Code No: 153CF

JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD B. Tech II Year I Semester Examinations, March - 2022 DISCRETE MATHEMATICS

(Common to CSE(AIML), CSE(DS), CSE(IOT))

Time: 3 Hours

Max. Marks: 75

Answer any five questions All questions carry equal marks

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- 1. Obtain the PDNF and PCNF of the following statement formula: $(P V Q) \rightarrow (P \leftrightarrow Q)$. [15]
- 2.a) Show that $(\exists x) (p(x) \land (Q(x) \Rightarrow (\exists x) (p(x) \land \exists (x) Q(x)).$
 - b) Symbolize the following argument and check for its validity:

All men are giants.

Not all birds can fly.

Some babies are illogical

There is a student who likes maths, but not history.

[7+8]

- 3.a) Use a Venn diagram to illustrate the relationships $A \subset B$ and $A \subset C$.
 - b) Prove that the relation "congruence modulom" given by $R=\{\langle x,y \rangle / x-y \text{ is divisible by m} \}$ over

the set of positive integers is an equivalence relation.

[6+9]

- 4.a) Give the definition and examples of reflexive symmetric, anti symmetric and transitive relations.
 - b) What is meant by Poset? Draw the Hasse diagram for the Poset. <{2,4,5,10,12,20,25}/> and compute LUB and GLB.

[7+8]

- 5.a) Conjecture a formula for the sum of the first *n* positive odd integers. Then prove your Conjecture using mathematical induction.
 - b) Express the linear search algorithm as a recursive procedure and explain. [8+7]
- 6.a) Prove that 2 divides n^2+n whenever n is a positive integer, using mathematical induction.
 - b) Give a recursive algorithm to compute the factorial of a number and explain. [8+7]
- 7. Solve the recurrence relation $a_n-7a_{n-1}+10a_{n-2}=0$ where $a_0=10$ and $a_1=41$. [15]
- 8.a) Find the degree sequence of k_4 graph.
 - b) What are the various ways of representing graphs? Explain them briefly with relevant examples. [6+9]