

# Gradient Extrapolation for Debiased Representation Learning

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## Abstract

*Machine learning classification models trained with empirical risk minimization (ERM) often inadvertently rely on spurious correlations. When absent in the test data, these unintended associations between non-target attributes and target labels lead to poor generalization. This paper addresses this problem from a model optimization perspective and proposes a novel method, Gradient Extrapolation for Debiased Representation Learning (GERNE), designed to learn debiased representations in both known and unknown attribute training cases. GERNE uses two distinct batches with different amounts of spurious correlations and defines the target gradient as a linear extrapolation of the gradients computed from each batch’s loss. Our analysis shows that when the extrapolated gradient points toward the batch gradient with fewer spurious correlations, it effectively guides training toward learning a debiased model. GERNE serves as a general framework for debiasing, encompassing ERM and Resampling methods as special cases. We derive the theoretical upper and lower bounds of the extrapolation factor employed by GERNE. By tuning this factor, GERNE can adapt to maximize either Group-Balanced Accuracy (GBA) or Worst-Group Accuracy (WGA). We validate GERNE on five vision and one NLP benchmarks, demonstrating competitive and often superior performance compared to state-of-the-art baselines. The project page is available at: <https://gerne-debias.github.io/>.*

## 1. Introduction

Deep learning models have demonstrated significant success in various classification tasks, but their performance is often compromised by datasets containing prevalent spurious correlations in the majority of samples [13, 18, 29, 52]. Spurious correlations refer to unintended associations between easy-to-learn, non-target attributes and target labels. These correlations often cause models trained with Empirical Risk Minimization (ERM) [45] to rely on these correlations instead of the true, intrinsic features of the classes

[10, 12, 40]. This occurs because the ERM objective optimizes for the average performance [45], thereby biasing the model toward the easy-to-learn features that are predictive for the majority of training samples. As a result, ERM-trained models often exhibit poor generalization when these spurious features are absent in the test data. For instance, in the Waterbirds classification task [46], where the goal is to classify a bird as either a waterbird or a landbird, the majority of waterbirds are associated with water backgrounds. In contrast, the majority of landbirds are associated with land backgrounds. A model trained with ERM might learn to classify the birds based on the background—water for waterbirds and land for landbirds—rather than focusing on the birds’ intrinsic characteristics. This reliance on the spurious feature allows the model to perform well on the majority of training samples, where these correlations hold, but fails to generalize to test samples where these correlations are absent (e.g., waterbirds on land). Examples of Waterbirds images shown in Fig. 1a. Avoiding spurious correlations is crucial across various applications, including medical imaging [25, 37], finance [11], and climate modeling [17].

This pervasive challenge has spurred extensive research into strategies for mitigating the negative effects of spurious correlations, particularly under varying levels of attribute information availability. The authors of [50] provide a comprehensive review of the methods and research directions aimed at addressing this issue. In an ideal scenario, where attribute information is available in both the training and validation sets, methods can leverage this information to counteract spurious correlations [16, 39, 48]. When attribute information is available only in the validation set, methods either incorporate this set into the training process [18, 32, 42] or restrict its use to model selection and hyperparameter tuning [27–29, 31, 35]. Despite these efforts, existing methods still struggle to fully avoid learning spurious correlations, especially when the number of samples without spurious correlations is very limited in the training dataset, leading to poor generalization on the test data where these correlations are absent.

In this paper, we adopt a different research approach, seeking to address the issue of spurious correlations from

a model optimization perspective. We propose a novel method, Gradient Extrapolation for Debiased Representation Learning (GERNE), to avoid reliance on spurious features and learn debiased representations. The core idea is to sample two types of batches with varying amounts of spurious correlations (Fig. 1b) and compute the two losses on these two batches. We assume that the difference between the gradients of these losses captures a debiasing direction. Therefore, we define our target gradient as the linear extrapolation of these two gradients toward the gradient of the batch with fewer amount of spurious correlations (Fig. 1c). The contributions of this paper can be summarized as follows:

- We propose GERNE as a general framework for debiasing, with methods such as ERM and Resampling being shown as special cases.
- We derive the theoretical upper and lower bounds of the extrapolation factor and establish a direct connection between the extrapolation factor and the risk for the worst-case group. We show that tuning this factor within these bounds enables GERNE to adaptively optimize for either Group-Balanced Accuracy or Worst-Group Accuracy.
- We validate our approach on six benchmarks spanning both vision and NLP tasks, under both known and unknown attribute cases, demonstrating competitive and often superior performance compared to state-of-the-art methods—particularly in scenarios where samples without spurious correlations are scarce.

## 2. Related Work

**Debiasing according to attribute annotations availability.** Numerous studies have leveraged attribute annotations to mitigate spurious correlations and learning debiased representation [3, 39, 51, 53, 55]. For instance, Group DRO [39] optimizes model performance on the worst-case group by directly minimizing worst-group loss during training. While effective, such methods rely on complete attribute annotations, which are often costly and labor-intensive to obtain. Consequently, recent works have explored approaches that reduce reliance on full annotations by using limited attribute information [18, 32, 42]. For example, DFR [18] enhances robustness by using a small, group-balanced validation set with attribute information to retrain the final layer of a pre-trained model. In cases where attribute information is only available for model selection and hyperparameter tuning [6, 16, 28, 31, 54], an initial or auxiliary ERM-trained model is often used to infer the attributes by partitioning the training data into majority and minority groups. Samples on which the model incurs relatively low loss (i.e., high-confidence predictions) are treated as “easy” examples—where spurious correlations are likely to hold—and these examples form the majority group. Conversely, high-loss samples are considered “hard” examples, and typ-

ically form the minority group where such correlations may not apply [49]. This process effectively creates “easy” and “hard” pseudo-attributes within each class, allowing debiasing methods that traditionally rely on attribute information to be applied. For example, JTT [28] first trains a standard ERM model and then trains a second model by up-weighting the misclassified training examples detected by the first model. Finally, a more realistic and challenging scenario arises when attribute information is entirely unavailable [4, 43]—not accessible for training, model selection, or hyperparameter tuning—requiring models to generalize without explicit guidance on non-causal features [50].

**Debiasing via balancing techniques.** A prominent family of solutions to mitigate spurious correlations across the aforementioned scenarios of annotation availability involves data balancing techniques [7, 16, 19, 21, 36, 40, 47]. These methods are valued for their simplicity and adaptability, as they are typically faster to train and do not require additional hyperparameters. Resampling underrepresented groups to ensure a more balanced distribution of samples [16, 19] or modifying the loss function to adjust for imbalances [38] are common examples of these techniques. We demonstrate in Sec. 5.3 that although the balancing techniques are effective, their performance is constrained in the presence of spurious correlations. In contrast, our proposed debiasing approach mitigates the negative effects of spurious correlations by guiding the learning process in a debiasing direction, proving to be more effective.

## 3. Problem Setup

We consider a standard multi-class classification problem with  $K$  classes and  $A$  attributes. Each input sample  $x_i \in \mathcal{X} = \{x_j \mid j = 1, \dots, N\}$  is associated with a class label  $y_i \in \mathcal{Y} = \{1, \dots, K\}$  and an attribute  $a_i \in \mathcal{A} = \{1, \dots, A\}$ , where  $N$  is the total number of samples in the dataset. We define a group  $\mathcal{X}_{y,a}$  for  $(y, a) \in \mathcal{G} = \mathcal{Y} \times \mathcal{A}$  as the set of input samples  $x_i$  with class label  $y$  and attribute  $a$ , resulting in  $|\mathcal{G}| = K \cdot A$  groups. For each class  $y$ , we denote by  $\mathcal{X}_y = \bigcup_{a \in \mathcal{A}} \mathcal{X}_{y,a}$  the set of all samples with label  $y$ . We assume all groups are non-empty, i.e.,  $\forall (y, a) \in \mathcal{G}, \mathcal{X}_{y,a} \neq \emptyset$ , and denote the cardinality of any group  $\mathcal{X}_m$  by  $|\mathcal{X}_m|$ .

Our goal is to learn the intrinsic features that define the labels, rather than spurious features present in a biased dataset, where spurious correlations are prevalent. This would ensure robust generalization when spurious correlations are absent in the test distribution. Following [39], we aim to learn a function parameterized by a neural network  $f^* : \mathcal{X} \rightarrow \mathbb{R}^K$  to minimize the risk for the worst-case group:

$$f^* = \arg \min_f \max_{g \in \mathcal{G}} \mathbb{E}_{x \sim p(x|(y,a)=g)} [\ell(y, f(x))], \quad (1)$$

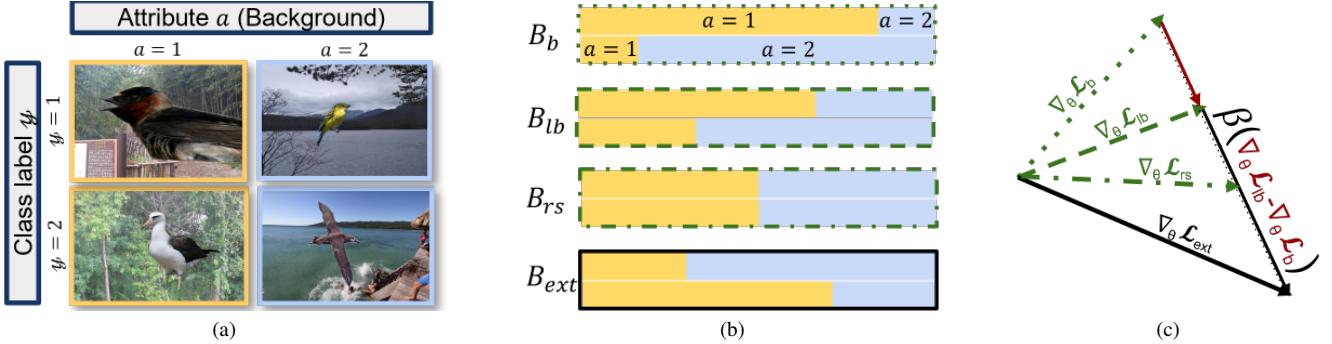


Figure 1. (a): Sample images from the waterbirds classification task. Most landbird images appear with land backgrounds (i.e.,  $y = 1, a = 1$ ), while most waterbird images appear with water backgrounds (i.e.,  $y = 2, a = 2$ ). This correlation between bird class and background introduces spurious correlations in the dataset. (b): Visualization of batch construction.  $B_b$  refers to a biased batch where the majority of images from class  $y = 1$  (top row) have attribute  $a = 1$  (yellow), and the majority of images from class  $y = 2$  (bottom row) have attribute  $a = 2$  (light-blue).  $B_{lb}$  represents a less biased batch, with a more balanced attribute distribution within each class, controlled by  $c$  (here  $c = \frac{1}{2}$ ).  $B_{rs}$  depicts a batch with group-balanced distribution and refers to the batch used in the Resampling method [16].  $B_{ext}$  simulates GERNE’s batch with  $c \cdot (\beta + 1) > 1$ , where the dataset’s minority groups appear as majorities in the batch. (c): A simplified 2D representation of gradient extrapolation where  $\theta \in \mathbb{R}^2$ .  $\nabla_\theta \mathcal{L}_b$  is the gradient computed on  $B_b$ ; training with this gradient is equivalent to training with ERM objective.  $\nabla_\theta \mathcal{L}_{lb}$  represents the gradient computed on  $B_{lb}$ .  $\nabla_\theta \mathcal{L}_{rs}$  is the gradient computed on  $B_{rs}$ , which is equivalent, in expectation, to an extrapolated gradient with  $c \cdot (\beta + 1) = 1$ . Finally,  $\nabla_\theta \mathcal{L}_{ext}$  is our extrapolated gradient, with the extrapolation factor  $\beta$  modulating the degree of debiasing based on the strength of spurious correlations present in the dataset.

where  $\ell(y, f(x)) \rightarrow \mathbb{R}$  is the loss function.

## 4. The Proposed Method: GERNE

We build GERNE with the goal of mitigating the impact of spurious correlations. The core idea of GERNE is to sample two batches with different amounts of spurious correlations, hereafter named the **biased batch**  $B_b$  and the **less biased batch**  $B_{lb}$  (Fig. 1b). Let  $\mathcal{L}_b, \mathcal{L}_{lb}$  be the losses calculated on  $B_b$  and  $B_{lb}$ , respectively. We assume that extrapolating the gradients of these two losses towards the gradient of  $\mathcal{L}_{lb}$  guides the model toward debiasing as illustrated in Fig. 1c. We first present GERNE for training with known attributes and then generalize GERNE to the unknown attribute case.

### 4.1. GERNE for the Known Attributes Case

In the following, we denote by  $p(y, a)$  the joint distribution of class label  $y$  and attribute  $a$  in a sampled batch. During training, we construct two types of batches with different conditional attribute distributions  $p(a|y)$ : the *biased* and the *less biased* batches. Our method defines the target loss as a linear extrapolation between the losses computed on these two batches. A simplified illustration is shown in Fig. 1. Finally, we derive the link between the extrapolation factor and the risk for the worst-case group in Eq. (1), and theoretically define the upper and lower bounds of this factor.

#### 4.1.1. Sampling the biased and the less biased batches

The biased batch and the less biased batches are sampled to satisfy the following two conditions:

1. Uniform sampling from classes, i.e.,  $\forall y \in \mathcal{Y}, p(y) = \frac{1}{K}$ .
2. Uniform sampling from groups, i.e.,  $\forall (y, a) \in \mathcal{G}, p(x|y, a) = \frac{1}{|\mathcal{X}_{y,a}|}$  for  $x \in \mathcal{X}_{y,a}$ .

The **biased batch** ( $B_b$ ) is sampled with a conditional attribute distribution  $p_b(a|y)$  within each class  $y$  to reflect the inherent bias present in the dataset. Specifically,  $p_b(a|y) = \alpha_{ya}$ , where:

$$\alpha_{ya} = \frac{|\mathcal{X}_{y,a}|}{|\mathcal{X}_y|}. \quad (2)$$

Note that to sample a biased batch, no access to the attributes is required, and uniformly sampling from  $\mathcal{X}_y$  for each label  $y$  satisfies Eq. (2). The **less biased batch** ( $B_{lb}$ ) is sampled with a conditional attribute distribution, denoted as  $p_{lb}(a|y)$ , which satisfies the following:  $\forall (y, a) \in \mathcal{G}$ :

$$\min\left(\frac{1}{A}, p_b(a|y)\right) \leq p_{lb}(a|y) \leq \max\left(\frac{1}{A}, p_b(a|y)\right). \quad (3)$$

That is,  $B_{lb}$  exhibits a more balanced group distribution than  $B_b$ , and  $\mathcal{L}_{lb}$  quantifies the loss when spurious correlations are reduced in the sampled batch. Choosing

$$p_{lb}(a|y) = (1-c) \cdot p_b(a|y) + c \cdot \frac{1}{A} = \alpha_{ya} + c \cdot \left(\frac{1}{A} - \alpha_{ya}\right) \quad (4)$$

satisfies the inequality in Eq. (3), where  $c \in (0, 1]$  is a hyperparameter that controls the degree of bias reduction. An example of the two types of batches is presented in Fig. 1b.

#### 4.1.2. Gradient extrapolation

We define our target loss  $\mathcal{L}_{ext}$  as follows:

$$\mathcal{L}_{ext} = \mathcal{L}_{lb} + \beta \cdot (\mathcal{L}_{lb} - \mathcal{L}_b), \quad (5)$$

where  $\beta$  is a hyperparameter, and the loss form given the joint distribution  $p(x, y, a)$  is defined as:

$$\mathcal{L} = \mathbb{E}_{(x,y,a) \sim p(x,y,a)} [\ell(y, f(x))]. \quad (6)$$

Given the set of parameters  $\theta$  of our model  $f$ , the gradient of  $\mathcal{L}_{ext}$  with respect to  $\theta$  can be derived from Eq. (5):

$$\nabla_{\theta} \mathcal{L}_{ext} = \nabla_{\theta} \mathcal{L}_{lb} + \beta \cdot (\nabla_{\theta} \mathcal{L}_{lb} - \nabla_{\theta} \mathcal{L}_b). \quad (7)$$

Our target gradient vector  $\nabla_{\theta} \mathcal{L}_{ext}$  in Eq. (7) is a linear extrapolation of the two gradient vectors  $\nabla_{\theta} \mathcal{L}_{lb}$  and  $\nabla_{\theta} \mathcal{L}_b$ , and accordingly, we refer to  $\beta$  as the extrapolation factor. Because the less biased batch has a less skewed conditional attribute distribution compared to the biased batch (as shown in Eq. (3)), extrapolating their gradients and toward the less biased gradient forms a new gradient ( $\mathcal{L}_{ext}$ ) that leads to learning even more debiased representation for some values of the extrapolation factor  $\beta > 0$ . A visual representation of extrapolation is shown in Fig. 1c.

#### 4.1.3. GERNE as a general framework for debiasing

Minimizing our target loss  $\mathcal{L}_{ext}$  simulates minimizing the loss of class-balanced batches with the following conditional distribution of  $(y, a) \in \mathcal{G}$ :

$$p_{ext}(a|y) = \alpha_{ya} + c \cdot (\beta + 1) \cdot \left( \frac{1}{A} - \alpha_{ya} \right). \quad (8)$$

We provide the full proof in Appendix A.

Based on Eq. (8), we can establish the link between GERNE and other methods for different values of  $\beta, c$ :

- For  $\beta = -1$ ,  $\mathcal{L}_{ext} = \mathcal{L}_b$  and GERNE is equivalent to class-balanced ERM method.
- For  $c = 1$  and  $\beta = 0$ ,  $p_{ext}(a|y) = \frac{1}{A}$ , and GERNE matches Resampling [16], which samples equally from all groups ( $B_{rs}$  in Fig. 1b, with gradient of the loss computed on it denoted as  $\nabla_{\theta} \mathcal{L}_{rs}$  in Fig. 1c).
- For  $c \cdot (\beta + 1) = 1$ , we also have  $p_{ext}(a|y) = \frac{1}{A}$ , and  $\mathcal{L}_{ext}$  is, in expectation, equivalent to  $\mathcal{L}_{rs}$ . However, their loss variances differ. In fact, GERNE permits controlling the variance of its loss through its hyperparameters  $(c, \beta)$ , which may help escape sharp minima [1] and improve generalization [23]. The derivation of the variance of GERNE's loss is detailed in Appendix B.
- For  $c \cdot (\beta + 1) > 1$ ,  $p_{ext}(a|y) > \frac{1}{A}$  if  $\alpha_{ya} < \frac{1}{A}$  (also  $p_{ext}(a|y) < \frac{1}{A}$  if  $\alpha_{ya} > \frac{1}{A}$ ). In this case, GERNE simulates batches where the underrepresented groups (i.e., those with  $\alpha_{ya} < \frac{1}{A}$ ) are oversampled.

#### 4.1.4. Upper and lower bounds of $\beta$

Having  $p_{ext}(a|y)$  in Eq. (8) within  $[0, 1]$ ,  $\beta$  should satisfy:

$$\max_{\substack{(y,a) \in \mathcal{G} \\ \alpha_{ya} \neq \frac{1}{A}}} \min(i_{ya}^1, i_{ya}^2) \leq \beta \leq \min_{\substack{(y,a) \in \mathcal{G} \\ \alpha_{ya} \neq \frac{1}{A}}} \max(i_{ya}^1, i_{ya}^2), \quad (9)$$

where:  $i_{ya}^1 = -\frac{\alpha_{ya}}{c \cdot (\frac{1}{A} - \alpha_{ya})} - 1$ ,  $i_{ya}^2 = \frac{1 - \alpha_{ya}}{c \cdot (\frac{1}{A} - \alpha_{ya})} - 1$ .

These bounds are used when tuning  $\beta$ . In Appendix C, we simplify these bounds to  $[\beta_{\min}, \beta_{\max}] = [-1, i_{y''a''}^1]$ , where  $(y'', a'') = \arg \max_{(y,a) \in \mathcal{G}} \alpha_{ya}$ . Note that  $\beta$  doesn't affect  $p_{ext}(a|y)$  for  $\alpha_{ya} = \frac{1}{A}$  according to Eq. (8).

#### 4.1.5. Tuning $\beta$ to minimize the risk for worst-case group

Eq. (5) can be rewritten as follows (detailed in Appendix A):

$$\mathcal{L}_{ext} = \frac{1}{K} \cdot \sum_{g=(y,a) \in \mathcal{G}} p_{ext}(a|y)(\beta) \cdot L_g, \quad (10)$$

where

$$L_g = \mathbb{E}_{x \sim p(x|(y,a)=g)} [\ell(y, f(x))]. \quad (11)$$

In the presence of spurious correlations, minority or less-represented groups often experience higher risks, primarily due to the model's limited exposure to these groups during training [20]. Taking this into consideration, we define  $g' = (y', a') = \arg \min_{(y,a) \in \mathcal{G}} \alpha_{ya}$ . Since  $L_{g'}$  is weighted by  $p_{ext}(a'|y')$ , increasing  $\beta$  beyond  $\frac{1}{c} - 1$  assigns more weight to  $L_{g'}$  in Eq. (10) than any other group loss (all groups' losses are equally weighted when  $c \cdot (\beta + 1) = 1$ ). This increase in  $\beta$  encourages the model to prioritize reducing the loss of the underrepresented group  $g'$  during training, therefore minimizing the risk for the worst-case group.

We outline the detailed steps of our approach for the known attribute case in Algorithm 1.

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#### Algorithm 1 GERNE for the known attribute case

**Input:**  $\mathcal{X}_{y,a} \subseteq \mathcal{X}$  for  $y \in \mathcal{Y}$  and  $a \in \mathcal{A}$ ,  $f$  with initial  $\theta = \theta_0$ , # epochs  $E$ , batch size per label  $B$ , # classes  $K$ , # attributes  $A$ , learning rate  $\eta$ .

- 1: Choose  $c \in (0, 1]$  and  $\beta \in [\beta_{\min}, \beta_{\max}]$  via grid search.
  - 2: **for** epoch = 1 to  $E$  **do**
  - 3:     Biased Batch  $B_b = \emptyset$ , Less Biased Batch  $B_{lb} = \emptyset$
  - 4:     **for**  $(y, a) \in \mathcal{G}$  **do**
  - 5:         Sample a mini-batch  $B_b^{y,a} = \{(x, y)\} \subseteq \mathcal{X}_{y,a}$  of size  $\alpha_{y,a} \cdot B$ ;
  - 6:          $B_b = B_b \cup B_b^{y,a}$
  - 7:         Sample a mini-batch  $B_{lb}^{y,a} = \{(x, y)\} \subseteq \mathcal{X}_{y,a}$  of size  $((1 - c) \cdot \alpha_{y,a} + \frac{c}{A}) \cdot B$
  - 8:          $B_{lb} = B_{lb} \cup B_{lb}^{y,a}$
  - 9:     **end for**
  - 10:    Compute  $\mathcal{L}_b, \mathcal{L}_{lb}$  on  $B_b, B_{lb}$ , respectively. Then, compute  $\nabla_{\theta} \mathcal{L}_b$  and  $\nabla_{\theta} \mathcal{L}_{lb}$ .
  - 11:    Compute  $\nabla_{\theta} \mathcal{L}_{ext}$  using Eq. (7).
  - 12:    Update parameters (SGD):  $\theta \leftarrow \theta - \eta \cdot \nabla_{\theta} \mathcal{L}_{ext}$
  - 13: **end for**
- 

#### 4.2. GERNE for the Unknown Attributes Case

If the attributes are unavailable during training, it is not possible to directly sample less biased batches. To address this,

we follow the previous work [28, 31, 54] by training a standard ERM model  $\tilde{f}$  and using its predictions to create pseudo-attributes  $\tilde{a}$ . Since  $\tilde{f}$  is trained on biased batches, it tends to rely on spurious correlations, resulting in biased predictions. Leveraging these predictions, we classify samples into easy—those with high-confidence predictions, where the spurious correlations likely hold—and hard—those with low-confidence predictions, where the spurious correlations may not hold. After training  $\tilde{f}$ , we select a threshold  $t \in (0, 1)$  and construct pseudo-attributes based on model predictions as follows: For each class  $y$ , we compute the predictions  $\tilde{y}_i = p(y|x_i) = \text{softmax}(\tilde{f}(x_i))_y$  for each  $x_i \in \mathcal{X}_y$ . We then split them into two non-empty subsets: The first subset contains the smallest  $\lfloor t \cdot |\mathcal{X}_y| \rfloor$  values, and the corresponding samples form the group  $\mathcal{X}_{y,\tilde{a}=1}$ . The remaining samples forms the group  $\mathcal{X}_{y,\tilde{a}=2}$ . This process ensures that each set  $\mathcal{X}_y$  is divided into two disjoint and non-empty groups. Consequently, the pseudo-attribute space consists of two values, denoted as  $\tilde{\mathcal{A}} = \{1, 2\}$  (i.e.,  $\tilde{A} = 2$ ) with  $\tilde{\mathcal{G}} = \mathcal{Y} \times \tilde{\mathcal{A}}$  replacing  $\mathcal{G}$  in the unknown attribute case.  $t$  is a hyperparameter, and we outline the detailed steps of GERNE for the unknown case in Appendix D.

#### 4.2.1. Tuning $\beta$ to control the unknown conditional distribution of an attribute $a$ in class $y$

After creating the pseudo-attributes and defining the pseudo-groups, we consider forming a new batch of size  $B$  by uniformly sampling  $\gamma \cdot B$  examples from group  $\mathcal{X}_{y,\tilde{a}=1}$  and  $(1 - \gamma) \cdot B$  examples from group  $\mathcal{X}_{y,\tilde{a}=2}$ , where  $\gamma \in [0, 1]$ ,  $\gamma \cdot B \in \mathbb{N}$ . The resulting conditional distribution of an attribute  $a$  given  $y$  in the constructed batch is:

$$p_B(a|y) = \sum_{\tilde{a} \in \tilde{\mathcal{A}}} p_B(\tilde{a}|y) \cdot p(a|\tilde{a}, y). \quad (12)$$

Because the max/min value of a linear program must occur at a vertex, we have for  $p(a|\tilde{a}, y) = p_{\tilde{a},y}(a)$ :

$$\forall \gamma \in [0, 1], \min_{\tilde{a} \in \tilde{\mathcal{A}}} p_{\tilde{a},y}(a) \leq p_B(a|y) \leq \max_{\tilde{a} \in \tilde{\mathcal{A}}} p_{\tilde{a},y}(a). \quad (13)$$

This means that if:  $\max_{\tilde{a}} p_{\tilde{a},y}(a) < \frac{1}{A} (\min_{\tilde{a}} p_{\tilde{a},y}(a) > \frac{1}{A})$ , then there is no value for  $\gamma$  can yield a batch with  $p_B(a|y) > \frac{1}{A} (p_B(a|y) < \frac{1}{A})$  via sampling from the pseudo-groups.

**Proposition 1.** In case of unknown attributes, GERNE can simulate creating batches with more controllable conditional attribute distribution (i.e.,  $p_B(a|y) > \max_{\tilde{a} \in \tilde{\mathcal{A}}} p_{\tilde{a},y}(a)$  or  $p_B(a|y) < \min_{\tilde{a} \in \tilde{\mathcal{A}}} p_{\tilde{a},y}(a)$ ). We provide the proof of this proposition in Appendix E.

## 5. Experiments

To evaluate the general applicability of GERNE, we assess its performance across five computer vision and one

natural language processing benchmarks: Colored MNIST (C-MNIST) [3, 27], Corrupted CIFAR-10 (C-CIFAR-10) [15, 31], Biased FFHQ (bFFHQ) [22, 27], Waterbird [46], CelebA [30], and CivilComments [5]. We categorize these datasets into two groups: Datasets-1 and Datasets-2. Datasets-1 comprises the first three datasets mentioned above and is used to evaluate GERNE’s performance without data augmentation. Datasets-2 consists of the remaining three datasets, for which we follow the experimental setup described in [50] to ensure a fair comparison.

### 5.1. Experiments on Datasets-1

**Datasets.** C-MNIST is an extension of the MNIST dataset [26] where each digit class is predominantly associated with a specific color. This introduces a spurious correlation between the digit label (target) and color (attribute). C-CIFAR-10 modifies CIFAR-10 by applying specific texture patterns to each object class [15], making texture a spurious feature. Both C-MNIST and C-CIFAR-10 include versions with varying degrees of spurious correlation, reflected by the minority group ratios of 0.5%, 1%, 2%, and 5% in the training and validation sets. The bFFHQ dataset comprises human face images, with “age” and “gender” as the target and spurious attributes, respectively. The majority of female faces are young, while the majority of males are old. The minority group ratio in the training set is 0.5%.

**Evaluation metrics.** We follow the evaluation protocols of prior work [27, 29, 31]. For C-MNIST and C-CIFAR-10, we report Group-Balanced Accuracy (GBA) on the test set. For bFFHQ, we evaluate performance based on the accuracy of the minority group.

**Baselines.** For the known attribute case, we compare GERNE with Group DRO [39] and Resampling [16]. For the unknown attribute case, we consider ERM [45], JTT [28], LfF [31], DFA [27], LC [29], and DeNetDM [44].

**Implementation details.** We adopt the same model architectures as the baselines and use SGD optimizer across all three datasets. More details are provided in Appendix F.1.

**Results.** Tab. 1 compares GERNE with baselines for both known and unknown attribute cases. All baseline results are adopted from [29], except DeNetDM, which is sourced from [44]. When the attributes are known, GERNE outperforms Group DRO by a significant margin on C-MNIST and C-CIFAR-10 datasets. The improvement in performance ranges from about 5% on C-CIFAR-10 with 5% of minority group and up to 16% on C-MNIST with 1% of minority group. Furthermore, GERNE outperforms Resampling [16] by over 13% on bFFHQ and consistently surpasses it

Table 1. Performance comparison of GERNE and baselines on the C-MNIST, C-CIFAR-10, and bFFHQ datasets. We report GBA (%) with standard deviation over three trials for C-MNIST and C-CIFAR-10 across varying minority ratios, and minority group accuracy (%) for bFFHQ. DeNetDM results are from [44], and Resampling results are generated using GERNE with  $c = 1, \beta = 0$ . All other results are from [29]. ✓/✗ indicate known/unknown training attributes. The **best** results are marked in bold, and the second-best are underlined.

Methods	Group Info	C-MNIST				C-CIFAR-10				bFFHQ
		0.5	1	2	5	0.5	1	2	5	
Group DRO	✓	63.12	68.78	76.30	84.20	33.44	38.30	45.81	57.32	-
Resampling	✓	$77.68 \pm 0.89$	$84.36 \pm 0.21$	$88.15 \pm 0.11$	$91.98 \pm 0.08$	$45.10 \pm 0.60$	$50.08 \pm 0.42$	$54.85 \pm 0.30$	$62.16 \pm 0.05$	$72.13 \pm 0.90$
GERNE (ours)	✓	<u><math>77.79 \pm 0.90</math></u>	<u><math>84.47 \pm 0.37</math></u>	<u><math>88.30 \pm 0.20</math></u>	<u><math>92.16 \pm 0.10</math></u>	<u><math>45.34 \pm 0.60</math></u>	<u><math>50.84 \pm 0.17</math></u>	<u><math>55.51 \pm 0.10</math></u>	<u><math>62.40 \pm 0.27</math></u>	<u><math>85.20 \pm 0.86</math></u>
ERM	✗	$35.19 \pm 3.49$	$52.09 \pm 2.88$	$65.86 \pm 3.59$	$82.17 \pm 0.74$	$23.08 \pm 1.25$	$28.52 \pm 0.33$	$30.06 \pm 0.71$	$39.42 \pm 0.64$	$56.70 \pm 2.70$
JTT	✗	$53.03 \pm 3.89$	$62.90 \pm 3.01$	$74.23 \pm 3.21$	$84.03 \pm 1.10$	$24.73 \pm 0.60$	$26.90 \pm 0.31$	$33.40 \pm 1.06$	$42.20 \pm 0.31$	$65.30 \pm 2.50$
LIF	✗	$52.50 \pm 2.43$	$61.89 \pm 4.97$	$71.03 \pm 1.14$	$84.79 \pm 1.09$	$28.57 \pm 1.30$	$33.07 \pm 0.77$	$39.91 \pm 1.30$	$50.27 \pm 1.56$	$62.20 \pm 1.60$
DFA	✗	$65.22 \pm 4.41$	$81.73 \pm 2.34$	$84.79 \pm 0.95$	$89.66 \pm 1.09$	$29.75 \pm 0.71$	$36.49 \pm 1.79$	$41.78 \pm 2.29$	$51.13 \pm 1.28$	$63.90 \pm 0.30$
LC	✗	<u><math>71.25 \pm 3.17</math></u>	<u><math>82.25 \pm 2.11</math></u>	<u><math>86.21 \pm 1.02</math></u>	<u><math>91.16 \pm 0.97</math></u>	<u><math>34.56 \pm 0.69</math></u>	<u><math>37.34 \pm 1.26</math></u>	<u><math>47.81 \pm 2.00</math></u>	<u><math>54.55 \pm 1.26</math></u>	<u><math>69.67 \pm 1.40</math></u>
DeNetDM	✗	-	-	-	-	$38.93 \pm 1.16$	$44.20 \pm 0.77$	$47.35 \pm 0.70$	$56.30 \pm 0.42$	$75.70 \pm 2.80$
GERNE (ours)	✗	<u><math>77.25 \pm 0.17</math></u>	<u><math>83.98 \pm 0.26</math></u>	<u><math>87.41 \pm 0.31</math></u>	$90.98 \pm 0.13$	<u><math>39.90 \pm 0.48</math></u>	<u><math>45.60 \pm 0.23</math></u>	<u><math>50.19 \pm 0.18</math></u>	<u><math>56.53 \pm 0.32</math></u>	<u><math>76.80 \pm 1.21</math></u>

across all other ratios. Our explanation behind GERNE superior performance over Resampling is that latter tends to present the majority and minority groups equally in the sampled batches during training, and the model  $f$  tends to prioritize learning the easy-to-learn spurious features associated with the majority group (e.g., the colors in C-MNIST), leading to learning biased representation and poorer generalization. In contrast, GERNE undermines learning the spurious features by directing the learning process more in the debiasing direction, thanks to the extrapolation factor. For the unknown attribute case, GERNE outperforms all baselines, except on C-MNIST with 5% of minority group (ranks second), while maintaining a lower standard deviation. At this 5% minority ratio, LC achieves slightly higher accuracy—likely benefiting from its use of data augmentation to increase the diversity of the samples in the minority group. We exclude DeNetDM’s results on C-MNIST, as the authors use a different version of this dataset.

## 5.2. Experiments on Datasets-2

**Datasets.** Waterbirds [46] contains bird images with spurious correlations between bird type and background: Most waterbirds appear with water backgrounds, while most landbirds appear with land backgrounds. CelebA [30] involves classifying hair color (blond, non-blond), with gender (male, female) as the spurious attribute: Most blond images depict females. CivilComments [5] is a binary toxic comment classification dataset, where the spurious attribute marks references to eight different demographic identities (male, female, LGBTQ, Christian, Muslim, other religions, Black, and White).

**Evaluation metrics.** We follow the same evaluation strategy from [50] for model selection and hyperparameter tuning. When attributes are known in both training and validation, we use the worst-group test accuracy as the evaluation metric. When attributes are unknown in training, but

known in validation, we use the worst-group validation accuracy. When attributes are unavailable in both, we use the worst-class validation accuracy.

**Baselines.** For each dataset, we select the best three methods reported in [50]. We end up with ERM [45], Group DRO [39], DFR [18], LISA [51], ReSample [19], Mixup [53], ReWeightCRT [21], ReWeight [19], CBLoss [7], BSoftmax [36] and SqrtReWeight [50]. We also report the results for CnC [54] as it adopts similar training settings.

**Implementation details.** We employ the same data augmentation techniques, optimizers and pretrained models described in [50]. Further details are in Appendix F.2.

**Results** Tab. 2 shows the worst-group accuracy (WGA) of the test set for GERNE compared to the baseline methods under the evaluation strategy explained above. In the known attributes case, GERNE achieves the highest accuracy on CelebA and CivilComments, and ranks second on Waterbirds, following DFR. In case of unknown attributes in the training set but known in validation, our approach again attains the best results on Waterbirds and CivilComments datasets and remains competitive on CelebA, closely following the top two baselines’ results. In particular, DFR uses the validation set to train the model, whereas GERNE employs it only for model selection and hyperparameter tuning. We include a comparison between DFR and GERNE when using the validation set for training in Appendix G. When attributes are unknown in both the training and validation sets, GERNE achieves the best results on Waterbirds and CelebA. However, we observe a significant drop in accuracy on CelebA compared to the second case (known attributes only in validation), while this drop is less pronounced on Waterbirds. The difference can be attributed to the use of worst-class accuracy as the evaluation metric.

In CelebA’s validation set, the majority of blond hair images exhibit spurious correlations (female images), leading the model selection process to favor the majority group while disregarding the minority group. In contrast, the validation set in Waterbirds is group-balanced within each class, leading to only a slight decrease in performance between the second and third case. This highlights the critical role of having access to the attributes in the validation set—or at least a group-balanced validation set—for model selection when using GERNE.

Table 2. Performance comparison of GERNE and baseline methods on Waterbirds, CelebA, and CivilComments. We report the worst-group test accuracy (%) and standard deviation over three trials for each dataset. Baseline results are sourced from [50] as the same experimental settings are adopted. ✓/✓ denotes known attributes in training and validation sets. ✗/✓ indicates attributes are known only in the validation set, while ✗/✗ signifies that attributes are unknown in both sets. **Best** results are highlighted in bold, and the second-best are underlined.

Methods	Group Info		Waterbirds	CelebA	Civil-Comments
	train/val attr.				
ERM	✓/✓		69.10 ± 4.70	62.60 ± 1.50	63.70 ± 1.50
Group DRO	✓/✓		78.60 ± 1.00	89.00 ± 0.70	70.60 ± 1.20
ReWeight	✓/✓		86.90 ± 0.70	89.70 ± 0.20	65.30 ± 2.50
ReSample	✓/✓		77.70 ± 1.20	87.40 ± 0.80	73.30 ± 0.50
CBLoss	✓/✓		86.20 ± 0.30	89.40 ± 0.70	73.30 ± 0.20
DFR	✓/✓		<b>91.00 ± 0.30</b>	90.40 ± 0.10	69.60 ± 0.20
LISA	✓/✓		88.70 ± 0.60	86.50 ± 1.20	73.70 ± 0.30
GERNE (ours)	✓/✓		<u>90.20 ± 0.22</u>	<b>91.98 ± 0.15</b>	<b>74.65 ± 0.20</b>
ERM	✗/✓		69.10 ± 4.70	57.60 ± 0.80	63.20 ± 1.20
Group DRO	✗/✓		73.10 ± 0.40	78.50 ± 1.10	69.50 ± 0.70
ReWeight	✗/✓		72.50 ± 0.30	81.50 ± 0.90	69.90 ± 0.60
DFR	✗/✓		<u>89.00 ± 0.20</u>	<u>86.30 ± 0.30</u>	63.90 ± 0.30
Mixup	✗/✓		78.20 ± 0.40	57.80 ± 0.80	66.10 ± 1.30
LISA	✗/✓		78.20 ± 0.40	57.80 ± 0.80	66.10 ± 1.30
BSoftmax	✗/✓		74.10 ± 0.90	83.30 ± 0.30	69.40 ± 1.20
ReSample	✗/✓		70.00 ± 1.00	82.20 ± 1.20	68.20 ± 0.70
CnC	✗/✓		88.50 ± 0.30	<b>88.80 ± 0.90</b>	68.90 ± 2.10
GERNE (ours)	✗/✓		<b>90.21 ± 0.42</b>	86.28 ± 0.12	<b>71.00 ± 0.33</b>
ERM	✗/✗		69.10 ± 4.70	57.60 ± 0.80	63.20 ± 1.20
Group DRO	✗/✗		73.10 ± 0.40	68.30 ± 0.90	61.50 ± 1.80
DFR	✗/✗		<u>89.00 ± 0.20</u>	73.70 ± 0.80	64.40 ± 0.10
Mixup	✗/✗		<u>77.50 ± 0.70</u>	57.80 ± 0.80	65.80 ± 1.50
LISA	✗/✗		<u>77.50 ± 0.70</u>	57.80 ± 0.80	65.80 ± 1.50
ReSample	✗/✗		70.00 ± 1.00	74.10 ± 2.20	61.00 ± 0.60
ReWeightCRT	✗/✗		76.30 ± 0.20	<u>70.70 ± 0.60</u>	64.70 ± 0.20
SqrtReWeight	✗/✗		71.00 ± 1.40	66.90 ± 2.20	<b>68.60 ± 1.10</b>
CRT	✗/✗		76.30 ± 0.80	69.60 ± 0.70	67.80 ± 0.30
GERNE (ours)	✗/✗		<b>89.88 ± 0.67</b>	<b>74.24 ± 2.51</b>	63.10 ± 0.22

### 5.3. GERNE vs. Balancing Techniques

Balancing techniques have been shown to achieve state-of-the-art results, while remaining easy to implement [16, 50]. While Resampling often outperforms Reweighting when combined with stochastic gradient algorithms [2], we show in Tab. 1 that GERNE consistently outperforms Resampling in both group-balanced accuracy (GBA) and minority group accuracy. This highlights the flexibility of GERNE to adapt to maximize both metrics, and its superior performance in

comparison to Resampling and other balancing techniques, as further supported by the results in Tab. 2. In Appendix B, we provide a detailed ablation study comparing GERNE to an equivalent “sampling+weighting” approach with matching loss expectation, and demonstrate how GERNE can leverage its controllable loss variance (by the hyperparameters  $c, \beta$ ) to escape sharp minima.

### 5.4. Ablation Study

**Tuning the extrapolation factor  $\beta$ .** The value of  $\beta$  in Eq. (7) plays a critical role in guiding the model toward learning debiased representation (i.e., reducing reliance on spurious features and improve generalization). In Fig. 2, we illustrate the effect of tuning  $\beta$  on the learning process using C-MNIST with 0.5% of minority group in the known attributes case. We show results for  $\beta \in \{-1, 0, 1, 1.2\}$  with  $c = 0.5$ . For  $\beta = -1$ , our target loss  $\mathcal{L}_{ext}$  in Eq. (5) equals the biased loss  $\mathcal{L}_b$ , which leads to learning a biased model that exhibits high accuracy on the majority group, yet demonstrates poor performance on both the minority group and the unbiased test set. As  $\beta$  increases (e.g.  $\beta = 0, \beta = 1$ ), the model starts learning more intrinsic features. This is evident from the improved performance on the minority group in the validation set, as well as on the unbiased test set. However, as the extrapolation factor  $\beta$  continues to increase, the model begins to exhibit higher variance during the training process, as shown for  $\beta = 1.2$ , ultimately leading to divergence when  $\beta$  exceeds the upper bound defined in Eq. (9) (1.22 in this case). While GERNE appears to be sensitive to small variations in  $\beta$  (e.g. 1.2 to 1.22), we show in Appendix C that  $\beta_{max}$  is inversely proportional to  $c, A$ . This implies that decreasing  $c$  allows for a wider feasible range of  $\beta$ . By comparing the accuracies on minority and majority training groups in case  $\beta = 0, \beta = 1$ , we can see that both cases have around 100% accuracy on minority but higher accuracy on majority for  $\beta = 0$ . However,  $\beta = 1$  results in better generalization overall. This highlights the importance of directing the training process toward a debiased direction early in training, especially when overfitting is likely to occur on the minority group (e.g., when it contains very few samples).

**How the selection of  $t$  influences the optimal value of  $\beta$ .** To answer this question, we conduct experiments on C-MNIST dataset with 0.5% of minority group. We first train a biased model  $\hat{f}$ , and use its predictions to generate the pseudo-attributes for five different values of the threshold  $t$ . Let’s refer to the pseudo-groups with  $\tilde{\alpha} = 1$  as the pseudo-minority groups. For each threshold, we tune  $\beta$  to achieve the best average test accuracy. Simultaneously, we compute the average precision and recall for the minority group. As shown in Fig. 3, with  $t = 5 \times 10^{-4}$ , the average precision reaches 1, indicating that all the samples in

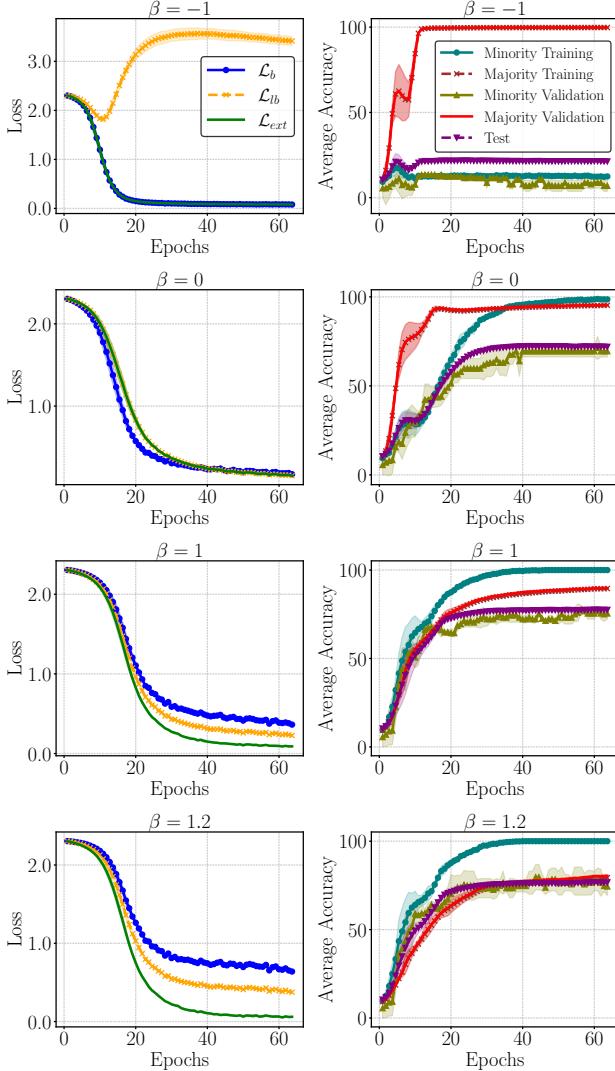


Figure 2. The impact of tuning  $\beta \in \{-1, 0, 1, 1.2\}$  on debiasing the model. On the left column, we plot the training losses  $\mathcal{L}_b$ ,  $\mathcal{L}_{lb}$  and the target loss  $\mathcal{L}_{ext}$ . On the right column, we plot the average accuracy of the minority and majority groups in both training and validation sets, as well as the average accuracy of the unbiased test set. Each plot represents the mean and standard deviation calculated over three runs with different random seeds.

the pseudo-minority groups are from the minority groups. However, these samples constitute less than 20% of the total minority groups, as indicated by the average recall. Despite this, GERNE achieves a high accuracy of approximately 70%, remaining competitive with other methods reported in Tab. 1 while using only a very limited number of minority samples ( $t = 5 \times 10^{-4}$  corresponds to about 28 samples versus 249 minority samples out of 55,000 samples in the training set). As  $t$  increases to  $10^{-3}$  and  $3 \times 10^{-3}$ , precision remains close to 1 while increasing the number of

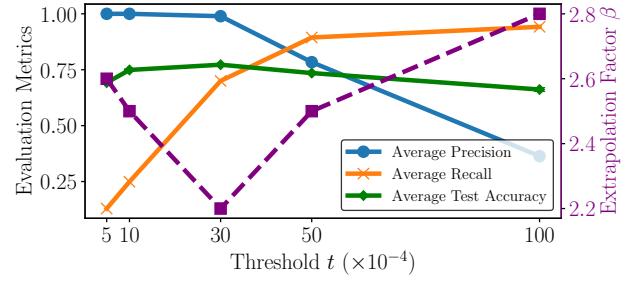


Figure 3. The effect of the threshold  $t$  used to generate pseudo-attributes on the extrapolation factor  $\beta$  and model performance. We plot the average precision and recall over pseudo-minority groups ( $y, \tilde{a} = 1$ ), averaged across all classes  $y$ . For each  $(y, \tilde{a} = 1)$ , precision is defined as the fraction of minority samples among all samples in that group, and recall is the fraction of those minority samples relative to all minority samples in class  $y$ . We also report the best achievable test accuracy, along with the corresponding extrapolation factor  $\beta$ , across different threshold values.

minority samples in the pseudo-minority groups. This increase introduces more diversity among minority samples within the pseudo-minority groups, allowing for lower  $\beta$  values to achieve the best average test accuracy. However, for even higher thresholds, such as  $t = 10^{-2}$ , minority samples constitute less than 40% in the pseudo-minority groups, prompting a need to revert to higher  $\beta$  values. We conclude that identifying the samples of minority groups (high average precision and high recall) is of utmost importance for achieving optimal results and this agrees with the results presented in both Tab. 1, Tab. 2 where we achieve the best results in the known attributes case.

## 6. Conclusion

We introduce GERNE, a novel debiasing approach that effectively mitigates spurious correlations by leveraging an extrapolated gradient update. By defining a debiasing direction from loss gradients computed on batches with varying degrees of spurious correlations, GERNE’s tunable extrapolation factor allows optimizing either Group-Balanced Accuracy (GBA) or Worst-Group Accuracy (WGA). Our comprehensive evaluations across vision and NLP benchmarks demonstrate GERNE’s superior performance over state-of-the-art methods, both for known and unknown attribute cases, without data augmentation. Furthermore, GERNE offers a general framework that encompasses methods like ERM and Resampling, extending its applicability to unbiased datasets. Future work will explore dynamic adaptation of the extrapolation factor and refine attribute estimation for the unknown attributes case.

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