# Math Notes

## K

## March 6, 2020

## Contents

| 1 | Table of Integrals                   | 2 |
|---|--------------------------------------|---|
|   |                                      | 2 |
|   | 1.2 Trigonometric Integrals          | 2 |
| 2 | Exponential and Logarithms Integrals | 3 |
| 3 | Hyperbolic Integrals                 | 4 |
| 4 | Additional Resources                 | 5 |

### 1 Table of Integrals

### 1.1 Basic Integrals

1. 
$$\int u^n du = \frac{u^{n+1}}{n+1} + C, n \neq -1$$

$$2. \int \frac{du}{u} = \ln|u| + C$$

$$3. \int e^u du = e^u + C$$

$$4. \int a^u du = \frac{a^u}{\ln a} + C$$

5. 
$$\int \sin u du = -\cos u + C$$

6. 
$$\int \cos u du = \sin u + C$$

7. 
$$\int \sec^2 u du = \tan u + C$$

8. 
$$\int \csc^2 u du = -\cot u + C$$

9. 
$$\int \sec u \tan u du = \sec u + C$$

10. 
$$\int \csc u \cot u du = -\csc u + C$$

11. 
$$\int \tan u du = \ln|\sec u| + C$$

12. 
$$\int \cot u du = \ln|\sin u| + C$$

13. 
$$\int \sec u du = \ln|\sec u + \tan u| + C$$

14. 
$$\int \csc u du = \ln|\csc u + \cot u| + C$$

15. 
$$\int \frac{du}{\sqrt{a^2 - u^2}} = \sin^{-1} \frac{u}{a} + C$$

16. 
$$\frac{du}{a^2+u^2} = \frac{1}{a} \tan^{-1} \frac{u}{a} + C$$

17. 
$$\int \frac{du}{u\sqrt{u^2-a^2}} = \frac{1}{a}\sec^{-1}\frac{u}{a} + C$$

### 1.2 Trigonometric Integrals

1. 
$$\int \sin^2 u du = \frac{1}{2}u - \frac{1}{4}\sin 2u + C$$

2. 
$$\int \cos^2 u du = \frac{1}{2}u + \frac{1}{4}\sin 2u + C$$

3. 
$$\int \tan^2 u du = \tan u - u + C$$

4. 
$$\int \cot^2 u du = -\cot u - u + C$$

5. 
$$\int \sin^3 u \, du = -\frac{1}{3} (2 + \sin^2 u) \cos u + C$$

6. 
$$\int \cos^3 u du = \frac{1}{3}(2 + \cos^2 u)\sin u + C$$

7. 
$$\int \tan^3 u du = \frac{1}{2} \tan^2 u \ln|\cos u| + C$$

8. 
$$\int \cot^3 u du = -\frac{1}{2} \cot^2 u - \ln|\sin u| + C$$

9. 
$$\int \sec^3 u du = \frac{1}{2} \sec u \tan u + \frac{1}{2} \ln|\sec u + \tan u| + C$$

10. 
$$\int \csc^3 u du = -\frac{1}{2} \sec u \cot u + \frac{1}{2} \ln|\csc u - \cot u| + C$$

11. 
$$\int \sin^n u du = -\frac{1}{n} \sin^{n-1} u \cos u + \frac{n-1}{n} \int \sin^{n-2} u du$$

12. 
$$\int \cos^n u du = \frac{1}{n} \cos^{n-1} u \sin u + \frac{n-1}{n} \int \cos^{n-2} u du$$

13. 
$$\int \tan^n u du = \frac{1}{n-1} \tan^{n-1} u - \int \tan^{n-2} u du$$

14. 
$$\int \cot^n u du = \frac{-1}{n-1} \cot^{n-1} u - \int \cot^{n-2} u du$$

15. 
$$\int \sec^n u du = \frac{1}{n-1} \tan u \sec^{n-2} u + \frac{n-2}{n-1} \int \sec^{n-2} u du$$

16. 
$$\int \csc^n u du = \frac{-1}{n-1} \cot u \csc^{n-2} u + \frac{n-2}{n-1} \int \csc^{n-2} u du$$

17. 
$$\int \sin au \cos bu du = \frac{\sin(a-b)u}{2(a-b)} - \frac{\sin(a+b)u}{2(a+b)} + C$$

18. 
$$\int \cos au \cos bu du = \frac{\sin(a-b)u}{2(a-b)} + \frac{\sin(a+b)u}{2(a+b)} + C$$

19. 
$$\int \sin au \cos bu du = \frac{\sin(a-b)u}{2(a-b)} + \frac{\cos(a+b)u}{2(a+b)} + C$$

20. 
$$\int u \sin u du = \sin u - u \cos u + C$$

21. 
$$\int u \cos u du = \cos u + u \sin u + C$$

22. 
$$\int u^n \sin u du = -u^n \cos u + n \int u^{n-1} \cos u du$$

23. 
$$\int u^n \cos u du = u^n \sin u - n \int u^{n-1} \sin u du$$

24. 
$$\int \sin^n u \cos^m u du = -\frac{\sin^{n-1} u \cos^{m+1} u}{n+m} + \frac{n-1}{n+m} \int \sin^{n-2} u \cos^m u du$$
$$= \frac{\sin^{n+1} u \cos^{m-1} u}{n+m} + \frac{m-1}{n+m} \int \sin^n u \cos^{m-2} u du$$

### 2 Exponential and Logarithms Integrals

1. 
$$\int ue^{au}du = \frac{1}{a^2}(au - 1)e^{au} + C$$

2. 
$$\int u^n e^{au} du = \frac{1}{a} u^n e^{au} - \frac{n}{a} \int u^{n-1} e^{au} du$$

3. 
$$\int e^{au} \sin bu du = \frac{e^{au}}{a^2 + a^b} (a \sin bu - b \cos bu) + C$$

4. 
$$\int e^{au}\cos bu du = \frac{e^{au}}{a^2 + b^2}(a\cos bu + b\sin bu) + C$$

5. 
$$\int \ln u du = u \ln u - u + C$$

6. 
$$\int u^n \ln u du = \frac{u^{n+1}}{(n+1)^2} [(n+1) \ln u - 1] + C$$

$$7. \int \frac{1}{u \ln u} du = \ln |\ln u| + C$$

# 3 Hyperbolic Integrals

1. ∫

#### 4 Additional Resources

#### Print

Calculus Study Guide: https://mt-jfk.com/ap-calculus-study-guide.pdf

#### Video

The Organic Chemistry Tutor: https://www.youtube.com/channel/UCEWpbFLzoYGPfuWUMFPSaoA

Black Pen Red Pen: https://www.youtube.com/user/blackpenredpen

Khan Academy: https://www.youtube.com/c/khanacademy

#### Websites

 $Khan\ Academy\ -\ AP/College\ Calculus\ BC: \ \texttt{https://www.khanacademy.org/math/ap-calculus-bc}$