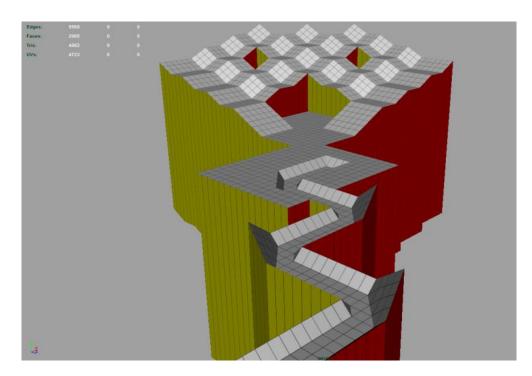
Game Technology

Lecture 9 – 12.12.2014 Physics 2





Dr.-Ing. Florian Mehm Dipl-Inf. Robert Konrad

Prof. Dr.-Ing. Ralf Steinmetz KOM - Multimedia Communications Lab

Preliminary timetable



| Lecture No. | Date | Topic |
|-------------|------------|-------------------------------|
| 1 | 17.10.2014 | Basic Input & Output |
| 2 | 24.10.2014 | Timing & Basic Game Mechanics |
| 3 | 31.10.2014 | Software Rendering 1 |
| 4 | 07.11.2014 | Software Rendering 2 |
| 5 | 14.11.2014 | Basic Hardware Rendering |
| 6 | 21.11.2014 | Animations |
| 7 | 28.11.2014 | Physically-based Rendering |
| 8 | 05.12.2014 | Physics 1 |
| 9 | 12.12.2014 | Physics 2 |
| 10 | 19.12.2014 | Procedural Content Generation |
| 11 | 16.01.2015 | Compression & Streaming |
| 12 | 23.01.2015 | Multiplayer |
| 13 | 30.01.2015 | Audio |
| 14 | 06.02.2015 | Scripting |
| 15 | 13.02.2015 | AI |

Announcement



Game Jams

Game development contest

Global Game Jam 2015@TUD

• Fr., 23.01.2015, 17:00 –

So, 25.01.2015, 17:00

- Vague theme (e.g. "10 seconds")
- Tight time constraints (e.g. 48 h)
- Starting from scratch (design, assets, code, ...)
- No excuses just submit something…

Registration (first-come-first-serve):

gamejam@kom.tu-darmstadt.de



The Head Wizards Course.



A Maze Thing, 2013



10 Seconds to Apocalypse, 2013



10sion, 2013

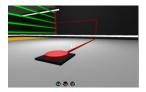




The Most Important 10 Seconds Of Your Life, 2013



As We Are, 2014



Neon Multiverse, 2014



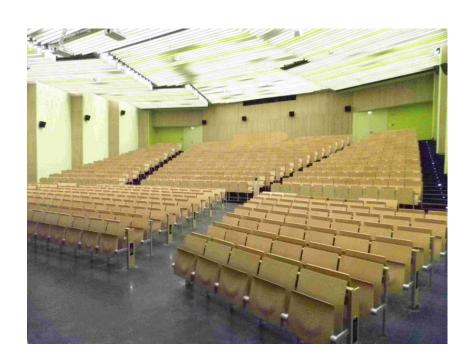
10Up Experiments: Mountain Brew, 2014

Announcement 2



The exam is now scheduled for

Friday, 06. March 2015 09-11 AM S101/A1



Adding Physics to Marbellous



Collision with the level

- Level supplied by artist as 3D mesh
- How to handle the collisions with the mesh?

Friction

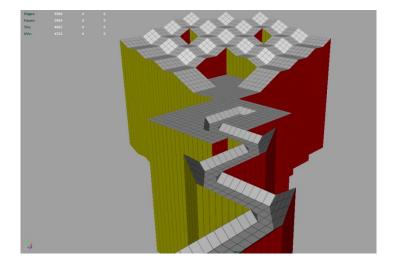
- Handle rotations
- Add friction

Controls

Apply forces when keys are pressed

(Camera control

- Keep the ball in view
- Don't follow every single movement)



Hand-placed colliders



Sometimes good placeholders for objects or level geometry

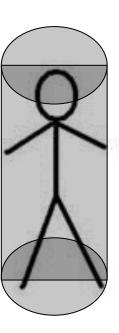
Planes

- Ground plane
- Simple intersection

Boxes

Spheres

Capsules



Height map

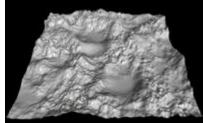


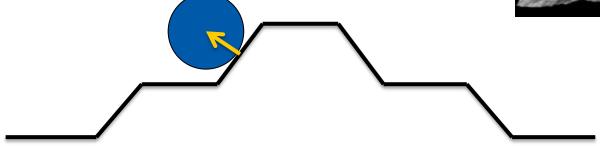
Supplied as a texture or generated

Gives height values at grid points

By interpolating, we can find the height of the mesh under the sphere and the normal







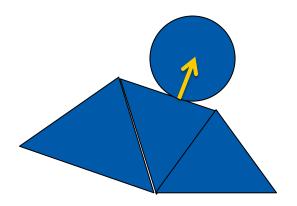
Using the mesh itself



Intersection with triangles

Check all triangles

If sphere intersects a triangle, handle the collision



Using the mesh itself



Intersection with triangles

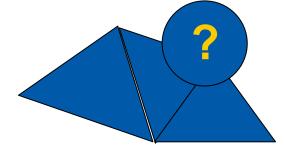
Check all triangles

If sphere intersects a triangle, handle the collision



If there are multiple collisions

- Handle only one (most prominent)
- Handle all



Separating Axis Test



If two objects are separated, there must be an axis which separates the two objects

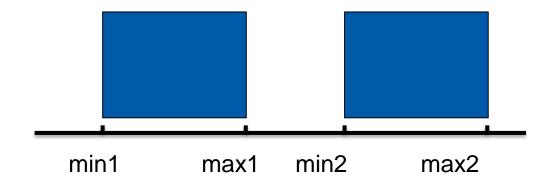
- ("Separating Axis Theorem" → Not a theorem follows from Hyperplane separation theorem by Hermann Minkowski)
- First mentioned in computer graphics in 1995

Separating Axis Test



More exact

- There must be points P1 and P2 of objects 1 and 2 such that the normal resulting from P2 P1 is a separating axis
- Separating Axis
 - Project all points of the objects onto the separating axis
 - We get the minimal and maximal points min1, min2 and max1, max2
 - The objects are separated iff max1 < min1 or max2 < min1</p>



Separating Axis Test



Infinite set of possible points to test for

It can be proven that an upper boundary exists

- Only the relevant axes have to be tested for
- If separation exists on any axis, the test is done → early out for positive test result
- If no separation exists, we still have to test all combinations of features → no early out for negative tests
 - Can be more efficient to reject the test based on other information, e.g. bounding boxes

For polygonal objects, the features are

- Faces
- Edges
- Vertices

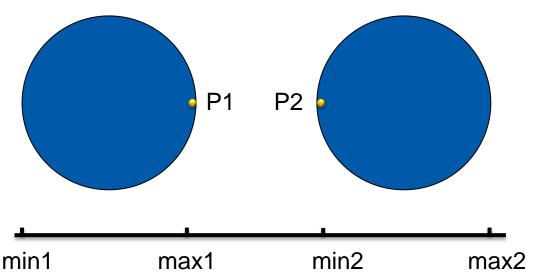
Separating axes for spheres



Spheres have no clear feature points

We have already used the separating axis test, though

- The relevant features for two spheres are the two closest points of the spheres
- We find them by finding the axis from one sphere's center to the other's center
- The intersection test in the previous lecture used this axis for testing intersections



Triangle-Sphere-Test



Relevant Features of the Triangle

- Face (x1)
- Vertices (x3)
- Edges (x3)

Relevant feature of the sphere

■ The point on the surface closest to the feature of the triangle

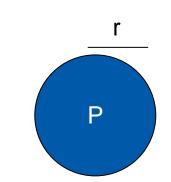
SAT: Testing the plane of the triangle



(We have done this test already – need to define the plane)

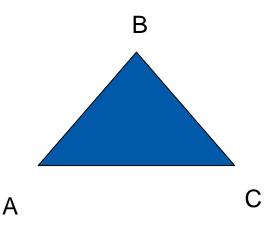
Normal: Use the cross product (very useful for finding normal vectors)

■ $n = normalize((B - A) \times (C - A))$



Distance

- Insert one of the points into the equation for distance
- n*A d = 0 (since A lies on the plane of the triangle)
- $\rightarrow n^*A = d$



Test for separation

Separation = distance(Plane, P) > r



Here shown for A (similar for B and C) Finding the sphere's feature

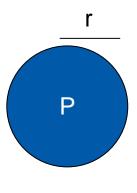
Along the line from A to P

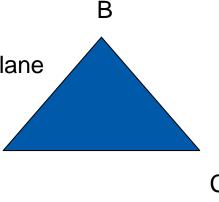
Compute distance from A to P

Separation (along this axis) iff

■ Distance d > r

And B and C lie on the opposite side of the separating plane

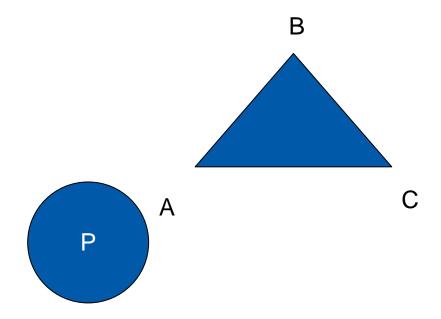




Α

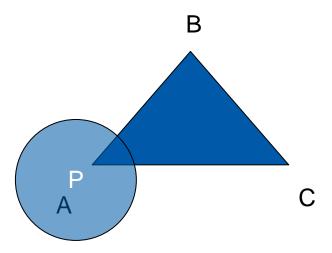


- Distance d > r
- And B and C lie on the opposite side of the separating plane



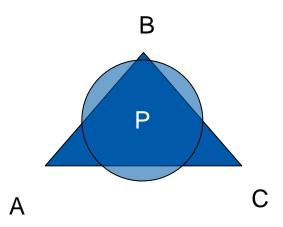


- Distance d > r
- And B and C lie on the opposite side of the separating plane



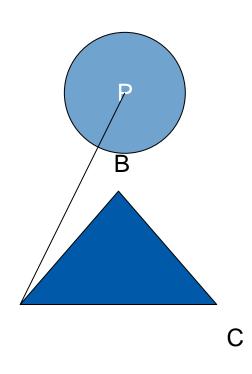


- Distance d > r
- And B and C lie on the opposite side of the separating plane





- Distance d > r
- And B and C lie on the opposite side of the plane
- → We assume that A-P is the separating axis
- → No check if A is the closest point
- → B and C might be separating axes!





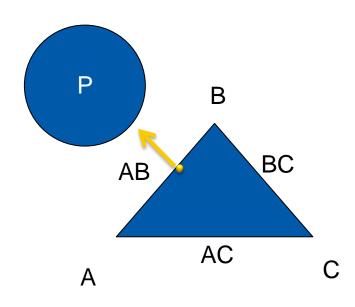
Here shown: AB

Find a point for Q for which Q-P is a normal vector orthogonal to AB

- → Projection of P onto AB
 - → Use the dot product (ideal for projecting vectors onto each other)

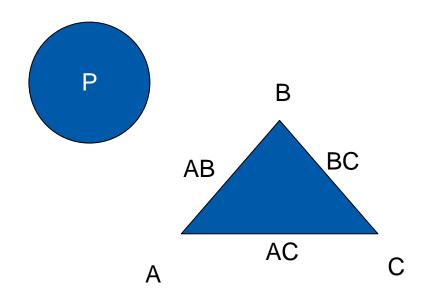
Determine the distance d of Q to P

- Distance d > r
- C lies on the other side of the plane through AB with normal PQ



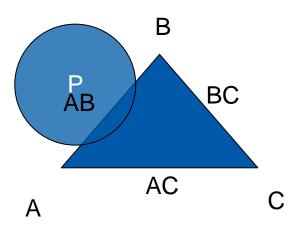


- Distance d > r
- C lies on the other side of the plane through AB with normal PQ



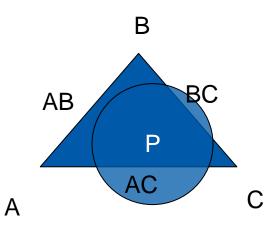


- Distance d > r
- C lies on the other side of the plane through AB with normal PQ





- Distance d > r
- C lies on the other side of the plane through AB with normal PQ



Speeding the calculation up

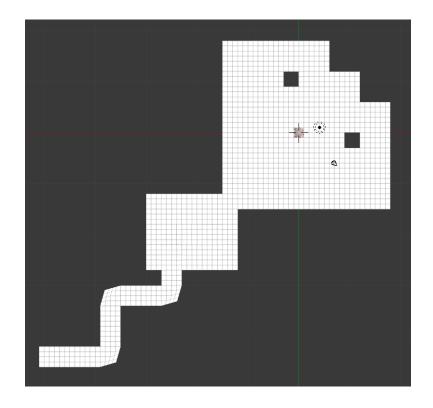


Note: In our case, the level is essentially 2D

Most of our collisions will be from the top of the level

Use a space partition

- Regular Grid
- Quadtree
- KD-Tree
- BSP



Regular grid



Subdivide space regularly

E.g. specify

- Cell size in units
- Start point

For each cell

- Test if an object intersects (partly) with the cell
- If so, save a reference to this object
- (Objects can be in several cells)

Advantages

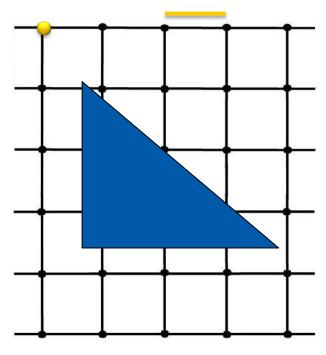
- Easy to compute
- Lookup of cells is trivial

Disadvantages

- Sparsity kills the performance
- Clusters

Start point

Cell size



Quadtree(2D), Octree(3D)



Start with a rectangular shape

Subdivide the space into 4 or 8 subdivisions of equal size if the number of contained objects is too large

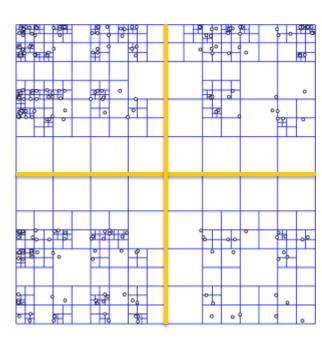
Until the required minimal number of objects per subdivision is found

Advantages

- Still simple lookup where an object is placed
- Can handle clusters better

Disadvantages

Can cope less with changing number and position of objects



KD-Tree



Similar idea to Quad/Octree Subdivide starting from a rectangular shape

Choose the subdividing line

E.g. median point of the contained objects (cutting them in half)

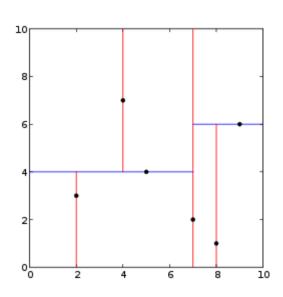
Alternate axes for subdivision

Advantages:

Well suited for clusters

Disadvantages

Lookup harder than octree



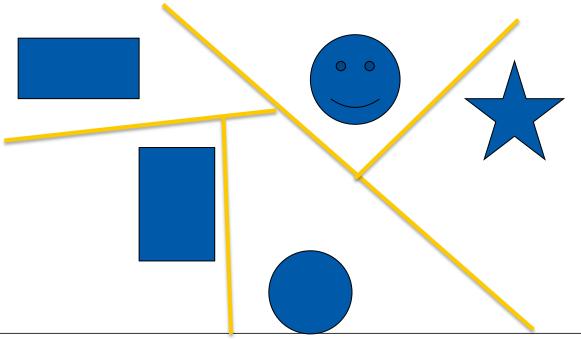
Binary Space Partition



Generalization of KD-Tree

Subdivide the space into half-spaces with arbitrary planes

Used previously to speed up rendering (Quake Engine)



Reducing the dimensionality



Many problems in 3D games are essentially 2D

- Heightmaps
- Top-down shooters
- Real-Time Strategy games
- **.**..

In Marbellous, we can expect that

- No overhangs are present in the level
- The sphere will stay close to the mesh at all times

If we look at the level from above, we can see that if we put a grid over the game world, only the triangles in the same 2D cell can be possibly colliding

→ During initial setup and the lookup, project everything into 2D

Lookup



Saving the triangles

- We should save only the triangles that are contained in the grid cell
- → We need to check intersection between a rectangle and a triangle

Minimizing storage

- Re-use the vertex and index buffer
- Save only the index of the triangle
 - (Ideally, we will not suffer from too many cache misses, since the goal in the first place is to reject most collision tests early)

Intersection between the triangles and the grid

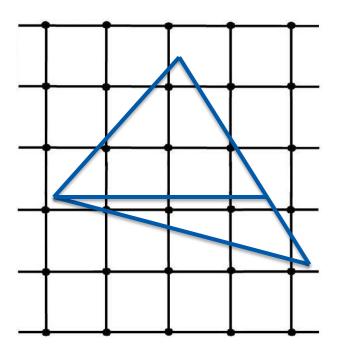


Re-use the scanline rasterization algorithm

- Very similar task
- But have to watch out due to larger cell size

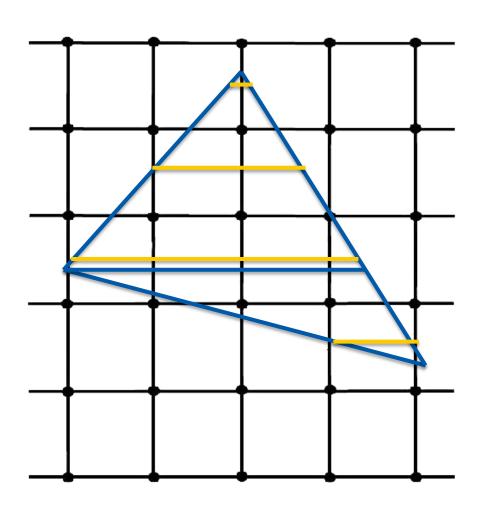
Original algorithm

- Find edge longest with biggest ydif
- Fill lines between long edge and other edge 1
- Fill lines between long edge and other edge 2



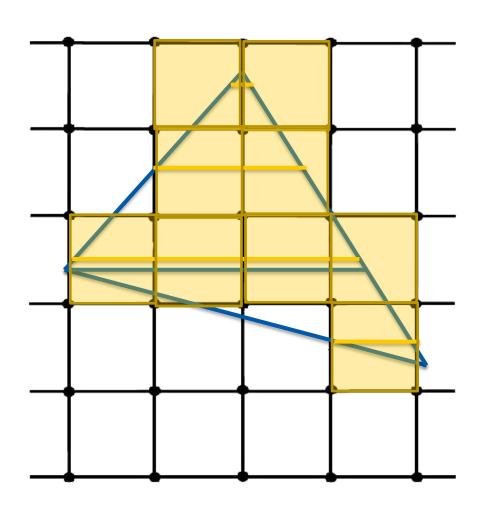
Triangle Rasterisation





Triangle Rasterisation





New algorithm



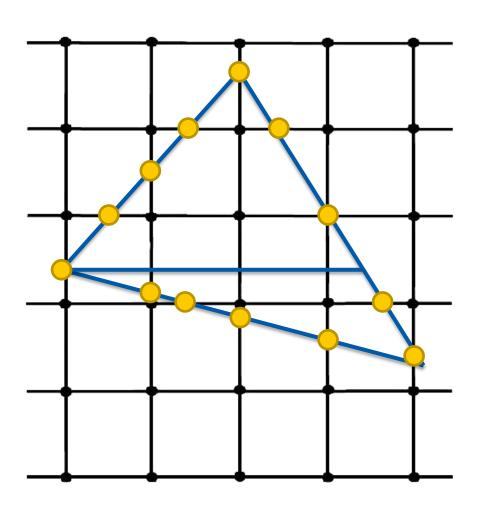
Calculate intersection with all grid lines

For each row

- Left extent is the minimal intersection point
- Right extent is the maximal intersection point

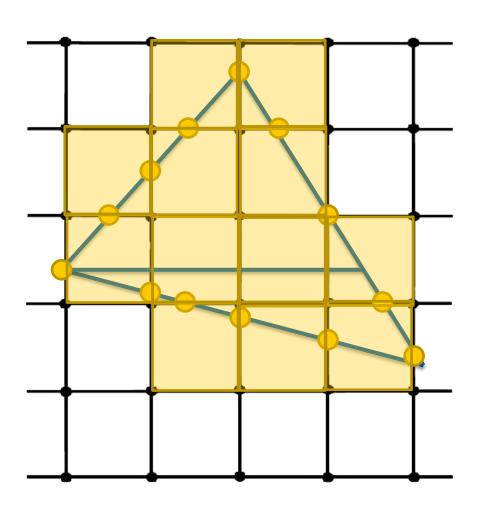
Triangle Rasterisation





Triangle Rasterisation





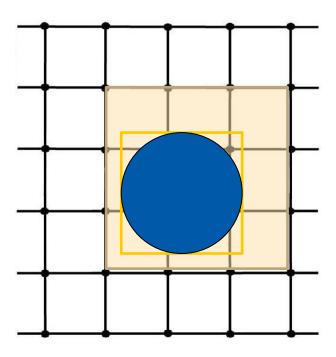
Intersection between the sphere and the grid



Use the bounding box of the sphere

Defined by the extents in the x-z-**Plane**

(Or implement rectangle-sphere intersection)



Is it worth it?



No (at least not for our exercise)

On a Core2 Duo @2.7 GHz, the intersection with the mesh takes about 0.908 ms in Release mode

But, for production code, larger meshes and more objects, it could become relevant

(Triangle-Sphere Intersection implemented with optimized code by Christer Ericson, http://realtimecollisiondetection.net/blog/?p=103)

Broad Phase vs. Narrow Phase



Broad Phase

Rule out as many possible collisions

Only call narrow phase if separation can not be proven here

Reduce the problem

- Use spatial data structures (grid, octree, etc.)
- Use bounding volumes (and bounding volume hierarchies)

Narrow Phase

Check for exact collisions

Use exact tests

E.g. based on SAT

Should be much slower than broad phase and therefore seldomly called

Provide collision data to resolver

Time Handling



Fixed Time Step

- Explicit Time Step → Our method
- (Semi-)Implicit Time Step Method
 - Try to predict the times of collisions and handle them at the beginning

Adaptive Time Step

- Retroactive Detection
 - If there is interpenetration at t +deltaT, use deltaT *= 0.5 and retry
- Conservative Advancement
 - Predict the next time of collision
 - Advance to this time

Continuous Collision Detection

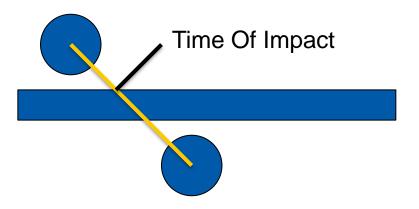


Check if an object moved through another in the frame

- On one side before, on one side after
- Swept shape algorithms

Time of impact ordering

Go to time of impact, resolve there

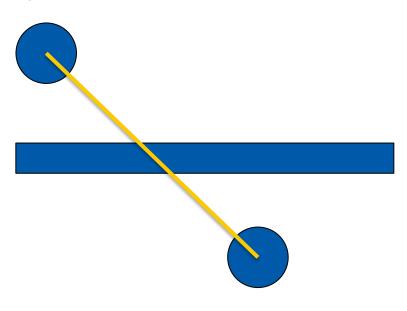


Speculative Contact



Calculate the distance to the collider

Remove just enough velocity so they touch in the next frame

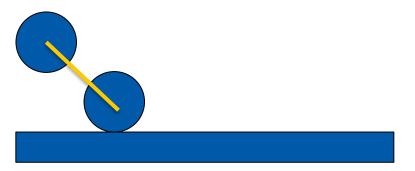


Speculative Contact



Calculate the distance to the collider

Remove just enough velocity so they touch in the next frame



Constraints



Stiff constraints

- Keep objects at an exact length compared to each other
- E.g. when attached to a steel cable



Springs

- Variable length between objects
- E.g. when attached to a bungee rope

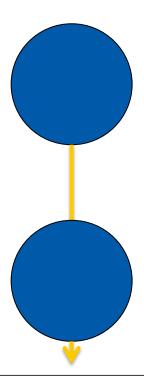


Stiff Constraints - Rods



Distance between two objects is determined to stay constant

→ Separating Velocity between the two objects along the vector from one to the other should be 0 at all times

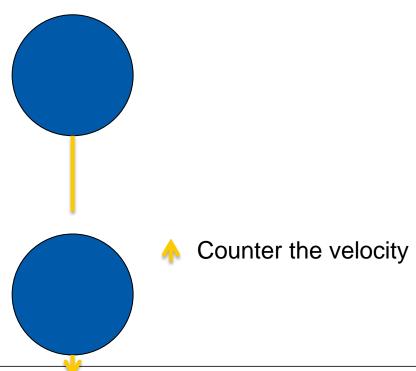


Stiff Constraints - Rods



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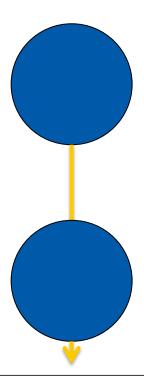


Stiff Constraints - Rods



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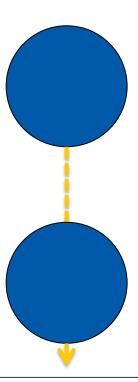
Spring Constraints



Model a spring between two objects (one might be stationary)

Spring force

- Rest length (no force)
- Stiffness
- (Breaking point)



Hooke's Law



$$F = -k * (I - I0)$$

F: Spring force

k: Spring constant (stiffness)

I: Current length of the spring

10: Rest length of the spring

Apply the resulting force to the objects that are attached (One might be immovable)

Stiffness



Also a property of numerical systems

The stiffer, the more problems we face \rightarrow exploding systems

J. D. Lambert: "If a numerical method with a finite region of absolute stability, applied to a system with any initial conditions, is forced to use in a certain interval of integration a steplength which is excessively small in relation to the smoothness of the exact solution in that interval, then the system is said to be stiff in that interval."

Particle networks



Connect multiple particles with springs

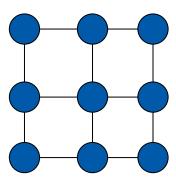
Approximation for deformable objects

Often used for cloth



Problems/Challenges

- Stiff constraints
- Self-intersections
- Stability



Deformable objects



Generalization of particle networks

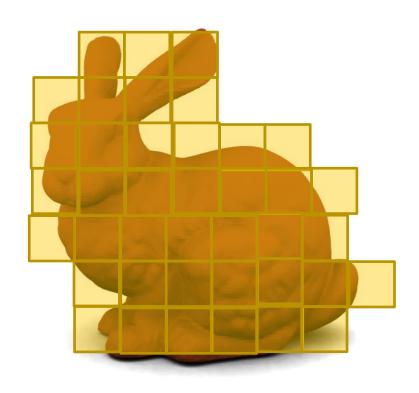
Finite Element Method from Mechanics

Model forces inside the object

- Stress
- Strain

Gasses, Liquids

- Discretize into a vector field
- Calculate flow by solving the Navier-Stokes-Equations



Collision handling schemes

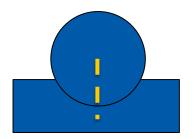


Impulse-based Micro-Collisions

What we are using

Spring-Based

- Insert a spring at the point where the collision is detected
- Forces the objects out again



Constraint-Based

Formulate the collisions as violations of constraints



Aka. Propagating Impulses

Stability

- Add iterations
- Solve impulses in order of importance



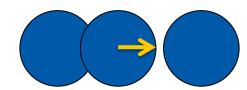
- Few, "large" contacts → need fewer iterations
- Many contacts → need more iterations



Aka. Propagating Impulses

Stability

- Add iterations
- Solve impulses in order of importance



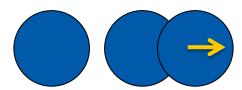
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Aka. Propagating Impulses

Stability

- Add iterations
- Solve impulses in order of importance



- Few, "large" contacts → need fewer iterations
- Many contacts → need more iterations



Aka. Propagating Impulses

Stability

- Add iterations
- Solve impulses in order of importance



- Few, "large" contacts → need fewer iterations
- Many contacts → need more iterations

Constraint-based



Constraint Vector

- For each collision or constraint
- Equality constraint
 - Objects should stay at a fixed relative position
- Inequality constraints
 - E.g. for separating objects after collisions

For each collision, add a constraint to the constraint vector

Results in a large system of equations

Solve via Linear Complementarity Problem (LCP)

Other integrators



Runge Kutta 4th order (RK 4)

Approximate from 4 values

$$y_{n+1} = y_n + \frac{h}{6} (k_1 + 2k_2 + 2k_3 + k_4)$$

$$t_{n+1} = t_n + h$$

$$k_1 = f(t_n, y_n),$$

$$k_2 = f(t_n + \frac{h}{2}, y_n + \frac{1}{2}k_1h),$$

$$k_3 = f(t_n + \frac{h}{2}, y_n + \frac{1}{2}k_2h),$$

$$k_4 = f(t_n + h, y_n + k_3h).$$

Velocity-less Verlet integration

- Uses no explicitly saved velocity
- Instead, uses position difference between this and previous calculation

Rotation



Angular Velocity, Acceleration

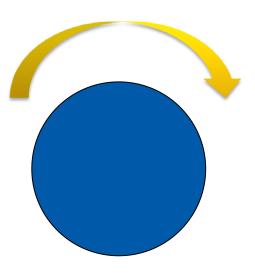
- Save as additional properties
- Velocity: 3-Vector, Rotations around x, y, z axis
- Accelaration: Change in angular velocity

Mass Moment of Inertia

Property that resists the change in angular velocity

Torque

Force acting off-center

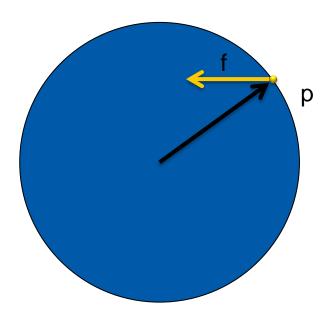


Torque



torque = p x fp is the point of application f is the force applied

Note: If p and f are in the same direction → No torque



Mass Moment of Inertia

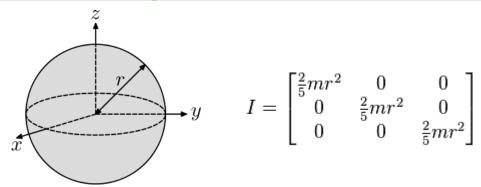


Inertia Tensor – Generalized version of a matrix

For purposes of games, most often 3x3

Diagonal Matrix for moments of inertia about x, y, z-axis Off-center entries encode product of inertia

See http://en.wikipedia.org/wiki/List_of_moments_of_inertia



Inverse Inertia Tensor

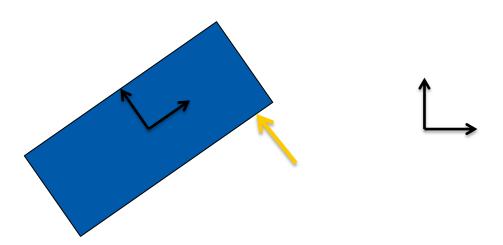


Remember the calculation of forces

$$F = m * a \rightarrow a = F / m$$

We need the inverse of the inertia tensor for the equivalent formula

Additionally, need to transform to the world coordinate system
→ Torques given in world coordinates



Integration



Add an accumulator for Torque (D'Alambert's Principle also works here)

Add all forces to linear accumulator

Calculate torque for each force

Add torques to torque accumulator

Integration

• Multiply inverse mass moment of inertia with sum of torques

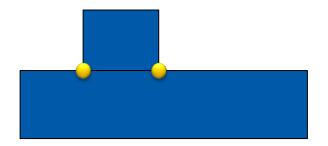
Handling non-spherical rigid bodies



E.g. a box

Can collide with any feature

- Face
- Vertex
- Edge



If we handle only one feature, the others would sink

Sequential impulses

- One part starts sinking into the floor
- Push up → Rotation
- Continue
- Needs iterations to get stable

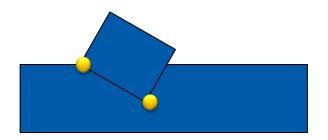
Handling non-spherical rigid bodies



E.g. a box

Can collide with any feature

- Face
- Vertex
- Edge



If we handle only one feature, the others would sink

Sequential impulses

- One part starts sinking into the floor
- Push up → Rotation
- Continue
- Needs iterations to get stable

Friction

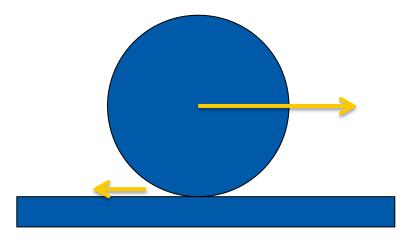


In the previous exercise, our spheres slided over the floor

- → No rotation
- →They came to rest because of dampening and not friction

Friction resists the spheres at the point of contact with the floor

- Rolling along the floor
- Different coefficients
 - Ice
 - Smooth floor
 - Sand
 - ...



Coulomb's Law



Depends on

- normal force that presses the surfaces together
- coefficient of friction
 - Most dry materials have a coefficient of friction of 0.1 to 0.6

Ff: Friction force

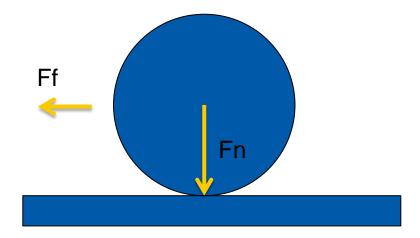
 μ : Coefficient of friction

Fn: Normal force

$$F_{\rm f} \leq \mu F_{\rm n}$$

In 3D

- Tangential plane
- Force lies in this plane



Friction



Static friction

- Keeps objects in place
- Start moving when the limit is overcome
- f_static <= k_static * |r|</p>
- k_static: Constant for friction between the involved materials
- r: Reaction force of the ground at the point of contact

Dynamic friction

- Force between the objects while they are sliding across
- f_dynamic = -v_planar * k_dynamic * |r|
- v_planar: The velocity of the object across the surface
- k_dynamic: Constant for dynamic friction

Contact basis

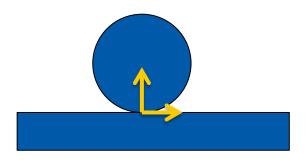


Calculating friction requires us to calculate the velocity along the contact

Handle collision with a collision basis

3 orthonormal vectors

- x: collision normal
- y, z: Perpendicular to x, define the plane of the contact



Calculating the contact basis



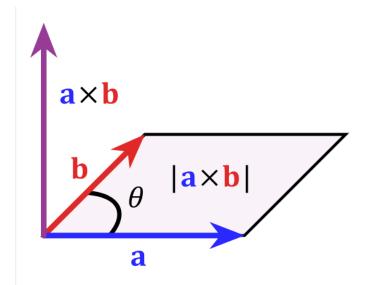
x: Contact normal

y: Choose a vector perpendicular to x

Cross product: A x B is perpendicular to A and B (unless they are parallel) Use an axis, e.g. global z $y = x \times (0, 0, 1)$

Choose third vector to be perpendicular to x and y

$$z = x \times y$$





Find contact basis

Calculate the change in velocity of the contact paint per unit impulse

Invert this to get a way to counter velocities

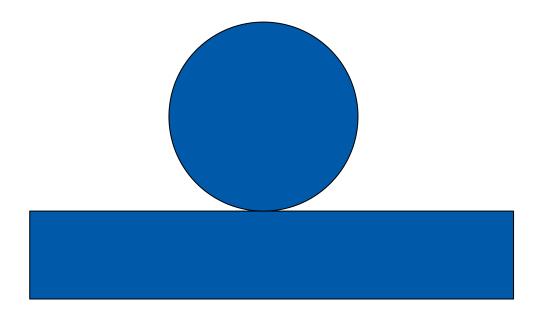
Calculate the x-term of the impulse (along the collision normal – our old calculation)

Calculate the y and z-terms of the impulse (for friction)

Apply the impulse

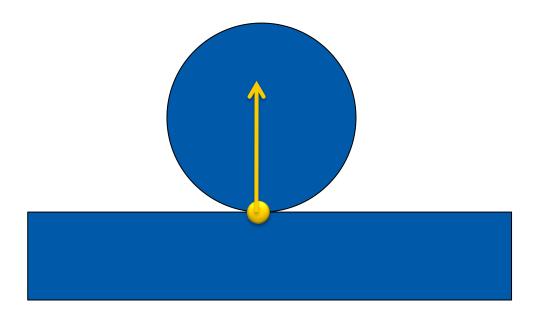


Find the collision collision normal and point of collision



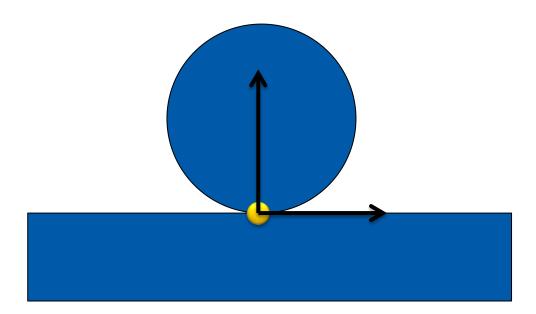


Find the collision collision normal and point of collision



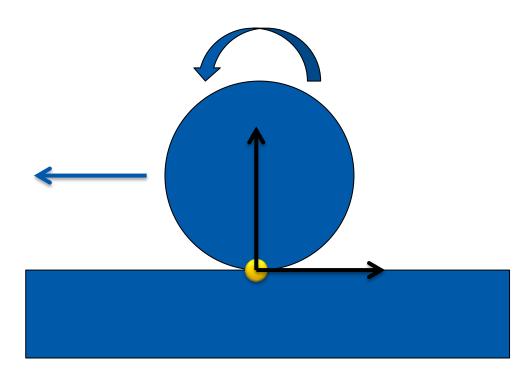


Find the collision basis



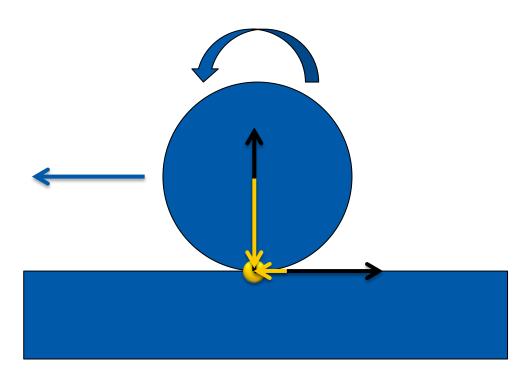
Identify the velocity of the collision point





Map velocity into the collision basis

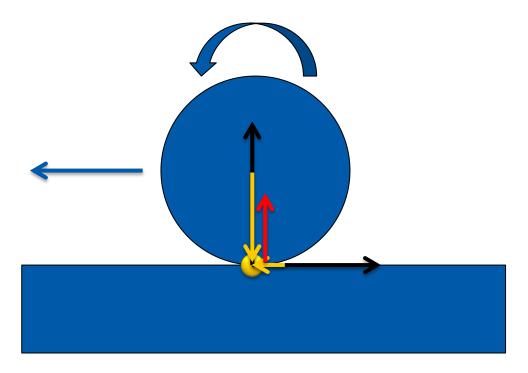




X-Axis (= collision Normal)



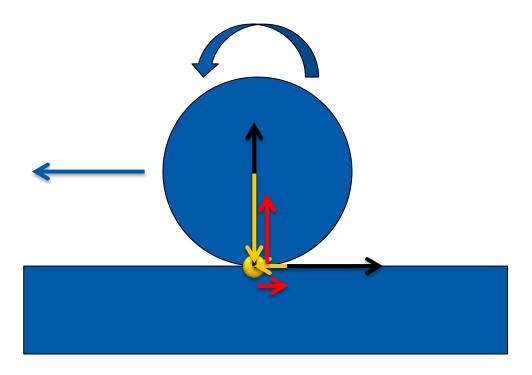
Separate the objects (what we did last lecture)



Y and Z-Axis



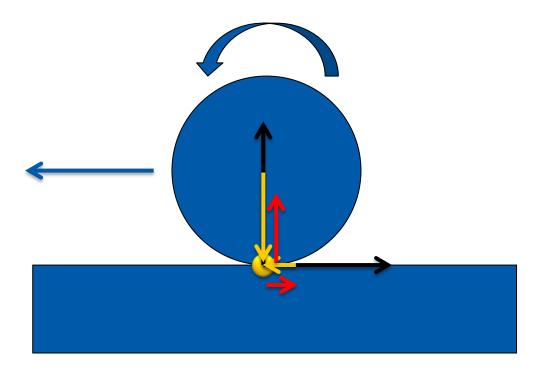
Handle Friction



Apply changes as impulses



Changes to velocity and rotation

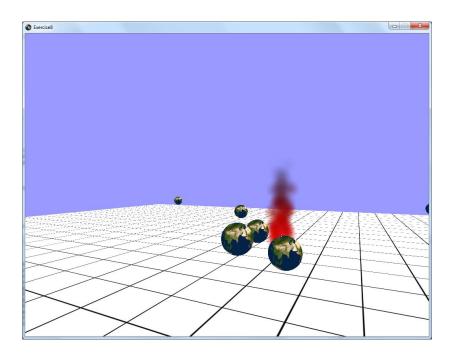


Exercise 8

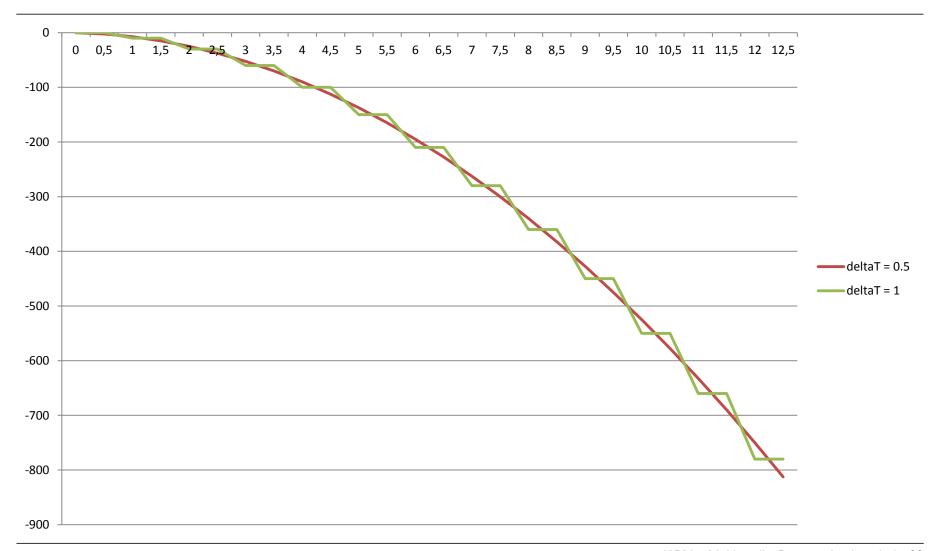


Practical Exercise

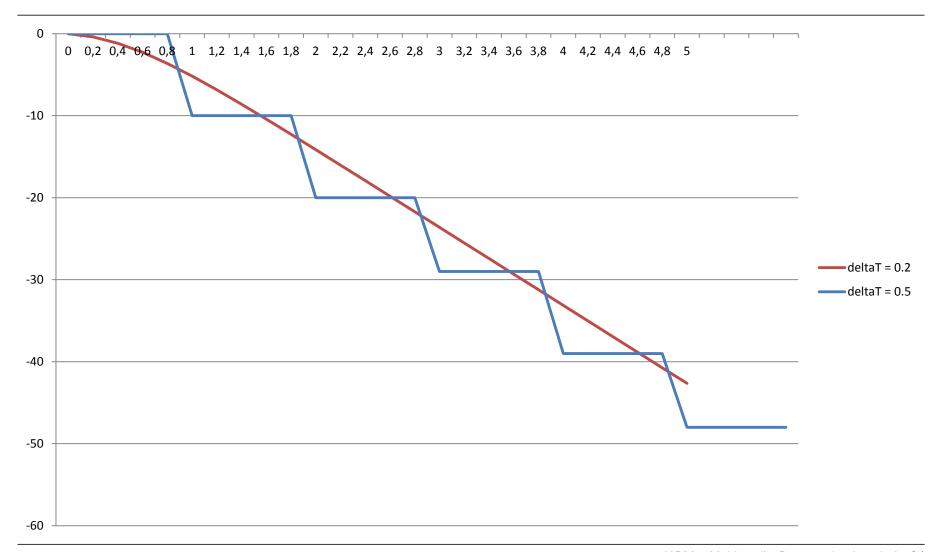
Solution will be uploaded













Build a matrix for billboarding that keeps the y-axis in place

- Using only the view matrix is a large restriction
- Easier to construct with knowledge of the object's position

Structure of the view matrix's rotation part

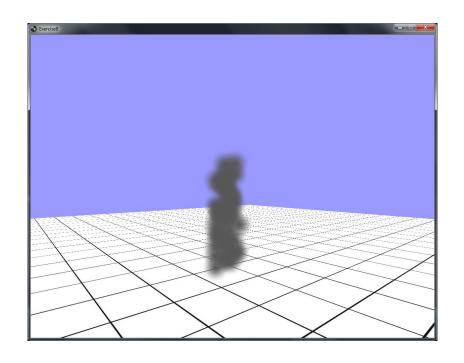
Change to

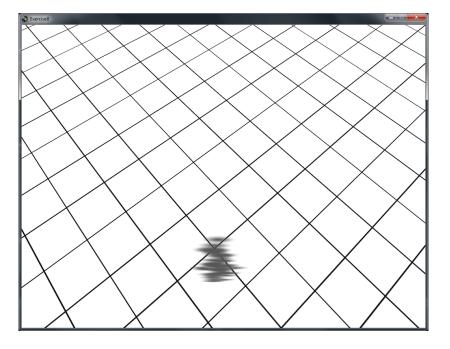
$$egin{pmatrix} 1 & up & 0 \ 0 & up & 0 \ 0 & up & 1 \end{pmatrix}$$

See also

http://www.lighthouse3d.com/opengl/billboarding/index.php3?billInt



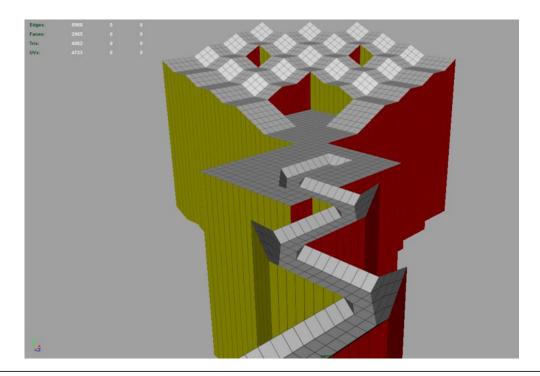




Exercise 9 – Practical Tasks



- 1.1 Triangle-Sphere-Intersection Check one of the SAT axes
- 1.2 Construct the collision basis
- 1.3 Implement a goal area See task 2.1



Exercise 9 – Theoretical Task

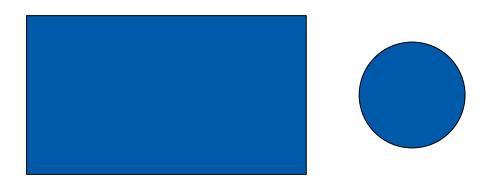


Build the foundation for task 1.3

Describe a box-sphere intersection test

Either

- Derive your own and describe it (does not have to be optimized)
- Describe one from the literature (name your source)



Questions & Contact







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