## No.2 Use the discrepancy principle and the regularized discrepancy principle to find values for a in both first and second order Tikhonov regularization.

#### Using the discrepancy principle

alpha11 = 2.5058e-05alpha12 = 2.5058e-05

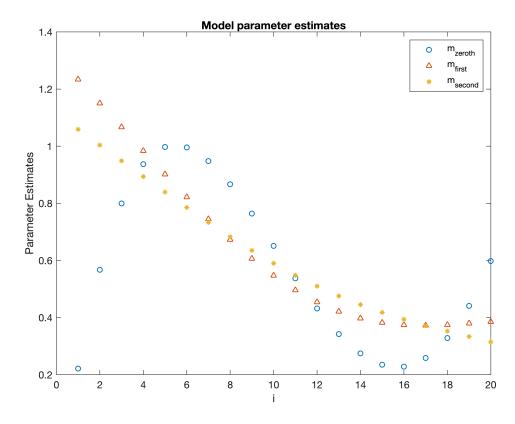
### Using regularised discrepancy principle

alpha21 = 0.0025alpha22 = 0.0148

# Comment on how they are similar or different, and the implications of the magnitude of these $\alpha$ in the optimization problem.

The discrepancy principle gives similar alpha values for both first and second order Tikhonov regularizations while the regularised discrepancy principle yields different values of alpha for both first and second order Tikhonov regularizations, the difference in these values of alpha is due to using different roughening matrices, the value of the standard deviation e.t.c. The magnitude of alpha values impact highly the shape of the curve for the model parameters.

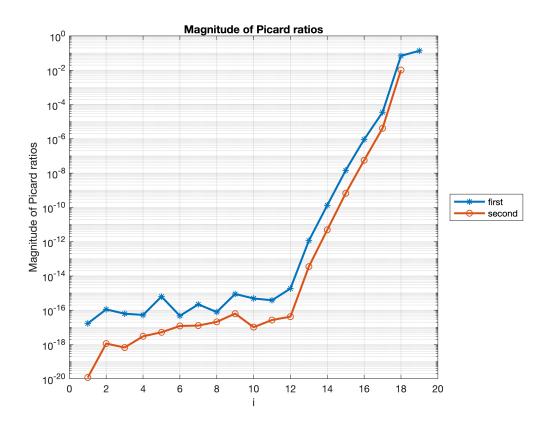
## No.3 Plot model parameter estimates using first and second order Tikhonov regularization



Discuss the difference between the first and second order estimates, and how they relate to estimates from zeroth order Tikhonov regularization in the previous activity.

A seen from the graph above, the first and second order estimates overlap each at certain ranges: i<7, 7<=i<17, and i=>17, however they almost coincide at certain indicies: i=7 and 8, and this is due to the different roughening matrices used to geenrate the values of alpha which affect the nature of the model parameters. The shape of the curve from the zeroth Tikhonov regularization is very different from that of the first and second order, this is due to the value of alpha for the zeroth order being very small compared to those of the first and second order and also the standard deviation used. Some of the second order points almost coincide with that of the zeroth order, and the alpha from the zeroth order acted as an intaial value for both first and second order, therefore, both depend on the value of the zeroth order.

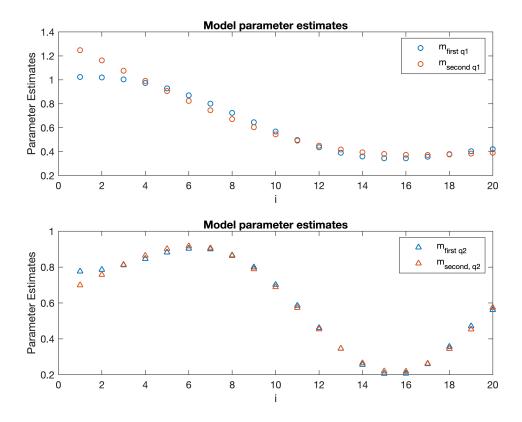
No.4 Plot the Picard ratios for first and second order Tikhonov regularization for one of the same values of a you used in 3.



Identify where smaller singular values in the GSVD may cause the model parameter estimates to become unstable.

At i > 12

No.5 Plot model parameter estimates using TGSVD, for both first and second order Tikhonov regularization, with 2 values for q in each case for which you get reasonable model parameter estimates.



### Discuss the accuracy and stability of these estimates.

The estimates obtained using a small vale of q are more accurate and stable compared to those with a larger value of q. We see unstability at i =7 for parameter estimates obtained using a larger value of q.