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% Numerical approximation to Poisson's equation over the square [a,b]x[a,b] with
% Dirichlet boundary conditions. Uses a uniform mesh with (n+2)x(n+2) total
% points (i.e, n interior grid points) on nine node.
% Input:
      ffun : the RHS of poisson equation (i.e. the Laplacian of u).
      gfun: the boundary function representing the Dirichlet B.C.
%
       a,b : the interval defining the square
%
         m : m+2 is the number of points in either direction of the mesh.
% Ouput:
         u : the numerical solution of Poisson equation at the mesh points.
%
%
       x,y: the uniform mesh.
function [u,x,y] = SOR(ffun,gfun,a,b,m,w)
h = (b-a)/(m+1); %mesh spacing
tol = 1e-16: %relative residual
maxiter = 10000; %maximum value of k
[x,y] = meshgrid(a:h:b); %Uniform mesh, including boundary points.
idx = 2:m+1;
idy = 2:m+1;
dx = 1:m+2;
dy = 1:m+2;
u = zeros(m+2);
% Compute boundary terms, south, north, east, west
            = feval(gfun,x(1,1:m+2),y(1,1:m+2));
u(1,1:m+2)
                                                          % Include corners
u(m+2, 1:m+2) = feval(gfun, x(m+2, 1:m+2), y(m+2, 1:m+2)); % Include corners
u(idy,m+2) = feval(gfun,x(idx,m+2),y(idy,m+2));
                                                           % No corners
u(idy,1)
              = feval(gfun,x(idy,1),y(idy,1));
                                                             % No corners
% Evaluate the RHS of Poisson's equation at the interior points.
f = feval(ffun, x(dy, dx), y(dy, dx));
for k = 0:maxiter
    %Iterate
    for j = 2:m+1
        for i = 2:m+1
            u(i,j) = (1-w)*u(i,j)+(w/5)*(u(i-1,j)+u(i+1,j)+u(i,j-1)+u(i,j+1))...
                +(w/20)*(u(i-1,j-1)+u(i+1,j-1)+u(i+1,j+1)+u(i-1,j+1))...
            -(h^2/20)*w*(4*f(i,j)+0.5*(f(i-1,j)+f(i+1,j)+f(i,j-1)+f(i,j+1)));
        end
    end
    %Compute the residual
    residual = zeros(m+2);
    for j = 2:m+1
        for i = 2:m+1
            residual(i,j) = -20*u(i,j)+4*(u(i-1,j)+u(i+1,j)+u(i,j-1)+u(i,j+1))...
            +(u(i-1,j-1)+u(i+1,j-1)+u(i+1,j+1)+u(i-1,j+1))...
            -(h^2)*(4*f(i,j)+0.5*(f(i-1,j)+f(i+1,j)+f(i,j-1)+f(i,j+1)));
        end
    end
    %Determine if convergence has been reached
        if norm(residual(:),2) < tol*norm(f(:),2)</pre>
                break
    end
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end
end
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Not enough input arguments.

Error in SOR (line 15)
h = (b-a)/(m+1); %mesh spacing
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