# presentation.sty: An Infrastructure for Presenting Semantic Macros in STFX\*

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#### Abstract

The presentation package is a central part of the STEX collection, a version of TEX/LATEX that allows to markup TEX/LATEX documents semantically without leaving the document format, essentially turning TEX/LATEX into a document format for mathematical knowledge management (MKM).

This package supplies an infrastructure that allows to specify the presentation of semantic macros, including preference-based bracket elision. This allows to markup the functional structure of mathematical formulae without having to lose high-quality human-oriented presentation in LATEX. Moreover, the notation definitions can be used by MKM systems for added-value services, either directly from the STEX sources, or after translation.

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#### 1 Introduction

The presentation package supplies an infrastructure that allows to specify the presentation of semantic macros, including preference-based bracket elision. This allows to markup the functional structure of mathematical formulae without having to lose high-quality human-oriented presentation in IATEX. Moreover, the notation definitions can be used by MKM systems for added-value services, either directly from the STEX sources, or after translation.

STEX is a version of TEX/LATEX that allows to markup TEX/LATEX documents semantically without leaving the document format, essentially turning TEX/LATEX into a document format for mathematical knowledge management (MKM).

The setup for semantic macros described in the STEX modules package works well for simple mathematical functions: we make use of the macro application syntax in TEX to express function application. For a simple function called "foo", we would just declare  $\sum_{foo}\{1]\{foo(\#1)\}$  and have the concise and intuitive syntax  $foo\{x\}$  for foo(x). But mathematical notation is much more varied and interesting than just this.

#### 2 The User Interface

In this package we will follow the STEX approach and assume that there are four basic types of mathematical expressions: symbols, variables, applications and binders. Presentation of the variables is relatively straightforward, so we will not concern ourselves with that. The application of functions in mathematics is mostly presented in the form  $f(a_1, \ldots, a_n)$ , where f is the function and the  $a_i$  are the arguments. However, many commonly-used functions from this presentational scheme: for instance binomial coefficients:  $\binom{n}{k}$ , pairs:  $\langle a, b \rangle$ , sets:  $\{x \in S \mid x^2 \neq 0\}$ , or even simple addition: 3+5+7. Note that in all these cases, the presentation is determined by the (functional) head of the expression, so we will bind the presentational infrastructure to the operator.

#### 2.1 Prefix & Postfix Notations

\prefix

The default notation for an object that is obtained by applying a function f to arguments  $a_1$  to  $a_n$  is  $f(a_1, \ldots, a_n)$ . The \prefix macro allows to specify a prefix presentation for a function (the usual presentation in mathematics). Note that it is better to specify \symdef{uminus}[1]{\prefix{-}{#1}} than just \symdef{uminus}[1]{-#1}, since we can specify the bracketing behavior in the former (see Section 2.4).

\postfix

The \postfix macro is similar, only that the function is presented after the argument as for e.g. the factorial function: 5! stands for the result of applying the factorial function to the number 5. Note that the function is still the first argument to the \postfix macro: we would specify the presentation for the factorial function with \symdef{factorial}[1]{\postfix{!}{#1}}.

\prefixa \postfixa

\prefix and \postfix have n-ary variants \prefixa and \postfixa that take

EdN:1

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an arbitrary number of arguments (mathematically; syntactically grouped into one  $T_{EX}$  argument). These take an extra separator argument.<sup>1</sup>

Note that in STEX the \prefix and \postfix macros should primarily be used in \symdef declarations. For marking up applications of symbolic functions in text we should use the \symdef-defined semantic macros direct. For applications of function variables we have two options:

i) direct prefix markup of the form f(x), where we have declared the symbol f to be a function via the function key of the enclosing environment — e.g. omtext (see [Koh15]).

\funapp

ii) using the \funapp macro as in \funapp{f}{x}, which leads to the same effect and is more general (e.g. for complex function variables, such as  $f'_1$ ). Note that the default prefix rendering of the function is sufficient here, since we can otherwise make use of a user-defined application operator.

#### 2.2 Mixfix Notations

For the presentation of more complex operators, we will follow the approach used by the Isabelle theorem prover. There, the presentation of an n-ary function (i.e. one that takes n arguments) is specified as  $\langle pre \rangle \langle arg_0 \rangle \langle mid_1 \rangle \cdots \langle mid_n \rangle \langle arg_n \rangle \langle post \rangle$ , where the  $\langle arg_i \rangle$  are the arguments and  $\langle pre \rangle$ ,  $\langle post \rangle$ , and the  $\langle mid_i \rangle$  are presentational material. For instance, in infix operators like the binary subset operator,  $\langle pre \rangle$  and  $\langle post \rangle$  are empty, and  $\langle mid_1 \rangle$  is  $\subseteq$ . For the ternary conditional operator in a programming language, we might have the presentation pattern if  $\langle arg_1 \rangle$ then  $\langle arg_2 \rangle$ else  $\langle arg_3 \rangle$ fi that utilizes all presentation positions.

\mixfix\*

The presentation package provides mixfix declaration macros  $\mbox{mixfixi}$ ,  $\mbox{mixfixi}$ i, and  $\mbox{mixfixii}$ i for unary, binary, and ternary functions. This covers most of the cases, larger arities would need a different argument pattern. The call pattern of these macros is just the presentation pattern above. In general, the mixfix declaration of arity i has 2n+1 arguments, where the even-numbered ones are for the arguments of the functions and the odd-numbered ones are for presentation material. For instance, to define a semantic macro for the subset relation and the conditional, we would use the markup in Figure 1.

\infix

For certain common cases, the presentation package provides shortcuts for the mixfix declarations. For instance, we provide the \infix macro for binary operators that are written between their arguments (see Figure 1).<sup>2</sup>

#### 2.3 *n*-ary Associative Operators

Take for instance the operator for set union: formally, it is a binary function on sets that is associative (i.e.  $(S_1 \cup S_2) \cup S_3 = S_1 \cup (S_2 \cup S_3)$ ), therefore the brackets are often elided, and we write  $S_1 \cup S_2 \cup S_3$  instead (once we have proven associativity). Some authors even go so far to introduce set union as a n-ary

 $<sup>^{1}\</sup>mathrm{EdNote}$ : think of a good example!

<sup>&</sup>lt;sup>1</sup>If you really need larger arities, contact the author!

<sup>&</sup>lt;sup>2</sup>EdNote: really?



**Example 1:** Declaration of mixfix operators

operator, i.e. a function that takes an arbitrary (positive) number of arguments. We will call such operators n-ary associative.

Specifying the presentation<sup>3</sup> of n-ary associative operators in \symdef forms is not straightforward, so we provide some infrastructure for that. As we cannot predict the number of arguments for n-ary operators, we have to give them all at once, if we want to maintain our use of TEX macro application to specify function application. So a semantic macro for an n-ary operator will be applied as \nunion{\langle a\_1 \rangle \ldots \langle a\_n \rangle \ldots \ldot

The \assoc macro is a convenient abbreviation of a \mixfixa that can be used in cases, where  $\langle pre \rangle$  and  $\langle post \rangle$  are empty (i.e. in the majority of cases). It takes two arguments: the presentation of a binary operator, and a commaseparated list of arguments, it replaces the commas in the second argument with the operator in the first one. For instance \assoc\cup{S\_1,S\_2,S\_3} will be formatted to  $S_1 \cup S_2 \cup S_3$ . Thus we can use \def\nunion#1{\assoc\cup{#1}} or even \def\nunion{\assoc\cup}, to define the n-ary operator for set union in TeX. For the definition of a semantic macro in STeX, we use the second form, since we are more conscious of the right number of arguments and would declare \symdef{nunion}[1]{\assoc\cup}#1}.

The \mixfixii macro has variants \mixfixia and \mixfixai which allow to make one or two arguments in a binary function associative. A use case for the

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\mixfixa

\assoc

\mixfixia

\mixfixai

EdN:4

 $<sup>^3{\</sup>rm EDNote}$ : introduce the notion of presentation above  $^4{\rm EDNote}$ : think about big operators for ACI functions

second macro is an nary function type operator \fntype, which can be defined via

 $\def\frac{1}{2}{mixfixai}{\#1}\rightarrow{\#2}{}\times$ 

and which will format \fntype{\alpha,\beta,\gamma}\delta as  $(\alpha \times \beta \times \gamma \rightarrow \delta)$ 

Finally, the \mixfixiii macro has the variants \mixfixaii, \mixfixiai, and \mixfixiia as above<sup>2</sup>. For instance we can use the first variant for a typing judgment using

which formats  $\typej{\Gamma, [x:\alpha], [y:\beta]}{f(x,y)}{\beta}$  as

$$(\Gamma, [x:\alpha], [y:\beta] \vdash_{\Sigma} f(x,y):\beta).$$

#### 2.4 Precedence-Based Bracket Elision

In the infrastructure discussed above, we have completely ignored the fact that we use brackets to disambiguate the formula structure. The general baseline rule here is that we enclose any presented subformula with (round) brackets to mark it as a logical unit. If we applied this to the following formula that combines set union and set intersection

$$\displaystyle \sum_{n\in \{a,b\}, n\in \{c,d\}}$$
 (1)

this would yield  $((a \cap b) \cup (c \cap d))$ , and not  $a \cap b \cup c \cap d$  as we are used to. In mathematics, brackets are elided, whenever the author anticipates that the reader can understand the formula without them, and would be overwhelmed with them. To achieve this, there are set of common conventions that govern bracket elision — " $\cap$  binds stronger than  $\cup$ " in (1). The most common is to assign precedences to all operators, and elide brackets, if the precedence of the operator is larger than that of the context it is presented in (or equivalently: we only write brackets, if the operator precedence is smaller or equal to the context precedence). Note that this is more selective that simply dropping outer brackets which would yield  $a \cap b \cup c \cap d$  for (2), where we would have liked  $(a \cup b) \cap (c \cup d)$ 

$$\displaystyle \begin{array}{ll} \begin{array}{ll} & & \\ & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & &$$

In our example above, we would assign  $\cap$  a larger precedence than  $\cup$  (and both a larger precedence than the initial precedence to avoid outer brackets). To compute the presentation of (2) we start out with the \ninters, elide its brackets (since the precedence n of  $\cup$  is larger than the initial precedence i), and set the context precedence for the arguments to n. When we present the arguments, we present

<sup>&</sup>lt;sup>2</sup>If you really need larger arities with associative arguments, contact the package author!

the brackets, since the precedence of  $\operatorname{nunion}$  is larger than the context precedence n

This algorithm — which we call **precedence-based bracket elision** — goes a long way towards approximating mathematical practice. Note that full bracket elision in mathematical practice is a reader-oriented process, it cannot be fully mechanical, e.g. in  $(a \cap b \cap c \cap d \cap e \cap f \cap g) \cup h$  we better put the brackets around the septary intersection to help the reader even though they could have been elided by our algorithm. Therefore, the author has to retain full control<sup>5</sup> over bracketing in a bracket elision architecture. Otherwise it would become impossible to explain the concept of associativity in  $(a \circ b) \circ c = a \circ (b \circ c)$ , where we need the brackets for this one time on an otherwise associative operation  $\circ$ .

Precedence	Operators	Comment
800	+,-	unary
800	^	exponentiation
600	$*, \wedge, \cap$	multiplicative
500	$+,-,\lor,\cup$	additive
400	/	fraction
300	$=, \neq, \leq, <, >, \geq$	relation

Figure 1: Common Operator Precedences

Furthermore, we supply an optional keyval arguments to the mixfix declarations and their abbreviations that allow to specify precedences: The key p key is used to specify the **operator precedence**, and the keys  $p\langle i\rangle$  can be used to specify the **argument precedences**. The latter will set the precedence level while processing the arguments, while the operator precedence invokes brackets, if it is smaller than the current precedence level — which is set by the appropriate argument precedence by the dominating operators or the outer precedence. The values of the precedence keys can be integers or **\ippec** for the infinitely large precedence or **\ippec** for the infinitely small precedence.

If none of the precedences is specified, then the defaults are assumed. The operator precedence is set to the default operator precedence, which defaults to 0. The argument precedences default to the operator precedence.

Figure 1 gives an overview over commonly used precedences. Note that most operators have precedences higher than the default precedence of 0, otherwise the brackets would not be elided. For our examples above, we would define

to get the desired behavior.

Note that the presentation macros uses round brackets for grouping by default. We can specify other brackets via two more keywords: lbrack and rbrack.

р

рi

pii piii

\iprec

\niprec

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lbrack rbrack

 $<sup>^5\</sup>mathrm{EdNote}$ : think about how to implement that. We need a way to override precedences locally

Note that formula parts that look like brackets usually are not. For instance, we should not define the finite set constructor via

where the curly braces are used as brackets, but as presented in section 2.3 even though both would format  $\{a,b,c\}$  as  $\{a,b,c\}$ . In the encoding here, an operator with suitably high operator precedence (it is the best practice u)would be able to make the brackets disappear. Thus the correct version of (3) is

Note that \prefix and \postfix and their variants declared in section 2.1 have brackets that do not participate (actively) in the precedence-based elision: function application brackets are not subject to elision. But the operator precedence p is still taken into account for outer brackets. The argument precedence pi has negative infinity as a default to avoid spurious brackets for arguments.

There is another use case for the \mixfixi macro that is not apparent at first glance. In some cases, we would naively construct presentations without a mixfix declaration, e.g.

$$\newcommand\half[1]{\frac{#1}2}$$
 (5)

The the problem here is that the fraction does not participate in the precedence-based bracketing system, and in particular, the numerator will often have too many brackets (the incoming precedence is just passe through the \half macro). A better way is to wrap the intended presentation in a (somewhat spurious) \mixfixi, which we give the precedence nobrackets, which suppresses all (outer and argument) brackets for one level:

#### 2.5 Flexible Elision

There are several situations in which it is desirable to display only some parts of the presentation:

- We have already seen the case of redundant brackets above
- Arguments that are strictly necessary are omitted to simplify the notation, and the reader is trusted to fill them in from the context.
- Arguments are omitted because they have default values. For example  $\log_{10} x$  is often written as  $\log x$ .
- Arguments whose values can be inferred from the other arguments are usually omitted. For example, matrix multiplication formally takes five arguments, namely the dimensions of the multiplied matrices and the matrices themselves, but only the latter two are displayed.

Typically, these elisions are confusing for readers who are getting acquainted with a topic, but become more and more helpful as the reader advances. For experienced readers more is elided to focus on relevant material, for beginners representations are more explicit. In the process of writing a mathematical document for traditional (print) media, an author has to decide on the intended audience and design the level of elision (which need not be constant over the document though). With electronic media we have new possibilities: we can make elisions flexible. The author still chooses the elision level for the initial presentation, but the reader can adapt it to her level of competence and comfort, making details more or less explicit.

\elide

To provide this functionality, the presentation package provides the \elide macro allows to associate a text with an integer visibility level and group them into elision groups. High levels mean high elidability.

Elision can take various forms in print and digital media. In static media like traditional print on paper or the PostScript format, we have to fix the elision level, and can decide at presentation time which elidable tokens will be printed and which will not. In this case, the presentation algorithm will take visibility thresholds  $T_g$  for every elidability group g as a user parameter and then elide (i.e. not print) all tokens in visibility group g with level  $l > T_g$ . We specify this threshold for via the \setegroup macro. For instance in the example below, we have a two type annotations par for type parameters and typ for type annotations themselves.

\setegroup

 $\label{lidepar} $$\mathbf{I}\leq {par}_{500}_{\alpha}\leq typ}_{100}_{\alpha} :=\lambda_{X}=0. $$$ 

Example 2: Elision with Elision Groups

The visibility levels in the example encode how redundant the author thinks the elided parts of the formula are: low values show high redundancy. In our example the intuition is that the type parameter on the  $\mathbf{I}$  combinator and the type annotation on the bound variable X in the  $\lambda$  expression are of the same obviousness to the reader. So in a document that contains  $\text{etegroup}\{\text{typ}\}\{0\}$  and  $\text{etegroup}\{\text{par}\}\{0\}$  Figure 2 will show  $\mathbf{I} := \lambda X.X$  eliding all redundant information. If we have both values at 600, then we will see  $\mathbf{I}^{\alpha} := \lambda X_{\alpha}.X$  and only if the threshold for typ rises above 900, then we see the full information:  $\mathbf{I}^{\alpha}_{\alpha \to \alpha} := \lambda X_{\alpha}.X$ .

In an output format that is capable of interactively changing its appearance, e.g. dynamic XHTML+MathML (i.e. XHTML with embedded Presentation MATHML formulas, which can be manipulated via JavaScript in browsers), an application can export the information about elision groups and levels to the target format, and can then dynamically change the visibility thresholds by user interaction. Here the visibility threshold would also be used, but here it only determines the default rendering; a user can then fine-tune the document dynamically to reveal elided material to support understanding or to elide more to increase conciseness.

The price the author has to pay for this enhanced user experience is that she has

to specify elided parts of a formula that would have been left out in conventional IATEX. Some of this can be alleviated by good coding practices. Let us consider the log base case. This is elided in mathematics, since the reader is expected to pick it up from context. Using semantic macros, we can mimic this behavior: defining two semantic macros: \logC which picks up the log base from the context via the \logbase macro and \logB which takes it as a (first) argument.

```
\provideEdefault{logbase}{10}
\symdef{logB}[2]{\prefix{\mathrm{log}\elide{base}{100}{_{#1}}}{#2}}
\abbrdef{logC}[1]{\logB{\fromEcontext{logbase}}{#1}}
```

\provideEdefault

\fromEcontext

setEdefault

Here we use the \provideEdefault macro to initialize a IATEX token register for the logbase default, which we can pick up from the elision context using \fromEcontext in the definition of \logC. Thus \logC{x} would render as  $\log_{10}(x)$  with a threshold of 50 for base and as  $\log_2$ , if the local TEX group e.g. given by the assertion environment contains a \setEdefault{logbase}{2}.

#### 2.6 Other Layout Primitives

Not all mathematical layouts are producible with mixfix notations. A prime example are grid layouts which are marked up using the array element in TeX/LaTeX, e.g. for definition by cases as the (somewhat contrived) definition of the absolute value function in the upper part of Figure 3. We will now motivate the need of special layout primitives with this example. But this does

```
|x| \cdot |x|
```

**Example 3:** A piecewise definition of the absolute value function

not work for content markup via semantic macros [KGA15], which wants to group formula parts by function. For definition by cases, we may want to follow the OpenMath piece1 content dictionary [], which groups "piecewise" definitions into a constructor piecewise, whose children are a list of piece constructors optionally followed by an otherwise. If we want to mimic this by semantic macros in STEX (these are defined via \symdef; see [KGA15] for details), we would naturally define \piecewise by wrapping an array environment

(see the last line in Figure 3). Then we would naturally be tempted to define \piece via \symdef{piece}[2]{#1&\text{if}\;{#2}\\} and \otherwise via \symdef{otherwise}[1]{#1&\text{else}}. But this does not support the generation of separate notation definitions for \piece and \otherwise: here LATEXMLhas to generate presentational information outside of the array context that provides the & and \\ command sequences<sup>3</sup>. Therefore the presentation package provides the macros \parrayline and \parraycell that refactor this functionality.

\parrayline

\parraycell

\parrayline{\langle cells\} {\langle cells\} \ and can thus be used to create array lines with one or more array cells:  $\langle cell \rangle$ \\ and can thus be used to create array lines with one or more array cells:  $\langle cell \rangle$  is the last array cell, and the previous ones are each marked up as \parraycell{\langle cell\}}, where  $\langle cell \rangle$  is the cell content. In last lines of Figure 3 we have used them to create the array lines for \piece and \otherwise. Note that the array cell specifications in \parrayline must coincide with the array specification in the main constructor (here rl in \piecewise).

#### 3 Limitations

In this section we document known limitations. If you want to help alleviate them, please feel free to contact the package author. Some of them are currently discussed in the STEX GitHub repository [sTeX].

1. none reported yet

## 4 The Implementation

#### 4.1 Package Options

The presentation package does not take options (at the moment), but we accept any and ignore them.

- 1 (\*package)
- 2 \DeclareOption\*{}
- 3 \ProcessOptions

We first make sure that the KeyVal package is loaded (in the right version). For LATEXML, we also initialize the package inclusions.

- 4 \RequirePackage{keyval}[1997/11/10]
- 5 \RequirePackage{amsmath}

We will first specify the default precedences and brackets, together with the macros that allow to set them.

- 6 \def\pres@default@precedence{0}
- 7 \def\pres@infty{1000000}
- 8 \def\pres@infty@minusone{999999}
- 9 \def\iprec{\pres@infty}

<sup>&</sup>lt;sup>3</sup>Note that this is not a problem when we only run latex if we assume that \piece and \otherwise are only used in arguments of \piecewise.

```
10 \def\niprec{-\pres@infty}
                        11 \def\pres@initial@precedence{0}
                        12 \def\pres@current@precedence{\pres@initial@precedence}
                        13 \def\pres@default@lbrack{(}\def\pres@lbrack{\pres@default@lbrack}
                        14 \ef\pres@default@rbrack{)} \ef\pres@rbrack{\pres@default@rbrack}
                        4.2
                                     The System Commands
                       \withprec will set the current precedence.<sup>6</sup>
\withprec*
                        15 \newcommand\withpreci[1] {\edef\pres@current@precedence{#1}}
                        16 \newcommand\withprecii[1]{\edef\pres@current@precedence{#1}}
                        17 \newcommand\withpreciii[1] {\edef\pres@current@precedence{#1}}
    \PrecSet \PrecSet will set the default precedence.
                        18 \newcommand\PrecSet[1] {\edef\pres@default@precedence{#1}}
                       \PrecWrite will write a bracket, if the precedence mandates it, i.e. if \pres@p is
\PrecWrite
                        greater than the current precedence specified by \pres@current@precedence
                        19 \def\PrecWrite#1{\ifnum\pres@p>\pres@current@precedence\else{#1}\fi}
                        20 \def\PrepostPrecWrite#1{\ifnum\pres@p@key>\pres@infty@minusone\else{#1}\fi}
                                     Prefix & Postfix Notations
                        We first define the keys for the keyval arguments for \prefix and \postfix.
                        21 \def\prepost@clearkeys{\def\pres@p@key{\pres@default@precedence}\def\pres@pi@key{\niprec}
                        22 \def\pres@lbrack{\pres@default@lbrack}\def\pres@rbrack{\pres@default@rbrack}}
                        23 \define@key{prepost}{lbrack}{\def\pres@lbrack{#1}}
                        24 \define@key{prepost}{rbrack}{\def\pres@lbrack{#1}}
                        25 \define@key{prepost}{p}{\def\pres@p@key{#1}}
                        26 \define@key{prepost}{pi}{\def\pres@pi@key{#1}}
                        27 \end{fine} \end{fine} $$ 17 \end{fine} \end{fine} $$ 17 \end{fine} $$
                        28 \def\pres@pi@key{-\pres@infty}}
      \prefix In prefix we always write the brackets.
                        29 \newcommand\prefix[3][]%key, fn, arg
                        30 {\prepost@clearkeys\setkeys{prepost}{#1}
                        31 {#2}\PrepostPrecWrite\pres@lbrack{\edef\pres@current@precedence{\pres@pi@key}#3}\PrepostPrecWri
    \postfix
                        32 \newcommand\postfix[3][]%key, fn, arg
                        33 {\prepost@clearkeys\setkeys{prepost}{#1}
                        34 \PrepostPrecWrite\pres@lbrack{\edef\pres@current@precedence{\pres@pi@key}#3}\PrepostPrecWrite\p
                             <sup>6</sup>EDNOTE:
                                                    need to implement this in LATEXML! it is used in power in
                        smglom/smglom/source/arithmetcis.tex. We also need to document it above!
```

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 $^7{
m EDNOTE}$ : need to implement this in LATEXML! Also document it above! On the other hand

it is never used.

#### 4.4 Mixfix Operators

We need to enable notation definitions of the operators that have argument- and precedence-aware renderings. To this end, we circumvent LATEXML's limitations induced by its internal processing stages, by pulling most of the argument rendering functionality to the XSLT which produces the final OMDoc result.

In the LATEXML bindings, the internal structure of the mixfix operators is generically preserved, via the <code>symdef\_presentation\_pmml</code> subroutine in the Modules package. Nevertheless, in the current module we add the promised syntactic enhancements to each element of the mixfix family. Also, we use the <code>argument\_precedence</code> subroutine to store the precedences given by the 'pi', 'pii', etc. keys as a temporary <code>argprec</code> attribute of the rendering, to be abolished during the final OMDoc generation. This setup is finally utilized by the XSLT stylesheet which combines the operator structure with the preserved precedences to produce the proper form of the argument render elements.

```
35 \def\clearkeys{\let\pres@p@key=\relax
                         36 \let\pres@pi@key=\relax%
                         37 \let\pres@pi@key=\relax%
                         38 \let\pres@pii@key=\relax%
                         39 \let\pres@piii@key=\relax}
                         40 \define@key{mi}{nobrackets}[yes]{\def\pres@p@key{\pres@infty}%
                         41 \def\pres@pi@key{-\pres@infty}}
                         42 \define@key{mi}{lbrack}{\def\pres@lbrack@key{#1}}
                         43 \define@key{mi}{rbrack}{\def\pres@lbrack@key{#1}}
                         44 \define@key{mi}{p}{\def\pres@p@key{#1}}
                         45 \define@key{mi}{pi}{\def\pres@pi@key{#1}}
                         46 \def\prep@keys@mi%
                         47 {\edef\pres@lbrack{\@ifundefined{pres@lbrack@key}\pres@default@lbrack\pres@lbrack@key}
                         48 \edef\pres@rbrack{\@ifundefined{pres@rbrack@key}\pres@default@rbrack\pres@rbrack@key}
                         49 \edef\pres@p{\@ifundefined{pres@p@key}\pres@default@precedence\pres@p@key}
                         50 \edef\pres@pi{\@ifundefined{pres@pi@key}\pres@p\pres@pi@key}}
\mixfixi
                         51 \newcommand\mixfixi[4][] %key, pre, arg, post
                         52 {\clearkeys\setkeys{mi}{#1}\prep@keys@mi%
                         53 \PrecWrite\pres@lbrack%
                         54 #2{\edef\pres@current@precedence{\pres@pi}#3}#4%
                         55 \PrecWrite\pres@rbrack}
  \@assoc We are using functionality from the LATEX core packages here to iterate over the
                         arguments.
                         56 \def\@assoc#1#2#3{\%} precedence, function, argv
                         57 \let\@tmpop=\relax% do not print the function the first time round
                         58 \ensuremath{\mbox{\sc 0}} := \#3\ensuremath{\mbox{\sc 0}} \ensuremath{\mbox{\sc 0}} = \#3\ensuremath{\mbox{\sc 0}} \ensuremath{\mbox{\sc 0}} = \#3\ensuremath{\mbox{\sc 0}} = \#3\ensurem
                         59 % write the i-th argument with locally updated precedence
                         60 {\edef\pres@current@precedence{#1}\@I}%
                         61 \def\@tmpop{#2}}}%update the function
```

```
\mixfixa
                             62 \newcommand\mixfixa[5][]%key, pre, arg, post, assocop
                             63 {\clearkeys\setkeys{mi}{#1}\prep@keys@mi%
                             64 \PrecWrite\pres@lbrack{#2}{\@assoc\pres@pi{#5}{#3}}{#4}\PrecWrite\pres@rbrack}
EdN:8
                   \mixfixA A variant of \mixfixa that puts the arguments into an array.<sup>8</sup>
                             65 \newcommand\mixfixA[5][]%key, pre, arg, post, assocop
                             66 {\clearkeys\setkeys{mi}{#1}\prep@keys@mi%
                             68 \PrecWrite\pres@lbrack% write bracket if necessary
                             69 #2{\begin{array}{1}\docsvlist{#3}\end{array}}%
                             70 #4\PrecWrite\pres@rbrack}
                             71 \define@key{mii}{nobrackets}[yes]{\def\pres@p@key{\pres@infty}%
                             72 \def\pres@pi@key{-\pres@infty}\def\pres@pii@key{-\pres@infty}}
                             73 \define@key{mii}{lbrack}{\def\pres@lbrack@key{#1}}
                             74 \define@key{mii}{rbrack}{\def\pres@lbrack@key{#1}}
                             75 \define@key{mii}{p}{\def\pres@p@key{#1}}
                             76 \define@key{mii}{pi}{\def\pres@pi@key{#1}}
                             77 \define@key{mii}{pii}{\def\pres@pii@key{#1}}
                             78 \def\prep@keys@mii{\prep@keys@mi%
                             79 \edef\pres@pii{\@ifundefined{pres@pii@key}\pres@p\pres@pii@key}}
                  \mixfixii
                             80 \newcommand\mixfixii[6][]%key, pre, arg1, mid, arg2, post
                             81 {\clearkeys\setkeys{mii}{#1}\prep@keys@mii%
                             82 \PrecWrite\pres@lbrack% write bracket if necessary
                             83 #2{\edef\pres@current@precedence{\pres@pi}#3}%
                             84 #4{\edef\pres@current@precedence{\pres@pii}#5}#6%
                             85 \PrecWrite\pres@rbrack}
                  \mixfixia
                             86 \newcommand\mixfixia[7][]%key, pre, arg1, mid, arg2, post, assocop
                             87 {\clearkeys\setkeys{mii}{#1}\prep@keys@mii%
                             88 \PrecWrite\pres@lbrack% write bracket if necessary
                             89 #2{\edef\pres@current@precedence{\pres@pi}#3}%
                             90 #4{\@assoc\pres@pii{#7}{#5}}#6%
                             91 \PrecWrite\pres@rbrack}
EdN:9
                  \mixfixiA A variant of \mixfixia that puts the arguments into an array.<sup>9</sup>
                             92 \newcommand\mixfixiA[7][]%key, pre, arg1, mid, arg2, post, assocop
                             93 {\clearkeys\setkeys{mii}{#1}\prep@keys@mii%
                             94 \renewcommand\do[1]{\@assoc\pres@pi{#7}{##1}{#7}\tabularnewline}%
                             95 \PrecWrite\pres@lbrack% write bracket if necessary
                             96 #2{\edef\pres@current@precedence{\pres@pi}#3}%
```

 $<sup>^8{</sup>m EDNote}$ : MK: this is very experimental now, if this works, we need to document this above and extend this to the other mixfix declarations. Also we could use a key for the array format argument.

 $<sup>^9\</sup>mathrm{EdNote}$ : MK: this is very experimental now, if this works, we need to document this above and extend this to the other mixfix declarations. Also we could use a key for the array format argument.

```
97 #4{\begin{array}{1}\docsvlist{#5}\end{array}}#6%
            98 \PrecWrite\pres@rbrack}
 \mixfixai
            99 \newcommand\mixfixai[7][] %key, pre, arg1, mid, arg2, post, assocop
           100 {\clearkeys\setkeys{mii}{#1}\prep@keys@mii%
           101 \PrecWrite\pres@lbrack% write bracket if necessary
           102 #2{\@assoc\pres@pi{#7}{#3}}%
           103 #4{\edef\pres@current@precedence{\pres@pii}#5}#6%
           104 \PrecWrite\pres@rbrack}
           105 \define@key{miii}{nobrackets}[yes]{\def\pres@p@key{\pres@infty}%
           106 \def\pres@pi@key{-\pres@infty}
           107 \def\pres@pii@key{-\pres@infty}
           108 \def\pres@pii@key{-\pres@infty}}
           109 \define@key{miii}{lbrack}{\def\pres@lbrack@key{#1}}
           110 \define@key{miii}{rbrack}{\def\pres@lbrack@key{#1}}
           111 \define@key{miii}{p}{\def\pres@p@key{#1}}
           112 \define@kev{miii}{pi}{\def\pres@pi@kev{#1}}
           113 \define@key{miii}{pii}{\def\pres@pii@key{#1}}
           114 \define@key{miii}{piii}{\def\pres@piii@key{#1}}
           115 \def\prep@keys@miii{\prep@keys@mii%
           116 \edef\pres@piii{\@ifundefined{pres@piii@key}{\pres@p}iii@key}}}
\mixfixiii
           117 \newcommand\mixfixiii[8][]%key, pre, arg1, mid1, arg2, mid2, arg3, post
           118 {\clearkeys\setkeys{miii}{#1}\prep@keys@miii%
           119 \PrecWrite\pres@lbrack% write bracket if necessary
           120 #2{\edef\pres@current@precedence{\pres@pi}#3}%
           121 #4{\edef\pres@current@precedence{\pres@pii}#5}%
           122 #6{\edef\pres@current@precedence{\pres@pii}#7}#8%
           123 \PrecWrite\pres@rbrack}
\mixfixaii
           124 \newcommand\mixfixaii[9][]%key, pre, arg1, mid1, arg2, mid2, arg3, post, sep
           125 {\clearkeys\setkeys{miii}{#1}\prep@keys@miii%
           126 \PrecWrite\pres@lbrack% write bracket if necessary
           127 #2{\@assoc\pres@pi{#9}{#3}}%
           128 #4{\edef\pres@current@precedence{\pres@pii}#5}%
           129 #6{\edef\pres@current@precedence{\pres@pii}#7}#8%
           130 \PrecWrite\pres@rbrack}
\mixfixiai
           131 \newcommand\mixfixiai[9][]%key, pre, arg1, mid1, arg2, mid2, arg3, post, assocop
           132 {\clearkeys\setkeys{miii}{#1}\prep@keys@miii%
           133 \PrecWrite\pres@lbrack% write bracket if necessary
           134 #2{\edef\pres@current@precedence{\pres@pi}#3}%
           135 #4{\@assoc\pres@pi{#9}{#5}}%
           136 #6{\edef\pres@current@precedence{\pres@pii}#7}#8%
           137 \PrecWrite\pres@rbrack}
```

```
\mixfixiia
                             138 \newcommand\mixfixiia[9][]%key, pre, arg1, mid1, arg2, mid2, arg3, post,assocop
                             139 {\clearkeys\setkeys{miii}{#1}\prep@keys@miii%
                             140 \PrecWrite\pres@lbrack% write bracket if necessary
                             141 #2{\edef\pres@current@precedence{\pres@pi}#3}%
                             142 #4{\edef\pres@current@precedence{\pres@pii}#5}%
                             143 #6{\@assoc\pres@pi{#9}{#7}}#8%
                             144 \PrecWrite\pres@rbrack}
                    \prefixa In prefix we always write the brackets.
                             145 \newcommand\prefixa[4][]%keys, fn, arg, sep
                             146 {\prepost@clearkeys\setkeys{prepost}{#1}%
                             147 {#2}\pres@lbrack{\@assoc\pres@pi@key{#4}{#3}}\pres@rbrack}
                   \postfixa
                             148 \newcommand\postfixa[4][]%keys, fn, arg, sep
                             149 {\prepost@clearkeys\setkeys{prepost}{#1}%
                             150 \pres@lbrack{\@assoc\pres@pi@key{#4}{#3}}\pres@rbrack{#2}}
                      \infix \infix<sup>10</sup> is a simple special case of \mixfixii.
EdN:10
                             151 \newcommand\infix[4][]{\mixfixii[#1]{}{#3}{#2}{#4}{}}
                      \assoc
                             152 \mbox{ newcommand\assoc[3][]{\mbox{mixfixa[#1]{}{#3}{}{#2}}}
                                     General Elision
                              4.5
                              11
EdN:11
                 \setegroup
                              The elision macros are quite simple, a group foo is internally represented by a
                              macro foo@egroup, which we set by a \gdef.
                             153 \def\setegroup#1#2{\expandafter\def\csname #1@egroup\endcsname{#2}}
                             Then the elision command is picks up on this (flags an error) if the internal macro
                              does not exist and prints the third argument, if the elision value threshold is
                              above the elision group threshold in the paper. 12 We test the implementation
EdN:12
                              with Figure 2.
                             154 \def\elide#1#2#3{\@ifundefined{#1@egroup}%
                             155 {\def\@elevel{0}
                             156 \PackageError{presentation}{undefined egroup #1, assuming value 0}%
                             157 {When calling \protect\elide{#1}... the elision group #1 has be have\MessageBreak
                             158 been set by \protect\setegroup before, e.g. by \protect\setegroup{an}{0}.}}%
                             159 {\edef\@elevel{\csname #1@egroup\endcsname}}%
                             160 \inv @elevel>#2\else{#3}\fi
                                ^{10}\mathrm{EdNote}: need infixl as well, use counters for precedences here.
```

<sup>&</sup>lt;sup>11</sup>EDNOTE: all of these still need to be tested and implemented in LaTeXML.

 $<sup>^{12}\</sup>mathrm{EdNote}$ : do we need to turn this around as well?

par	typ	result	expected
0	0	$\mathbf{I}^{\alpha}{}_{\alpha \to \alpha} := \lambda X_{\alpha}.X$	$\mathbf{I} := \lambda X.X$
600	600	$\mathbf{I} := \lambda X.X$	$\mathbf{I}^{\alpha} := \lambda X_{\alpha}.X$
600	1000	$\mathbf{I} := \lambda X.X$	$\mathbf{I}^{\alpha}_{\alpha \to \alpha} := \lambda X_{\alpha}.X$

Figure 2: Testing Elision with the example in Figure 2

```
\provideEdefault The \provideEdefault macro sets up the context for an elision default by locally
                                                         defining the internal macro \( \langle default \) \( \text{Qedefault} \) and (if necessary) exporting it
                                                         from the module.
                                                       161 \def\provideEdefault#1#2{\expandafter\def\csname#1@edefault\endcsname{#2}
                                                       162 \@ifundefined{this@module}{}%
                                                      163 {\tt expandafter\g@addto@macro\this@module\{\tt expandafter\def\csname\#1@edefault\endcsname\#2\}}\}}
            \setEdefault The \setEdefault macro just redefines the internal \default\@edefault in the
                                                         local group
                                                       164 \end{setEdefault} $$164 
         \from Econtext The \from Econtext macro just calls internal \langle default \rangle @edefault macro.
                                                       165 \def\fromEcontext#1{\csname #1@edefault\endcsname}
                                                                              Other Layout Primitives
                                                         4.6
                                                         The \parray, \parrayline and \parraycell macros are simple refactorings of
                                                         the array functionality on the LATEX side.
                            \parray
                                                      166 \newcommand\parray[2]{\begin{array}{#1}#2\end{array}}
```

174 \def\endx@mrowh#1{\\hline}

## 4.7 Deprecated Functionality

These macros may go away at any time.

```
\parraylineh
```

175 \newcommand\parraylineh[2]{#1#2\\hline}

\parraycell

176 \newcommand\parraycell[1]{#1&} 177  $\langle package \rangle$ 

## Index

Numbers written in italic refer to the page where the corresponding entry is described; numbers underlined refer to the code line of the definition; numbers in roman refer to the code lines where the entry is used.

*,	6	n-ary	OMDoc,		13
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