

Q: Find an eqⁿ for the line tangent to the curve at the point - defined by the given value of t . Also find the value of $\frac{dy}{dx}$ at this point.

- 1) $x = 2 \cos t$, $y = 2 \sin t$, $t = \pi/4$
- 2) $x = \sin 2\pi t$, $y = \cos 2\pi t$, $t = -1/6$
- 3) $x = 4 \sin t$, $y = 2 \cos t$, $t = \pi/4$
- 4) $x = \cos t$, $y = \sqrt{3} \cos t$, $t = 2\pi/3$
- 5) $x = t$, $y = \sqrt{t}$, $t = 1/4$
- 6) $x = \sec^2 t - 1$, $y = t \tan t$, $t = -\pi/4$
- 7) $x = \sec t$, $y = t \tan t$, $t = \pi/6$
- 8) $x = -\sqrt{t+1}$, $y = \sqrt{3t}$, $t = 3$
- 9) $x = 2t^2 + 3$, $y = t^4$, $t = -1$
- 10) $x = 1/t$, $y = -2 + \ln t$, $t = 1$
- 11) $x = t - \sin t$, $y = 1 - \cos t$, $t = \pi/3$
- 12) $x = \cos t$, $y = 1 + \sin t$, $t = \pi/2$
- 13) $x = \frac{1}{t+1}$, $y = \frac{t}{t-1}$, $t = 2$
- 14) $x = 1 + e^t$, $y = 1 - e^t$, $t = 0$

- 15) $x = 2 \cos t$, $y = 3 \sin t$, $t = \pi/2$
- 16) $x = \sin 2\pi t$, $y = \cos 2\pi t$, $t = 2$
- 17) $x = 4 \sin t$, $y = 6 \cos t$, $t = \pi/6$
- 18) $x = 2 \cos t$, $y = \sqrt{2} \cos t$, $t = 2\pi/3$
- 19) $x = 2 \cos t$, $y = 4 \sin t$, $t = \pi/3$
- 20) $x = t^2$, $y = \sqrt{t}$, $t = 2$
- 21) $x = 3t^3 + t$, $y = t^2$, $t = 1$
- 22) $x = 5 \sin t$, $y = 2 \cos t$, $t = \pi/4$
- 23) $x = 3t^4 + t^2$, $y = t^3$, $t = 2$
- 24) $x = 3t^2$, $y = t^4$, $t = 1$
- 25) $x = \cos t$, $y = 2 + \sin t$, $t = \pi/2$
- 26) $x = 2 \cos t$, $y = 3 \sin t$, $t = \pi/4$
- 27) $x = t$, $y = t^4$, $t = 1$
- 28) $x = 2$, $y = 2t$, $t = 0$

Q: Find the area;

29) enclosed by the y -axis and the curve $x = t - t^2$, $y = 1 + e^{-t}$.

30) enclosed by the ellipse $x = a \cos t$, $y = b \sin t$, $0 \leq t \leq 2\pi$.

Q: Find the area under $y = x^3$ over $[0, 1]$ using the following

31) $x = t^4$, $y = t^6$

32) $x = t^3$, $y = t^9$

Q: Find the length of the curves;

33) $x = \cos t$, $y = t + \sin t$, $0 \leq t \leq \pi$

34) $x = t^3$, $y = 3t^{5/2}$, $0 \leq t \leq \sqrt{3}$

35) $x = t^{3/2}$, $y = \frac{(2t+1)^{3/2}}{3}$, $0 \leq t \leq 4$

36) $x = \frac{(2t+3)^{3/2}}{3}$, $y = t + t^{3/2}$, $0 \leq t \leq 3$

37) $x = 8 \cos t + 8t \sin t$, $y = 8 \sin t - 8t \cos t$, $0 \leq t \leq \pi/2$

38) Q. Find the Surface Area of the Surface generated by revolving the curve about the indicated axis,

38) $x = \cos t$, $y = 2 + \sin t$, $0 \leq t \leq 2\pi$, x -axis.

39) $x = (2/3)t^{3/2}$, $y = 2\sqrt{t}$, $0 \leq t \leq 3$, y -axis.

40) $x = t + \sqrt{t}$, $y = (t^2/2) + \sqrt{2t}$, $-\sqrt{2} \leq t \leq \sqrt{2}$, y -axis.

Q. plot the following points. Then find all the polar coordinates of each point.

- 41) ~~41~~ $(3, \pi/4)$ 42) $(3, \pi/3)$ 43) $(-3, \pi/4)$, 44) $(4, \pi/2)$, 45) $(-\sqrt{2}, \pi/4)$
 46) $(-3, \pi/3)$ 47) $(2, \pi/2)$ 48) $(4, \pi)$, 49) $(5, \pi/3)$
 50) $(2, \pi/6)$ 51) $(-2, \pi/6)$ 52) $(1, \pi/4)$ 53) $(1, 0)$ 54) $(2, 2\pi/3)$
 55) $(1/2, \pi/3)$ 56) $(4, \pi/6)$ 57) $(-1/2, \pi/3)$ 58) $(-4, 2\pi/3)$ 59) $(2, \pi)$
 60) $(3, 2\pi/3)$ 61) $(3, \pi/2)$ 62) $(5, 2\pi/3)$ 63) $(1, 2\pi/3)$ 64) $(1, \pi/4)$
 65) $(4, 0)$ 66) $(\sqrt{3}, \pi/4)$ 67) $(\sqrt{3}, \pi/4)$ 68) $(2, 3\pi/2)$.

Q. Replace the polar equations with equivalent Cartesian equation.

The identify the graph. Graph the polar curve also

69) $r \cos \theta = 2$, 70) $r = -1 - \cos \theta$, 71) $r = 1/2 + \cos \theta$.

72) $r = 2 + \cos \theta$.

Also find the area of these regions.