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clear all;
close all;

%Setting up variables for plotting purposes.
LW = 'LineWidth' ;
lw = 1;
clr = [221 221 221]/255;
xlabel = 'Re( $ \ xi$ )';
ylabel = 'Im( $ \ xi$ )';
intrptr = 'Interpreter';
ltx = 'Latex';

%Stability domain for the method.
% Define the unit circle in the complex plane
N = 1000;
th = linspace(0,2*pi,N);
w = exp(1i*th);

%solution of the characteristic equation in terms of $ \xi$
f=@(w) 3*w.*(w.^2)-1)./(7*(w.^2)-2*w+1);
g=@(w) 12*(w.^3 - w.^2)./(23*w.^2 - 16*w + 5);

%Evaluate $f$ at the points on the unit circle and then plot the results:
xi = f(w);

plot(xi, 'k-', LW,lw), hold on
fill (real(xi), imag(xi), clr)
plot([min(real(xi)) max(real(xi))],[0 0],'b--',LW,lw)
plot([0 0], [min(imag(xi)) max(imag(xi))],'b--',LW,lw)
xlabel(xlbl,intrptr, ltx), ylabel(ylbl, intrptr,ltx)
xlim([min(real(xi))-0.3 max(real(xi))+0.3])
ylim([min(imag(xi))-0.3 max(imag(xi))+0.3])

%AB3
xii = g(w);
plot(xii, 'k-', LW,lw), hold on
fill (real(xii), imag(xii), clr)
plot([min(real(xii)) max(real(xii))],[0 0],'b--',LW,lw)
plot([0 0], [min(imag(xii)) max(imag(xii))],'b--',LW,lw)
xlabel(xlbl,intrptr, ltx), ylabel(ylbl, intrptr,ltx)
xlim([min(real(xii))-0.3 max(real(xii))+0.3])
ylim([min(imag(xii))-0.3 max(imag(xii))+0.3])

title('Stability Domain')
grid on

daspect([1 1 1]), hold off

%check for the root condition at a point inside and outside the apperent
%domain.

%compare
xii = 0.2 + 0.8*1i; %inside
xio = 0.2 - 0.4*1i; %outside
coeffii = [1 -7/3*xii (-1+2/3*xii) -xii/3];
coeffio = [1 -7/3*xio (-1+2/3*xio) -xio/3];

ep1=abs(roots(coeffii))
ep2=abs(roots(coeffio))

%for AB3
xiIA = 0.2 + 0.2*1i; %inside
xiOA = -0.4 - 0.6*1i; %outside
coeffiIA = [12 (-1-23)*xiIA (16*xiIA) -5*xiIA];
coeffiOA = [12 (-1-23)*xiOA (16*xiOA) -5*xiOA];
ep1A=abs(roots(coeffiIA))
ep2A=abs(roots(coeffiOA))

%intersection between the two domains
xis = 0.09534 + 0.7597*1i;
xio = 0.2 - 0.4*1i; %outside
coeffiis = [1 -7/3*xis (-1+2/3*xis) -xis/3];
coeffio = [1 -7/3*xio (-1+2/3*xio) -xio/3];

ep1s=abs(roots(coeffiis))
ep2s=abs(roots(coeffio))

fprintf('Compare and Contrast\n')
fprintf('Most of the region of the stability domain for AB3 lines in the negative real part of x and both in the negative and \n positive imagin
fprintf('Would you ever want to use this method?\n');

fprintf('I would never want to use this method because checking for root condition at the point\n inside to and outside to the apperent domain, a

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ep1 =

    1.1710
    1.1915
    0.1970

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ep2 =

    1.2252

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0.8707  
0.1397

ep1A =

0.7233  
0.4436  
0.3673

ep2A =

1.8750  
0.4071  
0.3936

ep1s =

1.3172  
1.0454  
0.1853

ep2s =

1.2252  
0.8707  
0.1397

Compare and Contrast

Most of the region of the stability domain for AB3 lines in the negative real part of  $x$  and both in the negative and positive imaginary part of  $x$ , while for the other LMS method, the stability domain lies in the positive real part of  $x$  and also both in the positive and negative imaginary part of  $x$ . However these two have a region in common.

Would you ever want to use this method?

I would never want to use this method because checking for root condition at the point inside to and outside to the apparent domain, at least one root has a modulus greater than one, hence the method is unconditionally unstable for all epsilon, inside and outside the domain.

