12/8/2020 BDF2

```
% The program uses BDF2 for the time integratorl instead of the trapezoidal
% Rule.
% f : function representing intial condition
\%~\text{g0} and g1 : function represents boundary conditions
% tspan : time span over
% \ N : Number of time steps
\%\ m : Number of points for the uniform spatial discretisation.
% u : Approximate solution at each time step (matrix)
% t : Vector containing all time steps
% x : Vector containing the spatial discretization.% This function Numerically solves the 1-D heat equation using the
% Crank-Nicolson scheme
% input
function [u,t,x] = BDF2(f,g0,g1,tspan,alp,N,m)
h = 1/(m+1);
k = tspan/N;
r = (2*alp*k)/(3*h^2);
%space and time steps
x = 0:h:1;
t = 0:k:tspan;
%Crank-Nicolson
u1 = cnhteq(f,g0,g1,tspan,alp,N,m);
U = zeros(m+2, m+2);
gl = zeros(m,1);
U0 = f(x);
U(1,:) = U0;
U1 = u1(2,:);
U(2,:) = U1;
%Matrix Coefficients
a= (1+2*r);
b = r:
\% Using the sparse library to transform A
A = sparse(toeplitz([a -b zeros(1, m-2)]));
for n = 3: N+1
    gl(1) = gO(t(n));
    gl(m) = gl(t(n));
    Un1 = U0(2:m+1)';
    Un2= U1(2:m+1);
    % The Right Hand Side
    B = (4/3)*Un2 - (1/3)*Un1 + r*gl;
   Un = A \setminus B;
    % Treating the boundary conditions
    Un = [gl(1), Un', gl(m)];
    U(n,:) = Un;
    %update solution
    U0 = U1;
   U1 = Un;
end
u = U;
end
```

```
Not enough input arguments.

Error in BDF2 (line 19)
h = 1/(m+1);
```

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