Equation Sheet 202A (Physics) 1

1.
$$v_f = v_0 + at$$

2.
$$x_f = x_0 + (v_0)t + \frac{1}{2}at^2$$

3.
$$v_f^2 = v_0^2 + 2a(\Delta x)$$
 where $\Delta x = x_f - x_0$

$$x_0$$
 = initial displacement

$$x_f = \text{final displacement}$$

$$v_0$$
 = inital velocity

$$v_f = \text{final velocity}$$

$$a = acceleration$$

$$t = \text{time interval for initial } \& \text{ final positions}$$

4. velocity
$$(v) = \frac{\Delta x}{\Delta t}$$

$$\Delta x = \text{displacement change}$$

$$\Delta t = \text{time interval}$$

5.
$$acceleration(a) = \frac{\Delta v}{\Delta t} \Delta v = velocitychange \Delta t = timeinterval$$

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Equation of straight line:

$$y = mx + b$$

$$b = y$$
-intercept

$$m = slope = \frac{\Delta x}{\Delta y}$$

1. Trigonometric Cheet-Sheet

$$h = \text{hypotenuse}$$

$$p = opposite$$

$$b = adjacent$$

(a)
$$\sin \theta = \frac{p}{h}$$

(b)
$$\cos \theta = \frac{b}{h}$$

(c)
$$\tan \theta = \frac{p}{h}$$

(d)
$$h^2 = p^2 + b^2$$

(e)
$$\sin^2 \theta + \cos^2 \theta = 1$$

(f)
$$180^{\circ} = \pi \cdot radian$$

2. Area of triangle =
$$\frac{1}{2} \cdot base \cdot height$$

3. Area of rectangle =
$$length \cdot width$$

 $Perimeter = 2(length + width)$

$$ax^{2} + bx + c = 0$$

$$x = \frac{-b \pm \sqrt{b^{2} - 4ac}}{2a}$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

- 5. 12 inch = 1 foot
 - 3 foot = 1 yard
 - 1 mile = 1.61 km
 - 1 km = 1000 m
 - 100 cm = 1 m
 - 10 mm = 1 cm
 - 1 hr = 3600 sec
 - 1 inch = 2.54 cm
- 6. x-component of \overrightarrow{A} :
 - $A_x = A\cos\theta$ y-component of \overrightarrow{A} :
 - $A_y = A\sin\theta$

 - $A_x^{2} + A_x^{2} = A^{2}$ $\tan \theta = \frac{A_y}{A_x}, \sin \theta = \frac{A_y}{A}, \cos \theta = \frac{A_x}{A}$
- 7. Acceleration due to gravity (g)
 - $g = 9.8m/s^2 = 10m/s^2$
- 8. Weight of mass m'
 - = mg =force of Earth on mass $(\overrightarrow{F}_{E \text{ on o}})$
- 9. $\mu_{max} = \frac{f_{s,max}}{F^{\perp}}$ $F^{\perp} = \text{normal force}$

 - $f_{s,max} = \text{limiting static friction}$
 - $\mu_{s,max}$ = coefficient of limiting static friction
- 10. $\mu_k = \frac{f_k}{F^{\perp}}$
 - $f_k = \text{kinetic friction}$
 - $\mu_k = \text{coefficient of kinetic friction}$
- 11. If the net force acting on an object is zero,

 - $\sum F_x = 0$ (net force along x-axis) $\sum F_y = 0$ (net force along y-axis)
- 12. Newton's 2^{nd} law of motion $a = \frac{\sum F}{m}$

 - m = mass
 - a = acceleration
 - $\sum F = \text{net force}$
- 13. For a projectile motion:
 - $a_x = 0$ (acceleration along the x-axis)
 - $a_y = -g(\text{acceleration along y-axis})$
 - If 'upward' is considered as 'positive' and 'downward' is considered as 'negative'.
- 14. Newton's 3^{rd} law of Motion

 - \overrightarrow{F}_{12} = force exerted by object 2 on object 1 \overrightarrow{F}_{21} = force exerted by object 1 on object 2

15. Circular Motion

- (a) Angular Velocity(ω) = $\frac{\Delta\theta}{\Delta t} = \frac{3\pi}{T}$ rad/s (T = time period)
- (b) frequency (f) = $\frac{1}{T}$
- (c) $v = r\omega$ r = radiusv = velocity
- (d) circumference of a circle = $2\pi r$
- (e) centripetal acceleration $(a_c) = \frac{v^2}{r}$
- (f) centripetal force $(F_c) = ma_c = \frac{mv^2}{r}$

16. Static Equilibrium

- (a) $\sum F = 0 \Rightarrow \sum F_x = 0$ (net force along x-axis) $\sum F_y = 0$ (net force along the y-axis)
- (b) Torque = $Fd \sin \theta$ F = force d = distance $\theta = \text{angle between } \overrightarrow{F} \& \overrightarrow{d}$

17. (a) linear momentum $(\overrightarrow{p}) = mass \cdot velocity$ = $m\overrightarrow{v}$

- (b) Impulse = $force \cdot time interval$ = $\overrightarrow{F}(\Delta t)$ = $m\overrightarrow{v}_f - m\overrightarrow{v}_0$ $\overrightarrow{v}_f = \text{final velocity}$ $\overrightarrow{v}_0 = \text{initial velocity}$
- (c) conservation of linear momentum $m_1v_{0,1} + m_2v_{0,2} = m_1v_{f,1} + m_2v_{f,2}$ $v_{0,1} = \text{Inital Velocity of mass } m_1$ $v_{0,2} = \text{Initial velocity of mass } m_2$ $v_{f,1} = \text{Final velocity of mass } m_1$ $v_{f,2} = \text{Final Velocity of mass } v_2$ $\sum_{initial} mv = \sum_{final} mv$
- (d) Momentum-impulse relation $I = p_f p_0$ $p_f = \text{final momentum}$ $p_0 = \text{Initial momentum}$

18. Work and Energy

(a) Work (w) = $Fd\cos\theta$ F = force d = displacement $\theta = \text{angle between } \overrightarrow{F} \& \overrightarrow{d}$

- (b) Kinetic Energy (K) = $\frac{1}{2}mv^2 = \frac{p^2}{2m}$ m = mass
 - v = velocity
 - p = mv = momentum
- (c) Gravitational potential energy $(U_q) = mgh$ m = mass
 - q = acceleration due to gravity
 - h = height from a reference level
- (d) power (P) = $\frac{Work}{time} = \frac{W}{t}$
- (e) Elastic potential energy $(v_e) = \frac{1}{2}kx^2$ k = spring constant (or force constant) x = extension (i.e., change in length)
- (f) Generalised work-energy principle
 - $K_0 + v_0 + W = K_f + v_f + \Delta v_{int}$
 - $K_0 = \text{Initial kinetic energy}$
 - $v_0 = \text{Initial potential energy}$
 - $K_f = \text{Final kinetic energy}$
 - $v_f = \text{Final potential energy}$
 - W = Work done by external force
 - $\Delta v_{int} = \text{change in internal energy}$
- (g) Hooke's law

 - $\overrightarrow{F_s} = -K\overrightarrow{x}$ $\overrightarrow{F_s} = \text{force due to spring}$ $\overrightarrow{x} = \text{extension or change in length}$
 - K =Spring constant or force constant
- 19. Total energy of a vibrating body (v)
 - $v = \frac{1}{2}mv^2 + \frac{1}{2}Kx^2$
 - (m = mass, v = velocity when displacement is x from equibrium position, K = Spring constant)
- 20. For simple pendulum,
 - $T=2\pi\sqrt{\frac{l}{a}}$
 - $(T = \text{time period}, l = \text{length of pendulum}, g = 9.81m/s^2)$
- 21. Angular velocity $(\omega) = \frac{\Delta \theta}{\Delta t} = \frac{2\pi}{T} = 2\pi f$ $(T = \text{Time period}, \Delta \theta = \text{angle in angle}, \Delta t = \text{time interval}, f = \text{frequency} = \frac{1}{T})$
- 22. Simple Harmonic motion:
 - $x = A\cos\omega t$
 - $=Acos(\frac{2\pi}{T}t)$
 - $(x = \text{displacement from equilibrium position}, A = \text{amplitude}, \omega = \text{angular velocity}, T =$ time period)

 $v = -v_{max}\sin\omega t$

$$v = -\omega A \sin \omega t$$

 $(v = \text{velocity at a time } t, v_{max} = \omega A = \text{maximum velocity})$

$$a = -a_{max}\cos\omega t$$

$$a = \omega^2 A \cos \omega t$$

$$a = -\omega^2 x$$

 $(a_{max} = \omega^2 A = \text{maximum acceleration}, a = \text{acceleration at time t})$

23.
$$T = 2\pi \sqrt{\frac{m}{K}}$$

(T = time period for horizontal/vertical spring-mass system, m = mass attached to the spring, K =spring constant)

24. Wave motion: $v: f\lambda$

$$(v = \text{velocity}, f = \text{frequency}, \lambda = \text{wavelength})$$

$$f = \frac{1}{T} (T = \text{time period})$$

25. waves in string fixed at both ends:

$$v = \sqrt{\frac{T}{\mu}}$$

 $(v = \text{velocity}, T = \text{tension}, \mu = mass/length)$

26. v = velocity of sound wave in air = 332m/s

27. Intensity of a wave (J)

$$I = \frac{P}{A}$$

 $I = \frac{P}{A}$ $P = \text{power emitted by source} = \frac{\Delta E}{\Delta t} = \text{energy emitted per unit time}$

$$A = \text{area} = 4\pi r^2$$

r = radius(with the source at the center)

28. Intensity level (β)

$$\beta = 10 \log_{10} \frac{J}{J_0}$$

I = Intensity at a point from the source of sound

 $I_0 = 10^{-2} W/m^2$ = reference intensity level