JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD B.Tech II Year I Semester Examinations, May/June - 2019 MATHEMATICAL FOUNDATIONS OF COMPUTER SCIENCE (Common to CSE, IT)

Time: 3 Hours Max. Marks: 75

Note: This question paper contains two parts A and B.

Part A is compulsory which carries 25 marks. Answer all questions in Part A.

Part B consists of 5 Units. Answer any one full question from each unit. Each question carries 10 marks and may have a, b, c as sub questions.

PART-A

Find the negative of $p \rightarrow q$. 1.a) [2] Test the validity of the following argument b)

 $p \wedge r \rightarrow \neg q$, $\neg q \rightarrow r$: $p \wedge r \rightarrow r$ [3]

If $f(x) = x^2 - 6 = y$, then find $f^{-1}(y)$. [2]

If $f: G_1 \to G_2$ is a homorphism and $a \in G$ then prove that $[f(a)]^{-1} = f(a^{-1})$. d) [3]

How many 5 digit numbers are possible, which are greater than 40000 with the digits e) 1, 2, 3, 4, 5. [2]

Find the number of positive integer solutions of x + y + z = 12. f) [3]

Solve the recurrence relation $u_{n+2} - u_{n+1} - 6u_n = 0$. g) [2]

Find the generating function of the sequence $1, 3, 3^2, 3^3$ h) [3]

If the adjacency matrix of the Graph is then draw the graph. i) [2] 0

If G is a k regular graph with 18 edges and the order of the graph is 9. Find the value of k. **i**) [3]

PART - B

(50 Marks)

(25 Marks)

2.a) Test the validity of the following argument.

If I study, I will not fail in the examination.

If I do not watch TV in the evenings, I will study.

I failed in the examination.

Therefore I must watch TV in the evenings.

b) Prove that the following argument is valid.

$$\neg \exists x (p(x) \land q(x))$$

p(a)

9/1/ $\therefore \neg q(a)$ [5+5]

- 3.a) Prove that $(p \uparrow q) \rightarrow r$ and $(p \land q) \lor r$ are logically equivalent.
 - b) Prove that the following argument is valid.

$$\forall x p(x) \rightarrow \neg q(x)$$

$$\neg \exists x ((r(x) \lor s(x)) \land \neg q(x))$$

r(a)

$$p(a)$$
 [5+5]

- 4.a) Let $X = \{1,2,3\}$ and f, g, h and s be functions from X to X given by $f = \{(1,2), (2,3), (3,1)\}$, $g = \{(1,2), (2,1), (3,3)\}$ h= $\{(1,1), (2,2), (3,1)\}$ Find fog, folog.
 - b) If $f: G_1 \to G_2$ is an isomorphism, then prove that $f^{-1}: G_2 \to G_1$ is also an isomorphism. [5+5]

OR

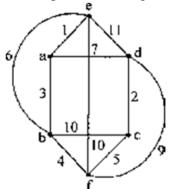
[5+5]

9/1/

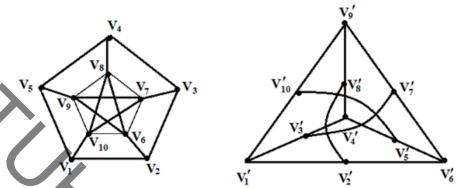
- 5.a) Prove that the relation a congruent to b mood H is an equivalence relation.
 - b) Prove that the set of even integers forms a group under addition.
- 6.a) Find the number of solutions of $x_1+x_2+x_3=19$ with the condition $x_1>1, x_2>2, x_3>1$.
 - b) Prove that if 11 integers are selected from among $\{1, 2, ... 20\}$, then the selection includes integer a and b such that a b = 2. [5+5]

OR

- 7.a) Find the number of integers < 250 and divisible by 3 or 5 or 11.
 - b) Suppose 14 students in a class appear at a university examination. Prove that there exists at least two among them whose seat number differ by a multiple of 13. [5+5]
- 8. Solve the recurrence relation. $u_n 2u_{n-1} 3u_{n-2} = 5^n$, $n \ge 2$, $u_0 = 1$, $u_1 = 1$ [10]
- 9. Solve the recurrence relation using generating function. $u_{n+2} 2u_{n+1} + u_n = 2^n$, $u_0 = 2$, $u_1 = 1$. [10]
- 10.a) Suppose that G is a non directed graph with 12 edges. Suppose that G has 6 vertices of degree 3 and the rest have degree less than 3. Determine the minimum number of vertices G can have.
 - b) Find the minimal spanning tree using Krushal's algorithm.



Show that the following graphs are isomorphic.



Prove that a graph G with at least one edge is 2-chromatic if and only if G has no cycle of odd length.

