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%Stability of linear systems.

fprintf('4a).\n');
%(a).Does this imply that  $x^{\wedge}$  is close to the exact solution  $x$ ?
fprintf('No, since the residual values are not near zero, then  $x_{hat}$  is not close to the exact solution. \n\n');

fprintf('4b).\n');
%Matrix A
A = 1./hankel(2:6,6:10);

%vector b
b = [0.882 0.744 0.618 0.521 0.447]';

%Accurate solution to the system
x = A\b

fprintf('\n');
fprintf('4c).\n');
%Obtain a condition number for A using this same software again
%condition number
C = cond(A)
fprintf('Since the Condition number of A is large then the system is ill-conditioned, therefore a small perturbation \n to the RHS can lead to large c|

fprintf('Consider a small perturbation on, db. \n');

db = [0.000002 0.000004 0.000008 0.00001 0.00007]'

Rl=C*norm(db,2)/norm(b,2)

%ddx due to perturbation on the RHS
ddx = x + A\db

%Relative error
RE = norm((ddx-x),2)/norm(x,2)

fprintf('Since the relative Error,RE<=Rl, and large then indeed this confirms that a very small residual\n after the system being perturbed on the RHS

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4a).
No, since the residual values are not near zero, then x_{hat} is not close to the exact solution.

4b).

$x =$

```

-2.5200000000000023
 5.0400000000000505
 2.5199999999998072
 7.5600000000002508
-10.080000000001057

```

4c).

$C =$

```

1.535043895304634e+06

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Since the Condition number of A is large then the system is ill-conditioned, therefore a small perturbation to the RHS can lead to large change in the system.

Consider a small perturbation on, db.

$db =$

```

1.0e-04 *

0.0200000000000000
0.0400000000000000
0.0800000000000000
0.1000000000000000
0.7000000000000000

```

$Rl =$

```

74.051562320624924

```

$ddx =$

```

-2.145300000001764
 0.551040000023523
18.217919999913303
-13.361039999880891
-0.667800000054639

```

RE =

2.007030225261566

Since the relative Error, $RE \leq R1$, and large then indeed this confirms that a very small residual after the system being perturbed on the RHS, is big enough to allow for the solution to be as far away.