Name: Brian KYANJO Comprehension 9-5 Chass: GEOPH 605 Accuracy 10 Presentation 5
Consider the following quadratic polynomial 2405 ylt) = m, + m/4 - 1/m3+2
y(t)=m,+ mb+- 1 m3+
Stimate: m, m, m, m, m, m, s Stormal whetak: y(E), s=1,, m
(a) Shan m =3, altotule planed at t, to all t3
$\begin{bmatrix} 1 & t_1 & -y_1 & t_1 \\ 1 & t_2 & -y_2 \\ 1 & t_3 & -y_3 \end{bmatrix} = \begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix}$
(b) flum m=2, altitude themal and ty, and tz
$\begin{bmatrix} 1 & t_1 & -\frac{1}{2}t_1^2 \\ 1 & t_2 & -\frac{1}{2}t_2^2 \end{bmatrix} \begin{bmatrix} m_1 \\ m_2 \\ m_3 \end{bmatrix} = \begin{bmatrix} y_1 \\ y_2 \end{bmatrix}$
2. Assume that
Mary = [0-18]

```
mtrue = [0.18 16.21 9.81]' %true m
```

```
\begin{array}{rl} \mathsf{mtrue} = 3 \times 1 \\ 0.1800 \\ 16.2100 \\ 9.8100 \end{array}
```

```
m = 20; %rows
n = 3; %columns

tj = linspace(0,3,m) %temporal domain
```

```
tj = 1×20
0 0.1579 0.3158 0.4737 0.6316 0.7895 0.9474 1.1053 · · ·
```

N_{0.2} a)

(i). Form G

```
%forming G matrix
G = zeros(m,n); %m by n container

for i = 1:n
    for j = 1:m
        G(j,1) = 1;
        G(j,2) = tj(j);
        G(j,3) = -0.5*tj(j)^2;
    end
end
disp(G)
```

```
1.0000
          0.1579
                  -0.0125
1.0000
1.0000
          0.3158
                  -0.0499
1.0000
          0.4737
                  -0.1122
          0.6316
                  -0.1994
1.0000
                  -0.3116
1.0000
          0.7895
                  -0.4488
1.0000
          0.9474
          1.1053
                  -0.6108
1.0000
1.0000
          1.2632
                  -0.7978
1.0000
          1.4211
                  -1.0097
1.0000
          1.5789
                  -1.2465
1.0000
          1.7368
                  -1.5083
          1.8947
                  -1.7950
1.0000
                  -2.1066
1.0000
          2.0526
1.0000
          2.2105
                  -2.4432
1.0000
          2.3684
                  -2.8047
          2.5263
                  -3.1911
1.0000
          2.6842
                  -3.6025
1.0000
1.0000
          2.8421
                  -4.0388
1.0000
          3.0000
                  -4.5000
```

(ii). Form dtrue

```
dtrue = G*mtrue;
disp(dtrue)
```

```
0.1800
2.6172
```

^{4.8098}

```
6.7579
8.4613
9.9202
11.1346
12.1043
12.8295
13.3102
13.5462
13.5377
13.2846
12.7869
12.0447
11.0579
9.8265
8.3506
6.6301
4.6650
```

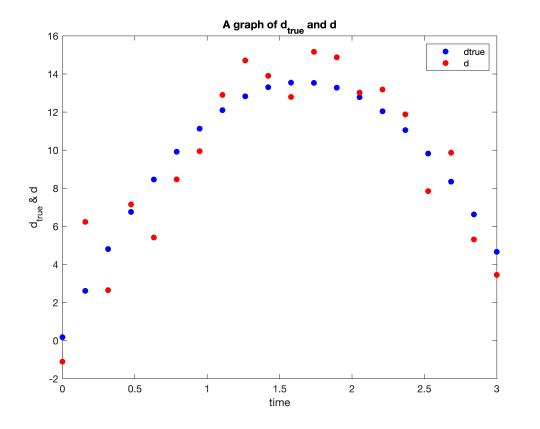
(iii). Form noisy data d

```
mean = 0;
std = 2;
%noise
noise = 2*randn(m,1);
%noise data
d = dtrue + noise;
disp(d)
```

```
-1.1014
 6.2349
 2.6501
7.1562
5.4193
8.4730
9.9481
12.9070
14.7138
13.9111
12.8001
15.1687
14.8824
13.0273
13.1872
11.8835
7.8526
9.8697
5.3157
3.4572
```

Plot dtrue and d as points on the same graph

```
figure(1)
plot(tj,dtrue,'b.','MarkerSize',20)
hold on
plot(tj,d,'r.','MarkerSize',20)
title('A graph of d_{true} and d')
legend('dtrue','d')
xlabel('time');
```



Discuss the difference between the data

Comparing the trud data, dtrue, (blue) and the noisy data, d, (red), its clearly shown d has alot of dispersed data points due to the effect of noise while dtrue is a smooth curve without any disturbances. Even though the noisy data is distorted it will still depicts the trend of the true data.

N_{0.2} b)

 $m = G \backslash d$

Solve Gm = d for m and plot y(t) using m and mtrue

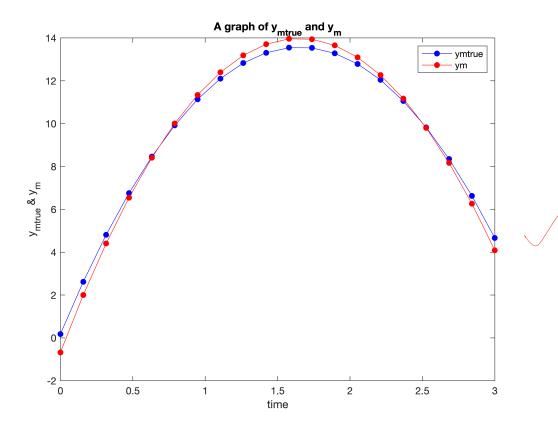
```
m = 3×1
    -0.6776
    17.8078
    10.8129

%function
y = @(t,m1,m2,m3) m1 + m2*t - 0.5*m3*t.^2;

%using mtrue
ymtrue = y(tj, mtrue(1), mtrue(2), mtrue(3));
%using m
ym = y(tj, m(1), m(2), m(3));

%plot y
figure(2)
```

```
plot(tj,ymtrue,'b.-','MarkerSize',20)
hold on
plot(tj, ym,'r.-','MarkerSize',20)
title('A graph of y_{mtrue} and y_{m}')
legend('ymtrue','ym')
xlabel('time');
ylabel('y_{mtrue} & y_{m}')
```



Discuss the difference between the trajectories.

There is a discrepancy between the trajectories: ymtrue (blue) and ym (red) obtained using mtrue and m values respectively. This is due to the noisy data ,d, used to obtain m and the forward model (y(t)) used to obtain y which is approximate, hence even the trajectory wont fit the the observed trajectory (ytrue) due to the distorted values of m. Therefore for what ever values of the m, the trajectories will never fit each other but will always have the same trend.