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% Numerical approximation to Poisson's equation over the square [a,b]x[a,b] with
% Dirichlet boundary conditions. Uses a uniform mesh with (n+2)x(n+2) total
% points (i.e, n interior grid points).
% Input:
%   ffun : the RHS of poisson equation (i.e. the Laplacian of u).
%   gfun : the boundary function representing the Dirichlet B.C.
%   a,b : the interval defining the square
%   m : m+2 is the number of points in either direction of the mesh.
% Output:
%   u : the numerical solution of Poisson equation at the mesh points.
%   x,y : the uniform mesh.

function [u,x,y] = fd2poissonsp(ffun,gfun,a,b,m)

h = (b-a)/(m+1); % Mesh spacing

[x,y] = meshgrid(a:h:b); % Uniform mesh, including boundary points.

idx = 2:m+1;
idy = 2:m+1;

% Compute boundary terms, south, north, east, west
ubs = feval(gfun,x(1,1:m+2),y(1,1:m+2)); % Include corners
ubn = feval(gfun,x(m+2,1:m+2),y(m+2,1:m+2)); % Include corners
ube = feval(gfun,x(idy,m+2),y(idy,m+2)); % No corners
ubw = feval(gfun,x(idy,1),y(idy,1)); % No corners

% Evaluate the RHS of Poisson's equation at the interior points.
f = feval(ffun,x(idy,idx),y(idy,idx));

% Adjust f for boundary terms
f(:,1) = f(:,1) - ubw/h^2; % West
f(:,m) = f(:,m) - ube/h^2; % East
f(1,1:m) = f(1,1:m) - ubs(idy)/h^2; % South
f(m,1:m) = f(m,1:m) - ubn(idy)/h^2; % North

f = reshape(f,m*m,1);

%Using sparse matrix capabilities to form D2x and D2y matrices
I = eye(m);
e = ones(m,1);
e1 = zeros(m,1);
%D2x
T = spdiags([e1 -2*e1 e1],[-1 0 1],m,m);
S = spdiags([e e],[-1 1],m,m);
D2x = (1/h^2)*(kron(I, T) + kron(S,I));
%D2y
Ty = spdiags([e -2*e e],[-1 0 1],m,m);
Sy = spdiags([e1 e1],[-1 1],m,m);
D2y = (1/h^2)*(kron(I, Ty) + kron(Sy,I));

% Solve the system
u = (D2x + D2y)\f;

% Convert u from a column vector to a matrix to make it easier to work with
% for plotting.
u = reshape(u,m,m);

% Append on to u the boundary values from the Dirichlet condition.
u = [ubs;[ubw,u,ube];ubn];

end

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Not enough input arguments.

Error in fd2poissonsp (line 15)  
h = (b-a)/(m+1); % Mesh spacing

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Published with MATLAB® R2020a