

Code No: 123BN

JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD**B.Tech II Year I Semester Examinations, April/May - 2018****MATHEMATICAL FOUNDATIONS OF COMPUTER SCIENCE****(Common to CSE, IT)****Time: 3 Hours****Max. Marks: 75****Note:** This question paper contains two parts A and B.

Part A is compulsory which carries 25 marks. Answer all questions in Part A.

Part B consists of 5 Units. Answer any one full question from each unit.

Each question carries 10 marks and may have a, b, c as sub questions.

PART- A**(25 Marks)**

- 1.a) Find the negations of the following quantified statements:

$$\forall x, \exists y, [(p(x, y) \wedge q(x, y)) \wedge r(x, y)] \quad [2]$$

- b) Construct a truth table to show that
- $(p \wedge q) \rightarrow p$
- is a tautology. [3]

- c) Let
- $X = \{1, 2, 3, 4, 5, 6\}$
- and
- R
- be a relation defined as
- $(x, y) \in R$
- if and only if
- $x - y$
- is divisible by 3. Find the elements of relation of
- R
- . [2]

- d) If 'a' is a generator of a cyclic group
- G
- , then show that
- a^{-1}
- is also a generator of
- G
- . [3]

- e) Find how many different words that can be formed with the letters in the word "MATHEMATICS"? [2]

- f) What is pigeon hole principle? [3]

- g) What is homogeneous recurrence relation? [2]

- h) Find the number of non-negative integer solutions of the equation
- $x_1 + x_2 + x_3 = 11$
- . [3]

- i) What is chromatic numbers? [2]

- j) Define Euler's circuit and Give an example. [3]

PART-B**(50 Marks)**

- 2.a) Verify the validity of the following arguments.

"Every living thing is a plant or an animal.

Logu's dog is alive and it is not a plant.

All animals have heart. Therefore Logu's dog has a heart."

- b) Find the formulas in Disjunctive Normal Form equivalent to the following well formed formulas

$$(\neg R) \rightarrow (((P \vee Q) \rightarrow R) \rightarrow \neg Q) \quad [5+5]$$

OR

3. Without using truth tables prove that

$$((P \vee Q) \wedge (\neg P \wedge (\neg Q \vee \neg R))) \vee (\neg P \wedge Q) \vee (\neg Q \wedge \neg R) \text{ is a tautology.} \quad [10]$$

4.a) Let $A = \{a, b, c\}$ be a set and relation R on A is as $= \{(a, a), (a, b), (b, c), (c, c)\}$. Is R.
i) Reflexive ii) Symmetric iii) Transitive.

b) Prove that $f^{-1} \circ g^{-1} = (g \circ f)^{-1}$, where $f : Q \rightarrow Q$ such that $f(x) = 2x$ and $g : Q \rightarrow Q$
Such that $g(x) = x + 2$ are two functions. [5+5]

OR

5.a) Prove that the intersection of any two subgroups of a group G is again subgroup of G.

b) In a lattice (L, \leq, \wedge, \vee) state and prove the laws idempotent, commutative, association and absorption. [5+5]

6.a) Find the number of integers between 1 and 250 that are divisible by any of the integers 2, 3 and 6.

b) Find the coefficient of $x^9 y^3$ in the expansion of $(2x - 3y)^{12}$. [5+5]

OR

7.a) How many bit strings of length 10 contain:

i) At most four 1's ii) At least four 1's iii) Exactly four 1's.

b) There are 40 computer programmers for a job. 25 know Java, 28 know Oracle and 7 know neither language. Using principle of inclusion exclusion find how many know both languages. [5+5]

8.a) Find a generating function for the recurrence relation

$$a_n - a_{n-1} + 6a_{n-2} = 0 \text{ for } n \geq 2$$

b) Express Fibonacci sequence of numbers 1, 1, 2, 3, 5, 8, 13, 21, 34,... in terms of general expression for the r^{th} number a_r and generating function. [5+5]

OR

9.a) Find the number of integer solutions of the equation

$$x_1 + x_2 + x_3 + x_4 + x_5 = 30$$

Under the constraints $x_i \geq 0$ for all $i = 1, 2, 3, 4, 5$ and further x_2 is even and x_3 is odd.

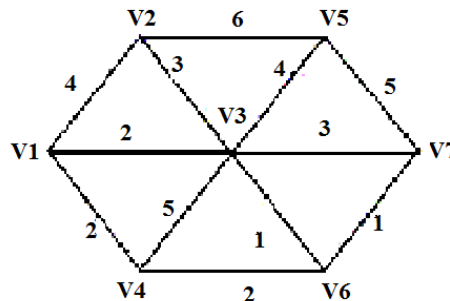
b) Solve the recurrence relation $a_n - 6a_{n-1} + 9a_{n-2} = 0$ for $n \geq 2$. [5+5]

10.a) Show that a simple complete digraph with n nodes has the maximum number of edges $n(n-1)$. Assuming that there are no loops.

b) State and explain graph coloring problem. Give its applications. [5+5]

OR

11.a) Find the minimum spanning tree by using kruskal's algorithm.



b) Write short notes on DFS and BFS. [5+5]