4주차 과제

11기 명재성

September 3, 2020

```
rm(list=ls())
```

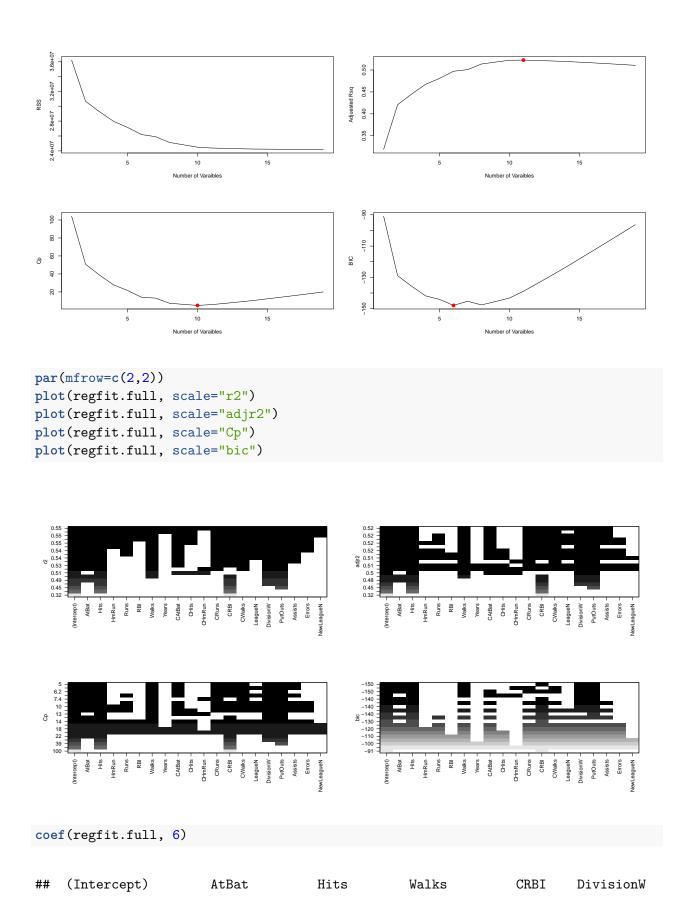
6.5 Lab 1: Subset Selection Methods

6.5.1 Best Subset Selection

```
library(ISLR)
fix(Hitters)
names(Hitters)
## [1] "AtBat"
                    "Hits"
                                                        "RBI"
                                "HmRun"
                                            "Runs"
                                                                    "Walks"
## [7] "Years"
                    "CAtBat"
                                "CHits"
                                            "CHmRun"
                                                                    "CRBI"
                                                        "CRuns"
## [13] "CWalks"
                    "League"
                                "Division"
                                            "PutOuts"
                                                        "Assists"
                                                                    "Errors"
## [19] "Salary"
                    "NewLeague"
dim(Hitters)
## [1] 322 20
sum(is.na(Hitters$Salary))
## [1] 59
Hitters = na.omit(Hitters)
dim(Hitters)
## [1] 263 20
```

```
sum(is.na(Hitters))
## [1] O
library(leaps)
regfit.full = regsubsets(Salary~., Hitters)
summary(regfit.full)
## Subset selection object
## Call: regsubsets.formula(Salary ~ ., Hitters)
## 19 Variables (and intercept)
               Forced in Forced out
##
## AtBat
                   FALSE
                               FALSE
## Hits
                   FALSE
                               FALSE
## HmRun
                   FALSE
                               FALSE
## Runs
                   FALSE
                               FALSE
## RBI
                   FALSE
                               FALSE
## Walks
                   FALSE
                               FALSE
## Years
                   FALSE
                               FALSE.
## CAtBat
                   FALSE
                               FALSE
## CHits
                   FALSE
                               FALSE
## CHmRun
                   FALSE
                               FALSE
## CRuns
                   FALSE
                               FALSE
## CRBI
                   FALSE
                               FALSE
## CWalks
                   FALSE
                               FALSE
## LeagueN
                   FALSE
                               FALSE
## DivisionW
                   FALSE
                               FALSE
## PutOuts
                   FALSE
                               FALSE
## Assists
                   FALSE
                               FALSE
## Errors
                   FALSE
                               FALSE
## NewLeagueN
                   FALSE
                               FALSE
## 1 subsets of each size up to 8
## Selection Algorithm: exhaustive
##
             AtBat Hits HmRun Runs RBI Walks Years CAtBat CHits CHmRun CRuns CRBI
## 1 (1)""
                                    11 11 11 11
                                               11 11
                                                                                  "*"
## 2 (1)""
                   "*"
                                                      11 11
                                                                                  "*"
## 3
     (1)""
                   "*"
                                                                                  "*"
      (1)""
                   "*"
                                                                                  "*"
## 4
                   "*"
                        11 11
                                                                                  "*"
      (1)"*"
## 5
                        11 11
                                               11 11
                                                                                  "*"
## 6
      (1)"*"
                   "*"
      (1)""
                               11 11
                   "*"
                        11 11
                                               11 11
                                                                           11 11
                                                                                  11 11
## 7
                                                             "*"
                                                                    "*"
                                                      11 11
                                                             11 11
## 8
      (1)"*"
                   "*"
                        11 11
                               11 11
                                      " "*"
                                               11 11
                                                                    "*"
                                                                           "*"
                                                                                  .. ..
##
             CWalks LeagueN DivisionW PutOuts Assists Errors NewLeagueN
      (1)""
                    11 11
                                        11 11
                                                11 11
                                                         11 11
## 1
## 2
     (1)""
                    11 11
## 3 (1)""
                                        "*"
                                                11 11
```

```
11 11
                                                             11 11
## 4 ( 1 ) " "
                   11 11
                           "*"
                                     "*"
                                                      11 11
## 5 (1)""
                   11 11
                           "*"
                                     "*"
                                              11 11
                                                      11 11
                                                             11 11
## 6 (1)""
                           "*"
                                      "*"
                                              11 11
## 7 (1)""
                           "*"
                                      "*"
                                              11 11
                                                      11 11
                                              11 11
## 8 (1)"*"
                   11 11
                           "*"
                                      "*"
regfit.full = regsubsets(Salary~., data=Hitters, nvmax=19)
reg.summary = summary(regfit.full)
names(reg.summary)
                                   "adjr2" "cp"
## [1] "which" "rsq"
                                                     "bic"
                                                              "outmat" "obj"
                         "rss"
reg.summary$rsq
   [1] 0.3214501 0.4252237 0.4514294 0.4754067 0.4908036 0.5087146 0.5141227
##
## [8] 0.5285569 0.5346124 0.5404950 0.5426153 0.5436302 0.5444570 0.5452164
## [15] 0.5454692 0.5457656 0.5459518 0.5460945 0.5461159
par(mfrow=c(2,2))
plot(reg.summary$rss, xlab="Number of Varaibles", ylab="RSS", type="1")
plot(reg.summary$adjr2, xlab="Number of Varaibles", ylab="Adjuested Rsq", type="l")
# which.max(req.summary$adjr2)
# [1] 11
points(11, reg.summary$adjr2[11], col="red", cex=2, pch=20)
plot(reg.summary$cp, xlab="Number of Varaibles", ylab="Cp", type="1")
# which.min(reg.summary$cp)
# [1] 10
points(10, reg.summary$cp[10], col="red", cex=2, pch=20)
plot(reg.summary$bic, xlab="Number of Varaibles", ylab="BIC", type="l")
# which.min(reg.summary$bic)
# [1] 6
points(6, reg.summary$bic[6], col="red", cex=2, pch=20)
```



```
## 91.5117981 -1.8685892 7.6043976 3.6976468 0.6430169 -122.9515338
## PutOuts
## 0.2643076
```

6.5.2 Forward and Backward Stepwise Selection

```
regfit.fwd = regsubsets(Salary~., data=Hitters, nvmax=19, method="forward")
summary(regfit.fwd)
## Subset selection object
## Call: regsubsets.formula(Salary ~ ., data = Hitters, nvmax = 19, method = "forward")
## 19 Variables (and intercept)
##
               Forced in Forced out
                   FALSE
## AtBat
                               FALSE
## Hits
                   FALSE
                               FALSE
## HmRun
                   FALSE
                               FALSE
## Runs
                   FALSE
                               FALSE
## RBT
                   FALSE
                               FALSE
## Walks
                   FALSE
                               FALSE
## Years
                   FALSE
                               FALSE
## CAtBat
                               FALSE
                   FALSE
## CHits
                   FALSE
                               FALSE
## CHmRun
                   FALSE
                               FALSE
## CRuns
                   FALSE
                               FALSE
## CRBI
                   FALSE
                               FALSE
## CWalks
                   FALSE
                               FALSE
## LeagueN
                   FALSE
                               FALSE
## DivisionW
                   FALSE
                               FALSE
## PutOuts
                   FALSE
                               FALSE
## Assists
                   FALSE
                               FALSE
## Errors
                   FALSE
                               FALSE
## NewLeagueN
                   FALSE
                               FALSE
## 1 subsets of each size up to 19
## Selection Algorithm: forward
              AtBat Hits HmRun Runs RBI Walks Years CAtBat CHits CHmRun CRuns CRBI
##
                                                                                     "*"
## 1
     (1)
                                 11 11
                                                                                     "*"
## 2
     (1)
                     11 * 11
## 3
      (1)
                     "*"
                                 11 11
                                        11
                                                 11 11
                                                                                     "*"
                                 11 11
                                      11 11
                                                 11 11
                                                                                     "*"
## 4
      (1)
                     "*"
## 5
      (1)
              "*"
                                 11 11
                                                 11 11
                                                                      11 11
                                                                                     "*"
                                                 11 11
## 6
      (1)
              "*"
              "*"
                     "*"
                                                                                     "*"
## 7
      (1)
              "*"
                                                                                     "*"
## 8
      (1)
              "*"
                                 11 11
                                                 11 11
                     "*"
                                           11 😼 11
                                                                              11 🛂 11
                                                                                     "*"
## 9
      ( 1
          )
                                                        11 14 11
                     "*"
                          11 11
                                                                      11 11
              "*"
                                                                                     "*"
## 10 (1)
```

```
"*"
                       "*"
                             11 11
                                             11
                                                       11 11
                                                              "*"
                                                                       11 11
                                                                              11 11
                                                                                      "*"
                                                                                              "*"
## 13
        (1
             )
## 14
        (1)
               "*"
                       "*"
                             "*"
                                    "*"
                                               "*"
                                                       11 11
                                                              "*"
                                                                              11 11
                                                                                      "*"
                                                                                              "*"
        (1)
                       "*"
                             "*"
                                    "*"
                                               "*"
                                                              "*"
                                                                      "*"
                                                                                      "*"
                                                                                              "*"
##
   15
               "*"
               "*"
                       "*"
                             11 * 11
                                    "*"
                                               11 * 11
                                                              11 * 11
                                                                                      || *||
                                                                                              "*"
   16
        ( 1
                                          "*"
                                                                      11 * 11
##
             )
                                                       11 11
                       "*"
                             "*"
                                    "*"
                                          الباا الباا
                                                              الياا
                                                                      "*"
                                                                              11
                                                                                      الباا
                                                                                              "*"
## 17
        (1)
               "*"
                                          "*" "*"
                                                              "*"
                                                                      "*"
                                                                              11 11
                       "*"
                             "*"
                                    "*"
                                                       "*"
                                                                                      11 * 11
                                                                                              "*"
##
   18
        (1)
               "*"
                                          "*" "*"
                                                              "*"
                                                                      "*"
##
   19
        (1)
                       "*"
                             "*"
                                    "*"
                                                                              "*"
                                                                                      "*"
                                                                                              "*"
##
               CWalks LeagueN DivisionW PutOuts Assists Errors NewLeagueN
                                  11 11
                                              11 11
                                                        11 11
       (1)
## 1
                                  11 11
                                              11 11
                                                        11 11
                                                                  11 11
##
   2
       (1)
                                              "*"
       (1)
## 3
                        11 11
                                  "*"
                                              "*"
## 4
         1)
       (
                                              "*"
                                                        11 11
## 5
         1
                11 11
                        11 11
                                  "*"
       (
                                  "*"
                                              "*"
                                                        11 11
               11 11
                        11 11
##
   6
       (
         1)
##
   7
       (
         1
                "*"
                                  "*"
                                              "*"
                                                        11 11
                "*"
                        11 11
                                  "*"
                                              "*"
                                                        11 11
## 8
       (
         1)
                                  "*"
                                              "*"
                                                        11 11
##
   9
       (1)
                "*"
                                  "*"
                                              "*"
               "*"
                                                        "*"
## 10
        (1)
                                  11 * 11
                                              11 * 11
                                                        11 * 11
               "*"
## 11
        ( 1
                                  "*"
                                              "*"
                                                        || *||
## 12
        (1
               "*"
                        "*"
             )
                                                        "*"
                                                                 "*"
                                  "*"
                                              "*"
                        "*"
##
   13
        ( 1
             )
               "*"
                                  "*"
                                              "*"
                                                        "*"
                                                                 "*"
##
   14
        ( 1
             )
               "*"
                        "*"
## 15
        (1)
                        "*"
                                  "*"
                                              "*"
                                                        "*"
                                                                 "*"
                        "*"
                                  "*"
                                              "*"
                                                        "*"
                                                                 "*"
                                                                          11 11
## 16
        (1)
               "*"
               "*"
                        "*"
                                  "*"
                                              "*"
                                                        "*"
                                                                 "*"
                                                                          "*"
## 17
        (1)
                        "*"
                                  "*"
                                              "*"
                                                        "*"
                                                                 "*"
                                                                          "*"
        ( 1
             )
               "*"
## 18
                                  "*"
                                              "*"
                                                        "*"
                                                                          "*"
        (1)"*"
                        11 😼 11
                                                                 11 11
## 19
regfit.bwd = regsubsets(Salary~., data=Hitters, nvmax=19, method="backward")
summary(regfit.bwd)
## Subset selection object
## Call: regsubsets.formula(Salary ~ ., data = Hitters, nvmax = 19, method = "backward")
## 19 Variables (and intercept)
                Forced in Forced out
##
## AtBat
                     FALSE
                                   FALSE
## Hits
                     FALSE
                                   FALSE
## HmRun
                                   FALSE
                     FALSE
## Runs
                     FALSE
                                   FALSE
## RBI
                     FALSE
                                   FALSE
## Walks
                     FALSE
                                   FALSE
## Years
                     FALSE
                                   FALSE
## CAtBat
                                   FALSE
                     FALSE
## CHits
                     FALSE
                                   FALSE
## CHmRun
                     FALSE
                                   FALSE
```

"*"

"*"

11

12

(1)"*"

(1)

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11 11

11 11

11 II II * II

"*"

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11 11

11 11

"*"

"*"

11 11

11 11

11 11

11 11

"*"

"*"

"*"

"*"

```
## CRBI
                        FALSE
                                       FALSE
                                       FALSE
## CWalks
                        FALSE
## LeagueN
                        FALSE
                                       FALSE
## DivisionW
                                       FALSE
                        FALSE
## PutOuts
                        FALSE
                                       FALSE
## Assists
                        FALSE
                                       FALSE
##
   Errors
                        FALSE
                                       FALSE
   NewLeagueN
                        FALSE
                                       FALSE
    1 subsets of each size up to 19
   Selection Algorithm: backward
##
                 AtBat Hits HmRun Runs RBI Walks Years CAtBat CHits CHmRun CRuns CRBI
                                                                                                 "*"
        (1)
## 1
   2
                  11 11
                          "*"
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                                                                                                         11
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##
        (1)
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                                                                                                 "*"
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                                                                                                           11
##
        (1)
                  "*"
##
   5
        ( 1
                  "*"
                          "*"
                                 11 11
                                         11 11
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                                                  11
                                                     "*"
                                                             11 11
                                                                     11 11
                                                                                 11
                                                                                       11 11
                                                                                                 "*"
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                  "*"
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                                 11 11
                                         11 11
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                                                  11
                                                     "*"
                                                             11 11
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                                                                               11
                                                                                 - 11
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                                                                                                 "*"
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##
   6
        (
          1)
##
                          "*"
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                                                  11
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                                                                                 11
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        (1)
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                                                                                                 "*"
                                         11
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                          "*"
                                                     "*"
                                                                                                 "*"
                                                                                                         "*"
##
   8
        (
          1)
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                                                     11 * 11
                                                             11
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                                                                     11 * 11
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##
   9
          1)
                  "*"
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                                                                                                         "*"
                                 11 11
                                         11 11
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                                                                                       11 11
##
         (1)
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   10
                 "*"
                                 11 11
                                                  11
                                                                                       11 11
                          "*"
                                         11 11
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                                                             11 11
                                                                     "*"
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##
   11
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                                                11
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                                                             11 11
                                                                                       11 11
                                                                                                         "*"
##
   12
         (1
                 "*"
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                                         "*"
                                                     "*"
                                                                     "*"
                                                                               11
                                                                                 - 11
                                                                                                 11 * 11
##
   13
         (1)
                          "*"
                                 11 11
                                         "*"
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                                                  11
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                                                             11 11
                                                                     "*"
                                                                               11 11
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                                                                                                 "*"
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                                         "*"
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                                                                     "*"
                                                                               11 11
                                                                                       11 11
                                                                                                 "*"
                                                                                                         "*"
##
   14
         ( 1
              )
                 "*"
                 "*"
                          "*"
                                 "*"
                                         "*"
                                                     "*"
                                                             11 11
                                                                     "*"
                                                                               "*"
                                                                                       11
                                                                                                 "*"
                                                                                                         "*"
##
   15
         ( 1
              )
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                                 "*"
                                         "*"
                                                "*"
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                                                                     "*"
                                                                                                 "*"
                                                                                                         "*"
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##
   16
                                                    "*"
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                                                                                                 11 🛂 11
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   17
         (1)
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                                                "*"
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                                                                                       11 11
                                                                                                         "*"
##
   18
         ( 1
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                          "*"
                                 "*"
                                                "*" "*"
                                                                     "*"
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                                                                                                 "*"
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                          "*"
                                 "*"
                                         "*"
                                                "*" "*"
                                                             "*"
                                                                     "*"
                                                                               "*"
                                                                                       "*"
                                                                                                 "*"
                                                                                                         "*"
##
   19
         (1)
##
                 CWalks LeagueN DivisionW PutOuts Assists Errors NewLeagueN
                           11 11
                  11 11
                                      11 11
                                                   11 11
                                                              11 11
                                                                         11 11
## 1
        (1)
                  11 11
                                      11 11
                                                   11 11
                                                               11 11
##
   2
        (1)
                                        11
                                                   "*"
                                                                 11
##
   3
        (1)
                  11 11
                           11
                                                   "*"
        (1)
##
   4
                  11 11
                           11
                                      11 11
                                                   "*"
                                                               11 11
##
   5
        (1)
                  11 11
                                                   "*"
##
   6
        (
          1
                           11
                                      "*"
                                      "*"
                                                   "*"
                                                               11 11
##
   7
        (
          1)
                  "*"
                           11
                             11
##
   8
        (1)
                  "*"
                           11 11
                                      "*"
                                                   "*"
                                                               11 11
                                                                         11 11
                  "*"
                           11 11
                                      "*"
                                                   "*"
                                                               11 11
                                                                         11 11
                                                                                   11
##
   9
        (1)
                                                   "*"
                                                               "*"
##
         (1)
                 "*"
                                      "*"
   10
## 11
         (1)
                 "*"
                           "*"
                                      "*"
                                                   "*"
                                                               "*"
                                                   "*"
                                                               "*"
                 "*"
                           "*"
                                      "*"
##
   12
         ( 1
               )
                 "*"
                           11 😼 11
                                      "*"
                                                   "*"
                                                               "*"
                                                                         "*"
##
   13
         ( 1
               )
                           "*"
                                      "*"
                                                   "*"
                                                               "*"
                                                                         "*"
##
   14
         (1
                 "*"
                                                    "*"
                                                               "*"
##
   15
         ( 1
              )
                 "*"
                           "*"
                                      "*"
                                                                         "*"
                                                                                   11
## 16
         ( 1
              )
                           "*"
                                      "*"
                                                   "*"
                                                               "*"
                                                                         "*"
                                                                                   11 11
```

CRuns

FALSE

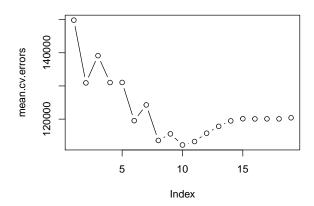
FALSE

```
"*"
                                                               "*"
                            "*"
                                       "*"
                                                       "*"
## 17 ( 1 ) "*"
                                                               "*"
## 18 (1) "*"
                    "*"
                            "*"
                                       "*"
                                               "*"
                                                       "*"
                                                       "*"
## 19 (1) "*"
                            "*"
                                       "*"
                                               "*"
                                                               "*"
```

6.5.3 Choosing Among Models Using the Validation Set Approach and Cross-Validation

```
set.seed(1)
train = sample(c(TRUE,FALSE), nrow(Hitters), rep=TRUE)
test=(!train)
regfit.best = regsubsets(Salary~., data=Hitters[train, ], nvmax=19)
test.mat = model.matrix(Salary~., data=Hitters[test, ])
val.errors = rep(NA, 19)
for(i in 1:19){
  coefi = coef(regfit.best, id=i)
  pred = test.mat[, names(coefi)] %*% coefi
  val.errors[i] = mean((Hitters$Salary[test] - pred)^2)
}
val.errors
## [1] 164377.3 144405.5 152175.7 145198.4 137902.1 139175.7 126849.0 136191.4
## [9] 132889.6 135434.9 136963.3 140694.9 140690.9 141951.2 141508.2 142164.4
## [17] 141767.4 142339.6 142238.2
which.min(val.errors)
## [1] 7
coef(regfit.best, 7)
                       AtBat
                                                               CRuns
                                                                           CWalks
##
  (Intercept)
                                     Hits
                                                  Walks
     67.1085369
                  -2.1462987
                                7.0149547
                                             8.0716640
                                                                       -0.8337844
##
                                                           1.2425113
      DivisionW
                     PutOuts
## -118.4364998
                   0.2526925
predict.regsubsets = function(object, newdata, id, ...){
  form = as.formula(object$call[[2]])
  mat = model.matrix(form, newdata)
  coefi = coef(object, id=id)
  xvars = names(coefi)
  mat[, xvars] %*% coefi
}
```

```
regfit.best = regsubsets(Salary~., data=Hitters, nvmax=19)
coef(regfit.best, 7)
## (Intercept)
                        Hits
                                    Walks
                                                CAtBat
                                                              CHits
                                                                          CHmRun
##
    79.4509472
                   1.2833513
                                3.2274264 -0.3752350 1.4957073
                                                                       1.4420538
     DivisionW
                    PutOuts
##
## -129.9866432
                   0.2366813
k = 10
set.seed(1)
folds = sample(1:k, nrow(Hitters), rep=TRUE)
cv.errors = matrix(NA, k, 19, dimnames=list(NULL, paste(1:19)))
for(j in 1:k){
 best.fit = regsubsets(Salary~., data=Hitters[folds != j, ], nvmax=19)
 for (i in 1:19){
   pred = predict.regsubsets(best.fit, Hitters[folds == j, ], id=i)
    # pred = predict(best.fit, Hitters[folds == j, ], id=i) ???
    cv.errors[j,i] = mean((Hitters$Salary[folds == j] - pred)^2)
  }
}
mean.cv.errors = apply(cv.errors, 2, mean)
mean.cv.errors
                   2
                                              5
## 149821.1 130922.0 139127.0 131028.8 131050.2 119538.6 124286.1 113580.0
                                    12
                  10
                           11
                                             13
                                                      14
## 115556.5 112216.7 113251.2 115755.9 117820.8 119481.2 120121.6 120074.3
         17
                  18
## 120084.8 120085.8 120403.5
plot(mean.cv.errors, type="b")
```



```
reg.best = regsubsets(Salary~., data=Hitters, nvmax=19)
coef(reg.best, 10)
```

```
##
    (Intercept)
                        AtBat
                                      Hits
                                                   Walks
                                                               CAtBat
                                                                              CRuns
    162.5354420
                  -2.1686501
                                 6.9180175
                                               5.7732246
                                                           -0.1300798
                                                                          1.4082490
##
##
           CRBI
                       CWalks
                                 DivisionW
                                                 PutOuts
                                                               Assists
      0.7743122
                  -0.8308264 -112.3800575
                                               0.2973726
                                                            0.2831680
##
```

6.6 Lab 2: Ridge Regression and the Lasso

```
x = model.matrix(Salary~., Hitters)[, -1]
y = Hitters$Salary
```

6.6.1 Ridge Regression

```
library(glmnet)
grid = 10^seq(10, -2, length=100)
ridge.mod = glmnet(x, y, alpha=0, lambda=grid)

dim(coef(ridge.mod))

## [1] 20 100
```

```
## [1] 11497.57
```

ridge.mod\$lambda[50]

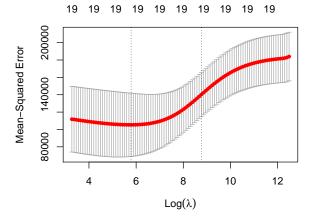
```
coef(ridge.mod)[, 50]
##
     (Intercept)
                          AtBat
                                          Hits
                                                        HmRun
                                                                        Runs
## 407.356050200
                    0.036957182
                                   0.138180344
                                                 0.524629976
                                                                0.230701523
##
             RBI
                          Walks
                                         Years
                                                       CAtBat
                                                                       CHits
     0.239841459
                    0.289618741
                                   1.107702929
                                                                0.011653637
##
                                                 0.003131815
##
          CHmRun
                                          CRBI
                                                       CWalks
                                                                    LeagueN
                          CRuns
     0.087545670
                    0.023379882
                                                                0.085028114
##
                                   0.024138320
                                                 0.025015421
##
       DivisionW
                        PutOuts
                                       Assists
                                                       Errors
                                                                 NewLeagueN
    -6.215440973
                    0.016482577
                                   0.002612988
                                                -0.020502690
                                                                0.301433531
##
sqrt(sum(coef(ridge.mod)[-1, 50]^2))
## [1] 6.360612
ridge.mod$lambda[60]
## [1] 705.4802
coef(ridge.mod)[, 60]
##
    (Intercept)
                        AtBat
                                       Hits
                                                   HmRun
                                                                  Runs
                                                                                 RBI
##
    54.32519950
                   0.11211115
                                0.65622409
                                              1.17980910
                                                            0.93769713
                                                                          0.84718546
##
          Walks
                        Years
                                     CAtBat
                                                    CHits
                                                                CHmRun
                                                                               CRuns
     1.31987948
                   2.59640425
                                                            0.33777318
                                                                          0.09355528
##
                                0.01083413
                                              0.04674557
##
           CRBI
                       CWalks
                                    LeagueN
                                               DivisionW
                                                               PutOuts
                                                                             Assists
     0.09780402
                               13.68370191 -54.65877750
##
                   0.07189612
                                                            0.11852289
                                                                          0.01606037
##
         Errors
                   NewLeagueN
    -0.70358655
                   8.61181213
sqrt(sum(coef(ridge.mod)[-1, 60]^2))
## [1] 57.11001
predict(ridge.mod, s=50, type="coefficients")[1:20, ]
##
     (Intercept)
                          AtBat
                                          Hits
                                                        HmRun
                                                                       Runs
    4.876610e+01 -3.580999e-01
                                 1.969359e+00 -1.278248e+00
                                                               1.145892e+00
##
##
             R.B.T
                                                                       CHits
                          Walks
                                         Years
                                                       CAtBat
    8.038292e-01
                  2.716186e+00 -6.218319e+00
                                                               1.064895e-01
##
                                                5.447837e-03
##
          CHmRun
                          CRuns
                                          CRBI
                                                       CWalks
                                                                     LeagueN
##
    6.244860e-01
                  2.214985e-01
                                 2.186914e-01 -1.500245e-01
                                                               4.592589e+01
                        PutOuts
       DivisionW
                                       Assists
                                                       Errors
                                                                 NewLeagueN
## -1.182011e+02 2.502322e-01
                                1.215665e-01 -3.278600e+00 -9.496680e+00
```

```
set.seed(1)
train = sample(1:nrow(x), nrow(x)/2)
test = (-train)
y.test = y[test]
ridge.mod = glmnet(x[train, ], y[train], alpha=0, lambda=grid, thres=1e-12)
ridge.pred = predict(ridge.mod, s=4, newx=x[test, ])
mean((ridge.pred - y.test)^2)
## [1] 142199.2
mean((mean(y[train]) - y.test)^2)
## [1] 224669.9
ridge.pred = predict(ridge.mod, s=1e10, newx=x[test, ])
mean((ridge.pred - y.test)^2)
## [1] 224669.8
ridge.pred = predict(ridge.mod, s=0, newx=x[test, ])
mean((ridge.pred - y.test)^2)
## [1] 167789.8
lm(y~x, subset=train)
##
## Call:
## lm(formula = y ~ x, subset = train)
## Coefficients:
## (Intercept)
                     xAtBat
                                    xHits
                                                xHmRun
                                                              xRuns
                                                                             xRBI
                    -0.3521
                                                5.8145
                                                             1.5424
                                                                           1.1243
##
      274.0145
                                  -1.6377
##
                     xYears
                                  xCAtBat
                                                xCHits
                                                            xCHmRun
        xWalks
                                                                          xCRuns
                                  -0.6412
##
        3.7287
                   -16.3773
                                                3.1632
                                                             3.4008
                                                                         -0.9739
                    xCWalks
                                           xDivisionW
                                                           xPutOuts
                                                                        xAssists
##
         xCRBI
                                xLeagueN
##
       -0.6005
                     0.3379
                                 119.1486
                                            -144.0831
                                                             0.1976
                                                                          0.6804
##
       xErrors xNewLeagueN
       -4.7128
                   -71.0951
##
```

```
predict(ridge.mod, s=0, type="coefficients")[1:20, ]
```

```
(Intercept)
##
                        AtBat
                                       Hits
                                                    HmRun
                                                                   Runs
                                                                                 RBI
    274.2089049
##
                   -0.3699455
                                 -1.5370022
                                               5.9129307
                                                             1.4811980
                                                                           1.0772844
##
          Walks
                        Years
                                     CAtBat
                                                    CHits
                                                                CHmRun
                                                                               CRuns
##
      3.7577989
                 -16.5600387
                                 -0.6313336
                                               3.1115575
                                                             3.3297885
                                                                          -0.9496641
##
           CRBI
                       CWalks
                                    LeagueN
                                               DivisionW
                                                               PutOuts
                                                                             Assists
                    0.3300136
##
     -0.5694414
                               118.4000592 -144.2867510
                                                             0.1971770
                                                                           0.6775088
##
         Errors
                   NewLeagueN
     -4.6833775
                 -70.1616132
##
```

```
set.seed(1)
cv.out = cv.glmnet(x[train, ], y[train], alpha=0)
plot(cv.out)
```



```
bestlam = cv.out$lambda.min
bestlam
```

```
## [1] 326.0828
```

```
ridge.pred = predict(ridge.mod, s=bestlam, newx=x[test, ])
mean((ridge.pred - y.test)^2)
```

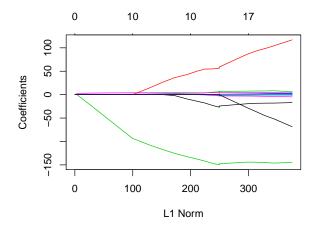
```
## [1] 139856.6
```

```
out = glmnet(x, y, alpha=0)
predict(out, type="coefficients", s=bestlam)[1:20, ]
```

```
(Intercept)
                        AtBat
                                      Hits
                                                   HmRun
                                                                                RBI
##
                                                                  Runs
                  0.07715547
                                0.85911581
                                                           1.06369007
                                                                         0.87936105
##
    15.44383135
                                              0.60103107
##
          Walks
                        Years
                                    CAtBat
                                                   CHits
                                                                CHmRun
                                                                              CRuns
##
     1.62444616
                   1.35254780
                                0.01134999
                                              0.05746654
                                                           0.40680157
                                                                         0.11456224
           CRBI
                       CWalks
                                   LeagueN
                                                              PutOuts
##
                                               DivisionW
                                                                            Assists
     0.12116504
                  0.05299202
                               22.09143189 -79.04032637
##
                                                           0.16619903
                                                                         0.02941950
                  NewLeagueN
##
         Errors
    -1.36092945
                  9.12487767
```

6.6.2 The Lasso

```
lasso.mod = glmnet(x[train, ], y[train], alpha=1, lambda=grid)
plot(lasso.mod)
```



```
set.seed(1)
cv.out = cv.glmnet(x[train, ], y[train], alpha=1)
plot(cv.out)
```

Mean-Sdnared Error 19 19 19 16 17 13 11 10 8 4 3 -4 -2 0 2 4 Log(λ)

```
bestlam = cv.out$lambda.min
lasso.pred = predict(lasso.mod, s=bestlam, newx=x[test, ])
mean((lasso.pred - y.test)^2)
```

[1] 143673.6

```
out = glmnet(x, y, alpha=1, lambda=grid)
lasso.coef = predict(out, type="coefficients", s=bestlam)[1:20, ]
lasso.coef
```

##	(Intercept)	AtBat	Hits	HmRun	Runs
##	1.27479059	-0.05497143	2.18034583	0.00000000	0.00000000
##	RBI	Walks	Years	\mathtt{CAtBat}	CHits
##	0.00000000	2.29192406	-0.33806109	0.00000000	0.00000000
##	CHmRun	CRuns	CRBI	CWalks	LeagueN
##	0.02825013	0.21628385	0.41712537	0.00000000	20.28615023
##	DivisionW	PutOuts	Assists	Errors	NewLeagueN
##	-116.16755870	0.23752385	0.00000000	-0.85629148	0.00000000

lasso.coef[lasso.coef != 0]

##	(Intercept)	AtBat	Hits	Walks	Years
##	1.27479059	-0.05497143	2.18034583	2.29192406	-0.33806109
##	$\tt CHmRun$	CRuns	CRBI	LeagueN	DivisionW
##	0.02825013	0.21628385	0.41712537	20.28615023	-116.16755870
##	PutOuts	Errors			
##	0.23752385	-0.85629148			