

Basic Principles of Financial Valuation Discounting

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Based on lecture materials from J. Weston, Rice University

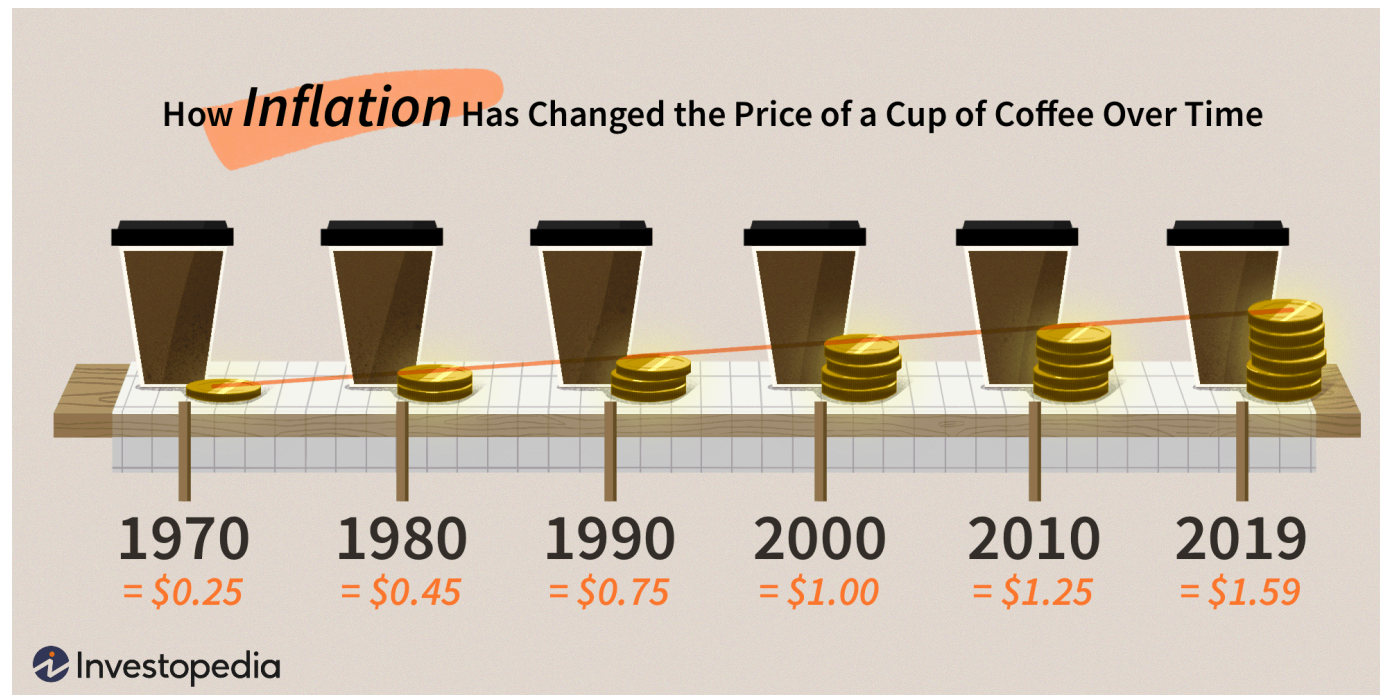
Money Now VS Later

- Money now:
 - allows me to invest in assets like stocks, bonds, real estate
 - allows me to pay my debt, to go out party etc.
- Money later
 - I need to be compensated for these lost opportunities to invest and spend
 - Things get expensive overtime
 - I may not be here or you may go broke

Time Value of Money: Opportunity Cost

- Opportunity cost represents the potential benefits an individual, investor, or business misses out on when choosing one alternative over another
 - One alternative: money now
 - The other alternative: money later
- I need to get more if you want me to be patient and give up all the opportunities to spend and invest now

Time Value for Money: Inflation



- Over time, prices tend to rise and money become less valuable over time
- If you want to give me money later, there has to be a little extra to account for the fact that the money will not buy as much in the future

Time Value of Money: Risk

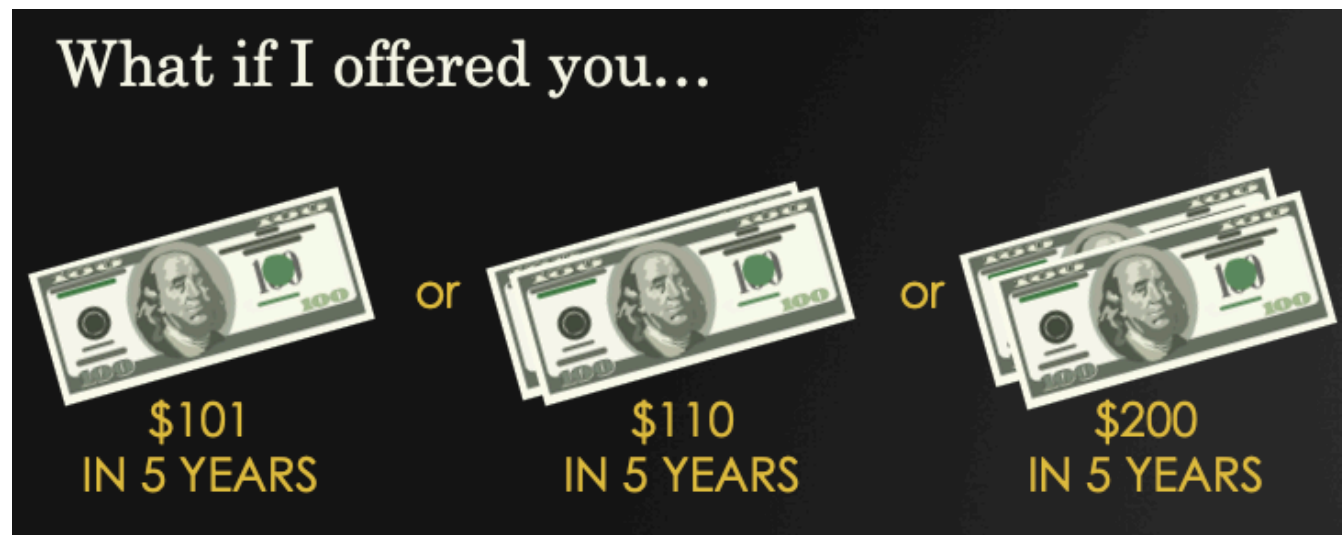
- No one knows what will happen tomorrow!
- I am at risk for being patient as things can change in the future for the worse
- Hence, greater risk needs to be accommodated with more compensation

Time Value of Money: Risk

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Interest Rate

- If I am willing to wait and get money later, how much does this worth?
- Instead of getting \$100 now:



- At some point, you will accept and we have put a price on time
- That price is the interest rate, and it incorporates opportunity costs, inflation expectations, and risk.

Interest rate = what you charge to wait

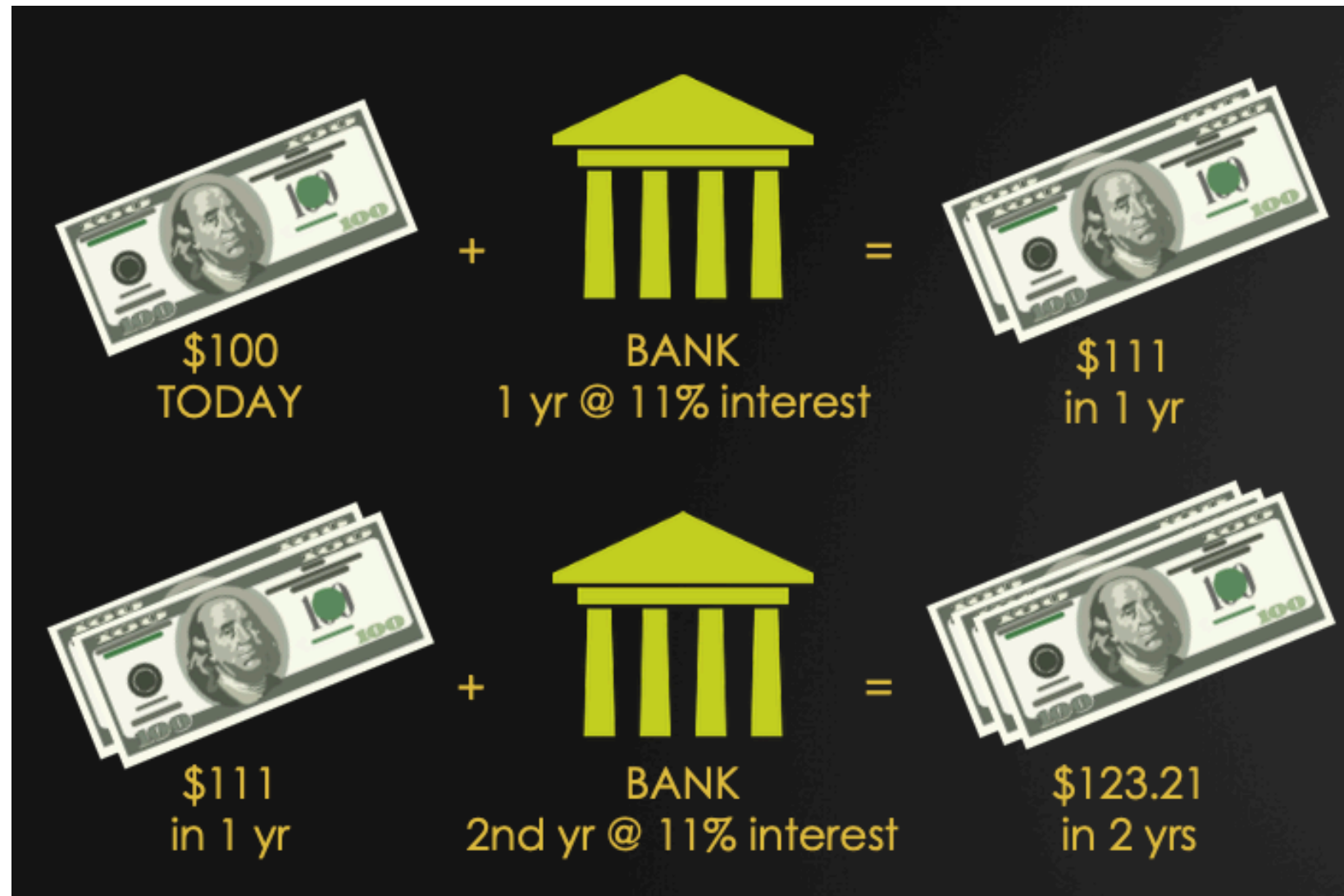
Changes in Real World Interest Rates

- Changes in opportunity costs
 - Better economic growth
- Changes in inflation expectations
 - Government prints more money
- Changes in risk
 - Wars, disasters, etc...

Interest Rates in the Economy

- The most important price in the economy
- The price of time
- The basis for all other prices

Compounding



- In the second year, you earn interest on the interest you earned in the first year - that is **compound interest**

FUTURE VALUE: MONEY IN THE BANK

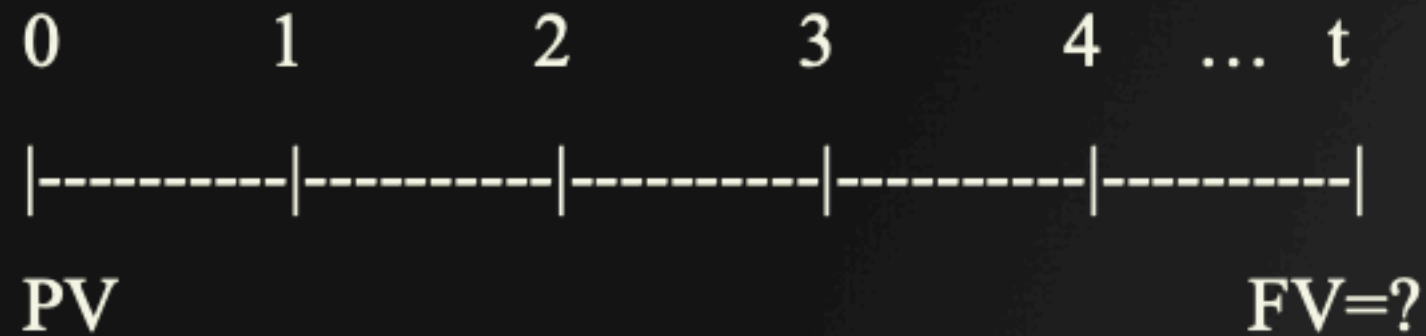
Interest rate = 11%

\$1,000 in bank for 5 years

Year	Amount
0	\$1,000
1	$\$1,110 = \$1,000 + \$1,000 * 11\% = \$1,000 * (1+11\%)$
2	$\$1,232 = \$1,110 * (1+11\%) = \$1,000 * (1+11\%)^2$
3	$\$1,368 = \$1,232 * (1+11\%) = \$1,000 * (1+11\%)^3$
4	$\$1,518 = \$1,368 * (1+11\%) = \$1,000 * (1+11\%)^4$
5	$\$1,685 = \$1,518 * (1+11\%) = \$1,000 * (1+11\%)^5$

\$1,685

FUTURE VALUE



$$FV = PV(1+r)^t$$

FV = Future Value

PV = Present Value

r = interest rate

t = time

In-class Exercises

- Suppose you put \$500 into a savings account today that will pay 8% interest for five years. How much will you have at the end of five years?
- What if I bought a painting for \$700 and then 3 years later sold it for \$825. How much did I earn on the painting on an annual basis?

Effective vs Nominal Rates

- Nominal = periodic rate times the number of periods
- Effective = compounded rate
- Example: monthly compounding
 - Nominal interest rate 6% per year (a.k.a 6% APR)
 - That is $6\% / 12 = 0.5\%$ per month
 - Effective rate = $(1 + 0.5\%)^{12} = 1.0617$ or 6.17%

EFFECTIVE VS. NOMINAL RATES

Generally:

$$R_{\text{effective}} = \left(1 + \frac{R_{\text{nominal}}}{n} \right)^n$$

The effective rate $>$ nominal

Bringing the Future into the Present

$$FV = PV(1+r)^t$$

$$PV = \frac{FV}{(1+r)^t}$$

Present Value

- If I offered you \$175 payable 5 years from now, how much would you pay for that offer today if interest rates were 4%?

Today					5 years from now
0	1	2	3	4	5
$\$175/(1+4\%)^5$	$\$175/(1+4\%)^4$	$\$175/(1+4\%)^3$	$\$175/(1+4\%)^2$	$\$175/(1+4\%)^1$	
\$ 143.84	\$ 149.59	\$ 155.57	\$ 161.80	\$ 168.27	\$ 175.00

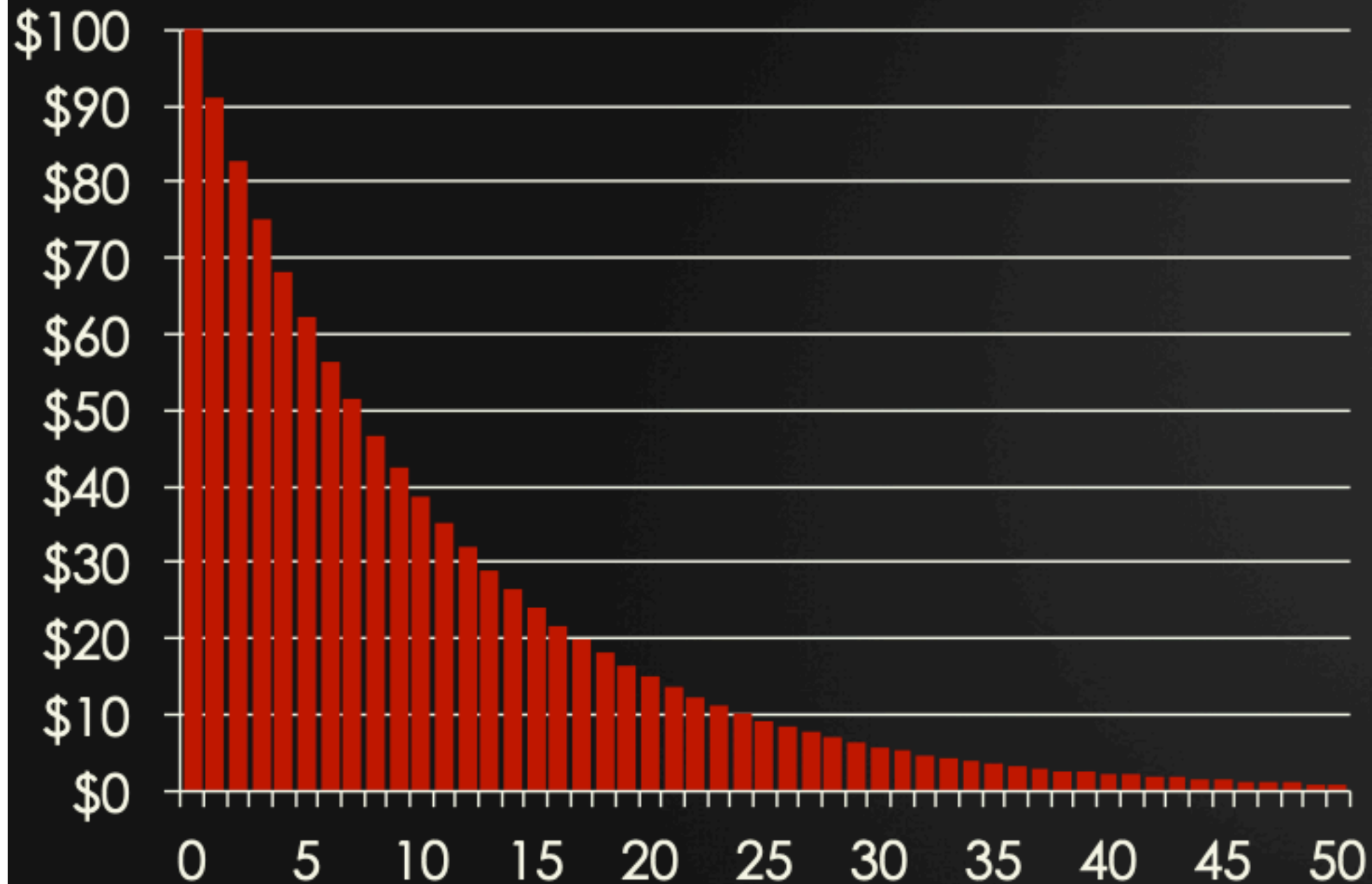
ANSWER: \$143.84

Present Value

- How much FV is discounted back to PV depends on:
 - How far out is the cash
 - How big is the interest rate

PRESENT VALUE

\$100 discounted at 10%



Discounted Cash Flows (DCF)

- Method of valuing an investment
- Uses all anticipated future cash flows
- Discounts all cash flows back to present value

Valuation by DCF

- Why do investors buy different assets?
 - Real estate, stocks, or bonds
- Because they want to earn a return and use the money later

What Gives an Investment Value

- How much cash is coming in?
- When is the cash coming in?
- With these two answers, we can put value on anything

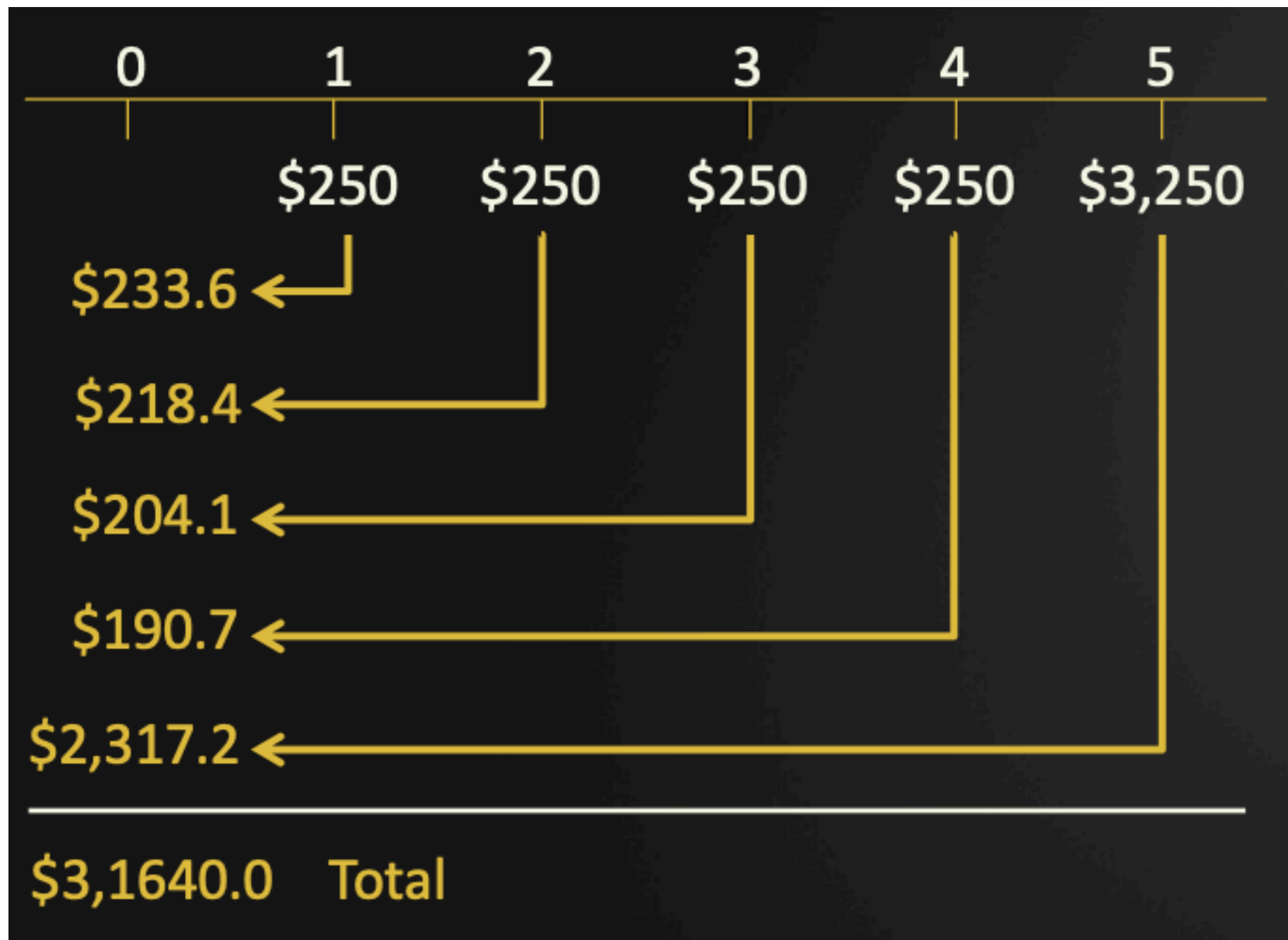
Bond

- Contract between an issuer and a bondholder
- Buyer of bond lends money (principal) to issuer
- Issuer pays interest on loan and repays principal at maturity

DCF: Simple Bond

- Consider a simple bond of \$3,000 that makes annual payments of \$250 for 5 years if the discount rate is 7%
- What is it worth?
 - Step 1: What are the cash flows
 - Step 2: What are they worth today
 - Step 3: Add up the present values

DCF: Simple Bond



DCF: Simple Bond

- In our example the bond is worth \$3,164
- That is how much money the bond would raise if sold today
- There is no reason anyone would pay more or less

DCF: Stock Valuation

- How much should a share of Bangkok Bank worth?
- Cash to Shareholders? When?
- Model both of these and DCF
- This is partly what stock analysts do

DCF: Other Assets

- Apply the principle to any asset:
 - Real Estate
 - Mergers and Acquisitions
 - Derivatives
- Cash and timing drive all valuation

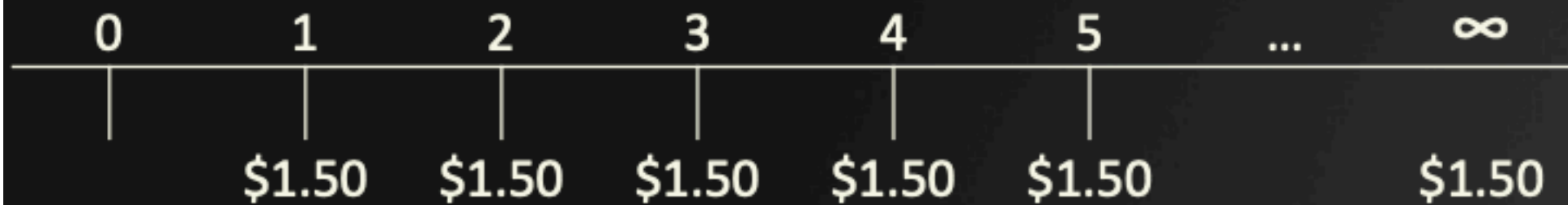
DCF: Practical Example

- A water well in the desert
 - If the well is dry, it does not worth anything
 - If it is connected to an active source of water, it is worth something
 - How much is it worth to sell or acquire?

DCF: Practical Example

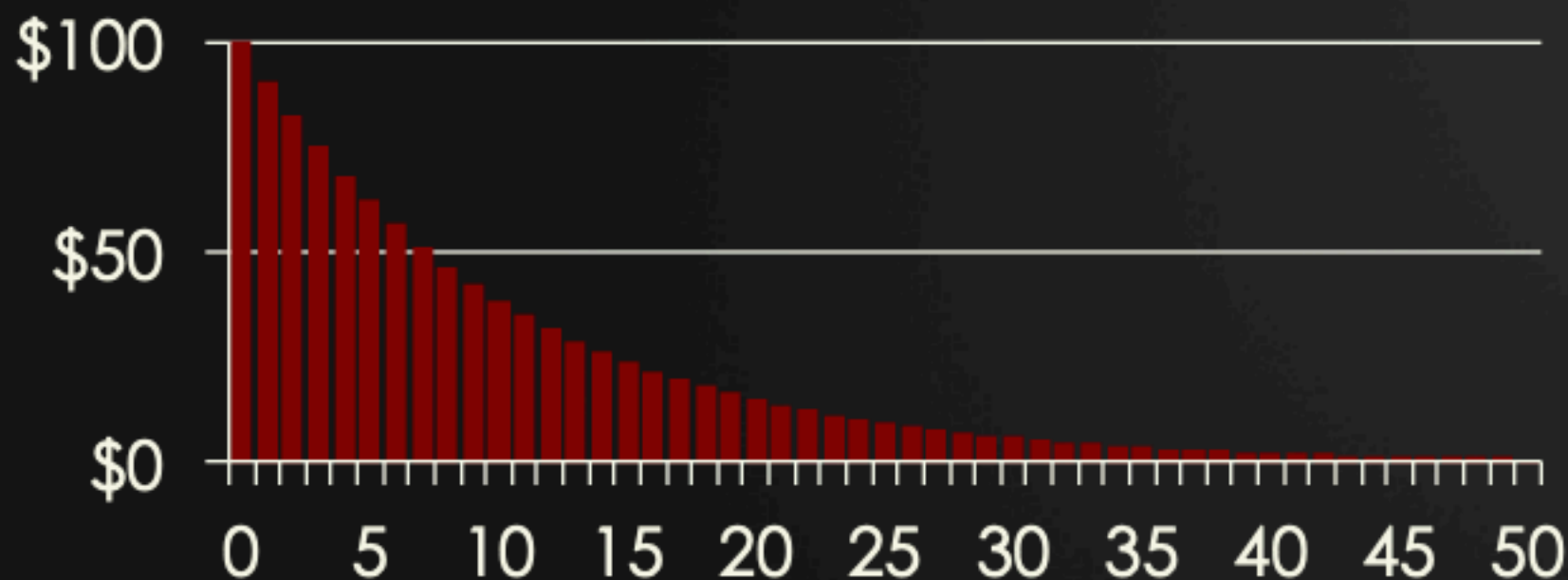
- How much water is there?
 - Let's say infinite
- How much does it produce?
 - 1 gallon/day
- How much cash flow?
 - Net \$1.50/day
- Can we put a realistic price on this asset?

DCF PRACTICAL EXAMPLE: WATER WELL



Problem: Is it worth infinity?

Remember:



DCF: Practical Example

- Discount rate: 15%
- Build a spreadsheet model
 - Step 1: What are the cash flows
 - Step 2: What are they worth today
 - Step 3: Add up the present values

Valuation by Comparables

- Practitioners often refer to “comps”
- Comparable transactions or prices
- Quick, easy, and dangerous!

Assumptions for Comps

- 1. You can identify close comparables
- 2. You have a value–relevant ratio
- 3. The market values comps similarly

Comparables in Use

- $(\text{Price} / \text{Attribute}) * \text{Your Attribute} = \text{Price of your asset}$
- Examples of attributes:
 - P/E ratios
 - Earnings Yield
 - Dividend Yield
 - Return on Assets
 - EBITDA multiples

P/E Ratios

- Price-to-earnings ratio is popular
- How much a dollar of current earnings costs?
 - “Trades at X times earnings”

P/E RATIOS: EXAMPLE

Value Lowes Corporation by comps

	Home Depot	Lowes
E (earnings)	\$6.80	\$2.46
P/E	25	--
Comp value	--	\$61.60

$$\begin{aligned}\text{Comp value of Lowes} &= P/E_{\text{Home Depot}} * E_{\text{Lowes}} \\ &= 25 * \$2.46 = \$61.60\end{aligned}$$

Lowes actual price in the market = \$74 (about 20% different)

Other Comps

- Return on Assets or Equity (ROA/ROE)
- Return on invested capital (ROI)
- Dividend yield
- PEG ratio (P/E ratio over Growth in E)

Measuring Comps

- Comps rely on historical averages
- Trailing 12m, most recent Q, past 3 years...?
- Negative earnings, negative prices?

Comps VS DCF

- Both can provide useful information
- Executed correctly, both are valid
- Comps often used (and abused) in practice
- Both require forecasts
- DCF is more appealing in theory and more accurate, but requires much more work
- Comps can be a good quick-and-dirty valuation, but be careful!

Examples and Applications: Bonds

- Simple debt instruments
- Promise coupons (interest) and face value
- U.S. treasury bonds, corporate bonds, municipals, sovereign debt
 - Different risks associated with each type of bonds
- Valuation: what cash and when

Treasury Bond Example

- Treasury issues 3 year bonds with a 2.5% coupon rate. If the six month interest rate is 1.2%, what is the price of the bond per \$100 of face value?

Examples and Applications: Mortgages

- Simple debt instrument
- Borrow money today to purchase real estate
- Each payment includes principal and interest
- Amortization schedule

Mortgage Example

- Assume a bank charges 7% interest per year. You borrow \$10,000 to be repaid in equal yearly installments of \$3,810.52 over 3 years. Let's amortize the loan schedule and compute interest and principle repayments.

Examples and Applications: Annuities

- Series of equal payments at regular intervals
 - Regular deposits to savings account
 - Monthly mortgage payments
 - Insurance premiums
 - Pension payments

Retirement Annuity Example

- You want to retire and maintain a monthly income of \$2,500 for the next 20 years. How much would it cost to purchase this annuity if discount rates are currently 4%?

USING COMPOUNDING AND DISCOUNTING TO MAKE DECISIONS

You have a choice between three options:

1. Take \$1,000 in cash now
2. Receive \$2,000 at the end of three years
3. Wait 10 years to receive \$3,000

Which is best choice if discount rate is 10%?

How does the answer change if $r = 5\%$?

What We Have Learned

- Time value of money
 - Opportunity cost, inflation, and risk
- Interest rates
- Compounding and discounting
- Valuation by Discounted Cash Flow (DCF)
- Valuation by Comparables
- Applications in bonds, mortgages, etc.