

Assignment 10

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Download codes from

<https://github.com/KUSUMAPRIYAPULAVARTY/assignment10>

Similarly, considering j^{th} column of \mathbf{C}

$$\gamma_j = \begin{pmatrix} \alpha_1 & \alpha_2 & \dots & \alpha_n \end{pmatrix} \begin{pmatrix} B_{1j} \\ B_{2j} \\ \vdots \\ B_{nj} \end{pmatrix} \quad (2.0.10)$$

$$= B_{1j}\alpha_1 + B_{2j}\alpha_2 + \dots + B_{nj}\alpha_n \quad (2.0.11)$$

$$\implies \gamma_j = \sum_{r=1}^n B_{rj}\alpha_r \quad (2.0.12)$$

which proves that columns of \mathbf{C} are linear combinations of columns of \mathbf{A}

1 QUESTION

Let \mathbf{A} be an $m \times n$ matrix and \mathbf{B} be an $n \times k$ matrix. Show that the columns of $\mathbf{C} = \mathbf{AB}$ are linear combinations of columns of \mathbf{A} . If $\alpha_1, \alpha_2, \dots, \alpha_n$ are the columns of \mathbf{A} and $\gamma_1, \gamma_2, \dots, \gamma_k$ are the columns of \mathbf{C} then,

$$\gamma_j = \sum_{r=1}^n B_{rj}\alpha_r \quad (1.0.1)$$

2 SOLUTION

$$\mathbf{C} = \mathbf{AB} \quad (2.0.1)$$

$$\mathbf{C} = \begin{pmatrix} \gamma_1 & \gamma_2 & \dots & \gamma_k \end{pmatrix} \quad (2.0.2)$$

$$\mathbf{A} = \begin{pmatrix} \alpha_1 & \alpha_2 & \dots & \alpha_n \end{pmatrix} \quad (2.0.3)$$

$$\mathbf{B} = \begin{pmatrix} \beta_1 & \beta_2 & \dots & \beta_k \end{pmatrix} \quad (2.0.4)$$

$$= \begin{pmatrix} B_{11} & B_{12} & \dots & B_{1k} \\ B_{21} & B_{22} & \dots & B_{2k} \\ \vdots & \vdots & \dots & \vdots \\ B_{n1} & B_{n2} & \dots & B_{nk} \end{pmatrix} \quad (2.0.5)$$

By matrix multiplication, we can write

$$\begin{pmatrix} \gamma_1 & \gamma_2 & \dots & \gamma_k \end{pmatrix} = \begin{pmatrix} \mathbf{A}\beta_1 & \mathbf{A}\beta_2 & \dots & \mathbf{A}\beta_k \end{pmatrix} \quad (2.0.6)$$

Consider γ_1

$$\gamma_1 = \mathbf{A}\beta_1 \quad (2.0.7)$$

$$= \begin{pmatrix} \alpha_1 & \alpha_2 & \dots & \alpha_n \end{pmatrix} \begin{pmatrix} B_{11} \\ B_{21} \\ \vdots \\ B_{n1} \end{pmatrix} \quad (2.0.8)$$

$$= B_{11}\alpha_1 + B_{21}\alpha_2 + \dots + B_{n1}\alpha_n \quad (2.0.9)$$