

# Ray Tracing in Entertainment Industry

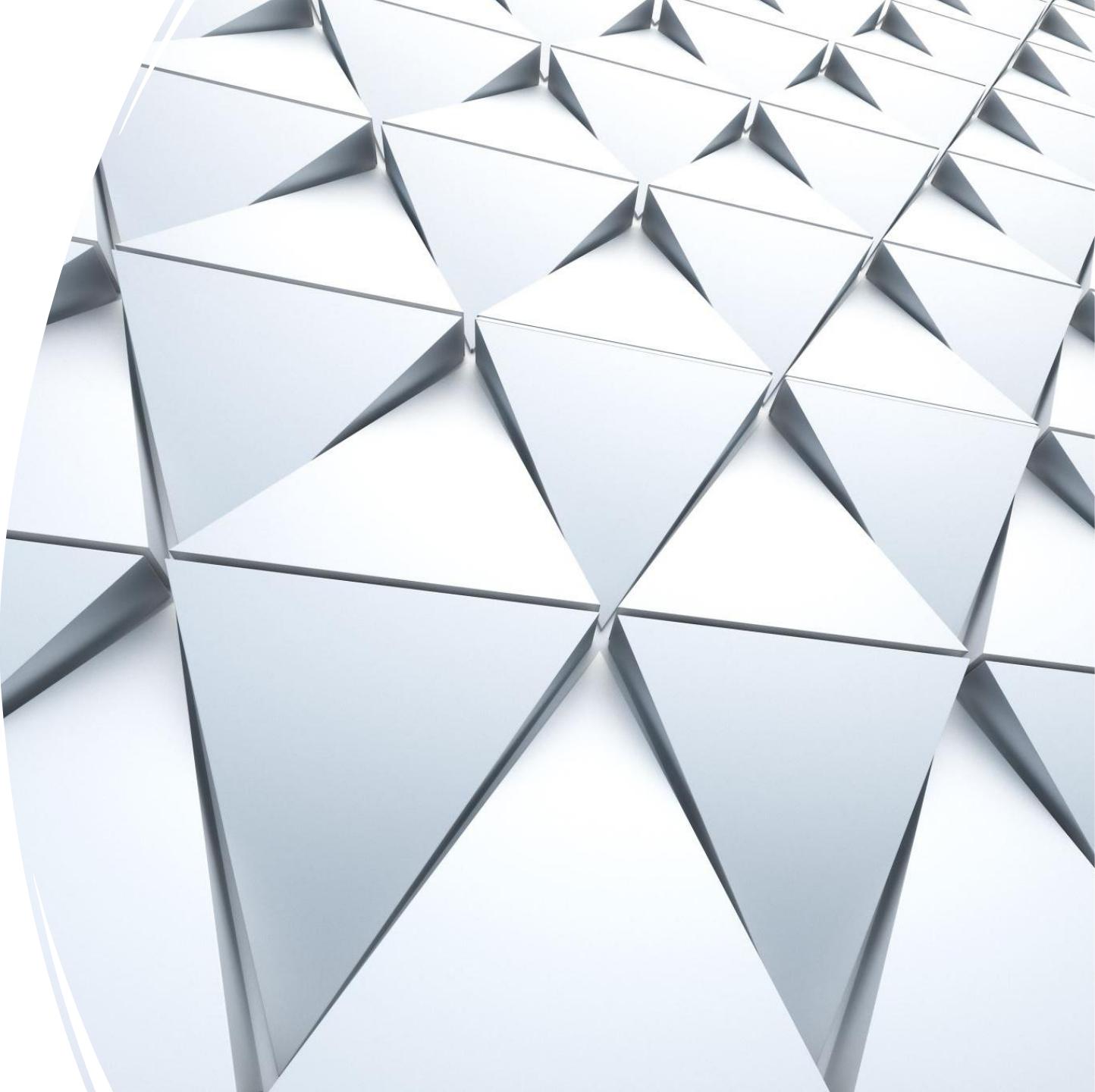
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Week 4  
Basic shapes and intersections

# Basic shapes and intersections

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- Sphere
- Quad
- Triangle (not available)



# More ray tracing components (classes)

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- Scene class
  - Handle scene objects and events.
- Integrator class
  - Solve the rendering equation.
- Material class
  - Fancy color ! - make objects colorful.
- Object class
  - Implement shapes and their ray-intersection method.

# Scene class

- Hold objects (sphere, quad, triangle, etc.) to setup a scene
- Attributes
  - A list of objects
  - A list of hit objects
- Methods
  - Add an object
  - Find an intersection by given a ray shot in the scene
  - Get a list of hit objects

# Method : find\_intersection()

## Input

- A generated ray from the camera.
- An interval of parameter 't'.

## Pseudocode

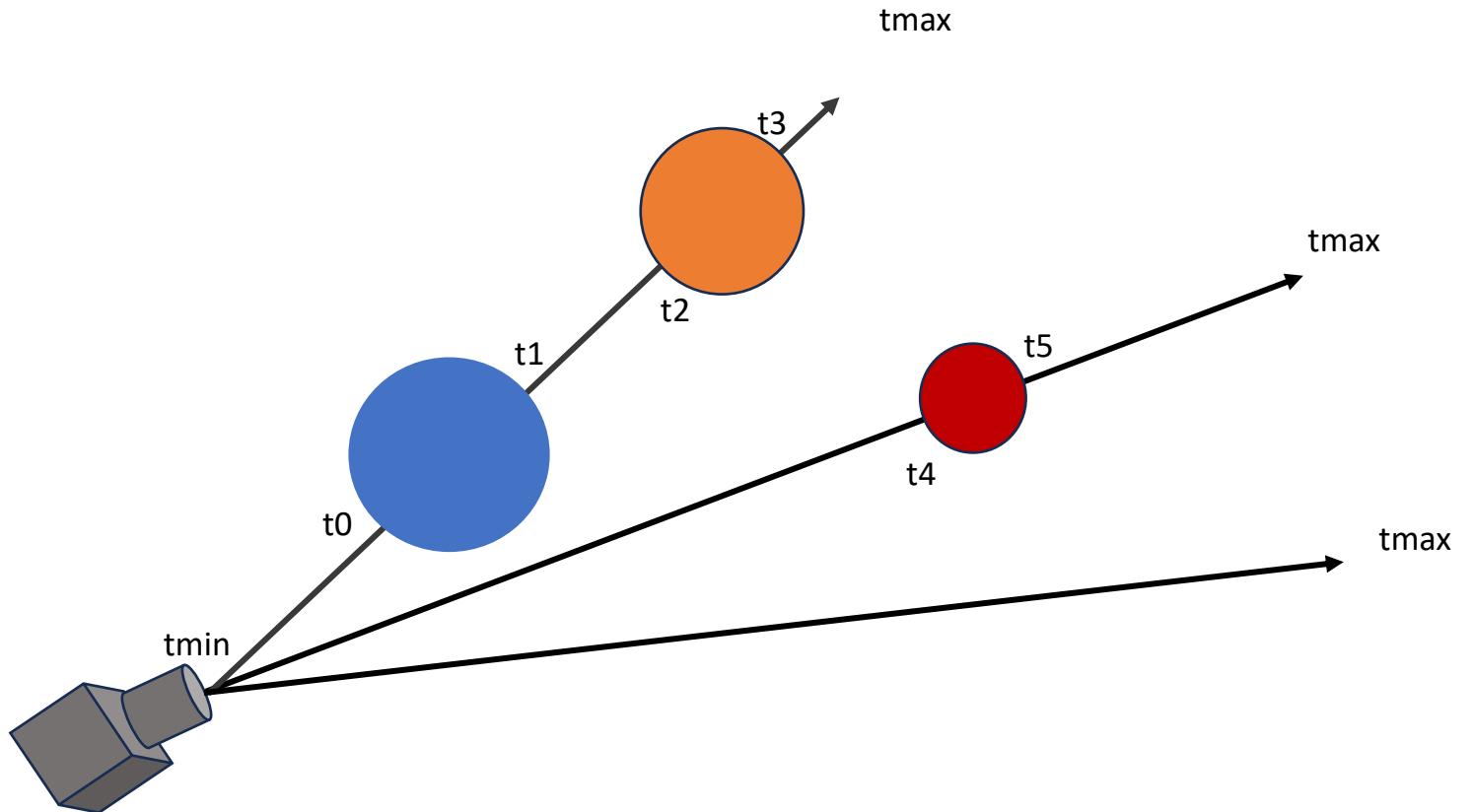
- Initialize the closet maximum of t.
- For each object in the given scene.
  - Get the hit info from the intersection between an object and the given ray.
  - If the object is hit by the given ray.
    - Update the closet maximum of t.
    - Update the hit list.
  - Return if found any hit or not.

# Illustration of the method

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## Pseudocode

- Initialize the closet maximum of  $t$ .
- For each object in the given scene.
  - Get the hit info from the intersection between an object and the given ray.
  - If the object is hit by the given ray.
    - Update the closet maximum of  $t$ .
    - Update the hit list.
- Return if found any hit or not.





# Integrator class

- Compute the radiance information of a generated ray given the scene.
  - Attributes
    - None
  - Methods
    - Compute scattering

# Method : compute\_scattering()

- Input
  - A generated ray
  - The scene
- Pseudocode
  - If the generated ray hits an object.
    - Get the hit info.
    - Get the material of the object.
    - Return the color.

# Material class

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- Appearance information (color and how the ray interacts with the object.)
- It is a base class.
- Attributes
  - None
- Methods
  - Virtual method : scattering()



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## A simple material

- Lambertian class
- It is derived from the 'material' class.
- It returns the color of the object.
- Attributes
  - Object's color --> called albedo
- Methods
  - Scattering()

# Creating an object

## Define an object base class

- Attributes
  - None – each children has its own parameters.
- Methods
  - Virtual method : intersect() - for handling ray-object intersection

The object class is then derived to child classes.

- Sphere
- Quad
- Triangle
- etc.

## Object class

An interface class to be derived.

It contains the following virtual methods.

- intersect()

# Sphere class

- Attributes
  - Center
  - Radius
  - Material
- Methods
  - Add material
  - intersect()

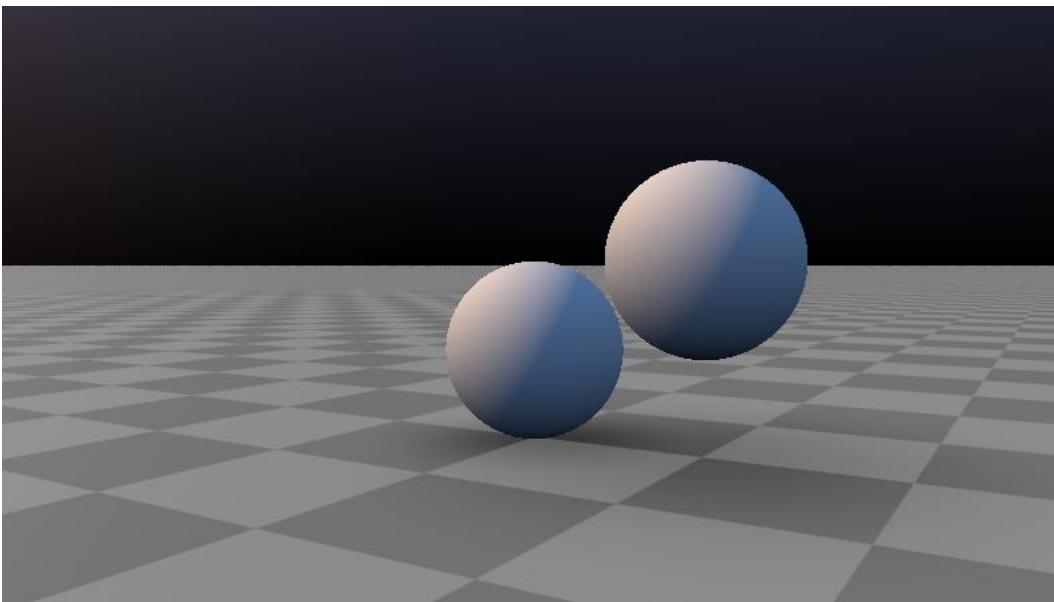


Image from [www.shadertoy.com/view/ltBSzK](http://www.shadertoy.com/view/ltBSzK)

# How a ray intersect a sphere ?

$$(x - C_x)^2 + (y - C_y)^2 + (z - C_z)^2 = r^2$$

Redefining the implicit form of sphere.

$$\rightarrow (\mathbf{P} - \mathbf{C}) \cdot (\mathbf{P} - \mathbf{C}) = r^2$$

A point  $\mathbf{P}$  on sphere with Center  $\mathbf{C}$

$$((\mathbf{A} + t\mathbf{b}) - \mathbf{C}) \cdot ((\mathbf{A} + t\mathbf{b}) - \mathbf{C}) = r^2$$

$$t^2\mathbf{b} \cdot \mathbf{b} + 2t\mathbf{b} \cdot (\mathbf{A} - \mathbf{C}) + (\mathbf{A} - \mathbf{C}) \cdot (\mathbf{A} - \mathbf{C}) - r^2 = 0$$

Look familiar ?

Quadratic solution :

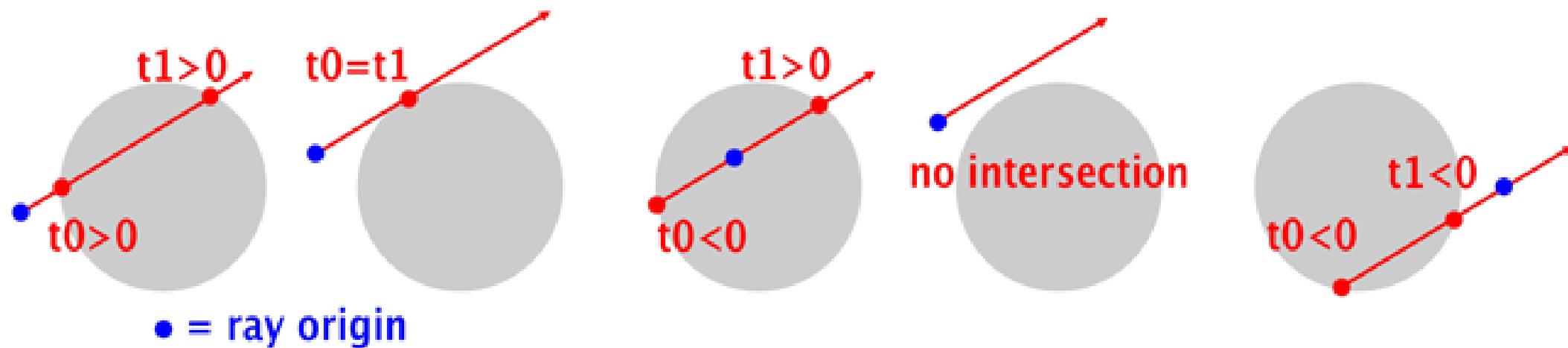
$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$a = \mathbf{b} \cdot \mathbf{b}$$

$$b = 2\mathbf{b} \cdot (\mathbf{A} - \mathbf{C})$$

$$c = (\mathbf{A} - \mathbf{C}) \cdot (\mathbf{A} - \mathbf{C}) - r^2$$

# Roots of the ray-sphere intersection



# Quadrilateral

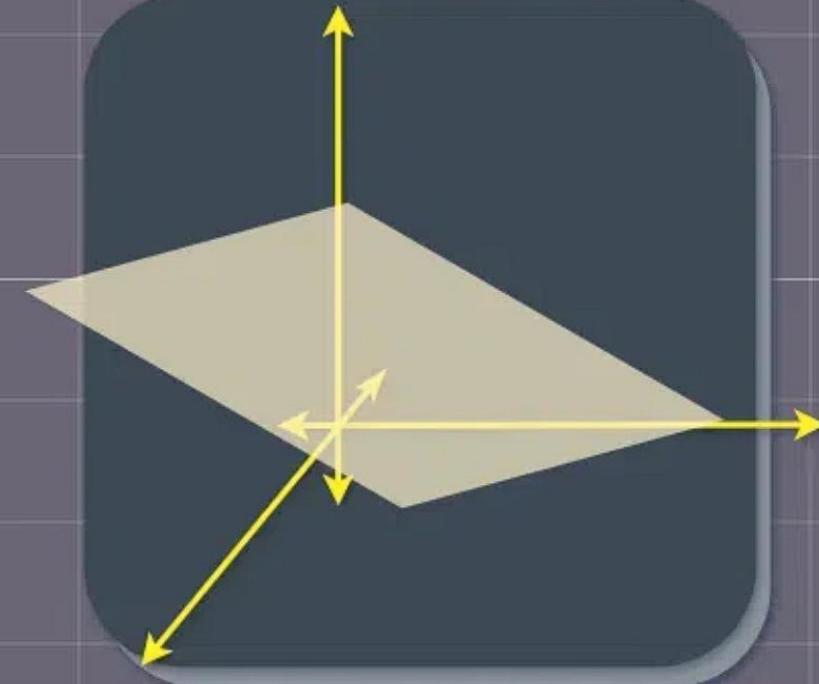
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- Definition
  - A quadrilateral, sometimes also known as a tetragon or quadrangle is a **four-sided polygon**. If not explicitly stated, all four polygon vertices are generally taken to lie in a plane. (If the points do not lie in a plane, the quadrilateral is called a skew quadrilateral.)
- Implicit form of a plane

$$Ax + By + Cz = D$$

# Quadrilateral (Plane) representations

# Equation of Plane



**General Form:**  $Ax + By + Cz + D = 0$

**Point-Normal Form:**  $\vec{n} \cdot (\vec{r} - \vec{r}_0) = 0$

**Intercept Form:**  $\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1$

**Vector Form:**  $\vec{r} = \vec{r}_0 + s\vec{v} + t\vec{w}$

# Ray-plane intersection

$$Ax + By + Cz = D$$

Given  $\mathbf{n}$  is the normal perpendicular to the plane.  
And  $\mathbf{v}$  is any point lying on the plane.



$$\mathbf{n} \cdot \mathbf{v} = D$$

$$\mathbf{n} \cdot (\mathbf{P} + t\mathbf{d}) = D$$

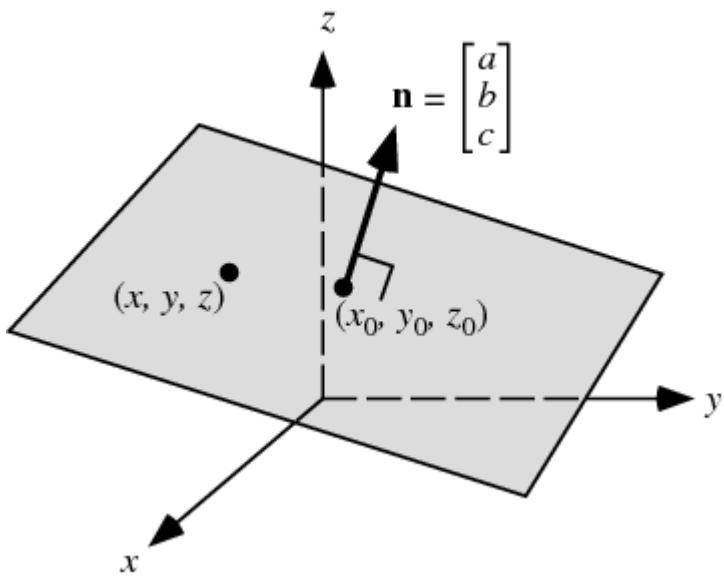
Substitute ray  
equation



$$\mathbf{n} \cdot \mathbf{P} + \mathbf{n} \cdot t\mathbf{d} = D$$

$$\mathbf{n} \cdot \mathbf{P} + t(\mathbf{n} \cdot \mathbf{d}) = D$$

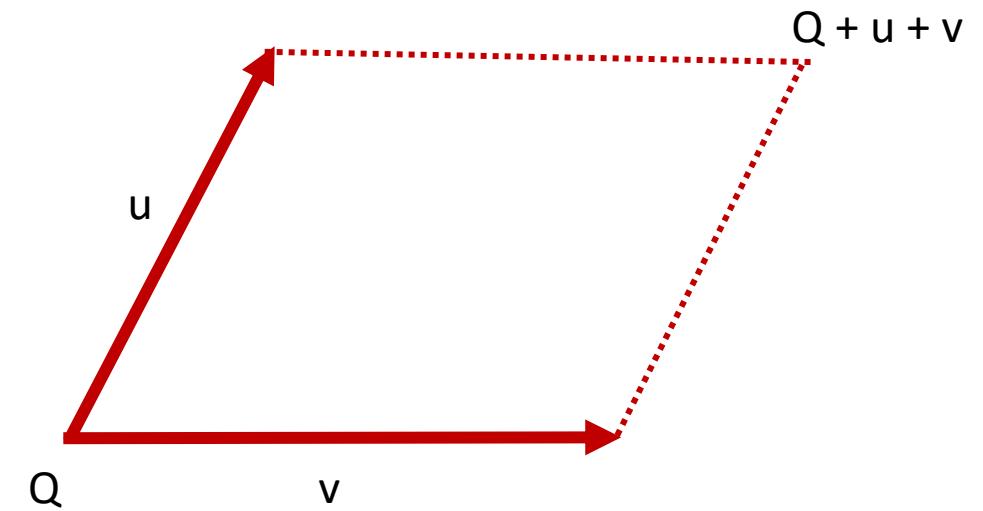
$$t = \frac{D - \mathbf{n} \cdot \mathbf{P}}{\mathbf{n} \cdot \mathbf{d}}$$



Solution where any parametric ray intersects the plane.

# Defining a quad

- $Q$  = a corner of the quad
- $u, v$  are vectors forming two sides of the quad



# Substituting values

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$$\mathbf{n} \cdot \mathbf{P} + \mathbf{n} \cdot t\mathbf{d} = D$$

What is  $\mathbf{n}$  (normal) ?



$$\mathbf{n} \cdot \mathbf{P} + t(\mathbf{n} \cdot \mathbf{d}) = D$$

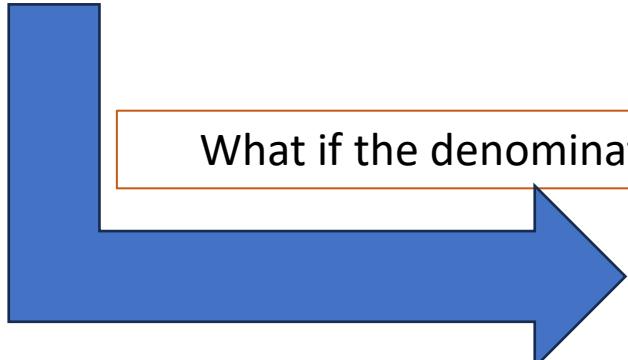
$$t = \frac{D - \mathbf{n} \cdot \mathbf{P}}{\mathbf{n} \cdot \mathbf{d}}$$

$$\mathbf{n} = \text{unit\_vector}(\mathbf{u} \times \mathbf{v})$$

$$\begin{aligned} D &= n_x Q_x + n_y Q_y + n_z Q_z \\ &= \mathbf{n} \cdot \mathbf{Q} \end{aligned}$$

What is D ?

What if the denominator is zero ?



Division by zero is undefined. That means the ray is parallel to the plane.

# Quad class

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## Attributes

- A point at a corner
- Vectors representing two sides from the defined corner
- Material
- Normal of the quad

## Methods

- Add material
- intersect()

# What is the ray-quad intersection solution ?

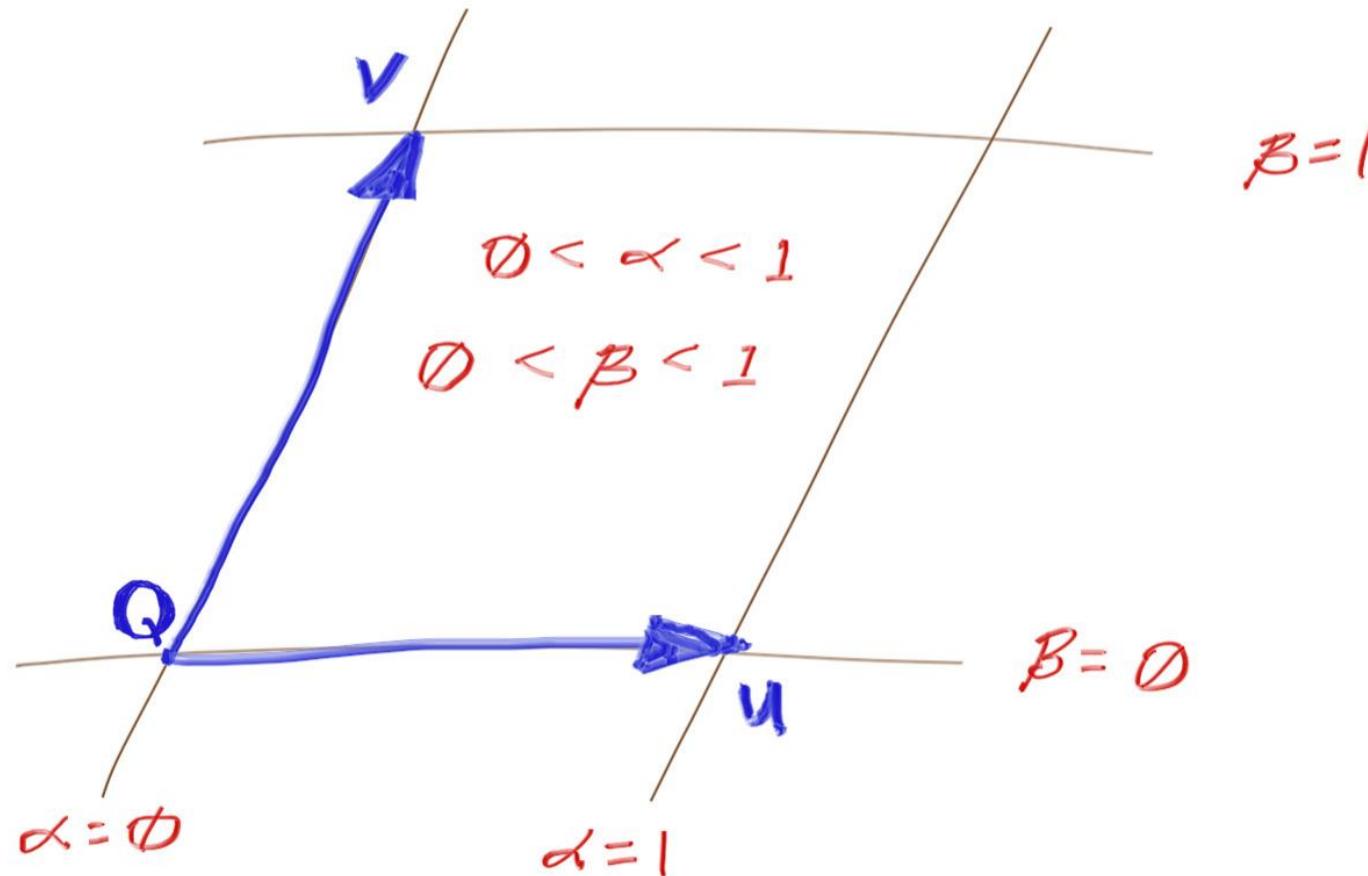
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- Adding a constraint to the solution.
- A quad can be defined by adding boundaries of the plane.
- One simple constraint is as follows.

$$\mathbf{P} = \mathbf{Q} + \alpha\mathbf{u} + \beta\mathbf{v}$$

How do alpha and beta parameters have impacts to the quad constraint ?

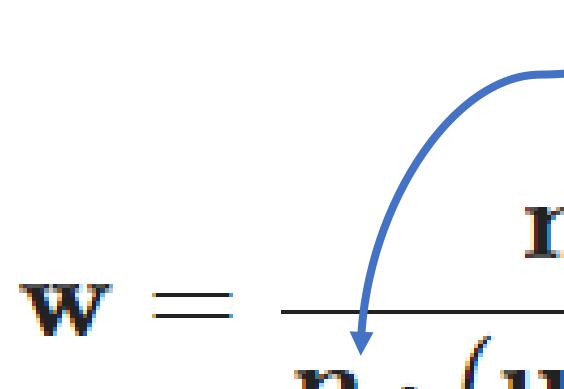
# Illustration of the constraint



# Calculating alpha and beta parameters

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These normal are  $U \times V$ .

$$\mathbf{w} = \frac{\mathbf{n}}{\mathbf{n} \cdot (\mathbf{u} \times \mathbf{v})} = \frac{\mathbf{n}}{\mathbf{n} \cdot \mathbf{n}}$$

$$\alpha = \mathbf{w} \cdot (\mathbf{p} \times \mathbf{v})$$
$$\beta = \mathbf{w} \cdot (\mathbf{u} \times \mathbf{p})$$

# Codes and class assignment !

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- Github : RT-python-week04
  - <https://github.com/KUGA-01418283-Raytracing/RT-python-week04>

