

$$k \log \|I - M^{-1}A\| \leq \log \epsilon - \log \|e_0\|$$

Since  $\log \|I - M^{-1}A\| < 0$ , then

$$k \geq \frac{\log \epsilon - \log \|e_0\|}{\log \|I - M^{-1}A\|}$$

$$k \geq \frac{\log(\epsilon / \|e_0\|)}{\log \|I - M^{-1}A\|}$$

\*) Since  $\rho(I - M^{-1}A)$  is the largest absolute value of the eigen values of  $(I - M^{-1}A)$ , and the number of iterations is given by

$$k \geq \frac{\log(\epsilon / \|e_0\|)}{\log \|I - M^{-1}A\|}$$

$$k \geq \frac{\log \epsilon}{\log \|I - M^{-1}A\|} - \frac{\log \|e_0\|}{\log \|I - M^{-1}A\|}$$