# Semantic Markup for Mathematical Statements\*

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#### Abstract

The statements package is part of the STEX collection, a version of TEX/LATEX that allows to markup TEX/LATEX documents semantically without leaving the document format, essentially turning TEX/LATEX into a document format for mathematical knowledge management (MKM).

This package provides semantic markup facilities for mathematical statements like Theorems, Lemmata, Axioms, Definitions, etc. in STEX files. This structure can be used by MKM systems for added-value services, either directly from the STEX sources, or after translation.

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## 1 Introduction

The motivation for the statements package is very similar to that for semantic macros in the modules package: We want to annotate the structural semantic properties of statements in the source, but present them as usual in the formatted documents. In contrast to the case for mathematical objects, the repertoire of mathematical statements and their structure is more or less fixed.

This structure can be used by MKM systems for added-value services, either directly from the STEX sources, or after translation. Even though it is part of the STEX collection, it can be used independently, like it's sister package sproofs.

STEX [sTeX:online; Koh08] is a version of TeX/IATeX that allows to markup TeX/IATeX documents semantically without leaving the document format, essentially turning TeX/IATeX into a document format for mathematical knowledge management (MKM). Currently the OMDoc format [Koh06] is directly supported.

## 2 The User Interface

The statements package supplies a semantically oriented infrastructure for marking up mathematical statements: fragments of natural language that state properties of mathematical objects, e.g. axioms, definitions, or theorems. The statement package provides an infrastructure for marking up the semantic relations between statements for the OMDoc transformation and uses the ntheorem package [MS] for formatting (i.e. transformation to PDF).

#### 2.1 Package Options

showmeta

The statements package provides the defindex option to STEX. If this is set, then definiend are automatically passed into the index of the document. Furthermore, the statements package passes the showmeta to the metakeys package. If this is set, then the metadata keys are shown (see [Koh15a] for details and customization options).

#### 2.2 Statements

All the statements are marked up as environments, that take a KeyVal argument that allows to annotate semantic information. Generally, we distinguish two forms of statements:

**block statements** have explicit discourse markers that delimit their content in the surrounding text, e.g. the boldface word "**Theorem:**" as a start marker and a little line-end box as an end marker of a proof.

flow statements do not have explicit markers, they are interspersed with the surrounding text.

display=

id=

Since they have the same semantic status, they must both be marked up, but styled differently. We distinguish between these two presentational forms with the display key, which is allowed on all statement environments. If it has the value block (the default), then the statement will be presented in a paragraph of its own, have explicit discourse markers for its begin and end, possibly numbering, etc. If it has the value flow, then no extra presentation will be added the semantic information is invisible to the reader. Another key that is present on all statement environments in the id key it allows to identify the statement with a name and to reference it with the semantic referencing infrastructure provided by the sref package [Koh15c].

#### 2.2.1 Axioms and Assertions

assertion

The assertion environment is used for marking up statements that can be justified from previously existing knowledge (usually marked with the monikers "Theorem", "Lemma", "Proposition", etc. in mathematical vernacular). The environment assertion is used for all of them, and the particular subtype of assertion is given in the type key. So instead of \begin{Lemma} we have to write \begin{assertion} [type=lemma] (see Example 1 for an example).

type=

```
\begin{assertion} [id=sum-over-odds,type=lemma] $$\sum_{i=1}^n{2i-1}=n^2$ \end{assertion} $$ will lead to the result $$ Lemma 2.1 $$\sum_{i=1}^n 2i-1=n^2$ $$
```

Example 1: Semantic Markup for a Lemma in a module context

Whether we will see the keyword "Lemma" will depend on the value of the optional display key. In all of the assertion environments, the presentation expectation is that the text will be presented in italic font. The presentation (keywords, spacing, and numbering) of the assertion environment is delegated to a theorem styles from the ntheorem environment. For an assertion of type  $\langle type \rangle$  the assertion environment calls the  $ST\langle type \rangle AssEnv$  environment provided by the statements package; see Figure 2 for a list of provided assertion types. Their formatting can be customized by redefining the  $ST\langle type \rangle AssEnv$  environment via the \renewtheorem command from the ntheorem package; see [MS] for details.

axiom

The axiom environment is similar to assertion, but the content has a different ontological status: axioms are assumed without (formal) justification, whereas assertions are expected to be justified from other assertions, axioms or definitions. This environment relegates the formatting to the STaxiomEnv environment, which can be redefined for configuration.

#### 2.2.2 Symbols

symboldec The symboldec environment can be used for declaring concepts and symbols. Note

Explanation				
an important assertion with a proof				
that the meaning of <b>theorem</b> (in this case the existence of a proof) is not enforced by Ooc applications. It can be appropriate to give an assertion the <b>theorem</b> , if the author is of a proof (e.g. in the literature), but has not formalized it in OMDoc yet.				
a less important assertion with a proof				
pecified here is even softer than the other ones, since e.g. s a chapter in a larger monograph, may make it necessary to main theorem of the paper) and give it the status of a lemma				
a simple consequence				
ked as a corollary to some other statement, if the proof is the case for important theorems that are simple to get from				
an assertion without proof or counter-example				
see semantic value is not yet decided, but which the author articular, there is no proof or counter-example.				
an aggertion with a country arrample				
an assertion with a counter-example				
o be false, i.e. it has a counter-example. Such assertions are istorical purposes.				
be false, i.e. it has a counter-example. Such assertions are				
be false, i.e. it has a counter-example. Such assertions are istorical purposes.				
b be false, i.e. it has a counter-example. Such assertions are istorical purposes.  an assertion on which a proof of another depends onvenient during the exploration of a mathematical theory.				
be false, i.e. it has a counter-example. Such assertions are istorical purposes.  an assertion on which a proof of another depends onvenient during the exploration of a mathematical theory. ater (or assumed as an axiom).				
be false, i.e. it has a counter-example. Such assertions are istorical purposes.  an assertion on which a proof of another depends onvenient during the exploration of a mathematical theory. ater (or assumed as an axiom).  a normative assertion				

**Example 2:** Types of Mathematical Assertions

the the symdef forms from the modules package will not do this automatically (but the definition environment and the \inlinedef macro will for all the definienda; see below). The symboldec environment takes an optional keywords argument with the keys id, role, title and name. The first is for general identification, the role specifies the OPENMATH/OMDOC role, which is one of object, type, sort, binder, attribution, application, constant, semantic-attribution, and error (see the OMDOC specification for details). The name key specifies the OPENMATH name of the symbol, it should coincide with the control sequence introduced by the corresponding \symdef (if one is present). The title key is for presenting the title of this symbol as in other statements. Usually, axiom and symboldec environments are used together as in Figure 3.

#### 2.2.3 Types

In many cases, we can give additional information for symbols in the form of type assignments. SIEX does not fix a type system, but allows types to be arbitrary mathematical objects that they can be defined in (imported) modules. The \symtype macro can be used to assign a type to a symbol:

\symtype

```
\symtype[\langle keys \rangle] \{\langle sym \rangle\} \{\langle type \rangle\}
```

assigns the type  $\langle type \rangle$  to a symbol with name  $\langle sym \rangle$ . For instance

```
\symtype[id=plus-nat.type,system=sts]{plus}{\fntype{\Nat,\Nat}\Nat}
```

assigns the type  $\mathbb{N} \times \mathbb{N} \to \mathbb{N}$  (in the sts type system) to the symbol plus. This states (type assignments are statements epistemologically) that addition is a binary function on natural numbers. The \symtype macro supports the keys id (for identifiers) and system for the type system.

typedec

Often, type assignments occur in informal context, where the type assignment is given by a natural language sentence or phrase. For this, the statements package supplies the typedec environment and the \inlinetypedec macro. Both take an optional keyval argument followed by the type. The phrase/sentence is the body of the typedec environment and the last argument of the \inlinetypedec macro. The symbol name is given in via the for key. For convenience, the macro \thedectype is bound to the type. So we can use

\thedectype

\begin{typedec}[for=plus,id=plus-nat.type]{\fntype{\Nat,\Nat}\Nat}
\$+:\thedectype\$ is a binary function on \$\Nat\$
\end{typedec}

instead of the \symtype above in an informal setting.

#### 2.2.4 Definitions, and Definienda

definition

\definiendum

The definition environment is used for marking up mathematical definitions. Its peculiarity is that it defines (i.e. gives a meaning to) new mathematical concepts or objects. These are identified by the \definiendum macro, which is used

```
\symdef{zero}{0}
 \begin{symboldec} [name=zero, title=The number zero, type=constant]
   The number zero, it is used as the base case of the inductive definition
   of natural numbers via the Peano Axioms.
 \end{symboldec}
 \symdef{succ}[1]{\prefix{s}{#1}}
\begin{symboldec} [name=succ, title=The Successor Function, type=application]
   The successor function, it is used for the step case of the inductive
   definition of natural numbers via the Peano Axioms.
\end{symboldec}
 \symdef{NaturalNumbers}{\mathbb{N}}
\begin{symboldec} [name=succ, title=The Natural Numbers, type=constant]
   The natural numbers inductively defined via the Peano Axioms.
 \end{symboldec}
\begin{axiom}[id=peano.P1,title=P1]
   $\zero$ is a natural number.
\end{axiom}
\begin{axiom}[id=peano.P5,title=P5]
   Any property $P$ such $P(\zero)$ and $P(\succ{k})$ whenever $P(k)$
  holds for all $n$ in $\NaturalNumbers$
\end{axiom}
will lead to the result
 Symbol zero: (The number zero)
The number zero, it is used as the base case of the inductive definition of natural
numbers via the Peano Axioms.
Symbol succ: (The Successor Function)
The successor function, it is used for the step case of the inductive definition of
natural numbers via the Peano Axioms.
Symbol succ: (The Natural Numbers)
The natural numbers inductively defined via the Peano Axioms.
Axiom 2.2 (P1) 0 is a natural number.
Axiom 2.6 (P5) Any property P such P(0) and P(\succ k) whenever P(k) holds
for all n in \mathbb{N}
```

**Example 3:** Semantic Markup for the Peano Axioms

as  $\langle sysname \rangle$  { $\langle text \rangle$ }. Here,  $\langle text \rangle$  is the text that is to be emphasized in the presentation and the optional  $\langle sysname \rangle$  is a system name of the symbol defined (for reference via  $\langle termref \rangle$ , see Section 2.3). If  $\langle sysname \rangle$  is not given, then  $\langle text \rangle$  is used as a system name instead, which is usually sufficient for most situations.

**Example 4:** A Definition based on Figure 3

defi The  $\langle word \rangle$  macro combines the functionality of the  $\langle word \rangle$  macro with index markup from the omdoc package [Koh15b]: use

```
\defi[\langle name \rangle] \{\langle word \rangle\} [\langle indexkeys \rangle]
```

to markup a definiendum  $\langle word \rangle$  with system name  $\langle name \rangle$  that appear in the index (where  $\langle indexkeys \rangle$  are passed to the  $\backslash omdoc@index$  macro from the omdoc package) — in other words in almost all definitions of single-word concepts. We also have the variants  $\backslash defii$  and  $\backslash defiii$  for (adjectivized) two-word compounds. Note that if the definiendum contains sematnic macros, then we need to specify the loadmodules key and also protect the semantic macro. For instance if  $\backslash eset$  is the semantic macro for  $\emptyset$ , then we would use

\defii[eset-comp]{\$\protect\eset\$}{compatible}[loadmodules]

\adefi for the definiendum markup. Finally, the variants \adefi, \adefii, and \adefiii \adefii have an additional first argument that allows to specify an alternative text; see \adefiii Figure 5. The main use of these is to mark up inflected forms as in

we speak of \adefi{lemmata}{lemma} in this case.

\defii

\defiii

\defis

\defiiis

As the greatest number of these are plurals, which tends to be regular (e.g. adding a trailing "s" in English), we provide the variants \defis, \defiis, and \defiiis for that case: \defiis{simple}{group} is equivalent to much longer \adefii{simple groups}{simple}{group}.

Note that the \definiendum, \defi, \defii, and \defiii macros can only be used inside the definitional situation, i.e. in a definition or symboldec environment or a \inlinedef macro. If you find yourself in a situation where you want to

source						
system name	result	index				
\defi{concept}						
concept	concept	concept				
\defi[csymbol]{concept}						
csymbol	concept	concept				
\adefi[csymbol]{concepts}{concept}						
csymbol	concepts	concept				
\defii{concept}{group}						
concept-group	oncept-group concept group					
		group - , concept				
\adefii\{small\}\{concept\}\{group\}						
small-concept-group	ot-group small concept group small concept group,					
		concept group - , small				

**Example 5:** Some definienda with Index

use it outside, you will most likely want to wrap the appropriate text fragment in a \begin{definition} [display=flow] ... and \end{definition}. For instance, we could continue the example in Figure 3 with the definition environment in Figure 4.

\inlinedef

Sometimes we define mathematical concepts in passing, e.g. in a phrase like "...s(o) which we call **one**.". For this we cannot use the **definition** environment, which presupposes that its content gives all that is needed to understand the definition. But we do want to make use of the infrastructure introduced for the **definition** environment. In this situation, we just wrap the phrase in an **\inlinedef** macro that makes them available. The **\inlinedef** macro accepts the same id and for keys in its optional argument, and additionally the **verbalizes** key which can be used to point to a full definition of the concept somewhere else.

Note that definiend can only be referenced via a \term element, if they are only allowed inside a named module, i.e. a module environment with a name given by the id= key or the theory= key on is specified on the definitional environment.

#### 2.2.5 Examples

example

The example environment is a generic statement environment, except that the for key should be given to specify the identifier what this is an example for. The example environment also expects a type key to be specified, so that we know whether this is an example or a counterexample.

\inlineex

The \inlineex is analogous to \inlinedef, only that it is used for inline examples, e.g. "...mammals, e.g. goats". Note that we have used an inline example for an inline example.

## 2.3 Cross-Referencing Symbols and Concepts

If we have defined a concept with the \definiendum macro, then we can mark up other occurrences of the term as referring to this concept. Note that this process cannot be fully automatized yet, since that would need advanced language technology to get around problems of disambiguation, inflection, and non-contiguous phrases<sup>1</sup>. Therefore, the \termref can be used to make this information explicit. It takes the keys

\termref

cdbase to specify a URI (a path actually, since LATEX cannot load from URIs) where the module can be found.

cd to specify the module in which the term is defined. If the cd key is not given, then the current module is assumed. If no cdbase is specified (this is the usual case), then the CD has to be imported via a \importmodule from the modules package [KGA15].

name to specify the name of the definiendum (which is given in the body of the \definiendum or the optional argument). If the name key is not specified, then argument of the \termref macro is used.

role is currently unused.

\termref[cd= $\langle cd \rangle$ ,name= $\langle name \rangle$ ] { $\langle text \rangle$ } will just typeset the link text  $\langle text \rangle$  with (if the hyperref package is loaded) a hyperlink to the definition in module  $\langle cd \rangle$  that defines the concept  $\langle name \rangle$ , e.g. that contains \defi[ $\langle name \rangle$ ] { $\langle text \rangle$ }.

Just as the \definiendum macro has the convenience variants \defi, \defii and \defiii, the \termref has variants \trefi, \trefii, and \trefiii that take two and three arguments for the parts of the compositum. In the same module, concepts that are marked up by \defi{\( name \)\} in the definition can be referenced by \trefii{\( name \)\}. Here the link text is just \( name \). Concepts defined via \defii{\( first \)\}{\( second \)\} can be referenced by \trefii{\( first \)\}{\( second \)\} (with link text "\( first \) \( second \)") and analogously for \defiii and \trefiii.

\trefi \trefii \trefiii \atref\*

We have variants \atrefi, \atrefii, and \atrefiii with alternative link text. For instance \atrefii{\large}text\{\large}{\large}text\}\{\large}text\}\{\large}text\}\{\large}text\}\{\large}text\}. Of course, if the system identifier is given explicitly in the optional argument of the definition form, as in \defii[\large|text\}\{\large}\}\{\large}\}\{\large}\}, then the terms are referenced by \trefi{\large}.

For referencing terms outside the current module, the module name can be specified in the first optional argument of the \\*tref\* macros. To specify the cdbase, we have to resort to the \termref macro with the keyval arguments.

Note that the \termref treatment above is natural for "concepts" declared by the \termdef macro from the modules package [KGA15]. Concepts are natural language names for mathematical objects. For "symbols", i.e. symbolic identifiers for mathematical objects used in mathematical formulae, we use the \symdef macro from the modules package. Sometimes, symbols also have an associated natural language concept, and we want to use the symbol name to reference it (instead of specifying cd and name which is more inconvenient). For this the

<sup>&</sup>lt;sup>1</sup>We do have a program that helps annotate larger text collections spotting the easy cases; see http://kwarc.info/projects/stex and look for the program termin.

\symref

statements package supplies the \symref macro. Like \termref, and invocation of \symref{ $\langle cseq \rangle$ }-{ $\langle text \rangle$ } will just typeset  $\langle text \rangle$  with a hyperlink to the relevant definition (i.e. the one that has the declaration for= $\langle cseq \rangle$  in the metadata argument.)

\term

The \term macro is a variant of the \termref macro that marks up a phrase as a (possible) term reference, which does not have a link yet. This macro is a convenient placeholder for authoring, where a \termref annotation is (currently) too tedious or the link target has not been authored yet. It facilitates lazy flexiformalization workflows, where definitions for mathematical concepts are supplied or marked up by need (e.g. after a grep shows that the number of \term annotations of a concept is above a threshold). Editors or active documents can also support the \term macro like a wiki-like dangling link: a click on \term{\langle phrase \rangle} could generate a new editor buffer with a stub definition (an definition environment with \definiendum macro and appropriate metadata).

## 3 Configuration of the Presentation

\defemph

The \defemph macro is a configuration hook that allows to specify the style of presentation of the definiendum. By default, it is set to \bf as a fallback, since we can be sure that this is always available. It can be customized by redefinition: For instance \renewcommand{\defemph}[1]{\emph{#1}}, changes the default behavior to italics.

\termemph

The \termenth macro does the same for the style for \termref, it is empty by default. Note the term might carry an implicit hyper-reference to the defining occurrence and that the presentation engine might mark this up, changing this behavior

\stDMemph

The  $\stDMemph$  macro does the same for the style for the markup of the discourse markers like "Theorem". If it is not defined, it is set to  $\bf$ ; that allows to preset this in the class file. <sup>2</sup>

\STpresent

Some authors like to lowercase the semantic references, i.e. use "axiom 2.6" instead of the default "Axiom 2.6" to refer to the last axiom in Figure 3. This can be achieved by redefining the \STpresent macro, which is applied to the keyword of the ST\*Env theorem environments.<sup>3</sup>

Finally, we provide configuration hooks in Figure 6 for the statement types provided by the statement package. These are mainly intended for package authors building on statements, e.g. for multi-language support. The language bindings are given in the smultiling [KG15] package not in statements itself.

EdN:1

EdN:2

EdN:3

<sup>&</sup>lt;sup>1</sup>EdNote: MK: we probably need multi-part variants for \*tref\*

<sup>&</sup>lt;sup>2</sup>EdNote: function declarations

<sup>&</sup>lt;sup>3</sup>EDNOTE: this does not quite work as yet, since **STpresent** is applied when the label is written. But we would really like to have it applied when the reference is constructed. But for that we need to split the label into keyword and number in package sref.

Environment	configuration macro	value
STtheoremAssEnv	\st@theorem@kw	Theorem
STlemmaAssEnv	\st@lemma@kw	Lemma
STpropositionAssEnv	\st@proposition@kw	Proposition
STcorollaryAssEnv	\st@corollary@kw	Corollary
STconjectureAssEnv	\st@conjecture@kw	Conjecture
STfalseconjectureAssEnv	ackslashst@falseconjecture@kw	Conjecture (false)
STpostulateAssEnv	\st@postulate@kw	Postulate
STobligationAssEnv	\st@obligation@kw	Obligation
STassumptionAssEnv	\st@assumption@kw	Assumption
STobservationAssEnv	\st@observation@kw	Observation
STruleAssEnv	\st@rule@kw	Rule
STexampleEnv	\st@example@kw	Example
STaxiomEnv	\st@axiom@kw	Axiom
STdefinitionEnv	\st@definition@kw	Definition
STnotationEnv	\st@notation@kw	Notation

**Example 6:** Configuration Hooks for statement types

## 4 Limitations

In this section we document known limitations. If you want to help alleviate them, please feel free to contact the package author. Some of them are currently discussed in the ST<sub>E</sub>X GitHub repository [sTeX].

1. none reported yet

## 5 The Implementation

### 5.1 Package Options

We declare some switches which will modify the behavior according to the package options. Generally, an option xxx will just set the appropriate switches to true (otherwise they stay false). First we have the general options

- 1 (\*package)
- 2 \newif\ifdef@index\def@indexfalse
- 3 \DeclareOption{defindex}{\def@indextrue}
- 5 \ProcessOptions
- 6 (/package)

The next measure is to ensure that some STEX packages are loaded: omdoc for the statement keys, modules since we need module identifiers for referencing. Furthermore, we need the ntheorem package for presenting statements. For LATEXML, we also initialize the package inclusions, there we do not need ntheorem, since the XML does not do the presentation.

```
8 \( \)*package \\
9 \\ RequirePackage \{ omtext \}
10 \\ RequirePackage \[ [base] \{ babel \}
11 \\ RequirePackage \[ [hyperref] \{ ntheorem \}
12 \\ theoremstyle \{ plain \}
13 \( / package \)
```

Now, we define an auxiliary function that lowercases strings

Sometimes it is necessary to fallback to symbol names in order to generate xml:id attributes. For this purpose, we define an auxiliary function which ensures the name receives a unique NCName equivalent.<sup>4</sup>

The following functions are strictly utility functions that makes our life easier later on

```
For the other languages, we set up triggers
14 \*package\
15 \AfterBabelLanguage{ngerman}{\input{statements-ngerman.ldf}}
16 \( /package \)
```

#### 5.2 Statements

\STpresent

```
 \begin{array}{l} 17 \; \langle \texttt{*package} \rangle \\ 18 \; \langle \texttt{providecommand} \rangle \\ 19 \; \langle \texttt{package} \rangle \\ \end{array}
```

\define@statement@env

EdN:4

We define a meta-macro that allows us to define several variants of statements. Upon beginning this environment, we first set the KeyVal attributes, then we decide whether to print the discourse marker based on the value of the display key, then (given the right Options were set), we show the semantic annotations, and finally initialize the environment using the appropriate macro. Upon ending the environment, we just run the respective termination macro.

```
20 \*package\
21 \def\define@statement@env#1{%
22 \newenvironment{#1}[1][] \metasetkeys{omtext}{##1}\sref@target%
23 \@in@omtexttrue%
24 \ifx\omtext@display\st@flow\else%
25 \ifx\omtext@title\@empty\begin{ST#1Env}\else\begin{ST#1Env}[\omtext@title]\fi%
26 \ifx\sref@id\@empty\else\label{#1.\sref@id}\fi
27 \csname st@#1@initialize\endcsname\fi% display
28 \ifx\sref@id\@empty\sref@label@id{\here}\else%
29 \sref@label@id{\STpresent{\csname ST#1EnvKeyword\endcsname}^\@currentlabel}\fi%
30 \ignorespaces}
31 {\csname st@#1@terminate\endcsname\ifx\omtext@display\st@flow\else\end{ST#1Env}\fi%
32 \omtext@post@skip\@in@omtextfalse}}
33 \(/package\)
```

 $<sup>^4{\</sup>rm EDNoTE}$ : Hard to be unique here, e.g. the names "foo\_bar" and "foo bar" would receive the same xml:id attributes... of course we can devise a more complex scheme for the symbol replacement.

```
assertion
```

- 34 \(\*package\)
  35 \newenvironment{assertion}[1][]{\metasetkeys{omtext}{#1}\sref@target\)
  36 \@in@omtexttrue\)
  37 \ifx\omtext@display\st@flow\itshape\noindent\ignorespaces\)
  38 \else\(\) display!=flow
  39 \ifx\omtext@title\@empty\begin{ST\omtext@type AssEnv}\)
  40 \else\begin{ST\omtext@type AssEnv}[\omtext@title]\fi\\fi\)
  41 \ifx\omtext@type\@empty\sref@label@id{\here}\else\(\)
  42 \sref@label@id{\STpresent{\csname ST\omtext@type AssEnvKeyword\endcsname}^\@currentlabel}\)
  43 \fi}\(\)\display=flow
  44 \{\ifx\omtext@display\st@flow\else\end{ST\omtext@type AssEnv}\@in@omtextfalse\\fi}\)
  45 \(\)/package\)
- \st@\*@kw We configure the default keywords for the various theorem environments.
  - 46 (\*package)
  - 47 \def\st@theorem@kw{Theorem}
  - 48 \def\st@lemma@kw{Lemma}
  - 49 \def\st@proposition@kw{Proposition}
  - 50 \def\st@corollary@kw{Corollary}
  - 51 \def\st@conjecture@kw{Conjecture}
  - 52 \def\st@falseconjecture@kw{Conjecture (false)}
  - 53 \def\st@postulate@kw{Postulate}
  - 54 \def\st@obligation@kw{Obligation}
  - 55 \def\st@assumption@kw{Assumption}
  - 56 \def\st@rule@kw{Rule}
  - 57 \def\st@observation@kw{Observation}

Then we configure the presentation of the theorem environments

- 58 \theorembodyfont{\itshape}
- 59 \theoremheaderfont{\normalfont\bfseries}

and then we finally define the theorem environments in terms of the statement keywords defined above. They are all numbered together with the section counter.

#### ST\*AssEnv

- 60 \newtheorem{STtheoremAssEnv}{\st@theorem@kw}[section]
- 61 \newtheorem{STlemmaAssEnv}[STtheoremAssEnv]{\st@lemma@kw}
- $62 \end{ST} proposition \verb|AssEnv| [ST theorem AssEnv] {\end{ST} proposition @kw} \\$
- $63 \verb|\newtheorem{STcorollaryAssEnv}| [STtheoremAssEnv] {\newtheorem{STcorollary@kw}}$
- $64 \mbox{ \conjectureAssEnv} [ST theorem AssEnv] {\conjecture@kw} \\$
- $65 \verb|\newtheorem{STfalseconjectureAssEnv}| [STtheoremAssEnv] {\newtheorem{st@falseconjecture@kw}} | $$ \newtheorem{STfalseconjecture@kw} | $$ \newtheorem{stable on jecture @kw} | $$ \newtheorem{stable on$
- $66 \end{STpostulateAssEnv} [ST theoremAssEnv] {\end{Stpostulate@kw}}$
- 67 \newtheorem{STobligationAssEnv}[STtheoremAssEnv]{\st@obligation@kw}
- $68 \verb|\newtheorem{STassumptionAssEnv}| [ST theorem AssEnv] {\newtheorem{sssumption@kw}}$
- 69 \newtheorem{STobservationAssEnv}[STtheoremAssEnv]{\st@observation@kw}
- 70 \newtheorem{STruleAssEnv}[STtheoremAssEnv]{\st@rule@kw}
- $71 \langle /package \rangle$

```
{\tt example} \quad ^5
EdN:5
                               72 (*package)
                               73 \def\st@example@initialize{}\def\st@example@terminate{}
                               74 \define@statement@env{example}
                               75 \def\st@example@kw{Example}
                               76 \theorembodyfont{\upshape}
                               77 \newtheorem{STexampleEnv}[STtheoremAssEnv]{\st@example@kw}
                               78 (/package)
                       axiom
                               79 (*package)
                               80 \def\st@axiom@initialize{}\def\st@axiom@terminate{}
                               81 \define@statement@env{axiom}
                               82 \def\st@axiom@kw{Axiom}
                               83 \theorembodyfont{\upshape}
                               84 \newtheorem{STaxiomEnv}[STtheoremAssEnv]{\st@axiom@kw}
                               85 (/package)
                   symboldec We use \symdef@type from the modules package as the visual cue.
                               86 (*package)
                               87 \srefaddidkey{symboldec}
                               88 \addmetakey{symboldec}{functions}
                               89 \addmetakey{symboldec}{role}
                               90 \addmetakey*{symboldec}{title}
                               91 \addmetakey*{symboldec}{name}
                               92 \addmetakey{symboldec}{subject}
                               93 \addmetakey*{symboldec}{display}
                               94 \newenvironment{symboldec}[1][]{\metasetkeys{symboldec}{#1}\sref@target\st@indeftrue%
                               95 \ifx\symboldec@display\st@flow\else{\noindent\stDMemph{\symdef@type} \symboldec@name:}\fi%
                               96 \ifx\symboldec@title\@empty~\else~(\stDMemph{\symboldec@title})\par\fi}{}
                               97 (/package)
                               5.2.1 Types
EdN:6
                    \symtype
                               98 \langle *package \rangle
                               99 \srefaddidkey{symtype}
                              100 \addmetakey*{symtype}{system}
                              101 \addmetakey*{symtype}{for}
                              102 \newcommand\type@type{Type}
                              103 \newcommand\symtype[3][]{\metasetkeys{symtype}{#1}\sref@target%
                              104 \noindent\type@type \ifx\symtype@\@empty\else (\symtype@system)\fi #2: $#3$}
                              105 (/package)
             \inlinetypedec
                                 ^5\mathrm{EdNote}: need to do something clever for the OMDoc representation of examples, in particular,
                               the usevocab should only be defined in example
```

 $^6\mathrm{EdNote}\colon\mathsf{MK@DG};$  the type element should percolate up.

```
106 (*package)
           \label{localization} 107 \end{10} $$10^{10} \operatorname{localization} {\mbox{\mbox{$1$}}} $$
           108 (/package)
   typedec We first define a theorem environment
           109 (*package)
           110 \def\st@typedec@kw{Type Declaration}
           111 \theorembodyfont{\upshape}
           112 \newtheorem{STtypedecEnv}[STtheoremAssEnv]{\st@typedec@kw}
            and then the environment itself.
           113 \newenvironment{typedec}[2][]{\metasetkeys{omtext}{#1}\sref@target%
           114 \def\thedectype{#2}%
           115 \ifx\omtext@display\st@flow\else%
           116 \ifx\omtext@title\@empty\begin{STtypedecEnv}\else\begin{STtypedecEnv}[\omtext@title]\fi%
           117 \ifx\sref@id\@empty\else\label{typedec.\sref@id}\fi
           118 \ifx\sref@id\@empty\sref@label@id{here}\else%
           119 \sref@label@id{\STpresent{\csname STtypedecEnvKeyword\endcsname}~\@currentlabel}\fi%
           120 \ignorespaces}
           121 {\ifx\omtext@display\st@flow\else\end{STtypedecEnv}\fi\omtext@post@skip}
           122 (/package)
definition The definition environment itself is quite similar to the other's but we need to
            set the \st@indef switch to suppress warnings from \st@def@target.
           123 (*package)
           124 \newif\ifst@indef\st@indeffalse
           125 \newenvironment{definition}[1][]{\metasetkeys{omtext}{#1}\sref@target\st@indeftrue%
           126 \ifx\omtext@display\st@flow\else%
           127 \ifx\omtext@title\@empty\begin{STdefinitionEnv}\else\begin{STdefinitionEnv}[\omtext@title]\fi\f
           128 \ifx\sref@id\@empty\sref@label@id{here}\else%
           129 \sref@label@id{\STpresent{\csname STdefinitionEnvKeyword\endcsname}~\@currentlabel}\fi%
           130 \ignorespaces}
           131 {\ifx\omtext@display\st@flow\else\end{STdefinitionEnv}\fi}
           132 \def\st@definition@kw{Definition}
           133 \theorembodyfont{\upshape}
           134 \mbox{ } [STtheoremAssEnv] {\tt ton@kw} \\
           135 (/package)
  notation We initialize the \def\st@notation@initialize{} here, and extend it with func-
            tionality below.
           136 (*package)
           137 \def\notemph#1{#1}
           138 \def\st@notation@terminate{}
           139 \def\st@notation@initialize{}
           140 \define@statement@env{notation}
           141 \def\st@notation@kw{Notation}
           142 \theorembodyfont{\upshape}
           143 \mbox{ } \mbox{$143 \rightarrow Env] {\tt STheoremAssEnv] {\tt st@notation@kw} } \\
```

144 (/package)

the next macro is a variant of the \sref@target macro provided by the sref package specialized for the use in the \definiendum, \defi, \defii, and \defiii macros. \st@def@target{ $\langle opt \rangle$ }{ $\langle name \rangle$ } makes a target with label  $sref@\langle opt\rangle@\langle modulename\rangle@target$ , if  $\langle opt\rangle$  is non-empty, else with the label sref@\(name\)@\(modulename\)@target. Also it generates the necessary warnings for a definiendum-like macro.

```
145 (*package)
146 \def\st@def@target#1#2{\def\@test{#1}%
147 \ifst@indef% if we are in a definition or such
148 \@ifundefined{mod@id}% if we are not in a module
149 {\PackageWarning{statements}{definiendum in unidentified module\MessageBreak
150 \protect\definiendum, \protect\defi,
151 \protect\defii, \protect\defiii\MessageBreak
152 can only be referenced when called in a module with id key}}%
153 {\edgh{@cd{\ifx}\owtext{@theory}\edgh{else}\owtext{@theory}fi}\%} \\
154 \edef\@@name{\ifx\@test\@empty{#2}\else{#1}\fi}%
156 \ifmetakeys@showmeta\metakeys@show@keys{\@@cd}{name:\@@name}\fi}%
157 \else% st@indef
158 \PackageError{statements}%
159 {definiendum outside definition context\MessageBreak
160 \protect\definiendum, \protect\defi,
161 \protect\defii, \protect\defiii\MessageBreak
162 do not make sense semantically outside a definition.\MessageBreak
163 Consider wrapping the defining phrase in a \protect\inlinedef}%
164 \fi}
165 (/package)
```

The \definiendum and \notatiendum macros are very simple.

\@termdef This macro is experimental, it is supposed to be invoked in \definiendum to define a macro with the definiendum text, so that can be re-used later in term assignments (see the modules package). But in the current context, where we rely on T<sub>F</sub>X groupings for visibility, this does not work, since the invocations of \definiendum are in definition environments and thus one group level too low. Keeping this for future reference.

```
166 (*package)
 167 \newcommand\@termdef[2][]{\def\@test{#1}%
 168 \end{indefined} {\end{indefined} {\end{indefined} {\end{indefined} {\end{indefined} } } $$ \end{indefined} $$$ \end{indefine
169 \termdef{\mod@id @\@@name}{#2}}}
170 (/package)
```

\definiendum

```
171 (*package)
172 \newcommand\definiendum[2][]{\st@def@target{#1}{#2}\defemph{#2}}
173 \newcommand\definiendum[2][]{\st@def@target{#1}{#2}\defemph{#2}}
174 (/package)
```

```
\notatiendum the notatiendum macro also needs to be visible in the notation and definition
                             environments
                           175 (*package)
                           176 \newcommand\notatiendum[2][]{\notemph{#2}}
                           177 (/package)
                                    We expand the LATEXML bindings for \defi, \defii and \defiii into two
                             instances one will be used for the definition and the other for indexing.
              \defi We split the \defi macro in two: \defi does the definiendum bit and \@defi
                             handles the last optional argument and does the indexing. The information flow
                             between them goes via the local \Ophrase macro.
                           178 (*package)
                            179 \end{defi[2][} {\end{defi[2]}[} {\end{defi[2]}[} {\end{defi[2]}} \end{defi[2]} 
                           180 \newcommand\@defi[1][]{\ifdef@index\omdoc@index[#1]{\@phrase}\fi\xspace}
                           181 \end{tabular} 181 \end{tabular} 181 \end{tabular} 181 \end{tabular} 2s \end{tabular} 181 \end{ta
                           182 (/package)
            \adefi Again we split the \adefi macro into two parts: \adef does the definiendum bit
                             and \@adefi handles the last optional argument and does the indexing.
                           183 (*package)
                           184 \newcommand\adefi[3][] {\\def\\@name{#1}\\def\\@verb{#3}\%
                           185 \st@def@target{#1}{#3}\defemph{#2}\@adefi}
                           186 \newcommand\@adefi[1][]{%
                           187 \ifdef@index%
                           188 \ifx\@name\@empty\omdoc@index[#1]{\@verb}%
                           189 \else\omdoc@index[at=\@name,#1]{\@verb}\fi%
                           190 \fi\xspace}
                           191 (/package)
            \defii
                           192 (*package)
                           193 \newcommand\@defii[1][]{\ifdef@index\@twin[#1]{\@pone}{\@ptwo}\fi\xspace}
                           194 \newcommand\defii[3][]{\def\q}one{\#2}\def\q}%
                           195 \st@def@target{#1}{#2-#3}\defemph{#2 #3}\@defii}
                           196 \newcommand\defiis[3][]{\def\@pone{#2}\def\@ptwo{#3}%
                           197 \st@def@target{#1}{#2-#3}\defemph{#2 #3s}\@defii}
                           198 (/package)
          \adefii analogous to \adefi
                           199 (*package)
                           200 \newcommand\adefii[4][]{\def\@name{#1}\def\@pone{#3}\def\@ptwo{#4}%
                           201 \st@def@target{#1}{#3-#4}\defemph{#2}\@adefii}
                           202 \newcommand\@adefii[1][]{%
                           203 \ifdef@index%
                           204 \ifx\@name\@empty\@twin[#1]{\@pone}{\@ptwo}%
                           205 \else\@twin[at=\@name,#1]{\@pone}{\@ptwo}\fi%
                           206 \fi\xspace
```

207 (/package)

```
\defiii similar to \defii
                        208 (*package)
                        209 \newcommand\defiii[4][]{\def\@pone{#2}\def\@ptwo{#3}\def\@pthree{#4}%
                        210 \st@def@target{#1}{#2-#3-#4}\defemph{#2 #3 #4}\@defiii}
                        211 \newcommand\@defiii[1][]{\ifdef@index\@atwin[#1]{\@pone}{\@ptwo}{\@pthree}\fi\xspace}
                        212 \newcommand\defiiis [4] [] {\def\@pone{#2}\def\@ptwo{#3}\def\@pthree{#4}%
                        213 \st@def@target{#1}{#2-#3-#4}\defemph{#2 #3 #4s}\@defiii}
                        214 (/package)
    \adefiii
                        215 (*package)
                        216 \end{align} $$216 \end{a
                        217 \t @def@target{#1}{#3-#4-#5}\defemph{#2}\@adefiii}
                        218 \newcommand\@adefiii[1][]{%
                        219 \ifdef@index%
                        220 \ifx\@name\@empty\@atwin[#1]{\@pone}{\@ptwo}{\@pthree}%
                        221 \else\@atwin[at=\@name,#1]{\@pone}{\@ptwo}{\@pthree}\fi%
                        222 \fi\xspace}
                        223 (/package)
  \inlineex
                        224 (*package)
                        225 \newcommand\inlineex[2][]{\metasetkeys{omtext}{#1}%
                        226 \sref@target\sref@label@id{here}#2}
                        227 (/package)
\inlineass
                        228 (*package)
                        229 \newcommand\inlineass[2][]{\metasetkeys{omtext}{#1}%
                        230 \sref@target\sref@label@id{here}#2}
                        231 (/package)
\inlinedef
                        232 (*package)
                        233 \newcommand\inlinedef[2][]{\metasetkeys{omtext}{#1}%
                        234 \if@in@omtext\else% we are not in an omtext or statement
                        235 \PackageError{modules}{\protect\inlinedef\space outside a statement!}%
                        236 {Try wrapping the paragraph in a\MessageBreak
                        237 \protect\begin{omtext}, \protect\begin{assertion}, \protect\begin{axiom}, ... \MessageBreak
                        238 whatever is suitable semantically}\fi%
                        239 \sref@target\sref@label@id{here}\st@indeftrue #2}
                        240 (/package)
                                         Cross-Referencing Symbols and Concepts
    \termref We delegate to the worker macro \st@termref after setting the default for the cd
                           key.
```

241 (\*package)

```
242 \addmetakey*{termref}{cd}
            243 \addmetakey*{termref}{cdbase}
            244 \addmetakey*{termref}{name}
            245 \texttt{\addmetakey*\{termref\}\{role\}}
            246 \newcommand\termref[2][]{\metasetkeys{termref}{#1}%
            247 \ifx\termref@cd\@empty\def\termref@cd{\mod@id}\fi%
            248 \text{st@termref{#2}}
            249 (/package)
             The next macro is where the actual work is done.
\st@termref If the cdbase is given, then we make a hyper-reference, otherwise we punt to
             \mod@termref, which can deal with the case where the cdbase is given by the
             imported cd.
            250 (*package)
            251 \newcommand\st@termref[1]{\ifx\termref@name\@empty\def\termref@name{#1}\fi%
            252 \ifx\termref@cdbase\@empty\mod@termref\termref@cd\termref@name{#1}%
            253 \else\sref@href@ifh\termref@cdbase{#1}\fi}
            254 (/package)
     \tref*
            255 (*package)
            256 \newcommand\atrefi[3][]{\def\@test{#1}%
            257 \ifx\@test\@empty\termref[name=#3]{#2}\else\termref[cd=#1,name=#3]{#2}\fi}
            258 \newcommand\atrefii[4][]{\atrefi[#1]{#2}{#3-#4}}
            259 \newcommand\atrefiii[5][]{\atrefi[#1]{#2}{#3-#4-#5}}
     \tref*
            260 \newcommand\trefi[2][]{\atrefi[#1]{#2}{#2}}
            261 \newcommand\trefii[3][]{\atrefi[#1]{#2 #3}{#2-#3}}
            262 \newcommand\trefiii[4][]{\atrefi[#1]{#2 #3 #4}{#2-#3-#4}}
            263 \newcommand\trefis[2][]{\atrefi[#1]{#2s}{#2}}
            264 \newcommand\trefiis[3][]{\atrefi[#1]{#2 #3s}{#2-#3}}
            265 \newcommand\trefiiis[4][]{\atrefi[#1]{#2 #3 #4s}{#2-#3-#4}}
            266 (/package)
                 Now we care about the configuration switches, they are set to sensible values,
             if they are not defined already. These are just configuration parameters, which
             should not appear in documents, therefore we do not provide LATEXML bindings
             for them.
     267 (*package)
            268 \providecommand{\termemph}[1]{#1}
            269 \providecommand{\defemph}[1]{{\textbf{#1}}}
            270 \providecommand{\stDMemph}[1]{{\textbf{#1}}}
            271 (/package)
```

```
EdN:7
                     \term The \term macro is used for wiki-style dangling links with editor support.
                           272 (*package)
                           273 \newcommand\term[2][]{\def\@test{#1}%
                           274 \ifx\@test\@empty\else
                           275 \@ifundefined{module@defs@#1}{\PackageWarning{statements}%
                           276 {{\protect\term} specifies module #1 which is not in
                                scope\MessageBreak import it via e.g. via \protect\importmhmodule}}{}
                           278 \fi%
                           279 \PackageWarning{statements}%
                           280 {Dangling link (\protect\term) for "#2" still needs to be specified}%
                           281 \texttt{\textcolor{blue}{\underline{#2}}} \\
                           282 (/package)
                   \symref The \symref macros is quite simple, since we have done all the heavy lifting in
                            the modules package: we simply apply \mbox{mod@symref}(arq1) to (arq2).
                           283 (*package)
                            284 \newcommand\symref[2]{\@nameuse{mod@symref@#1}{#2}}
                            285 (/package)
                                  Deprecated Functionality
                            In this section we centralize old interfaces that are only partially supported any
                            more.
                    \
                           286 (*package)
                           287 \newcommand\defin[2][]{\defi[#1]{#2}%
                           288 \PackageWarning{statements}{\protect\defin\space is deprecated, use \protect\defi\space instead
                           289 \newcommand\twindef[3][]{\defii[#1]{#2}{#3}%
                           290 \PackageWarning{statements}{\protect\twindef\space is deprecated, use \protect\defii\space inst
                           291 \newcommand\atwindef[4][]{\defiii[#1]{#2}{#3}{#4}%
                           293 \newcommand\definalt[3][]{\adefi[#1]{#2}{#3}%
                           294 \PackageWarning{statements}{\protect\definalt\space is deprecated, use \protect\adefi\space ins
                           295 \newcommand\twindefalt[4][]{\adefii[#1]{#2}{#3}{#4}%
                           296 \PackageWarning{statements}{\protect\twindefalt\space is deprecated, use \protect\adefii\space
                           297 \newcommand\atwindefalt[5][]{\adefiii[#1]{#2}{#3}{#4}{#5}%
                           298 \PackageWarning{statements}{\protect\atwindefalt\space is deprecated, use \protect\adefiii\spac
                    \ensuremath{\mbox{\width}}
                           299 \newcommand\twinref[3][]{\trefii[#1]{#2}{#3}%
                           300 \PackageWarning{statements}{\protect\twinref\space is deprecated, use \protect\trefii\space ins
```

303 (/package)

302 \PackageWarning{statements}{\protect\atwindef\space is deprecated, use \protect\trefiii\space i

301 \newcommand\atwinref[4][]{\atrefiii[#1]{#2}{#3}{#4}%

<sup>&</sup>lt;sup>7</sup>EDNOTE: MK: document above

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