

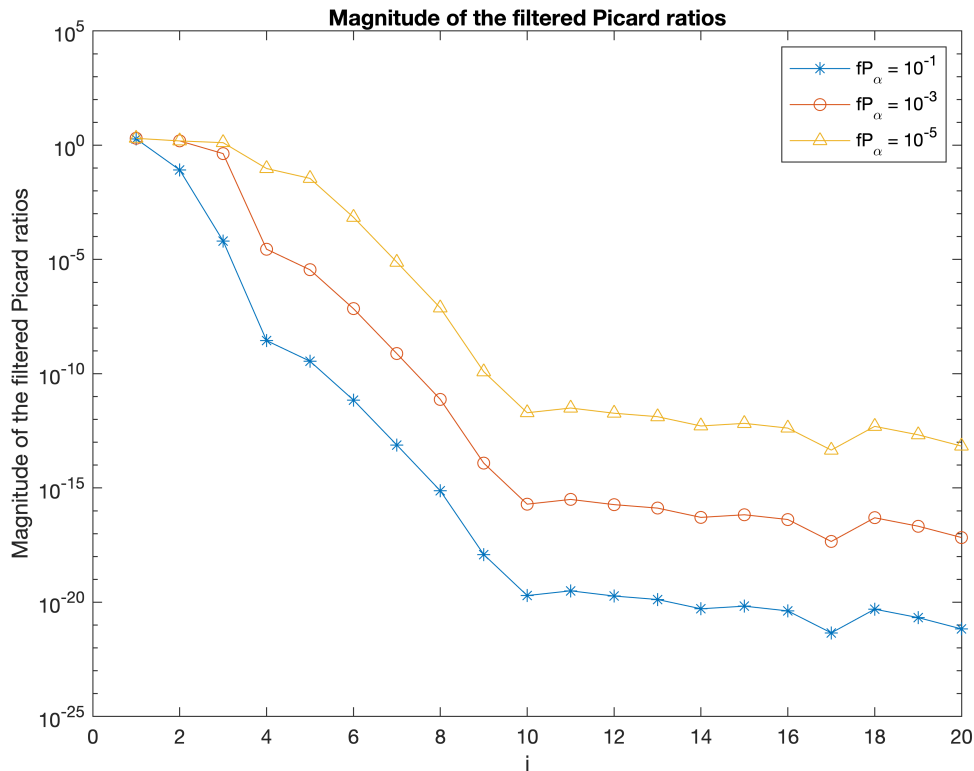
N0.1

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chi_tsvd_i = 0.9433
chi_tsvd_i_1 = 0.9437
chi_mtrue = 22.4482
expected_value = 0
```

Discuss the values you calculated in relationship to each other, and to the expected value.

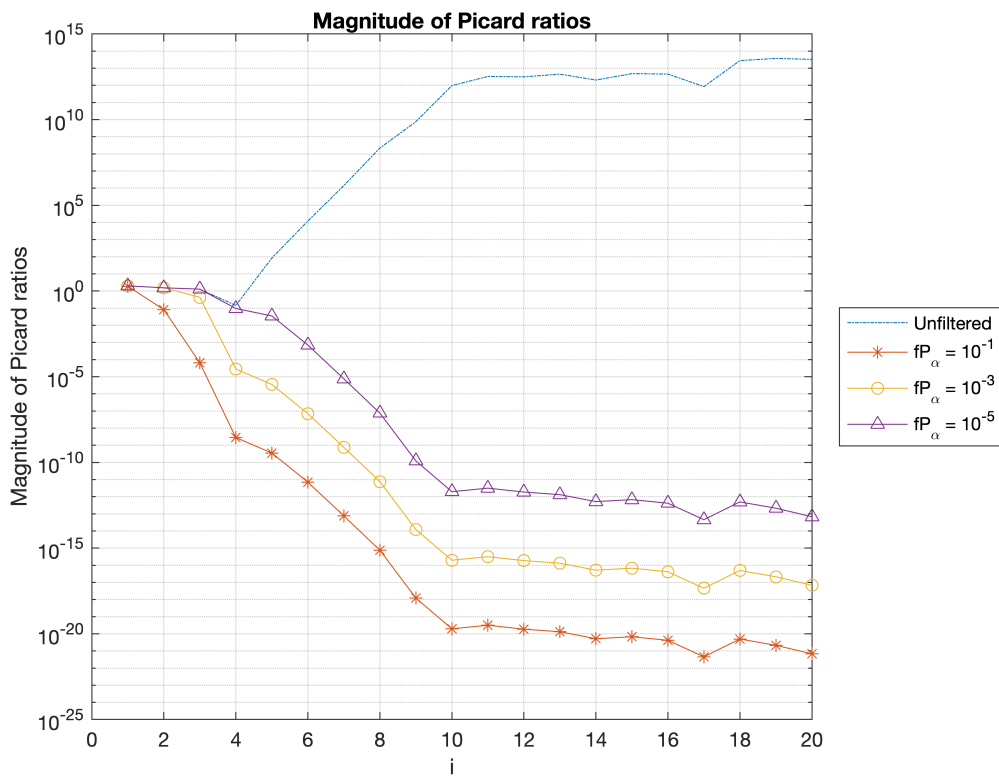
The χ^2 for the TSVD parameter estimates is almost the same and way too small compared to that of the true estimates which is 22.4482. However, the χ^2 for the TSVD near to the expected value, $\nu = 0$ compared to that of the true estimates. This means that the true parameter estimates don't follow a chi-square distribution.

N0.2

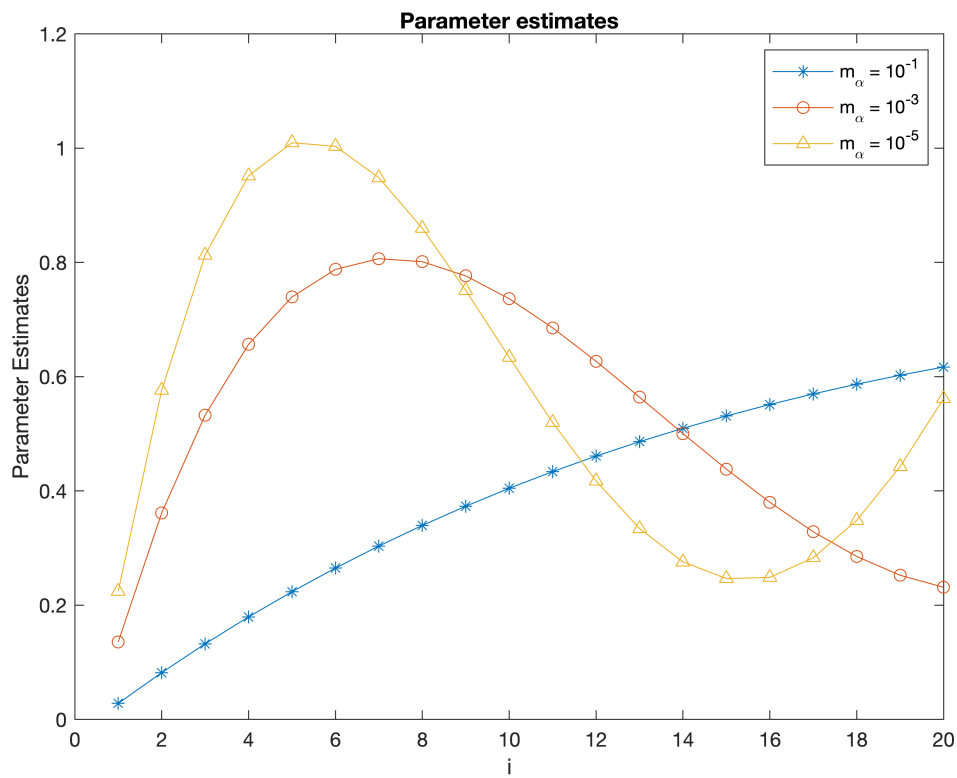


Discuss how they compare to the unfiltered Picard ratios in the Ch3: Discrete ill-posed problems individual activity.

As seen from the graph below, they filtered and unfiltered all start at the same point, however, after $i = 4$, the unfiltered one increases rapidly up to $i = 10$, and then somehow tends to flatten, while the filtered ones, decreases in the same sense depending for the value of α .

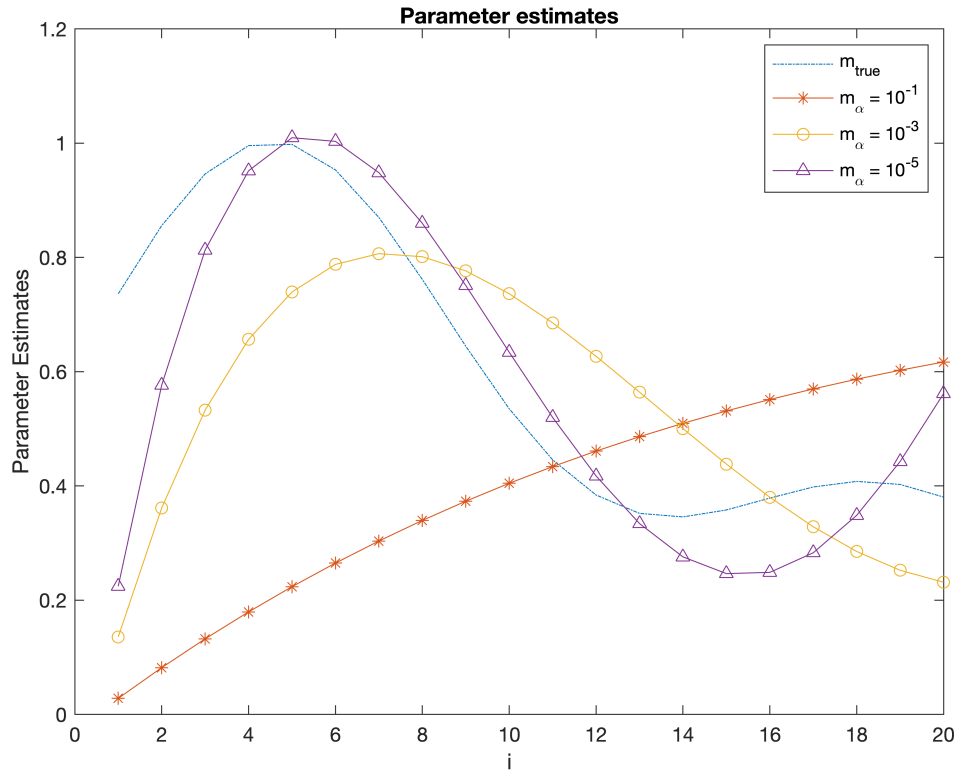


N0.3 Plot the estimates for each value of α on the same graph.



Discuss the accuracy of the model parameter estimates with different values of α , and relate them to the Picard ratios in 2.

Based on the graph below, comparing the model parameter estimates at different values of alpha to the true model, tells us that the smaller the alpha the more close the estimates are to the true estimates, and the bigger the alpha, the further the estimates are, a way form the true estimates, which means the more we increase alpha, we are over smoothing the data. This is also well exhibited in the Picard ratio plot in figure(3), as alpha increase, the more the graph diverges away from the true solution.



Report the χ^2_{obs} values for each value of α .

residual_a1 = 3.2498e+05

residual_a2 = 38.4176

residual_a3 = 0.9433

Compare them to the values you found in 1.

The χ^2_{obs} for the different values of alpha, are far away from the expected value 0, except for $\alpha = 10^{-5}$ which means that the data follows a χ^2 distribution for only $\alpha = 10^{-5}$ and is equivalent to the χ^2_{obs} obtained for TSVD parameter at $i = 4$