APPENDDIX

```
sig = @(t) (1e-3)*exp(t);
mprior = [2.5 0.5]';
CM = [6.7 0; 0 0.07];
tmean = [2.5411;0.2595];

Y = @(t,m) (m(1).*exp(m(2).*t));
t = [1 2 4 5 8]';
y = [3.2939 4.2699 7.1749 9.3008 20.259]';

J = @(t,m) [(exp(m(2)*t)), (m(1)*t.*exp(m(2)*t))]; %exact jacobian

max_iter = 1e6;
tol = 1e-7;

warning('off','all')

%generate roughening matrices
n =2;
L0 = eye(n);
N0.1 a)
% convariance matrix
CD = (1e-6)*[0.7 0 0 0 0; 0 0.08 0 0 0;0 0 0.3 0 0; 0 0 0 0.1 0;0 0 0 0 0.2];
func = @(CD,CM,mprior,m) [(CD^(-0.5))*Y(t,m);(CM^(-0.5))*m] - [(CD^(-0.5))*y;(CM^(-0.5))*mprior];
jac = @(CD,CM,m) [(CD^(-0.5))*J(t,m); CM^(-0.5)];

[MAP, iter] = lm(CD,CM,func, jac, mprior, tol, max_iter);
disp(['Resulting MAP estimates = [',num2str(MAP'),']']);
disp(['Resulting number of iterations = ',num2str(iter)]);
b)
[m,n] = size(J(t,mprior));
Im = eye(m);
CD = (sig(t).^2).*Im;

[MAP, iter] = lm(CD,CM,func, jac, mprior, tol, max_iter);
disp(['Resulting MAP estimates = [',num2str(MAP'),']']);
disp(['Resulting number of iterations = ',num2str(iter)]);
N0.2
mprior = tmean -  0.25*tmean;
stdm =  0.25*tmean;
CM = diag(stdm.^2)
%noise in the data
stdd = Y(t,tmean) - y;

CD = diag(stdd.^2)
[MAP, iter] = lm(CD,CM,func, jac, mprior, tol, max_iter)
disp(['Resulting MAP estimates = [',num2str(MAP'),']']);
disp(['Resulting number of iterations = ',num2str(iter)]);
% Covariance matrix
C = inv(J(t,MAP)'*(inv(CD))*J(t,MAP) + inv(CM));
covariance_matrix = C
```

```matlab
% %confidence interval
za = 1.96; % 95% confidence interval

% first parameter
s1 = sqrt(C(1,1)); % standard deviation

% confidence intervals
format long
c1 = MAP(1) - za*s1;
c2 = MAP(1) + za*s1;

cf = [c1 c2];
disp(['Resulting cofidence_interval for the first estimate =  [',num2str(cf,16),']']);

% Second parameter
s2 = sqrt(C(2,2)); % standard deviation

% confidence intervals
c11 = MAP(2) - za*s2;
c22 = MAP(2) + za*s2;

cs = [c11 c22];
disp(['Resulting cofidence_interval for the first estimate =  [',num2str(cs,16),']']);

%Correlation matrix
rho1 = C(1,1)/sqrt(C(1,1)*C(1,1));
rho12 = C(1,2)/sqrt(C(1,1)*C(2,2));
Correlation_matrix = [rho1 rho12;rho12 rho1]
%Linearised ellipsoid
Delta = chi2inv(0.95,2); %Delta2

figure(1)
plot_ellipse(Delta,C,MAP); hold on
plot(MAP(1),MAP(2),'.r',MarkerSize=17)
grid on
title('Error Ellipsoid')
xlabel('MAP_1'); ylabel('MAP_2')
```