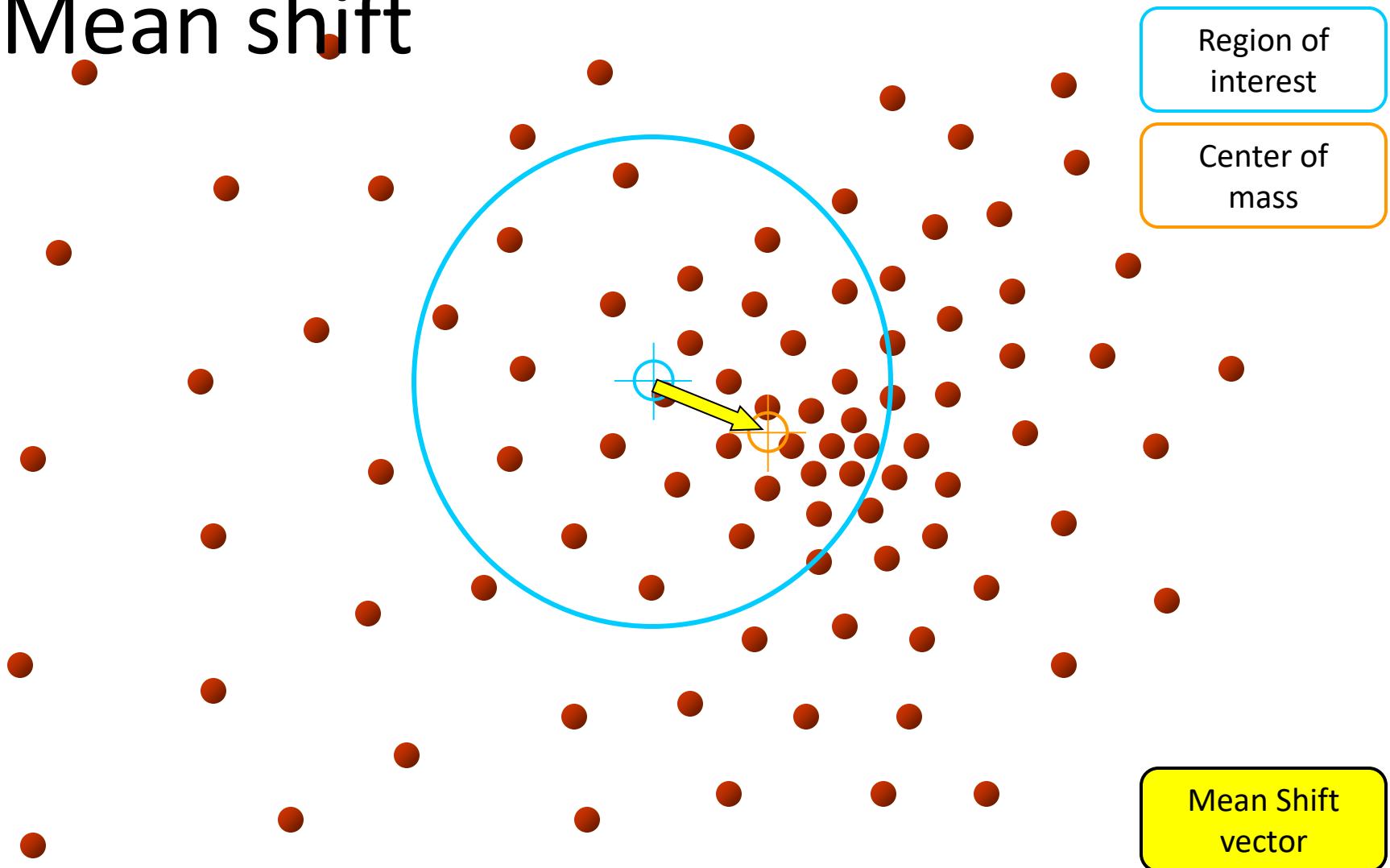
Mean shift



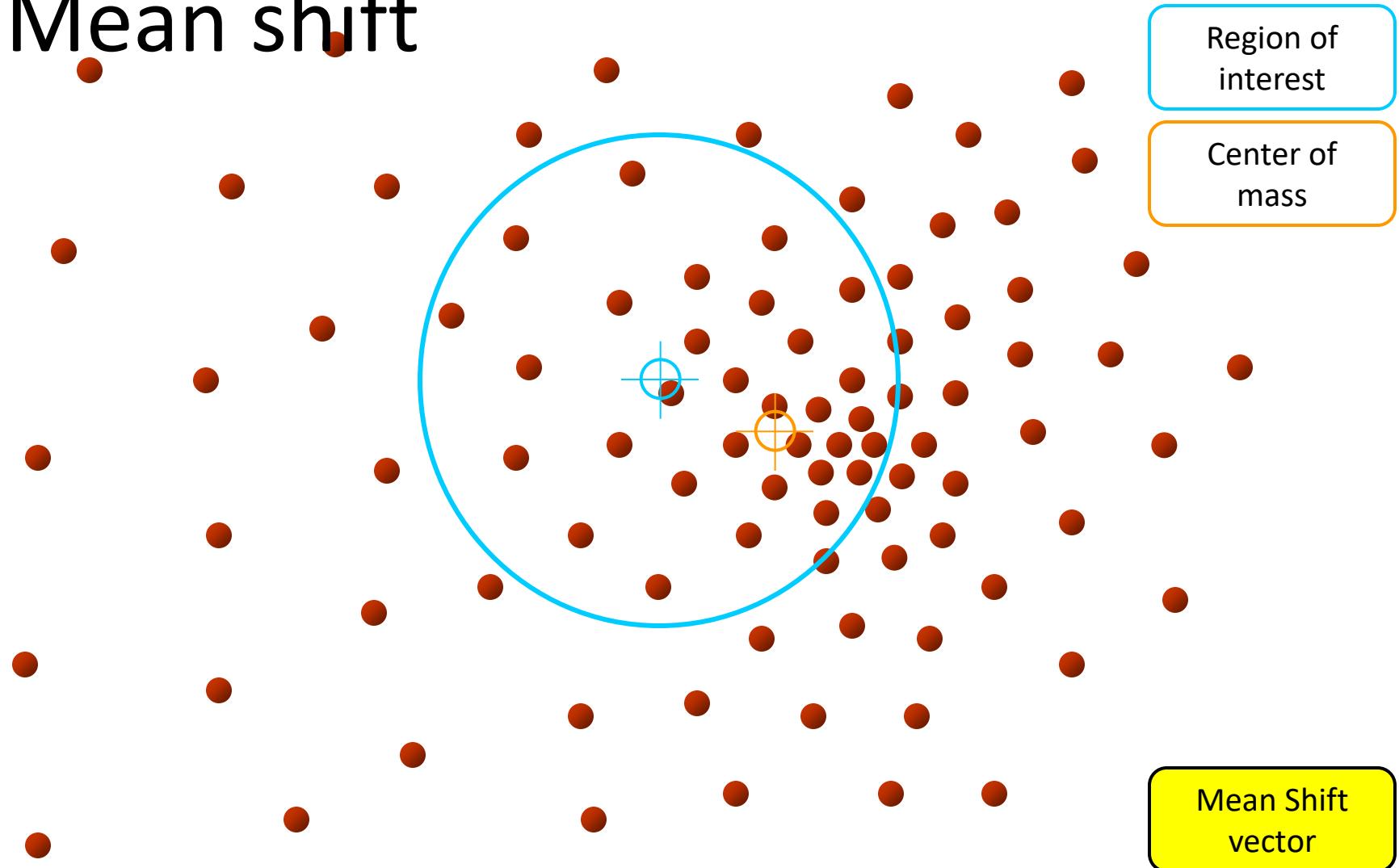
Mean shift



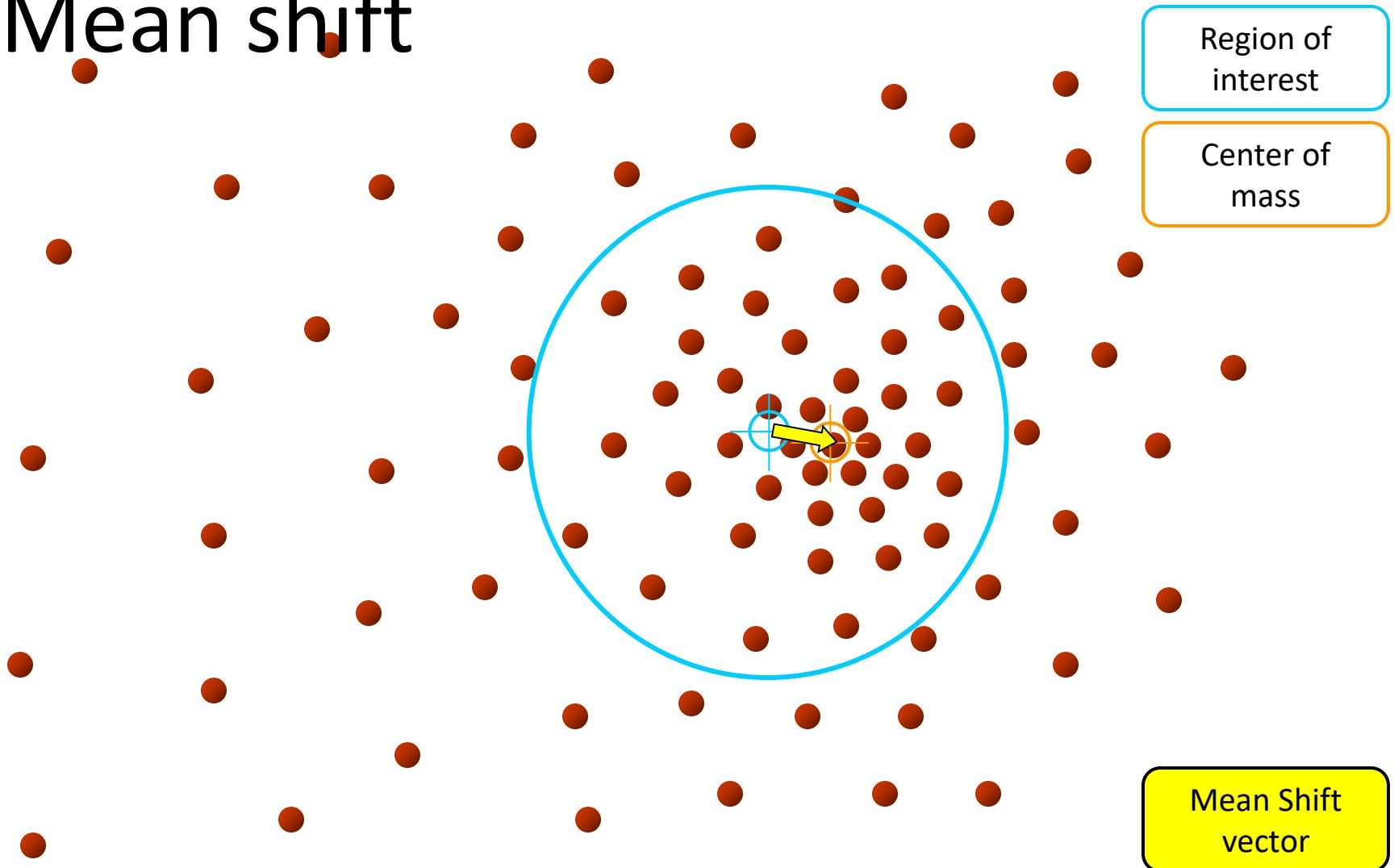
Mean shift



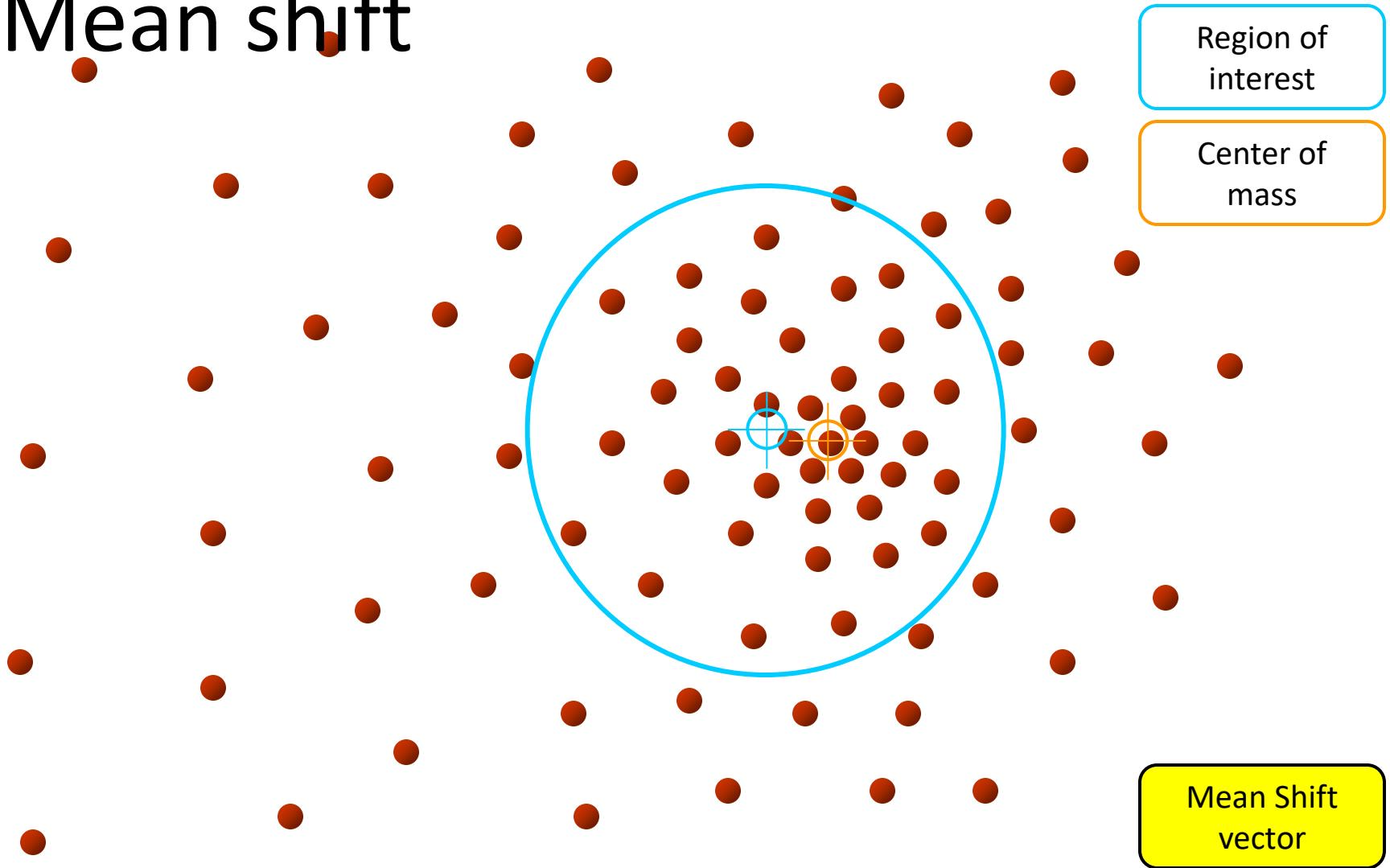
Mean shift



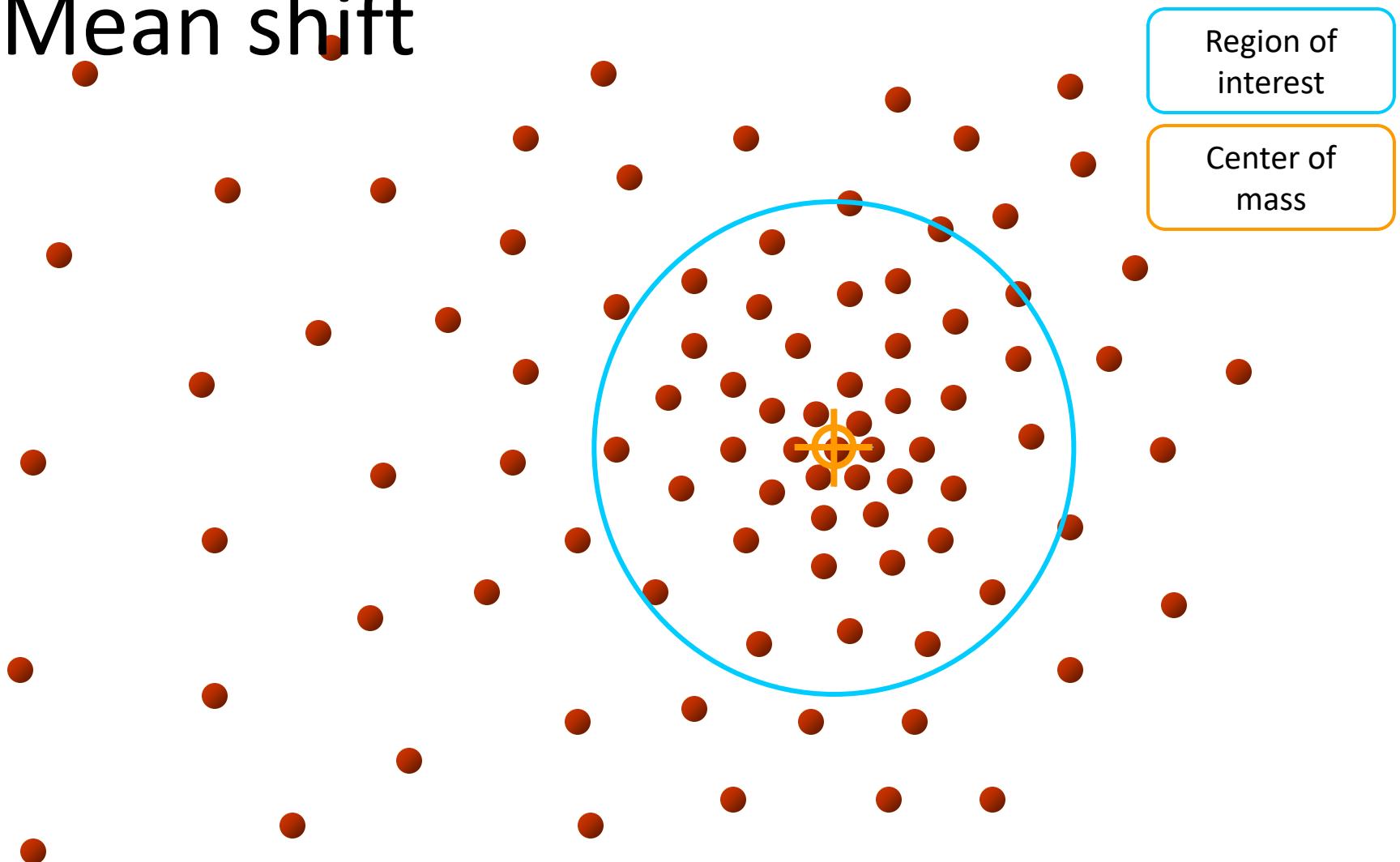
Mean shift



Mean shift



Mean shift



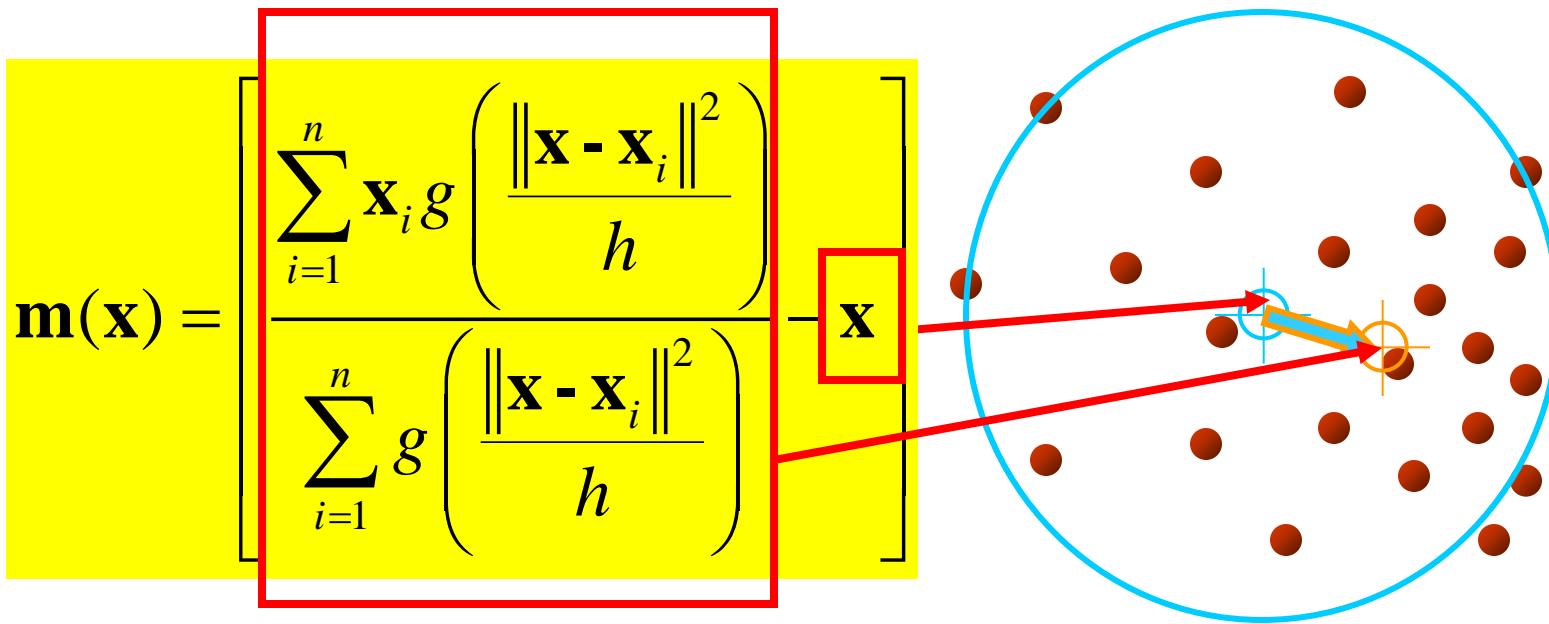
Region of
interest

Center of
mass

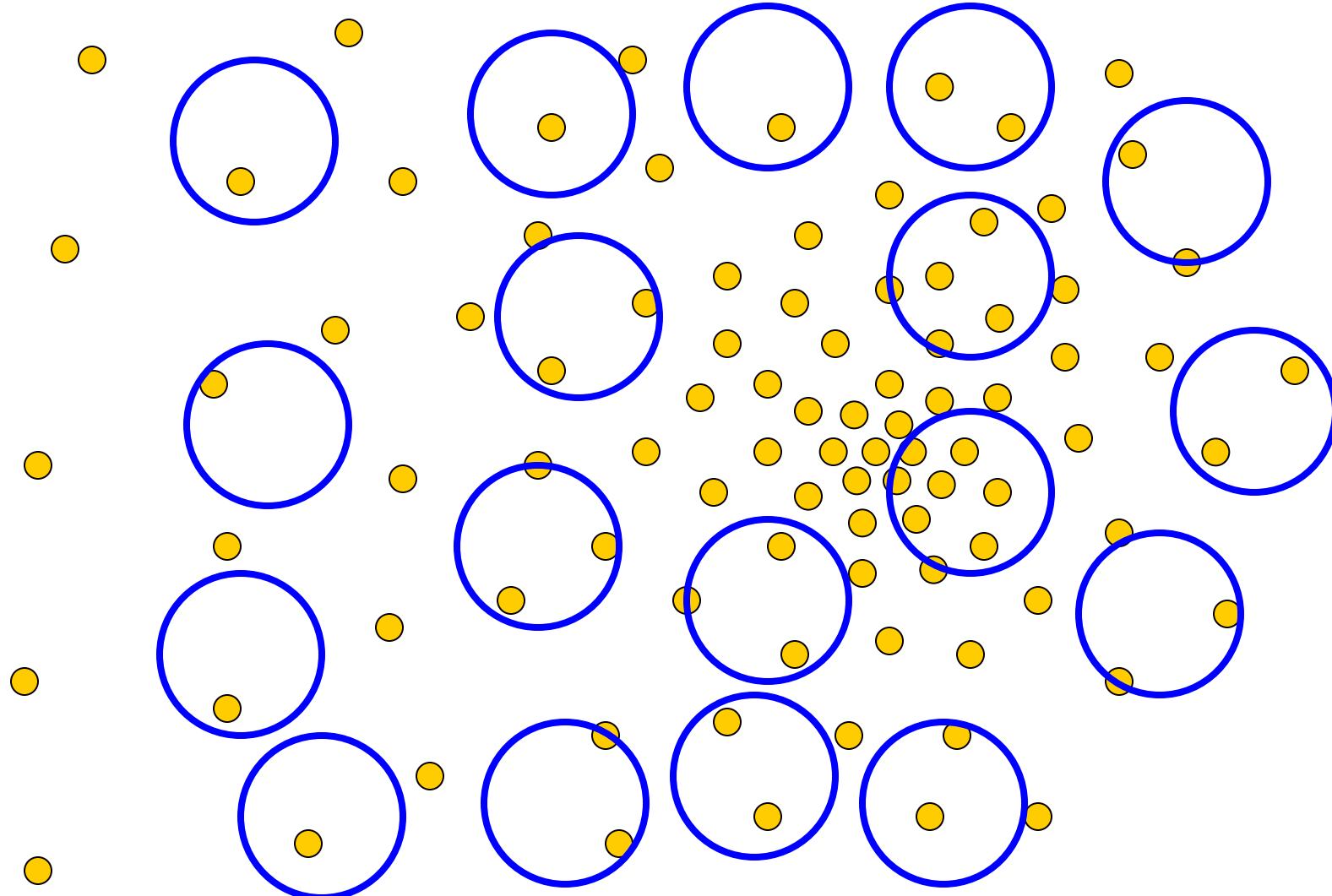
Computing the Mean Shift

Simple Mean Shift procedure:

- Compute mean shift vector
- Translate the Kernel window by $\mathbf{m}(\mathbf{x})$

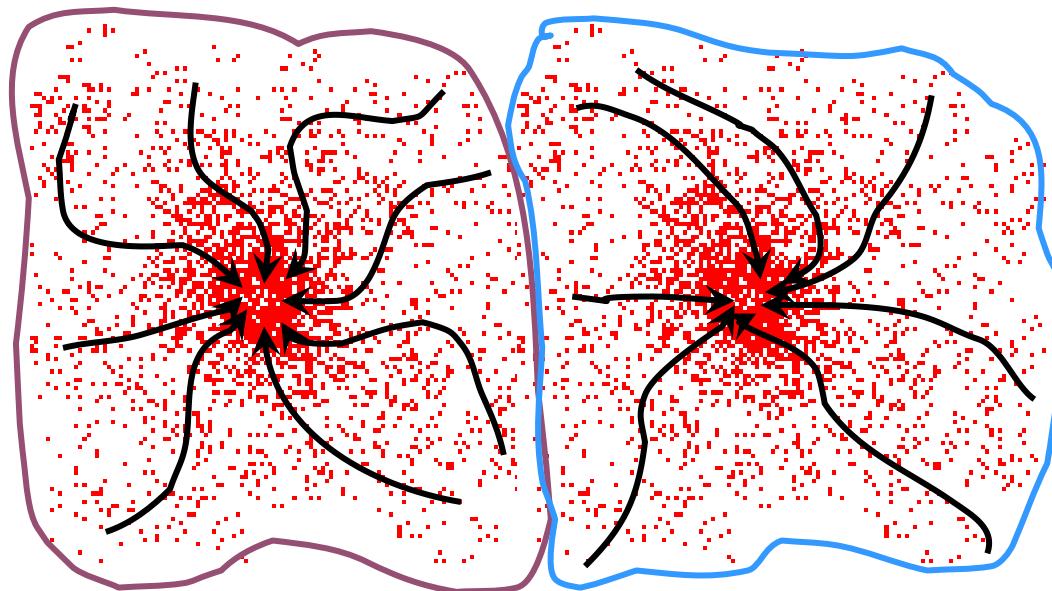
$$\mathbf{m}(\mathbf{x}) = \left[\frac{\sum_{i=1}^n \mathbf{x}_i g\left(\frac{\|\mathbf{x} - \mathbf{x}_i\|^2}{h}\right)}{\sum_{i=1}^n g\left(\frac{\|\mathbf{x} - \mathbf{x}_i\|^2}{h}\right)} \right] \mathbf{x}$$


Real Modality Analysis

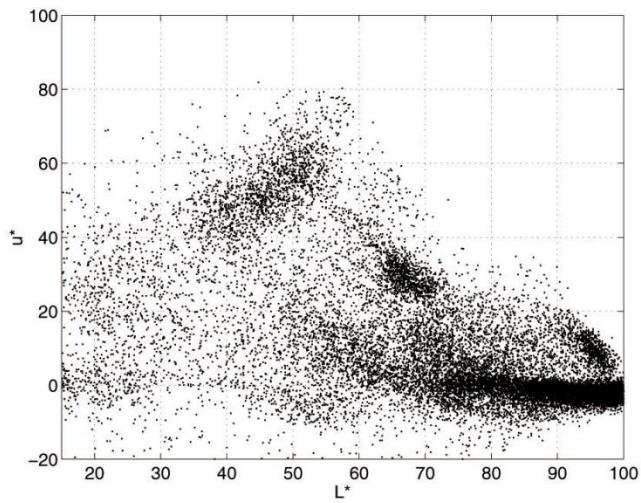


Attraction basin

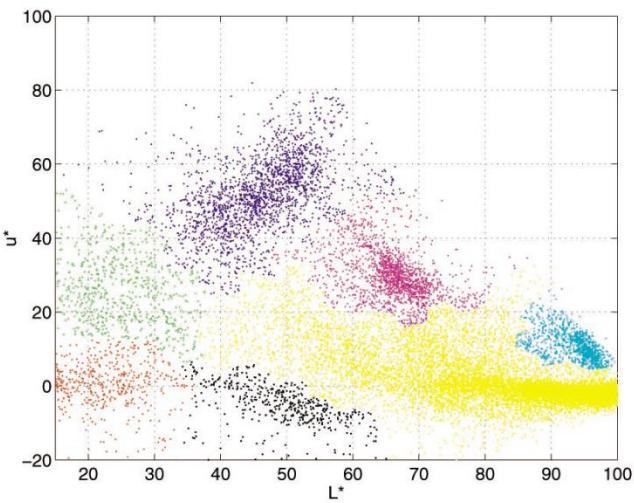
- **Attraction basin:** the region for which all trajectories lead to the same mode
- **Cluster:** all data points in the attraction basin of a mode



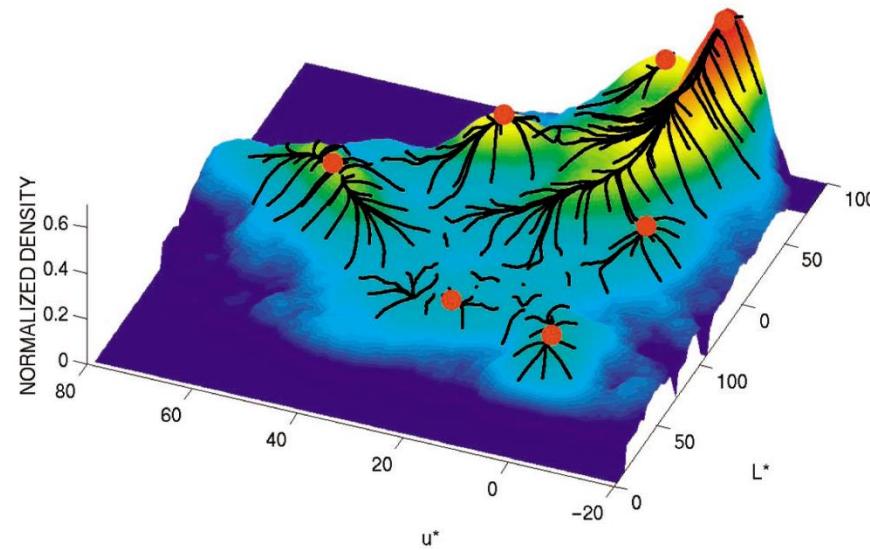
Attraction basin



(a)



(b)

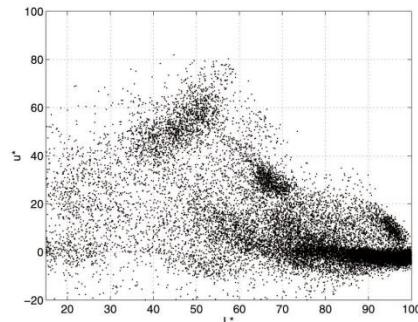


Mean shift clustering

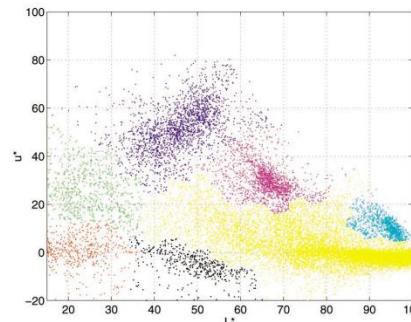
- The mean shift algorithm seeks *modes* of the given set of points
 1. Choose kernel and bandwidth
 2. For each point:
 - a) Center a window on that point
 - b) Compute the mean of the data in the search window
 - c) Center the search window at the new mean location
 - d) Repeat (b,c) until convergence
 3. Assign points that lead to nearby modes to the same cluster

Segmentation by Mean Shift

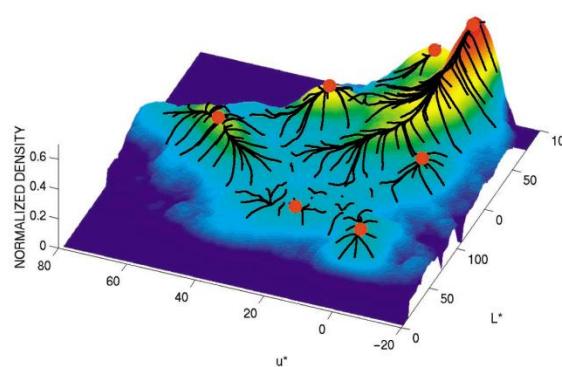
- Compute features for each pixel (color, gradients, texture, etc); also store each pixel's position
- Set kernel size for features K_f and position K_s
- Initialize windows at individual pixel locations
- Perform mean shift for each window until convergence
- Merge modes that are within width of K_f and K_s



(a)

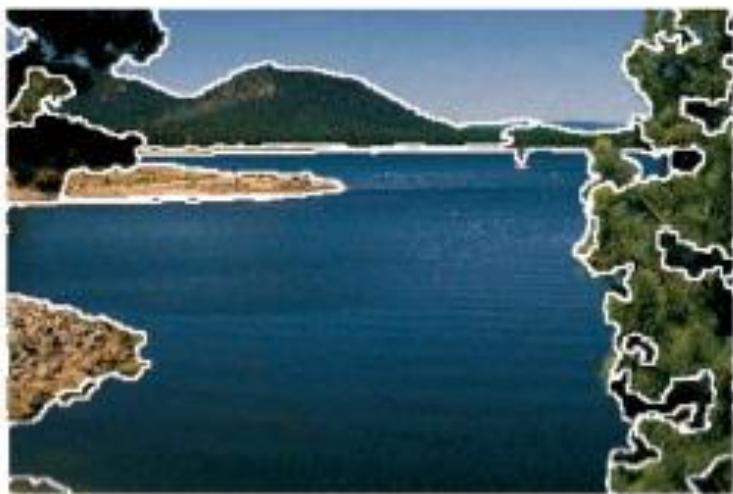
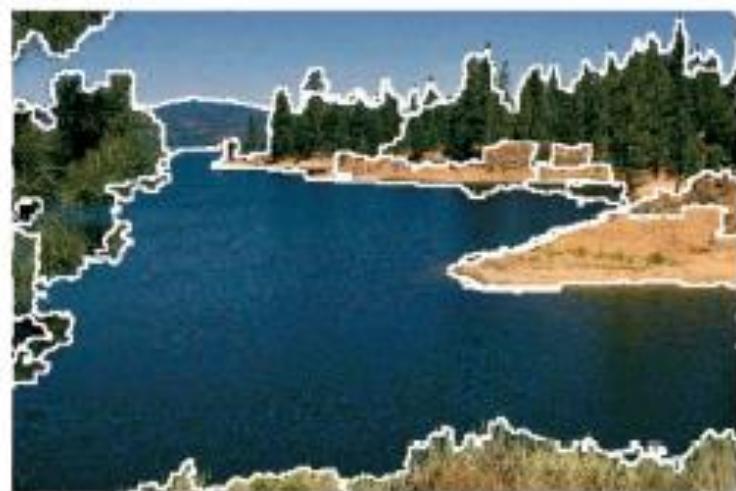


(b)



Mean shift segmentation results



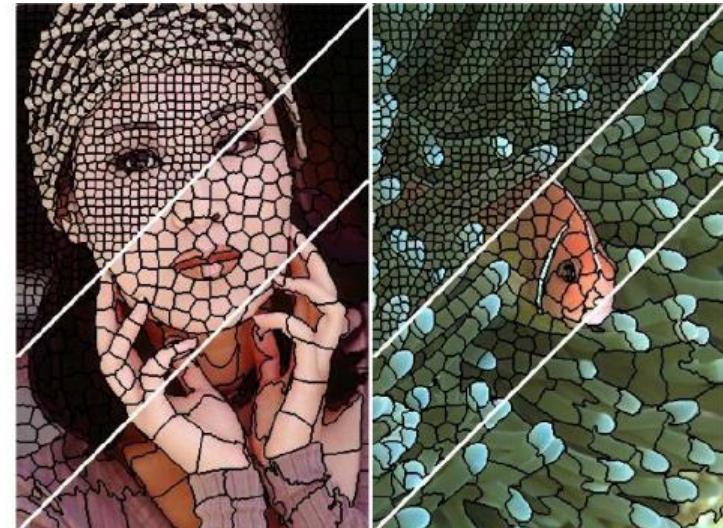


<http://www.caip.rutgers.edu/~comanici/MSPAMI/msPamiResults.html>

Modern Superpixel Methods

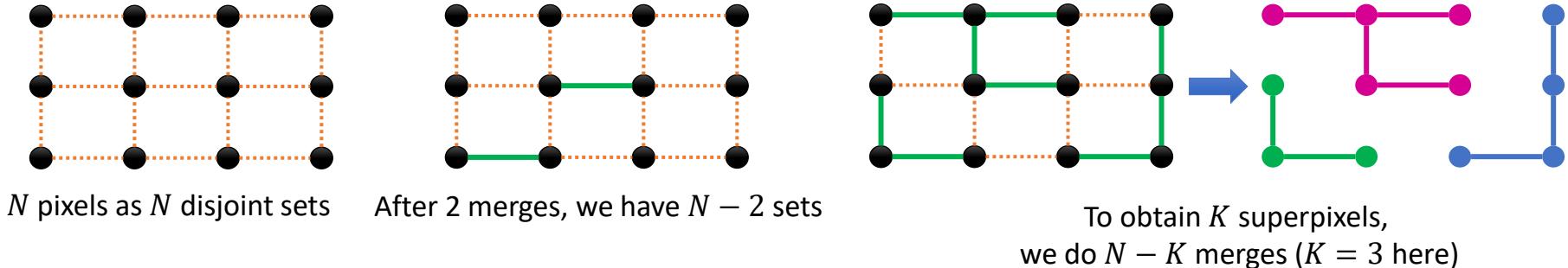
What Are Superpixels?

- Most image processing algorithms use the pixel grid as the underlying representation.
 - Processing time grows with the number of pixels.
- Superpixels are grouping of pixels.
 - Pixels in the same superpixel are near and visually similar (local and edge-preserving)
 - A good superpixel segmentation algorithm should be efficient
 - Processing time depends on the number of superpixels (regardless of image resolution)



Graph-Based Algorithms

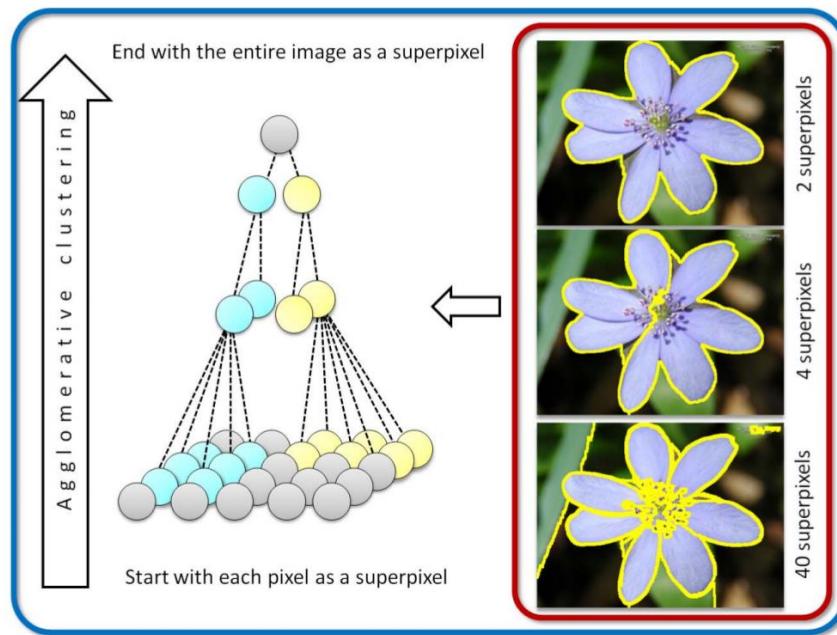
- FH [Felzenszwalb and Huttenlocher, IJCV 2004]
- GBVS [Grundmann et al., CVPR 2010]
- ERS [Liu et al., CVPR 2011]



- P. F. Felzenszwalb and D. P. Huttenlocher. Efficient graph-based image segmentation. *IJCV*, 2004
- M. Grundmann, V. Kwatra, M. Han, and I. Essa. Efficient hierarchical graph-based video segmentation. In *CVPR*, 2010
- M.-Y. Liu, O. Tuzel, S. Ramalingam, and R. Chellappa. Entropy-rate superpixel segmentation. In *CVPR*, 2011

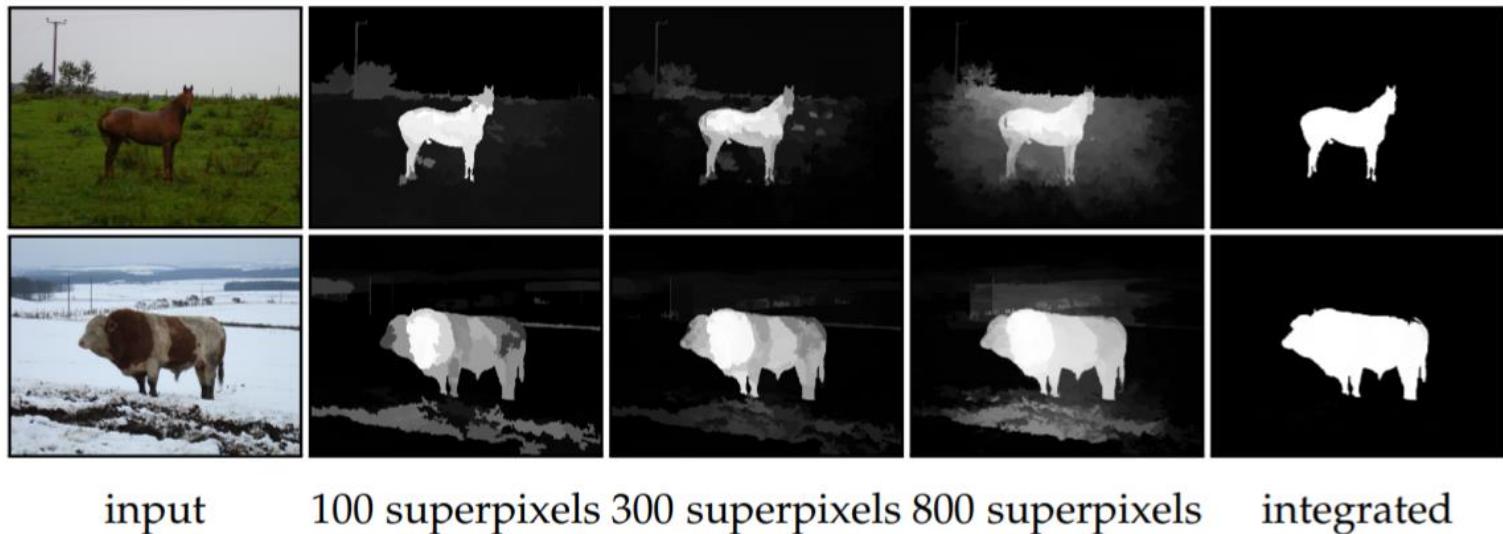
Graph-Based Algorithms

- Graph-based methods are able to generate **superpixel hierarchy**



Graph-Based Algorithms

- Graph-based methods are able to generate **superpixel hierarchy**



Example of salient object segmentation based on the superpixel hierarchy

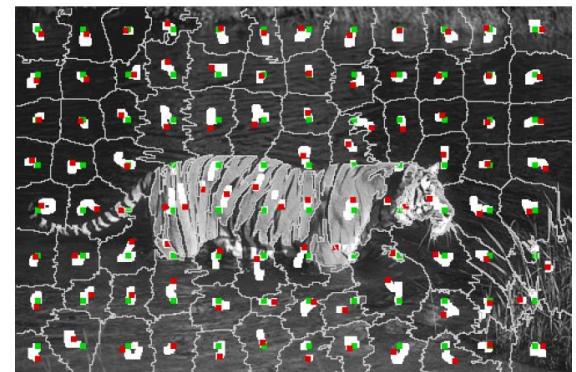
Clustering-Based Algorithms

- SLIC (Simple Linear Iterative Clustering)
 - RGB → CIELab
 - 5D feature (L, a, b, x, y)
 - Initialize the K superpixel centers on the uniform grid
 - Localized K -means clustering in $2S \times 2S$ region

$$d_{lab} = \sqrt{(l_k - l_i)^2 + (a_k - a_i)^2 + (b_k - b_i)^2}$$

$$d_{xy} = \sqrt{(x_k - x_i)^2 + (y_k - y_i)^2}$$

$$D_s = d_{lab} + \frac{m}{S} d_{xy}, \quad m \text{ is a constant}$$



Localized k-means

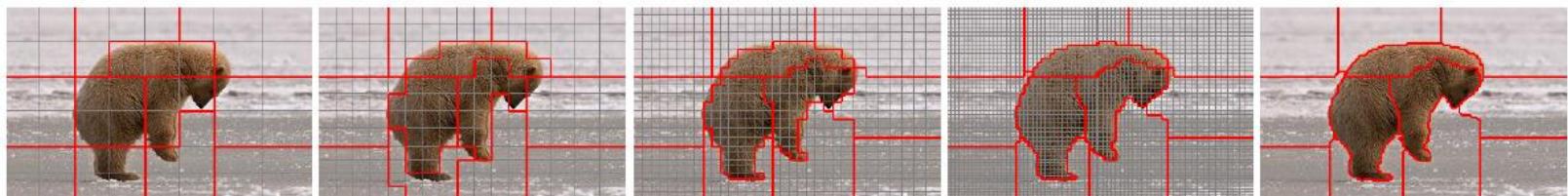
- R. Achanta, A. Shaji, K. Smith, A. Lucchi, P. Fua, and S. Susstrunk. "SLIC superpixels compared to state-of-the-art superpixel methods." *TPAMI*, 2012

Other SLIC-Like Algorithms

- LSC [Li and Chen, CVPR 2015]
 - 10D feature + localized K-means
 - Manifold-SLIC [Liu et al., CVPR 2016]
 - Project 5D feature to a 2D space + localized K-means
 - SNIC [Achanta and Susstrunk, CVPR 2017]
 - 5D feature + iteration free clustering
-
- Z. Li and J. Chen. Superpixel segmentation using linear spectral clustering. In *CVPR*, 2015
 - Yong-Jin Liu, Cheng-Chi Yu, Min-Jing Yu, and Ying He. Manifold slic: A fast method to compute content-sensitive superpixels. In *CVPR*, 2016
 - R. Achanta and S. Susstrunk. Superpixels and polygons using simple non-iterative clustering. In *CVPR*, 2017

Grid-Based Algorithms

- SEEDS [Van den Bergh et al., IJCV 2015]
 - Superpixels as an energy optimization (color consistency, boundary shape, ...)
 - Switch nearby blocks if it makes the total energy lower
 - Coarse to fine strategy

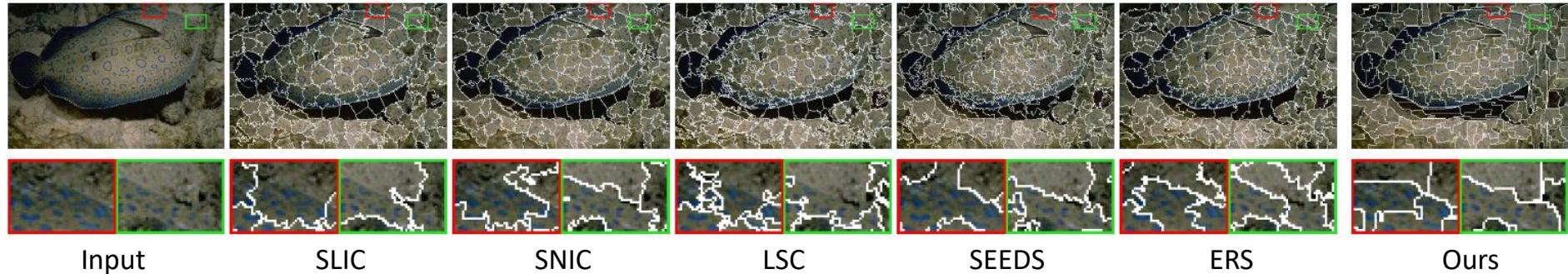


Multi-scale block switching

- M. Van den Bergh, X. Boix, G. Roig, and L. Van Gool. SEEDS: Superpixels extracted via energy-driven sampling. *IJCV*, 2015

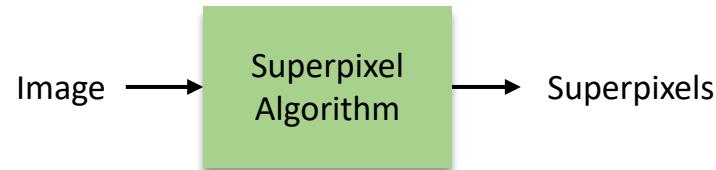
Drawbacks of Existing Methods

- All above methods are based on hand-crafted features to compute pixel distances/affinities
 - They often fail to preserve weak object boundaries



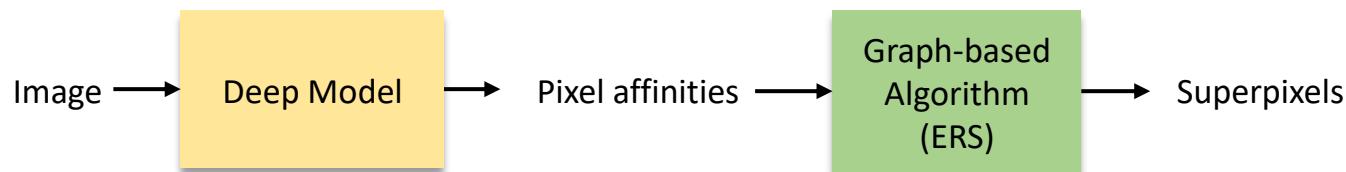
Superpixels Meet Deep Learning

- Supervised learning is not easy
 - There is no ground-truth
 - Label indices are interchangeable
 - Superpixel algorithms are non-differentiable



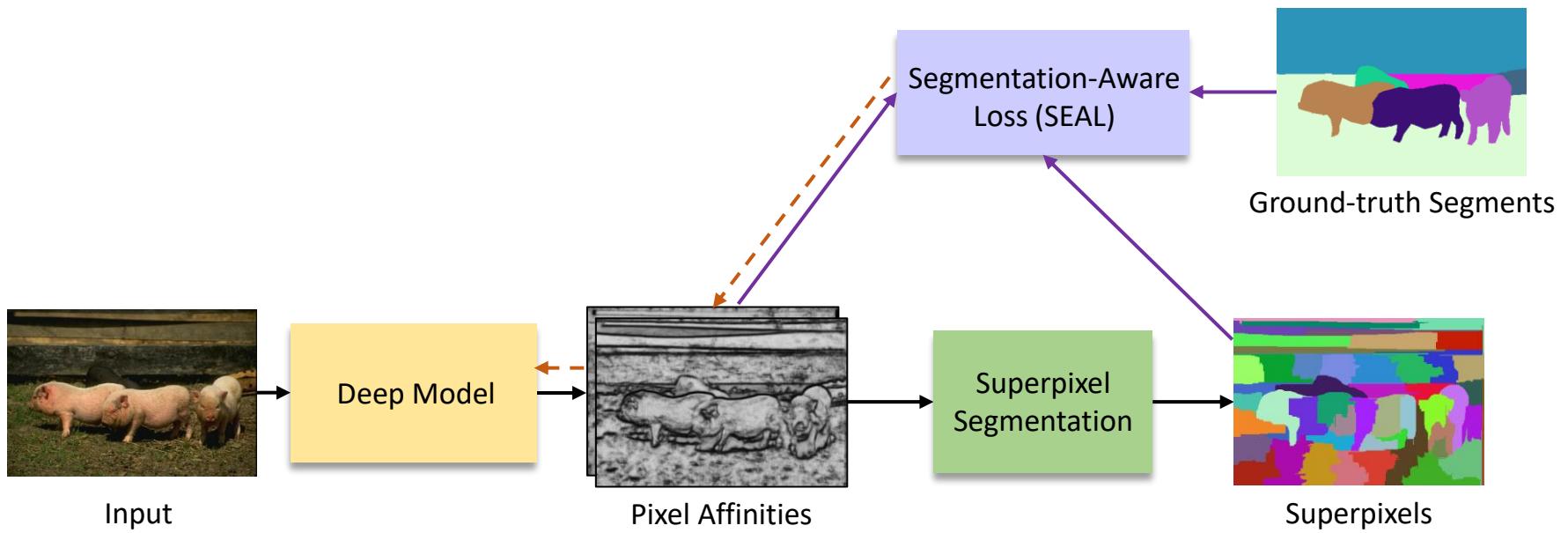
Superpixels Meet Deep Learning

- Supervised learning is not easy
 - There is no ground-truth
 - Label indices are interchangeable
 - Superpixel algorithms are non-differentiable
- Our main idea: learning pixel affinities (distances) for the graph-based algorithms
[Tu et al., CVPR 2018]



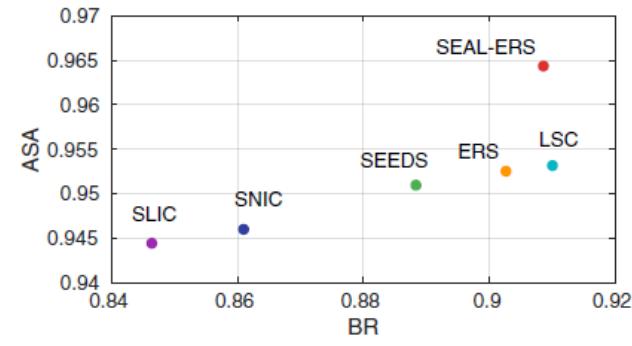
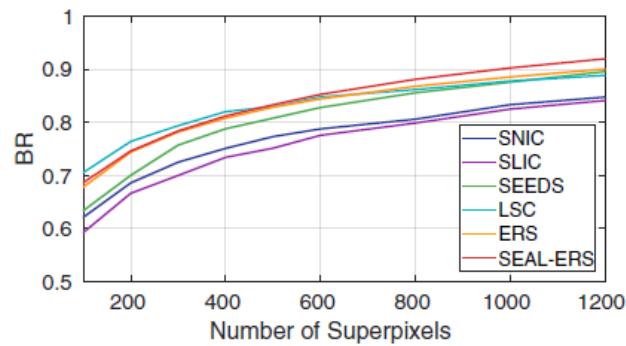
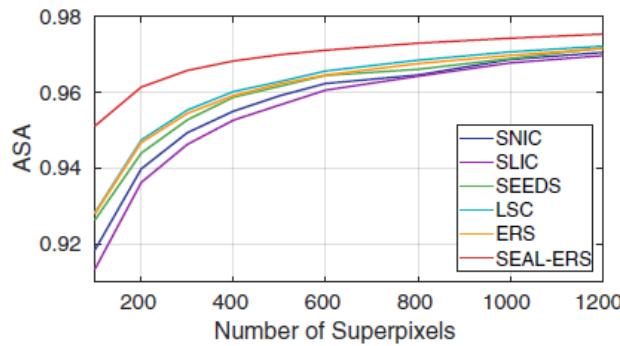
Wei-Chih Tu, Ming-Yu Liu, Varun Jampani, Deqing Sun, Shao-Yi Chien, Ming-Hsuan Yang, Jan Kautz.
Learning superpixels with segmentation-aware affinity loss. In *CVPR*, 2018

Segmentation-Aware Loss



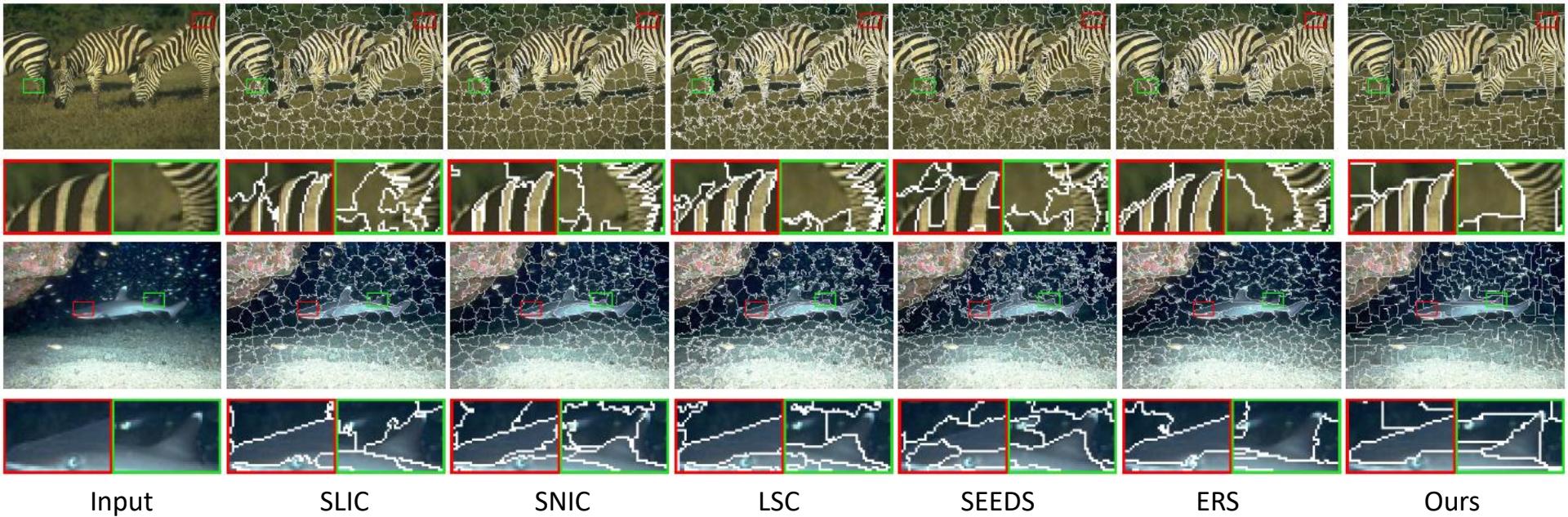
Comparisons with the State-of-the-Arts

- Results on BSDS500
 - SEAL-ERS = learned affinities + ERS algorithm (proposed)



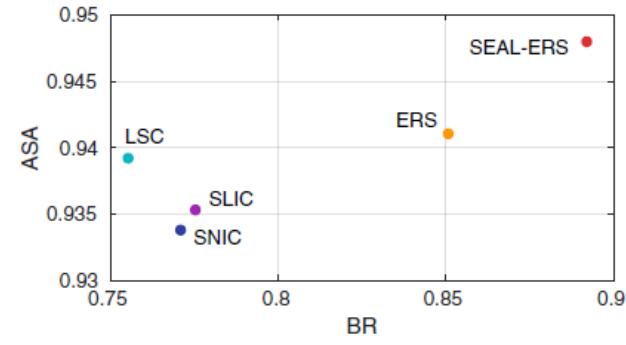
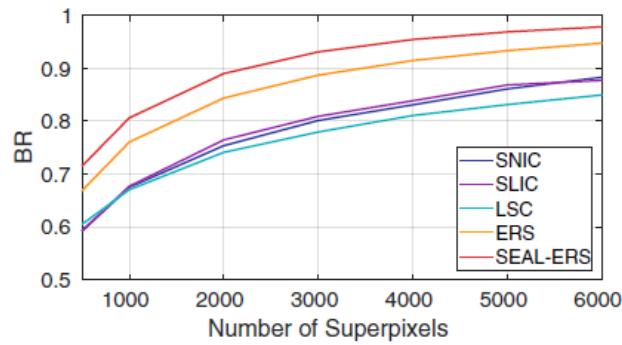
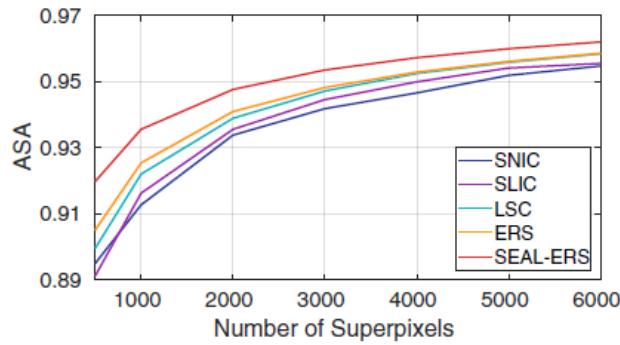
Wei-Chih Tu, Ming-Yu Liu, Varun Jampani, Deqing Sun, Shao-Yi Chien, Ming-Hsuan Yang, Jan Kautz.
Learning superpixels with segmentation-aware affinity loss. In CVPR, 2018

Comparisons with the State-of-the-Arts



Comparisons with the State-of-the-Arts

- Results on Cityscapes



Wei-Chih Tu, Ming-Yu Liu, Varun Jampani, Deqing Sun, Shao-Yi Chien, Ming-Hsuan Yang, Jan Kautz.
Learning superpixels with segmentation-aware affinity loss. In CVPR, 2018

Image Segmentation: Semantic Segmentation

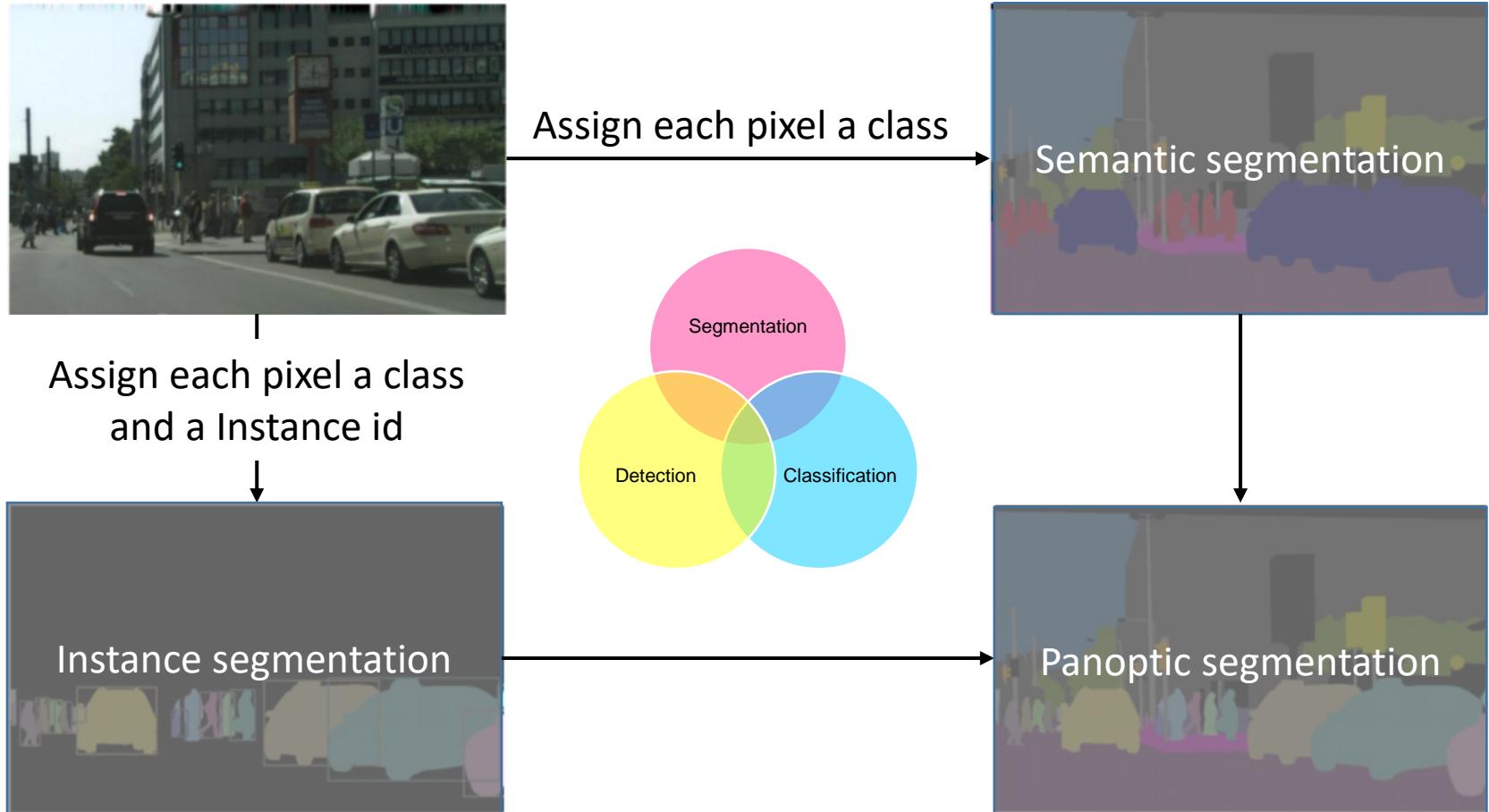


Image Segmentation: Semantic Segmentation

- Fully convolutional networks (FCN)
- DeepLab



What is Semantic Segmentation?

- Segmentation + labeling



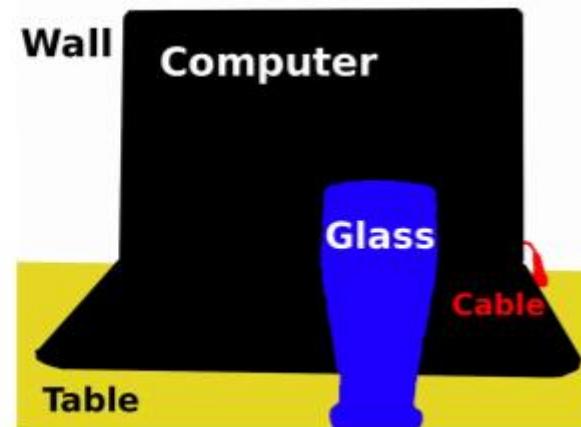
(a) Image

(b) Ground Truth

Example from ADE20K dataset.

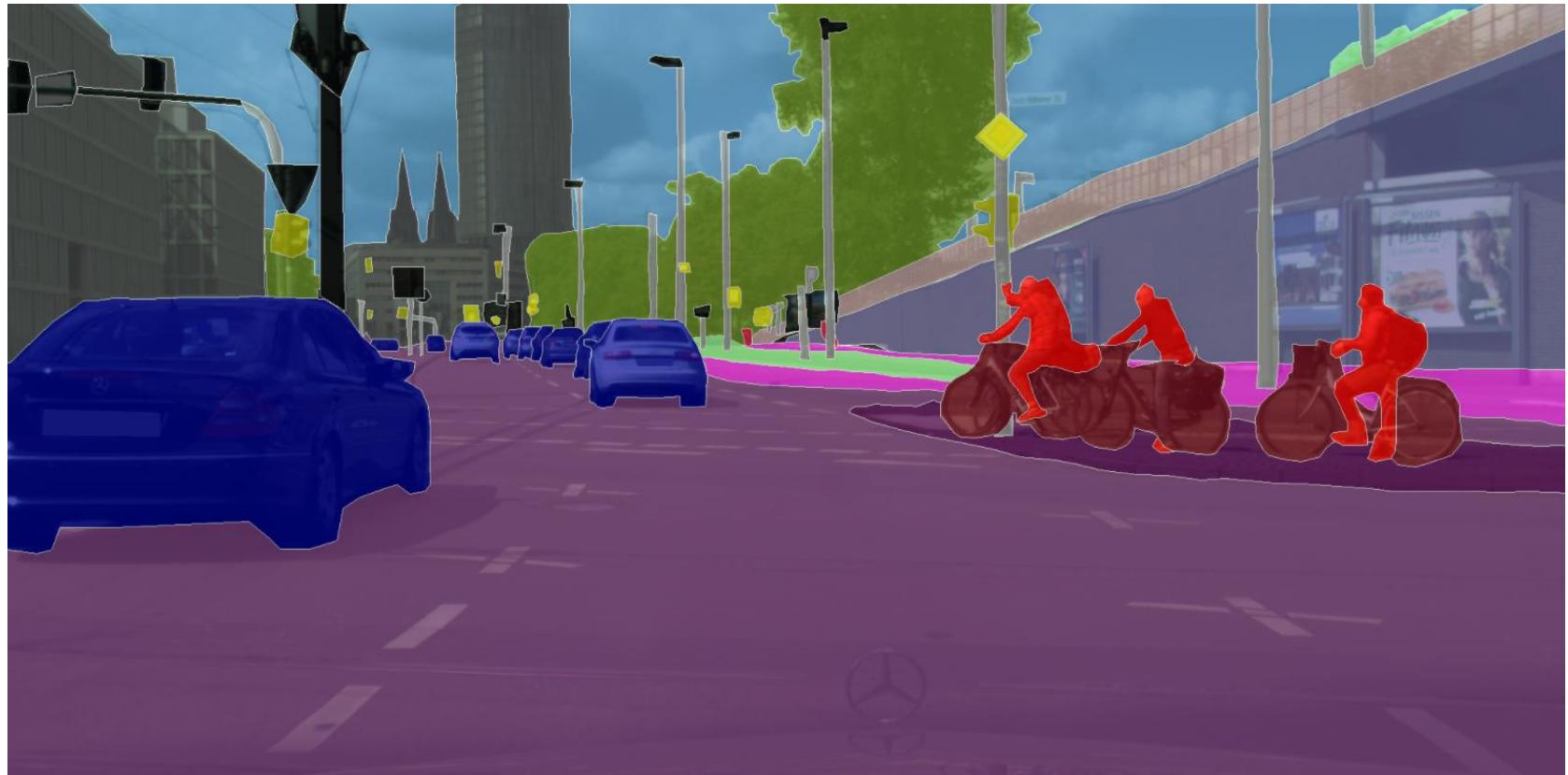
Why Semantic Segmentation?

- As a vision aid for the blind



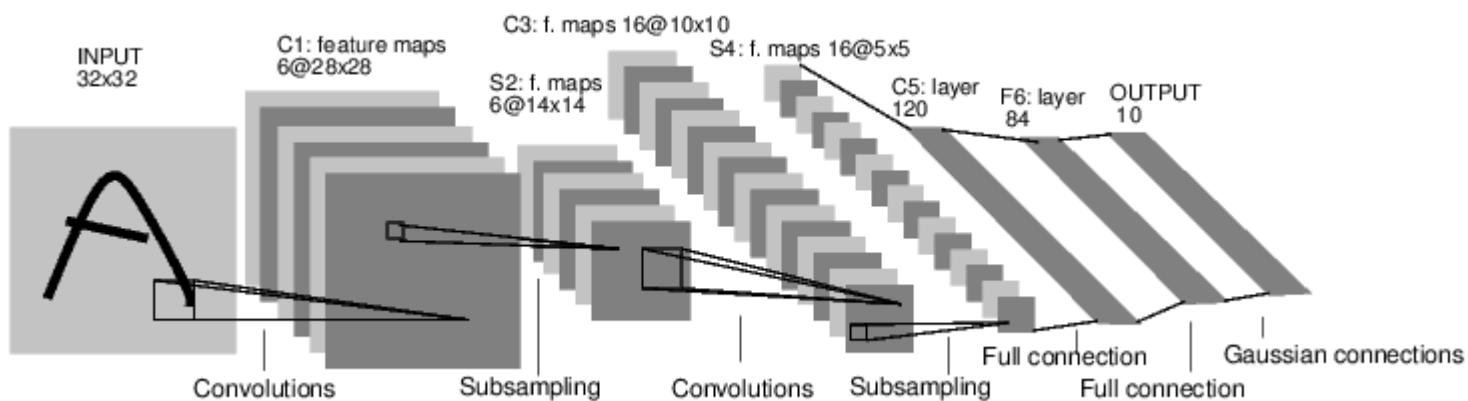
Why Semantic Segmentation?

- Autonomous driving



Previous Image Recognition Networks

- LeNet, AlexNet or their successors take fixed size input and produce non-spatial outputs.



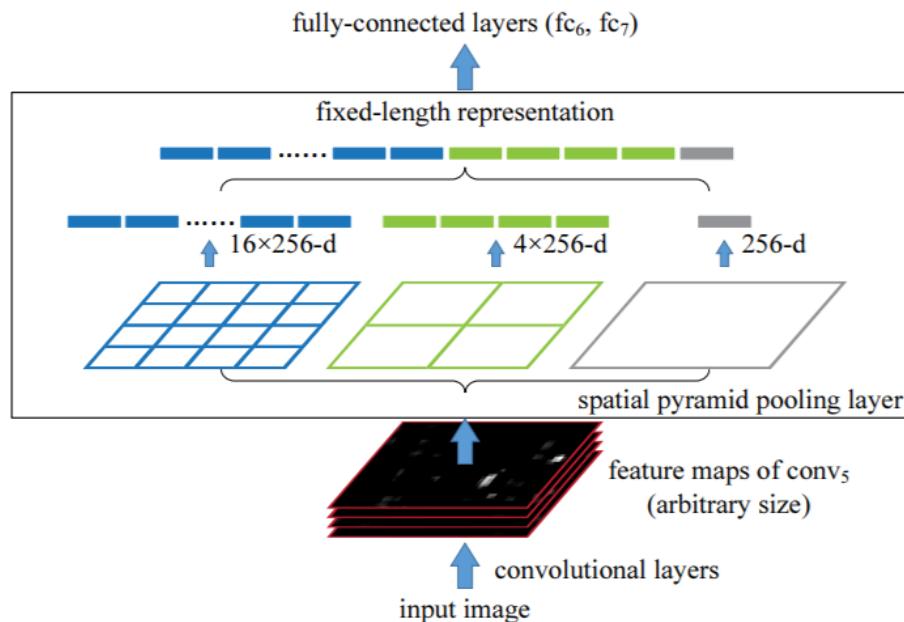
Previous Image Recognition Networks

- Spatial pyramid pooling can take arbitrary size input but still no spatial output.



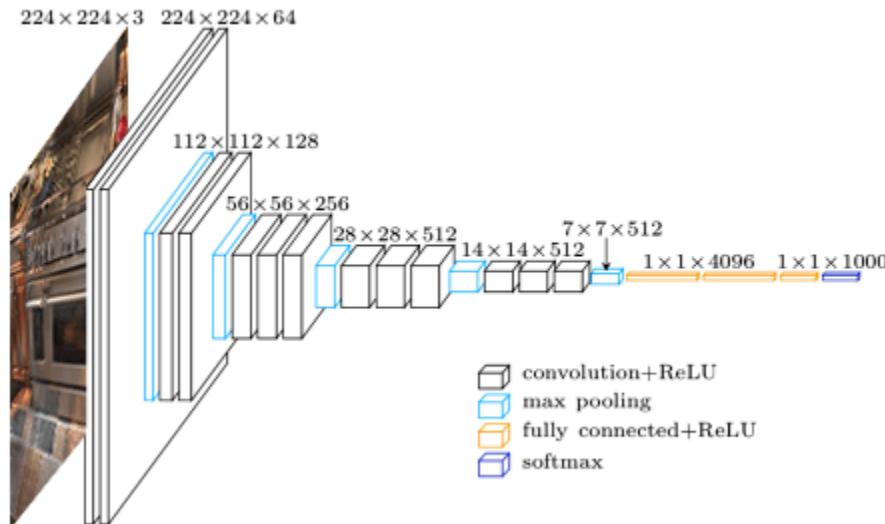
Previous Image Recognition Networks

- Spatial pyramid pooling can take arbitrary size input but still no spatial output.



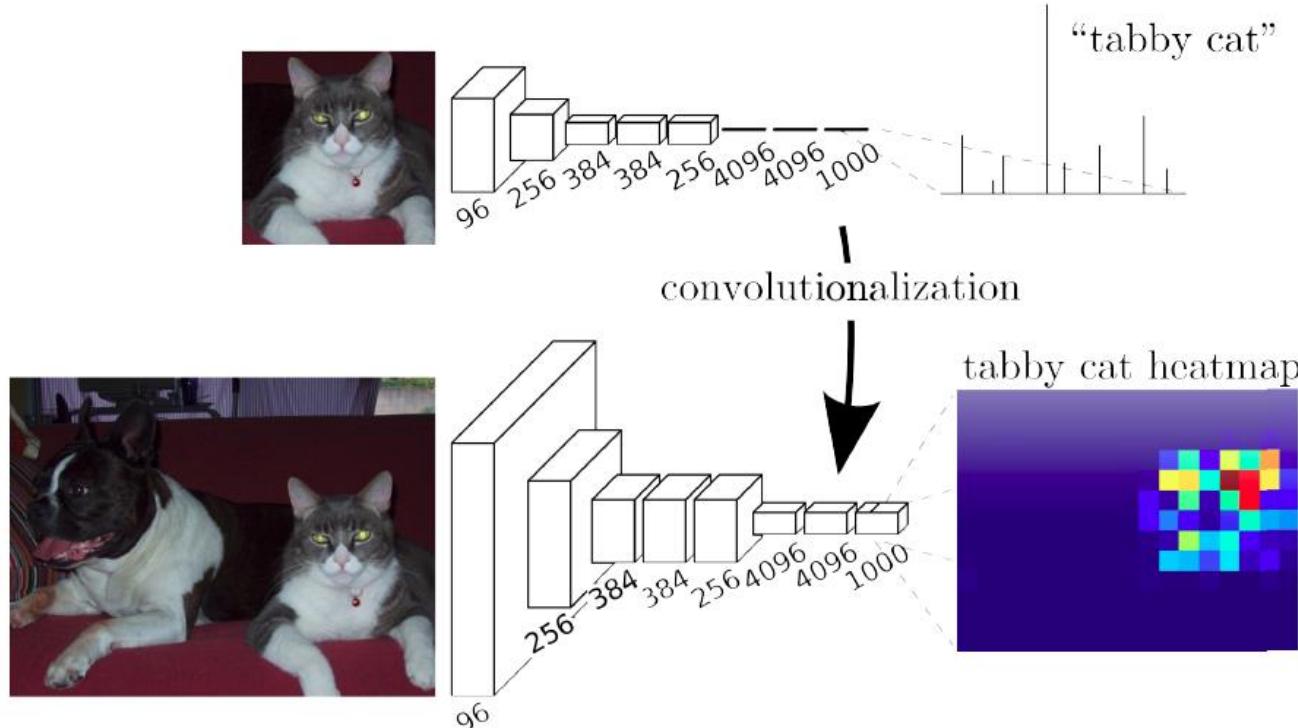
VGG16 Model

- Pre-trained on image classification



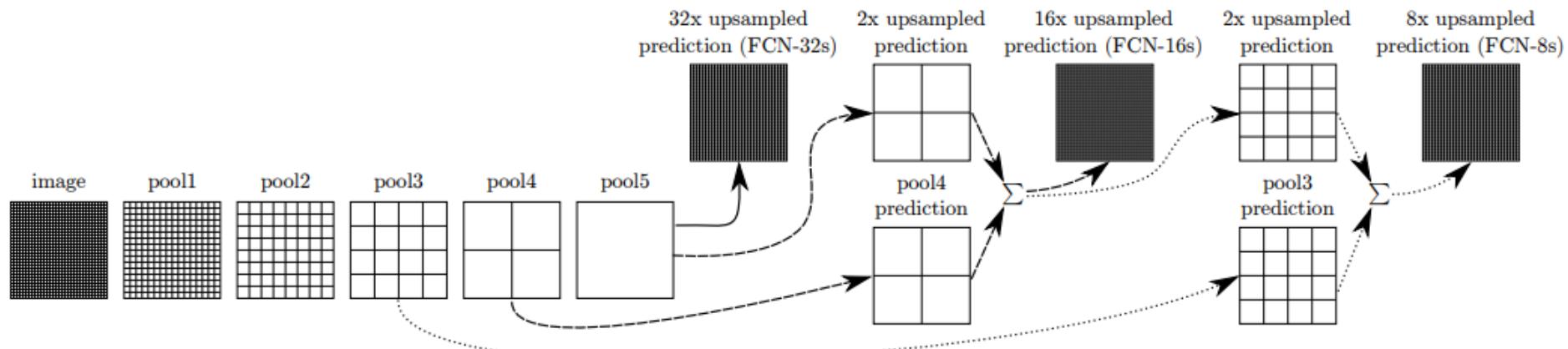
Fully Convolutional Networks (FCN)

- Fully connected layers can also be viewed as convolutions with kernels that cover their entire input regions



FCN Architecture

- Fully connected layers are replaced by convolutions
- Append 1x1 convolution with channel dimension 21 in the end (20 classes + 1 background class)

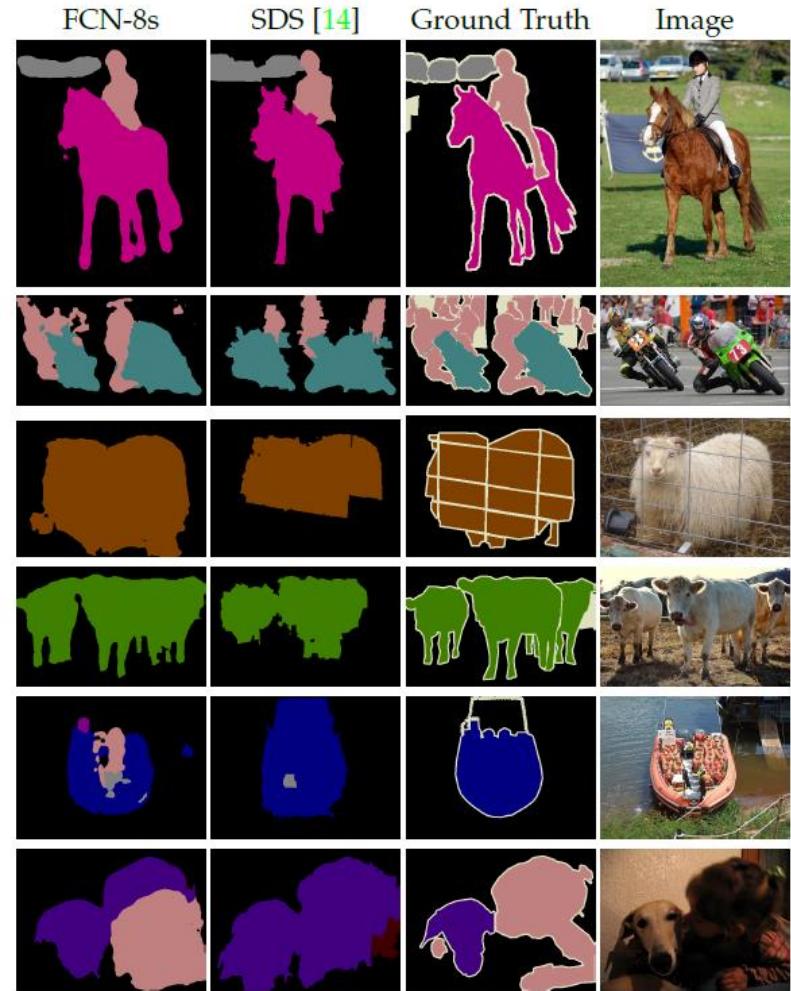


Fully Convolutional Networks (FCN)

- Results

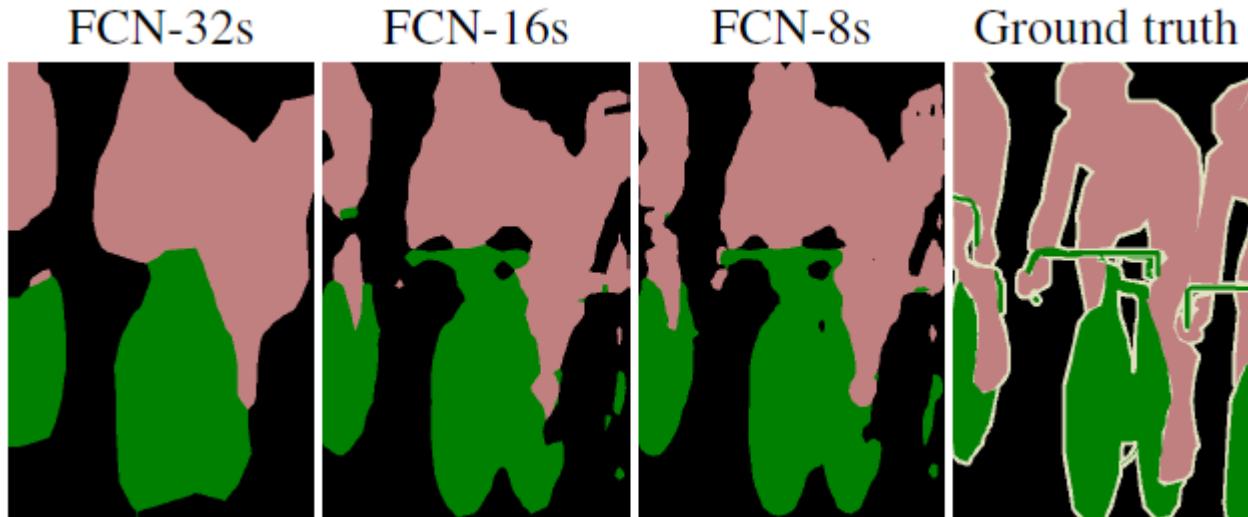
	mean IU VOC2011 test	mean IU VOC2012 test
R-CNN [5]	47.9	-
SDS [14]	52.6	51.6
FCN-8s	67.5	67.2

- Definition
 - n_{ij} : number of pixels in class i predicted to be class j
 - $t_i = \sum_j n_{ij}$ be the total number of pixels in class i
 - n_{cl} : number of classes
- Pixel accuracy
 - $\sum_i n_{ii} / \sum_i t_i$
- Mean accuracy
 - $\frac{1}{n_{cl}} \sum_i n_{ii} / t_i$
- Mean IU (intersection over union)
 - $\frac{1}{n_{cl}} \sum_i \frac{n_{ii}}{t_i + \sum_j n_{ji} - n_{ii}}$



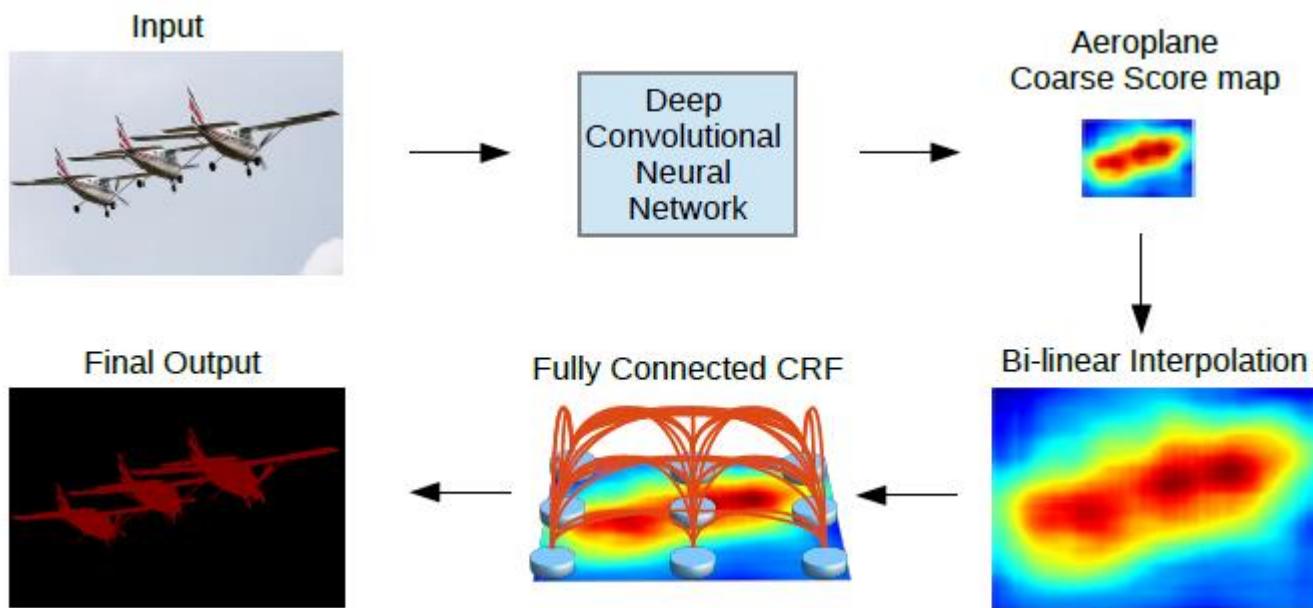
Fully Convolutional Networks (FCN)

- FCN is still not good at segmenting objects...



DeepLab

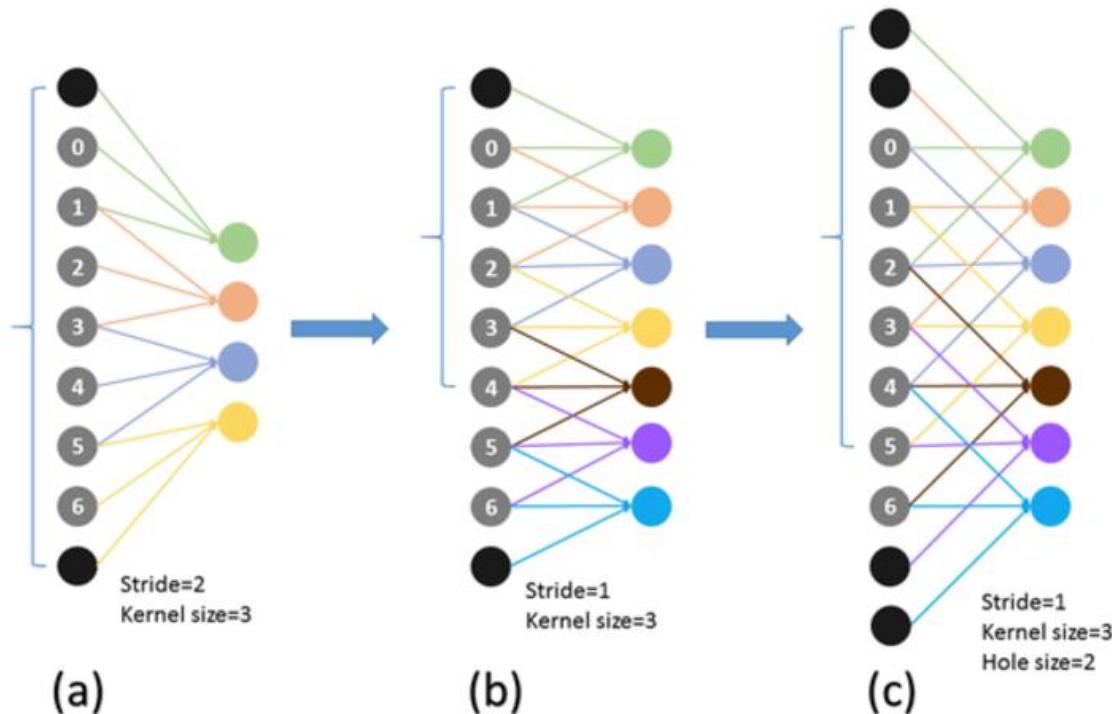
- FCN + Atrous convolution + dense CRFs (conditional random field)



Semantic image segmentation with deep convolutional nets and fully connected CRFs, ICLR 2015

DeepLab

- Atrous convolution (dilated convolution)



Semantic image segmentation with deep convolutional nets and fully connected CRFs, ICLR 2015

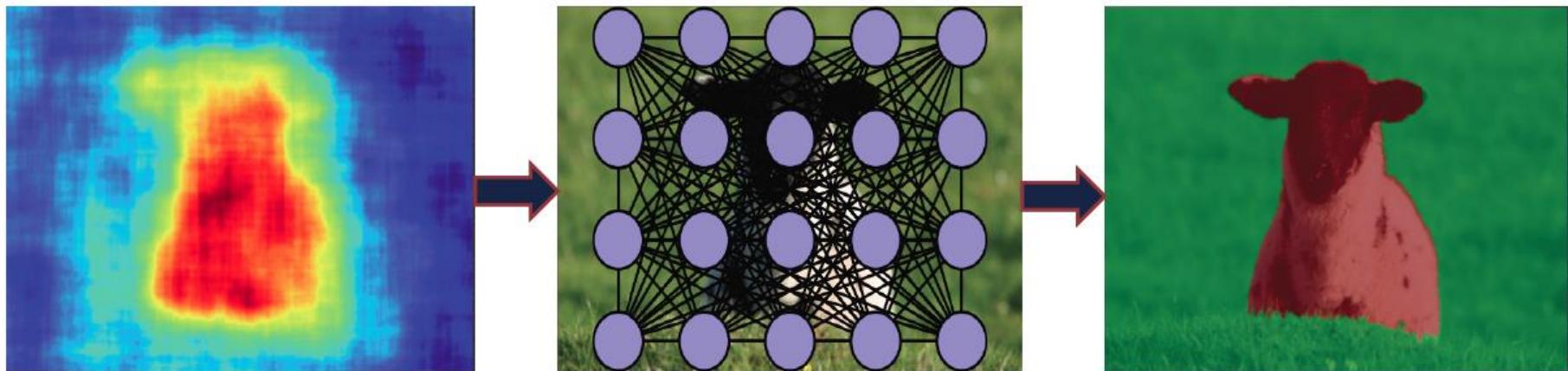
DeepLab

- Dense CRFs

From FCN output

$$E(\mathbf{x}) = \sum_i \underbrace{\psi_u(x_i)}_{\text{unary term}} + \sum_i \sum_{j \in \mathcal{N}_i} \underbrace{\psi_p(x_i, x_j)}_{\text{pairwise term}}$$

From input image



Coarse output from the
pixel-wise classifier

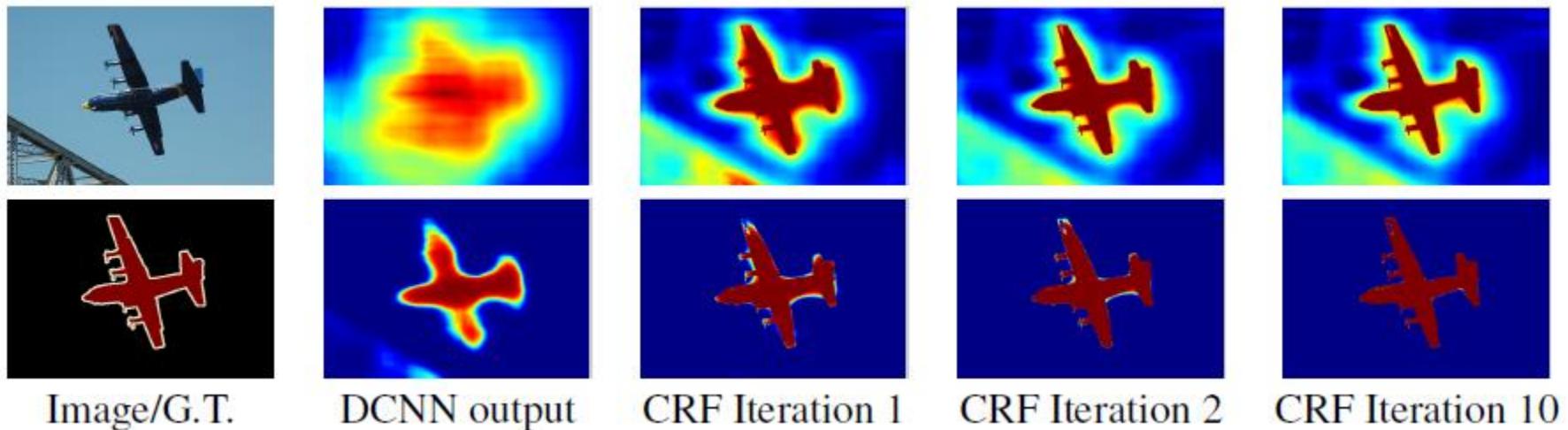
CRF modelling

Output after the CRF
inference

Efficient inference in fully connected CRFs with Gaussian edge potentials, NIPS 2011

DeepLab

- Effect of dense CRF refinement



Problem:

1. No joint training
2. More number of iterations means longer inference time

Semantic image segmentation with deep convolutional nets and fully connected CRFs, ICLR 2015

DeepLab

- Results on PASCAL VOC 2012 test set

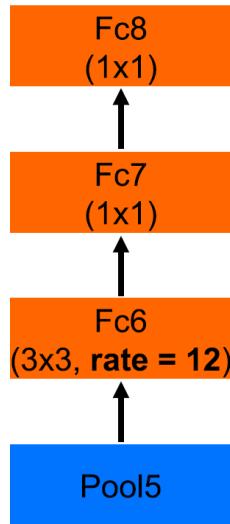
Method	mean IOU (%)
DeepLab	59.80
DeepLab-CRF	63.74
DeepLab-MSc	61.30
DeepLab-MSc-CRF	65.21
DeepLab-7x7	64.38
DeepLab-CRF-7x7	67.64
DeepLab-LargeFOV	62.25
DeepLab-CRF-LargeFOV	67.64
DeepLab-MSc-LargeFOV	64.21
DeepLab-MSc-CRF-LargeFOV	68.70

Method	mean IOU (%)
MSRA-CFM	61.8
FCN-8s	62.2
TTI-Zoomout-16	64.4
DeepLab-CRF	66.4
DeepLab-MSc-CRF	67.1
DeepLab-CRF-7x7	70.3
DeepLab-CRF-LargeFOV	70.3
DeepLab-MSc-CRF-LargeFOV	71.6

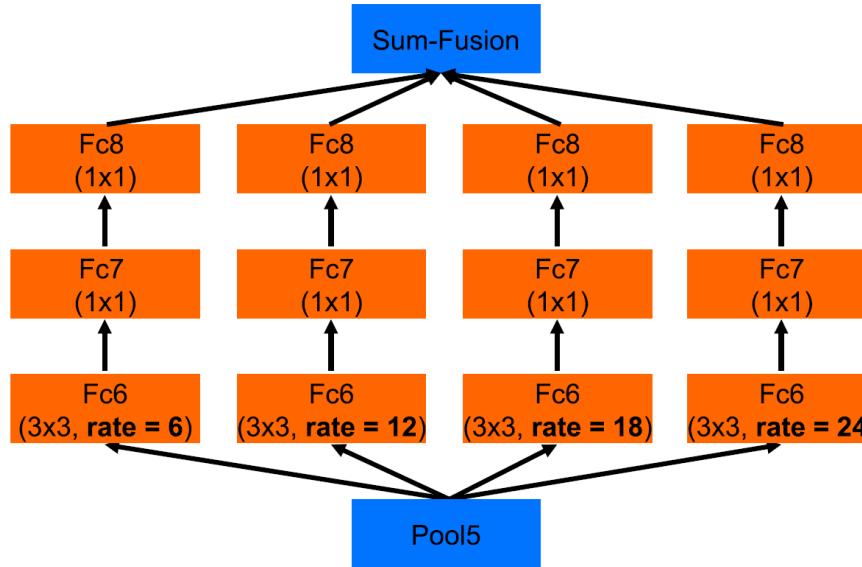
Semantic image segmentation with deep convolutional nets and fully connected CRFs, ICLR 2015

DeepLabv2

Based on VGG16



(a) DeepLab-LargeFOV

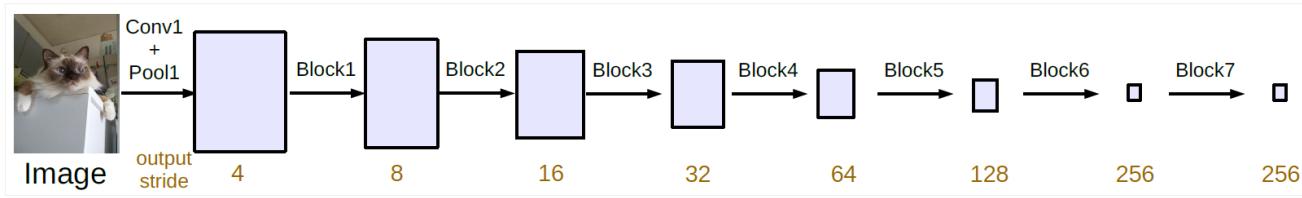


(b) DeepLab-ASPP (Atrous Spatial Pyramid Pooling)

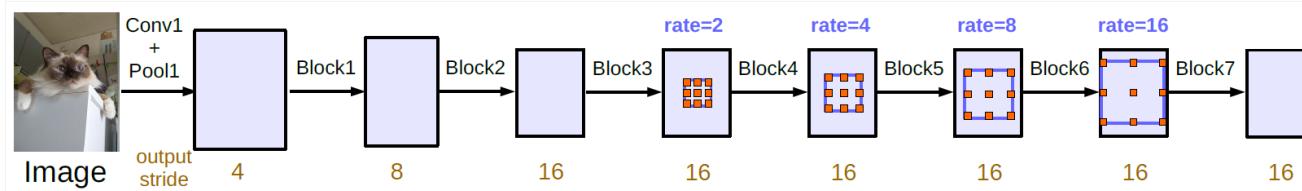
- The other improvement strategy is to replace the backbone with ResNet-101

DeepLabv3

- Based on ResNet, go deeper

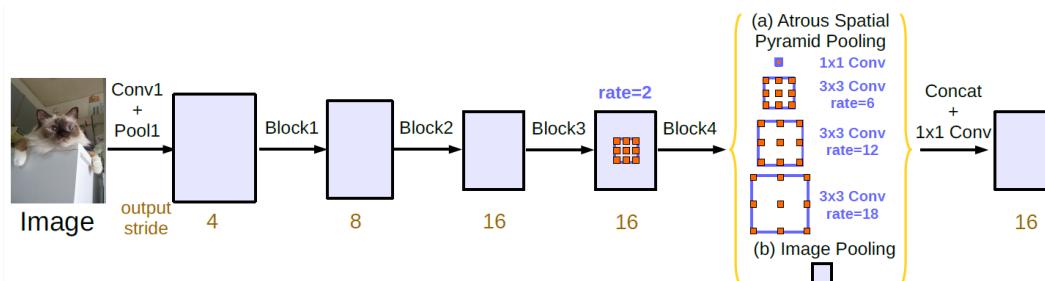


(a) Going deeper without atrous convolution.



(b) Going deeper with atrous convolution. Atrous convolution with $rate > 1$ is applied after block3 when *output_stride* = 16.

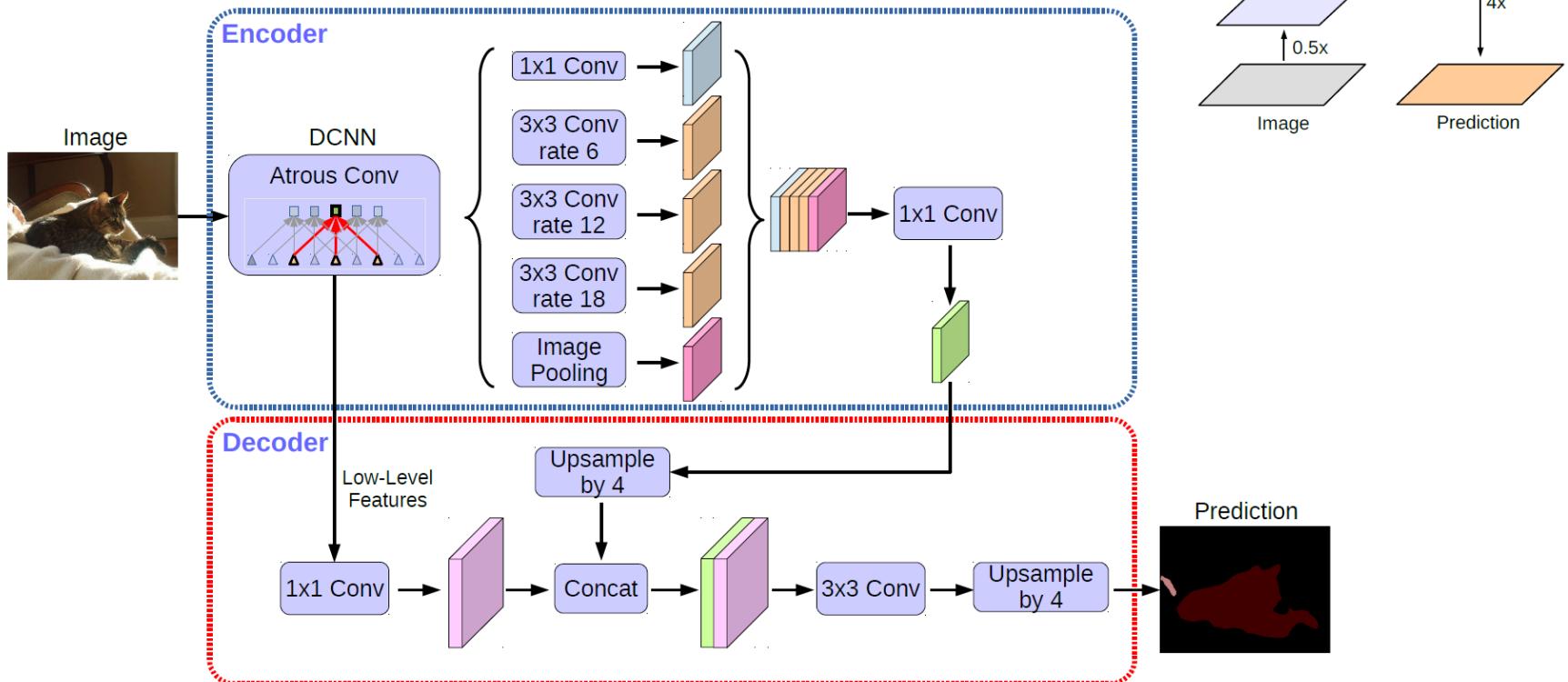
- ASPP augmented with image-level features



L.-C. Chien, G. Papandreou, F. Schroff, and H. Adam, “Rethinking atrous convolution for semantic segmentation,” *arXiv:1706.05587v3*, Dec. 2017.

DeepLabv3+

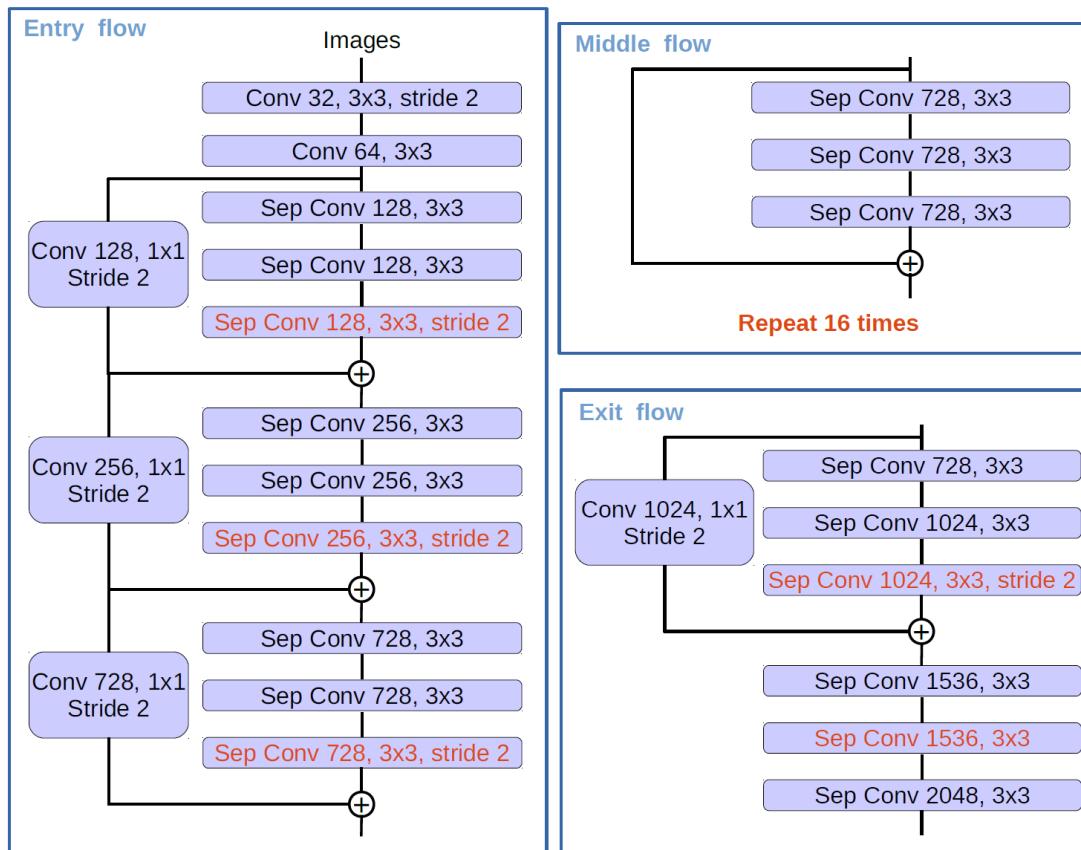
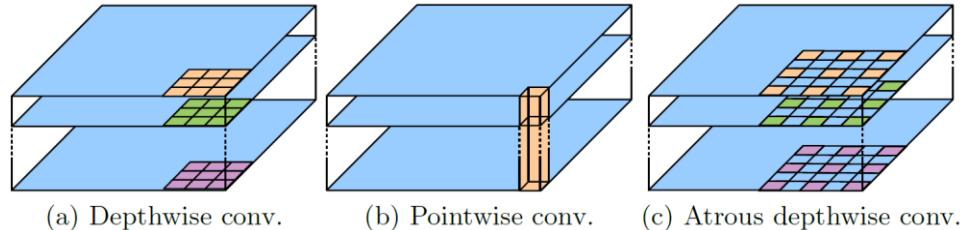
- Encoder-decoder architecture



L.-C. Chen, Y. Zhu, G. Papandreou, F. Schroff, and H. Adam, “Encoder-decoder with atrous separable convolution for semantic image segmentation,” *ECCV 2018*.

DeepLabv3+

- Xception



L.-C. Chen, Y. Zhu, G. Papandreou, F. Schroff, and H. Adam, “Encoder-decoder with atrous separable convolution for semantic image segmentation,” *ECCV 2018*.

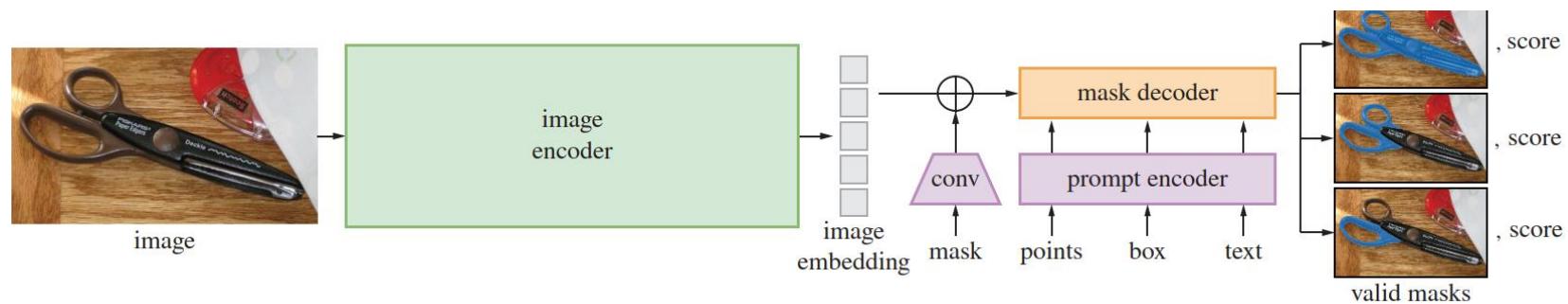
DeepLabv3+

- Test results on PASCAL VOC 2012

Method	mIOU
Deep Layer Cascade (LC) [82]	82.7
TuSimple [77]	83.1
Large_Kernel_Matters [60]	83.6
Multipath-RefineNet [58]	84.2
ResNet-38_MS_COCO [83]	84.9
PSPNet [24]	85.4
IDW-CNN [84]	86.3
CASIA_IVA_SDN [63]	86.6
DIS [85]	86.8
DeepLabv3 [23]	85.7
DeepLabv3-JFT [23]	86.9
DeepLabv3+ (Xception)	87.8
DeepLabv3+ (Xception-JFT)	89.0

L.-C. Chen, Y. Zhu, G. Papandreou, F. Schroff, and H. Adam, “Encoder-decoder with atrous separable convolution for semantic image segmentation,” *ECCV 2018*.

Segment Anything Model (SAM)



- <https://segment-anything.com/>

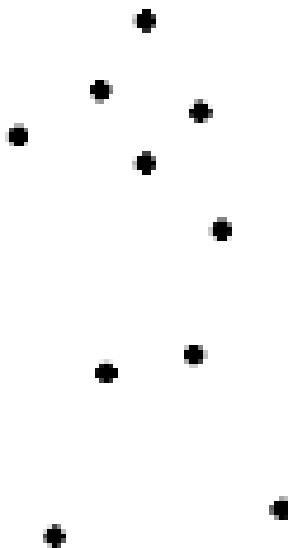
Motion and Perceptual Organization

- Sometimes, motion is foremost cue



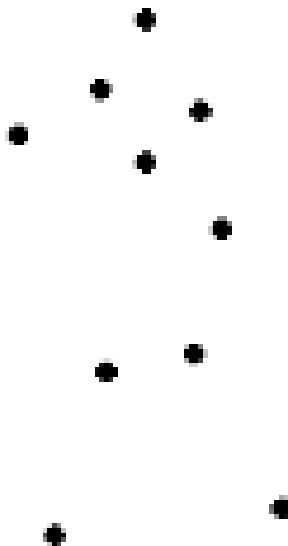
Motion and Perceptual Organization

- Even “impoverished” motion data can evoke a strong percept



Motion and Perceptual Organization

- Even “impoverished” motion data can evoke a strong percept



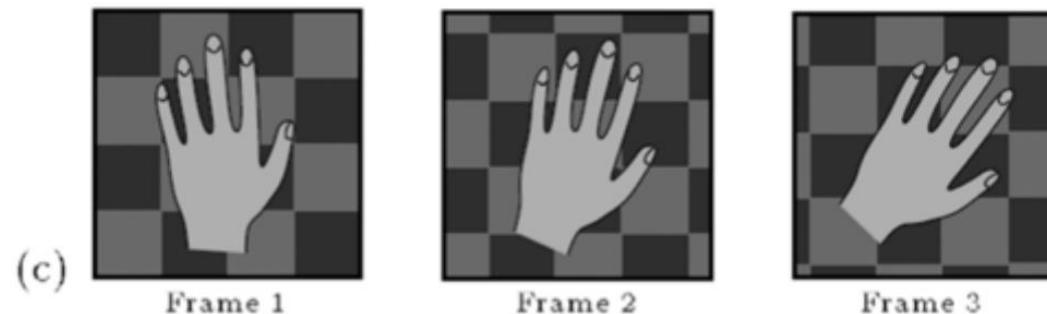
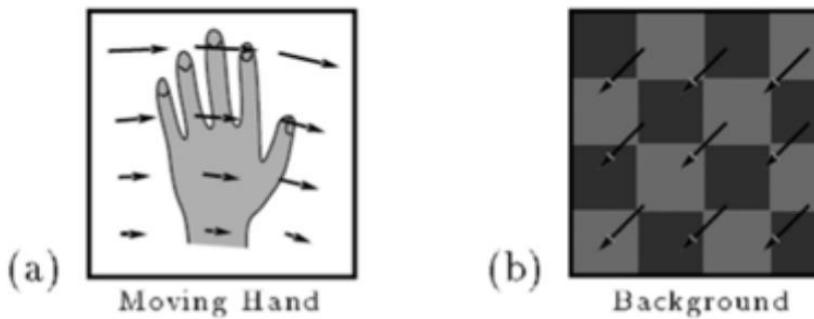
Video Segmentation: Segmentation in Motion Field

- Break image sequence into “layers” each of which has a coherent (affine) motion



Video Segmentation: Segmentation in Motion Field

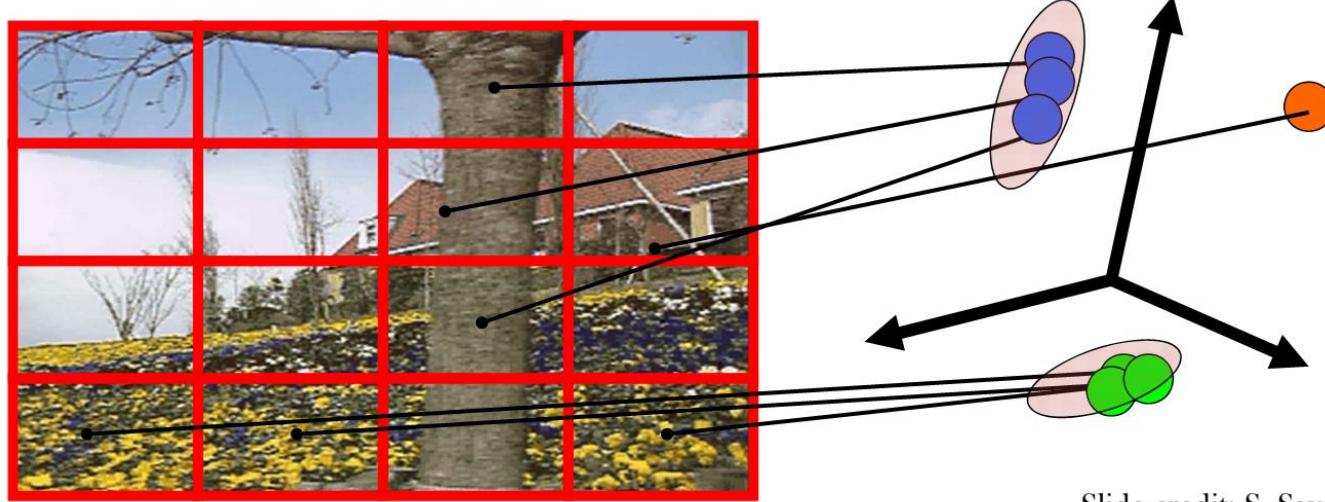
- What are layers?
 - Each layer is defined by an alpha mask and a motion model (such as affine model)



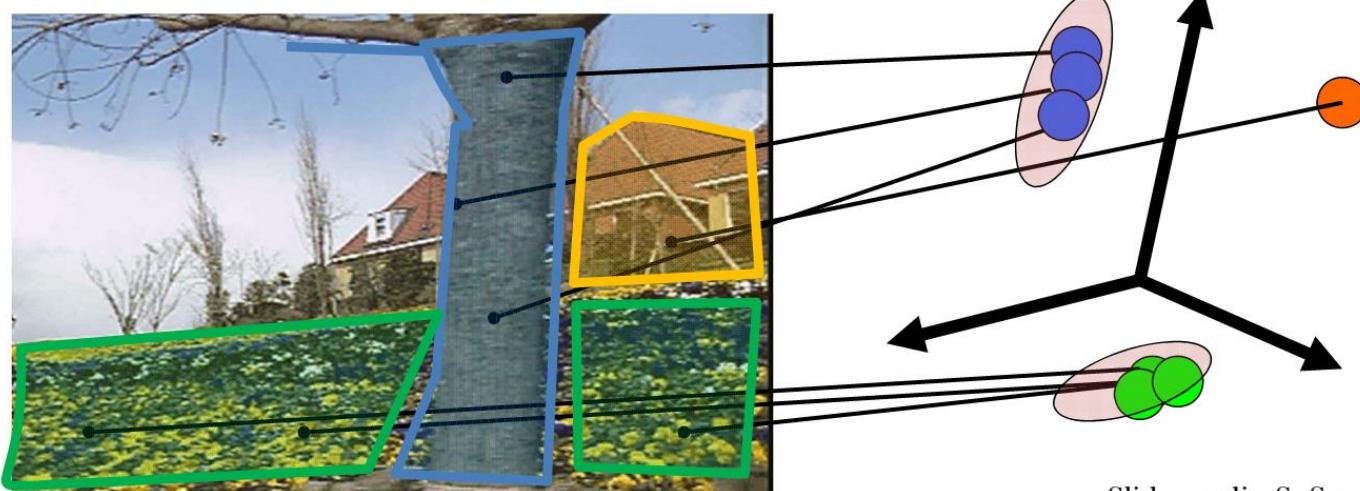
Video Segmentation: Segmentation in Motion Field

- 1. Obtain a set of initial affine motion hypotheses
 - Divide the image into blocks and estimate affine motion parameters in each block by least squares
 - Eliminate hypotheses with high residual error
 - Map into motion parameter space
 - Perform k-means clustering on affine motion parameters
 - Merge clusters that are close and retain the largest clusters to obtain a smaller set of hypotheses to describe all the motions in the scene
- 2. Iterate until convergence:
 - Assign each pixel to best hypothesis
 - Pixels with high residual error remain unassigned
 - Perform region filtering to enforce spatial constraints
 - Re-estimate affine motions in each region

Video Segmentation: Segmentation in Motion Field



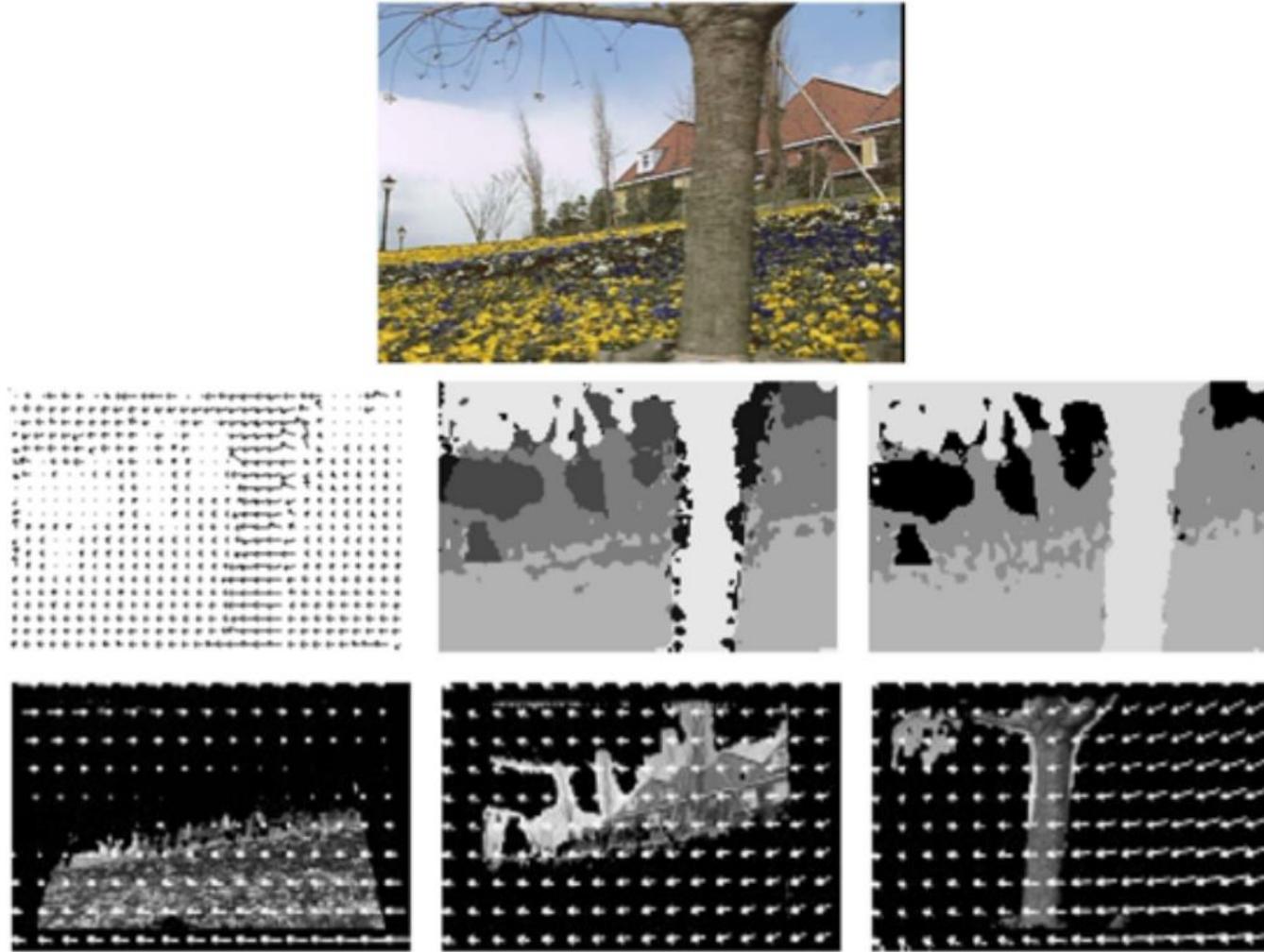
Slide credit: S. Savarese

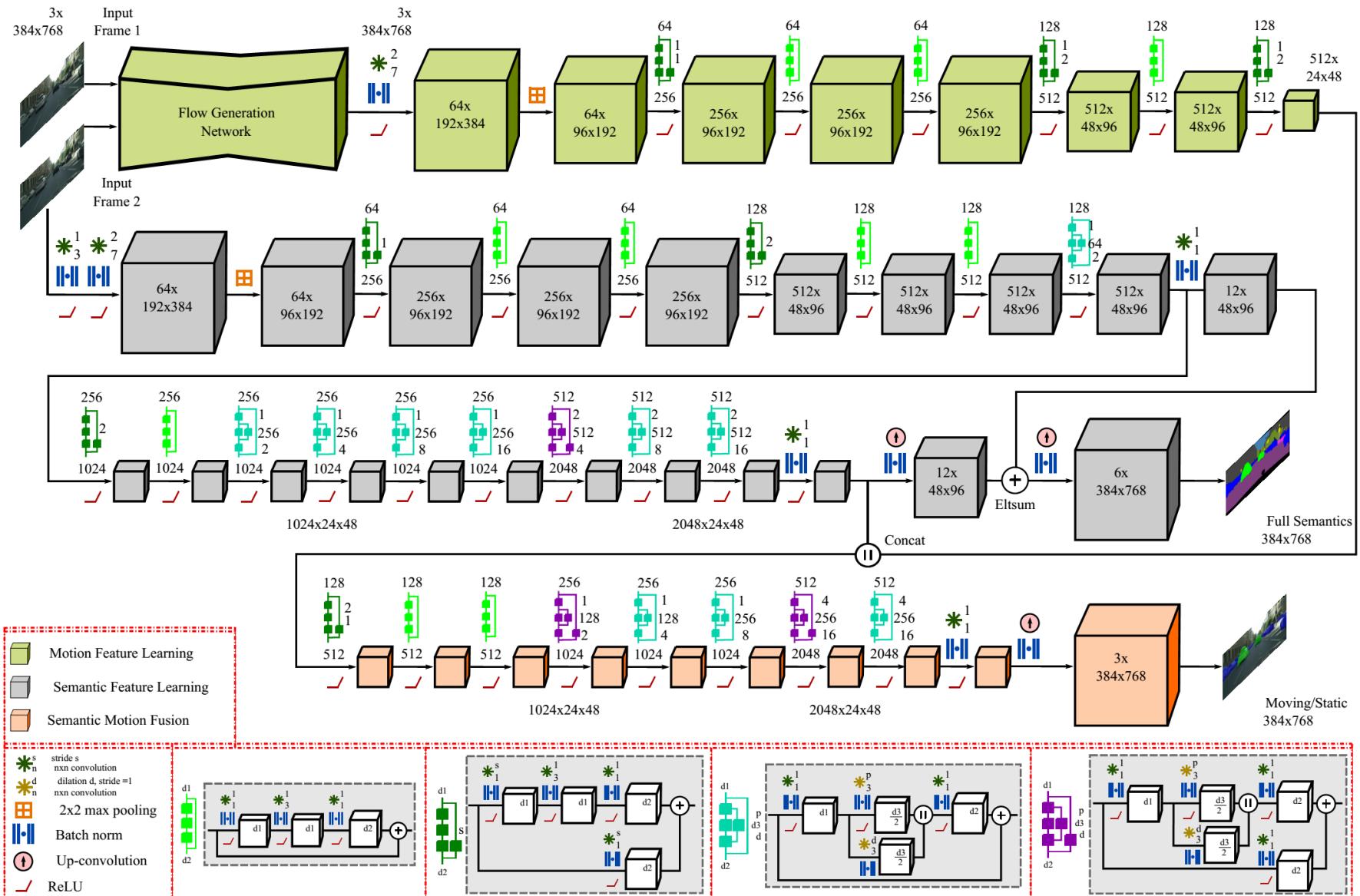


90

Slide credit: S. Savarese

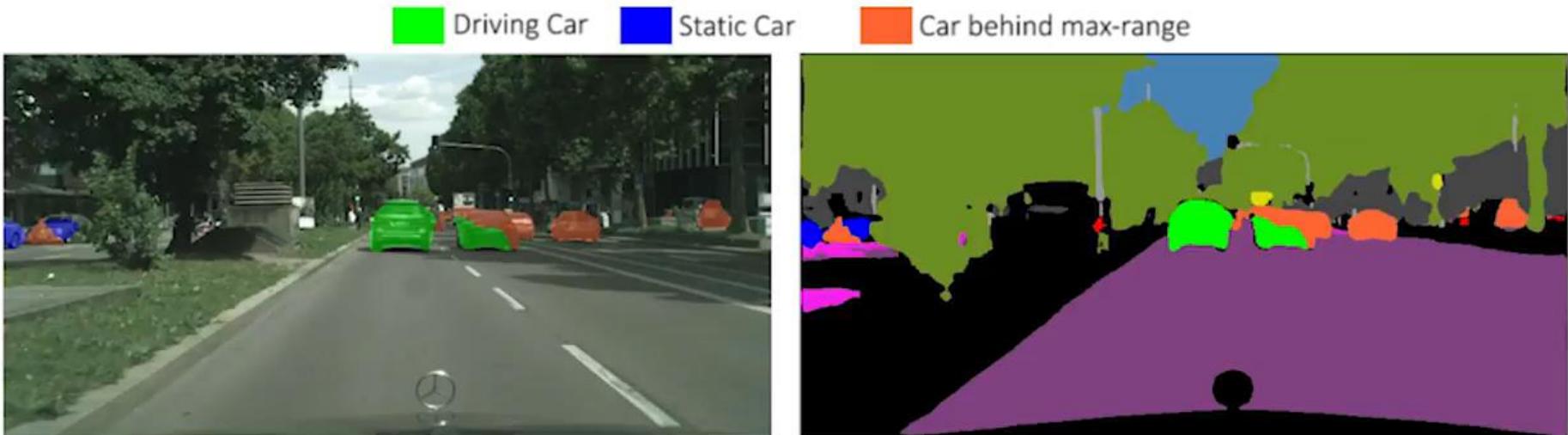
Video Segmentation: Segmentation in Motion Field





Ref: J. Vertens, A. Valada, and W. Burgard, "SMSnet: Semantic Motion Segmentation using Deep Convolutional Neural Networks," Proceedings of the IEEE/RSJ International Conference on Intelligent Robots and Systems, Vancouver, Canada, 2017.

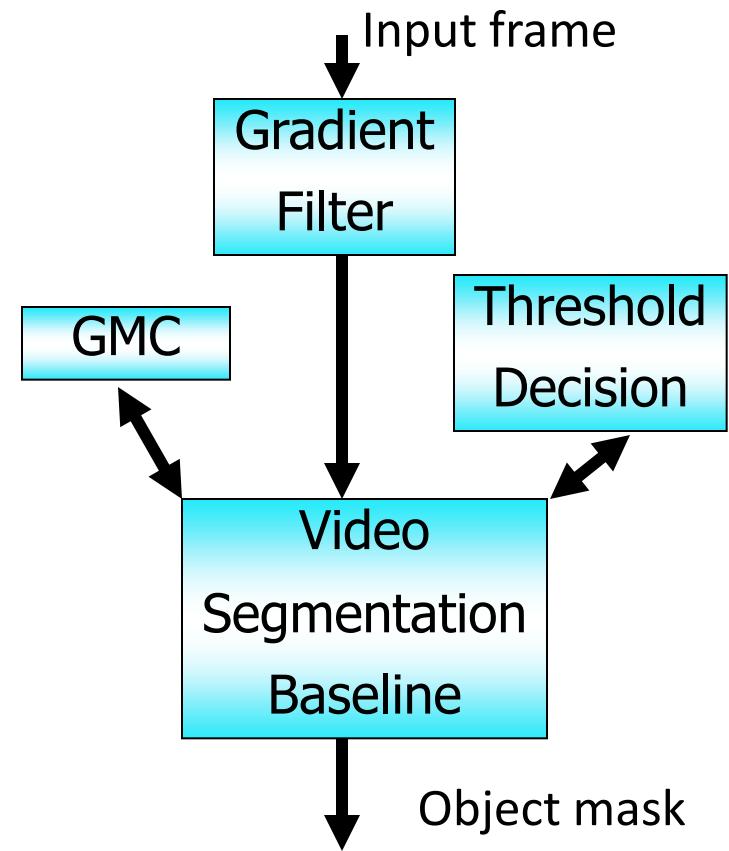
Qualitative Results- Cityscapes



Model trained with a maximum-range of 40m and EFS. All presented results are achieved by training SMSnet on City-KITTI-Motion.

Video Segmentation: Change Detection Method

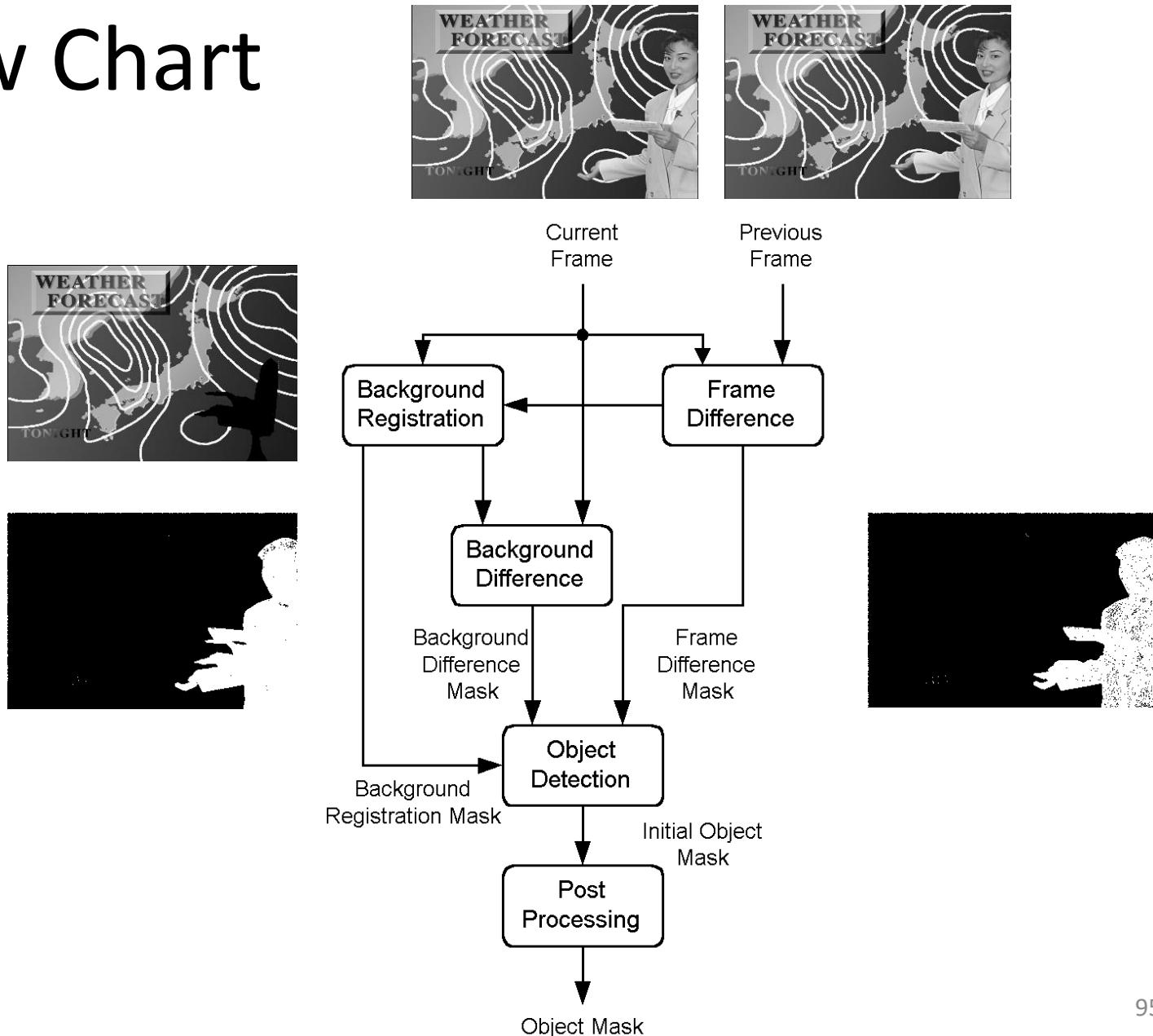
- Background subtraction
- 4 modes
 - Baseline mode
 - Shadow cancellation mode (SC mode)
 - Global motion compensation mode (GMC mode)
 - Adaptive threshold mode (AT mode)



Ref: Shao-Yi Chien, Yu-Wen Huang, Bing-Yu Hsieh, Shyh-Yih Ma, and Liang-Gee Chen, "Fast video segmentation algorithm with shadow cancellation, global motion compensation, and adaptive threshold techniques," *IEEE Transactions on Multimedia*, vol. 6, no. 5, pp. 732–748, Oct 2004.

Shao-Yi Chien, Shyh-Yih Ma, and Liang-Gee Chen, "Efficient moving object segmentation algorithm using background registration technique," *IEEE Transactions on Circuits and Systems for Video Technology*, vol. 12, no. 7, pp. 577 –586, July 2002.

Flow Chart



Background Registration



Segmentation Results



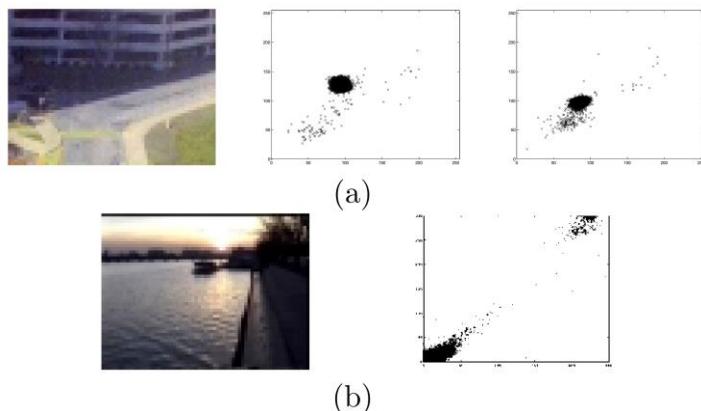
Segmentation Results



Video Segmentation: Change Detection Method

- Background modeling with Gaussian Mixture Model (GMM)
 - Background information is modeled as:

Variation of background information



- Every new pixel value, X_t , is checked against the existing K Gaussian distributions, until a match is found. A match is defined as a pixel value **within 2.5 standard deviations** of a distribution.
- Background model updating:

$$\mu_t = (1 - \rho)\mu_{t-1} + \rho X_t$$

$$\sigma_t^2 = (1 - \rho)\sigma_{t-1}^2 + \rho(X_t - \mu_t)^T(X_t - \mu_t)$$

where

$$\rho = \alpha\eta(X_t | \mu_k, \sigma_k)$$