

```

%The program uses idct and dct ad procedures (a)-(c) to solve problem from
%4(c)

a=0; b=2*pi;
m=99;

h=(b-a)/(m+1);
j=[0:m+1]';
xj=a+j*h;
k=[1:m+1]';

%take v(0) to be 0.000002 since at k=0, uap is undefined, so uap(0) can be
%choosen arbitrary.
v=[0.000002;(2*cos((pi*k)/(m+1)))-2];
f=-4*cos(2*xj);

%obtaining fcap
fcap=dct(f);

%obtaining uap
uap=(h^2)*fcap./v;

%obtaining u
uap=idct(uap);

%relative two norm
L2norm=RelL2Norm(uex,uap);
fprintf('%10s %16.8e\n','Relative two norm =',L2norm);
fprintf('According to the results from the two graphs, we can conclude that the results are the same.');
```

%ploting the solution of u

```

figure(1);
plot(xj,uap,'*');
hold on;
uex=u_ex(xj);
plot(xj,uex);
legend('Numerical','true solution')
ylabel('u(x)');
xlabel('x');
title('A graph of u against x');
```

figure(2);

```

err=er(uex,uap);
plot(xj,err);
ylabel('error');
xlabel('x');
title('A graph of error against x');
```

%exact solution

```

function uexact=u_ex(xj)
uexact=cos(2*xj);
end
```

%error

```

function error=er(uex,uap)
error=abs(uex - uap);
end
```

%relative two norm of the error

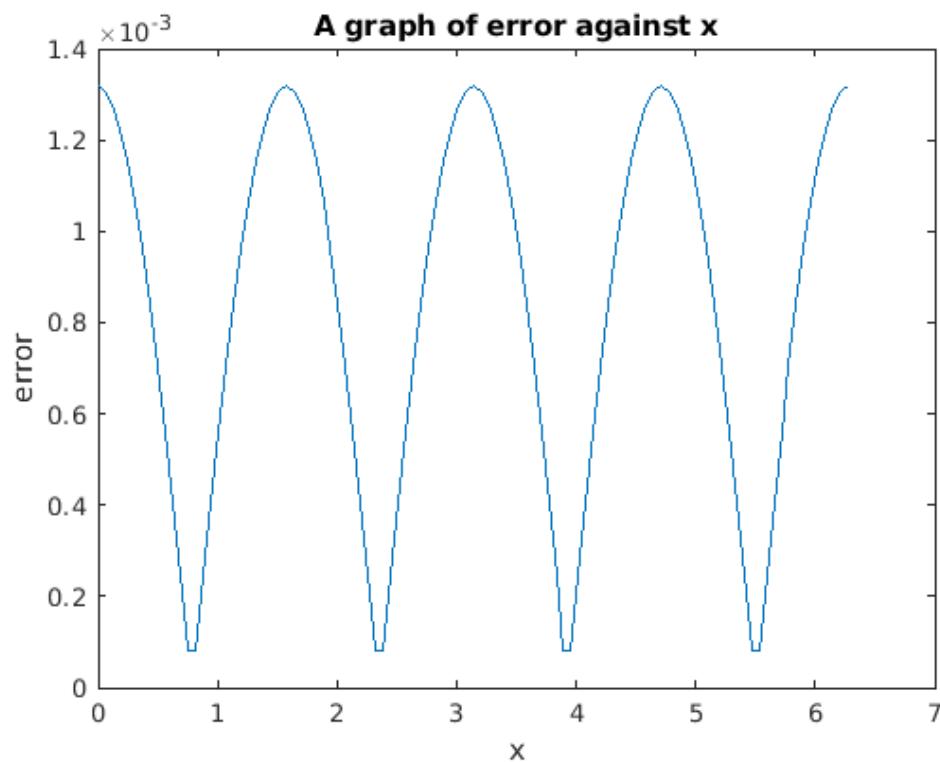
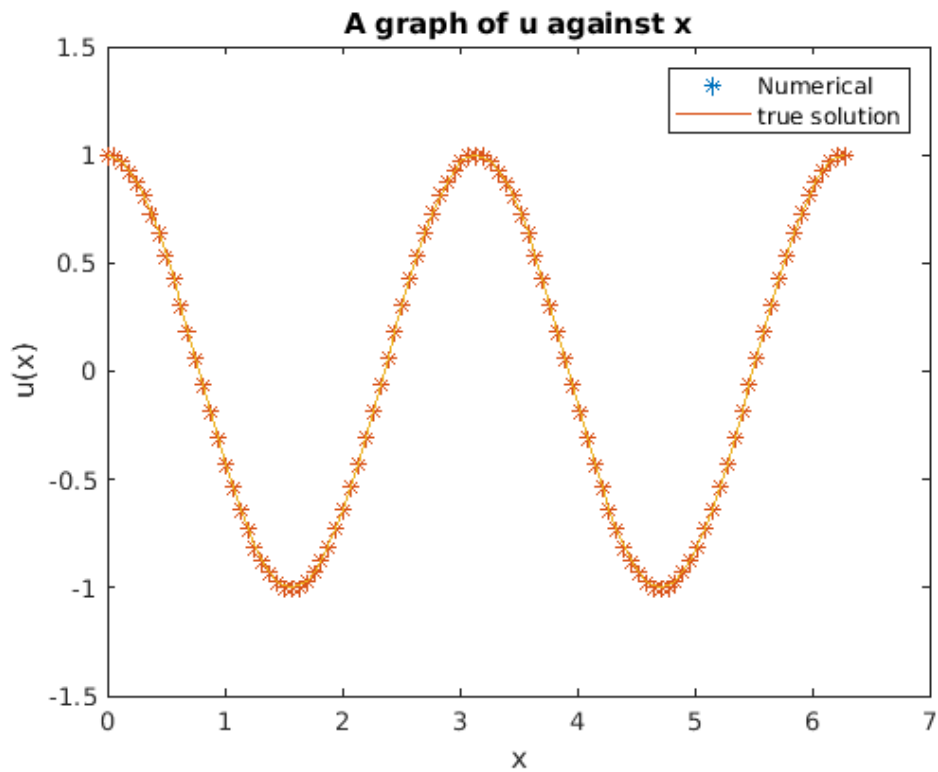
```

function L2 = RelL2Norm(uex,uap)
```

```
R = (uex - uap).^2;  
L2 = sqrt(sum(R)/sum(uap.^2));  
end
```

Relative two norm = 1.31525476e-03

According to the results from the two graphs, we can conclude that the results are the same.



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