Natural Language Processing Lecture V. N-gram Language Models and TF-IDF

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Outline

Why language models

Language models

n-gram models

Smoothing and Discounting

Naïve Bayes spam filter

For many applications, the output is a sequence of words.

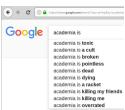
Example 1: Machine translation (MT):

Sprechen Sie MATLAB? \Rightarrow Do you speak MATLAB?

Example 2: Automatic Speech Recognition (ASR):

 $\gamma \sim 10^{-10} M_{\odot} \sim$

Example 3: Spell checking or spell suggestion



- ► The system needs to evaluate/rank a set of candidates, e.g., "\$2M seed from Sequoia?" over "\$2M seed from DFJ!"
- An easy way is to compute the likelihood that a candidate is a "making-sense" sentence.

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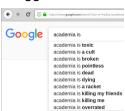
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Ranking candidate text strings

- For example, we can compute a probability for each string below:
- S1: "Please CALL me in 10 minutes."
- S2: "Please ALL me in 10 minutes."
- ▶ Which one is bigger? $P(S_1)$ or $P(S_2)$?

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 - In the example above, the system will compare the probabilities $P(w_1 = \text{``$2M"}, w_2 = \text{``seed"}, w_3 = \text{``from"}, w_3 = \text{``Sequoia"})$ and
- ► By chain rule, we have

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- Let's generalize: $P(w_1, \dots, w_l) = \prod_{i=1}^l P(w_i|w_1, \dots, w_{i-1})$
- ► Use a shorter history (*n*-th order Markov property):

$$\prod_{i=1}^{l} P(w_i | w_1, \dots, w_{i-1}) \approx \prod_{i=1}^{l} P(w_i | w_{i-(n-1)}, \dots, w_{i-1})$$

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- ▶ When n = 1, 2 or 3, it's unigram, bi-gram or tri-gram respectively.
- Yes, unigram means no history but just the word itself. No order between words is considered.
- ► N-gram is one (simple but widely used) way to represent language models.



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The bag of words and the background words as seen in Gates building, CMU

- A bag-of-words (BOW) model is basically a uni-gram model: an orderless representation of a document.
- ► A common use of a BOW model is create feature vectors using the frequencies of words, i.e., term frequency.
- Background words are those of extreme high frequency. They are earlier called stop words.
- When many researchers use the term "bigram" or "trigram", they are actually talking about bag-of-double-words or bag-of-triple-words.
- ➤ See https: //en.wikipedia.org/wiki/Bag-of-words_model.
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- We may also add a gap between words.
- ▶ 1-degree Skip-grams from the sentence "I am a PhD student": ("I", "a"), ("am", "PhD"), ("a", "student").
- ► A language model using skip-gram:

$$P(w_i|w_{i-k},\ldots,w_{i-1}, w_{i+1},\ldots,w_{i+k})$$

- ► NOT THE CASE!
- ► Instead of estimating the probability giving the neighboring words, a skip-gram language model actually estimates the probabilities of neighboring words given a word:

$$\sum_{j \in [-k..-1] \cup [1..k]} \log P(w_{i+j}|w_i)$$

► The first equation is actually called Continues BOW (CBOW) model.



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 The first equation is actually called Continues BOW (CBOW) model



- We may also add a gap between words.
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Order of n-grams and interpolation

- ► Larger *n*: the string is specific but sparse, e.g., "academia is vicious" may not be in training data.
- ► Smaller *n*: dense but general, e.g., lots of "academia is" or maybe "is vicious"
- ► To balance, mix different orders by interpolation:

$$\lambda_3 P(w_i|w_{i-1}, w_{i-2}) + \lambda_2 P(w_i|w_{i-1}) + \lambda_1 P(w_i)$$

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- ► The problem is known as OOV (out of vocabulary)
- ▶ Lazy way: ignore them closed vocabulary.
- For uni-gram:

$$P_{\text{smoothed}}(w_i) = \lambda P_{\text{model}}(w_i) + (1 - \lambda) \frac{1}{N}$$

- * is the number of total vocabulary
- A is the probability that a word is known to the model (it can be take).
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- Observation: some words have more words following it while others have fewer.
- Make the smoothing depend on the context, i.e., λ is not the same for all words.
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Other language models

Other ways to estimate $P(w_1, ..., w_l)$ beyond n-gram:

- Exponential language models: maximum entropy language models, log-bilinear language models.
- neural language models: based on neural networks, embedding

- A classical application of the BOW model
- ► Two classes: Spam (S) vs ham (H, non-spam)
- Based on Bayes theorem, given one word w, the chances that a message is spam: $P(S|w) = \frac{P(S,w)}{P(w)} = \frac{P(w|S)P(S)}{P(w|H)P(H) + P(w|S)P(S)}$
- ▶ Usually we further assume that P(H) = P(S). Thus $P(S|w) = \frac{P(w|S)}{P(w|H) + P(w|S)}$. Takeaway: all you need is P(w|H) and P(w|S) which can be obtained via counting.
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- Given a search term, e.g., "matlab", and a bunch of documents, how to rank all documents that match the query?
- ▶ Intuition 1: If a document has lots occurences of "matlab" then the document is strongly about MATLAB.
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