Process Book: Visualizing Error in Materials Informatics

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Abstract We present a website for visualizing the error associated with machine learning predictions in materials science.

Keywords Machine Learning \cdot Band Gap \cdot Density Functional Theory \cdot Ensemble Learning \cdot Inorganic Solids

1 Project Proposal

1.1 Background and Motivation

This project comes from the research of Steven Kauwe who investigates the use of materials informatics for predicting material properties as a Ph.D student in the Department of Materials Science and Engineering. The current state of research in that area has focused on showing proof of concept machine learning using various data types. Because materials science is inherently chemistry based, researchers have found it is useful to represent chemical systems based on their constituent elements. This is the foundation for what we will refer to as the composition-based feature vector (CBFV). The CBFV is a common method of vectorizing chemistry space, allowing a representation of physical composition to be parsed into traditional machine learning frameworks. Because of the relatively new interest in this area, some fundamental ideas have yet to be implemented in an open and accessible way. In particular, to our knowledge there exists no central tool for researchers to evaluate the effect constituent elements have in prediction error. This project aims to provide

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a proof of concept tool for just such composition based error exploration.

1.2 Project Objective

This project looks to answer the question whether certain chemistries are more prone to error in machine learnign models that are build from compositional information. In particular, we would like to know if this error is caused by the chemistry itself of by the lack or representation in the dataset. Using a variety of visual techinqes, we hope to give the user the ability to answer the following questions:

- 1. What elements have the most error associated with them?
- 2. Are non-real compositions less accurate that real compositions for this data?
- 3. How does the relationship between elemental properties affect the emergent properties of the molecule
- 4. Are there patterns in error relative to feature values?
- 5. Do compounds with similar elements cluster close to each other in feature space, and predictions?

1.3 Data Acquisition

Data is collected from the computational materials property repositories: Automatic - Flow for Materials Discovery (AFLOW), and The Materials Project (MP) who do high throughput density functional calculations (DFT) to compute material properties as a part of the Materials Genome Initiative. The AFLOW data was retrieved directly from their search tool after selecting the required electronic property, Band Gap aflowlib.org. The

MP data was obtained via a third party, Citrine Informatics, at citrination.com: data set #150675. The data is then vectorized via composition and used in a machine learning scheme that saves the cross-validation predictions and trains a model for future predictions. The error associated with the cross-validation results comprise the interactive aspect of the project.

1.4 Data Processing

The data may have duplicate entries and compositions that do not represent real compounds. The duplicates values can be solved by averaging all reported values. The non-real entries will not be rejected from the data set, but will instead be marked to let researchers know how this effects model error. To do this, we will need to cross-checked all AFLOW and MP data against a crystal structure database. This will be done with the Pearson Crystal Database (PCD).

We expect to derive a predicted value of band gap from our data. Error metrics for all cross-validation predictions will also be obtained during model creation. Before use online, we will need to classify the data entries by the constituent elements and whether we could confirm if a real structure is reported for the composition. The compositions will also be vectorized in a composition-based feature vector (CBFV) which is used in the machine learning. This will start as a vector with approximately 250 elements, however principal component analysis (PCA) and t-Distributed Stochastic Neighbor Embedding (t-SNE) will reduce this down to 2-5 dimensions for human interaction.

Data processing will be implemented in python 3 using the pandas and sk-learn libraries. All data will be processed offline then compactly represented as CSVs or JSONs.

2 Visualization Design

This data will mostly be displayed using scatter plots, distribution plots, trees, and a interactive periodic table. The markers will typically represent individual chemical compounds.

The user should be able to interact with a periodic table to select compounds of interest. These, in turn, will be highlighted in the other views to allow the user to quickly and intuitively explore the interaction of composition with error. The user could interact with a distribution plot to filter for values they would like to consider. It could also be possible for the user to put in their own composition and generate a prediction.

There will be three pages: overview, elements, and search. Each page will independently operate, providing a specific use for the user. The overview will show overall trends in the data and allow for high level exploration. The elements is designed to let users to see specific information associated with the individual elements and the formulae they are a part of. The search page allows users to see previous searches and generate new predictions.

This three page design is made to be captivating while simple to interact with. It gives the user enough choices to spend significant time on the webpage, but also limits the available information to prevent a feeling of being overwhelmed. The representation of data is standard for most publications in the field and is appropriate.

2.0.1 Must-Have Features

Completion of the overview page would constitute success. This is the main aspect of the project and provides the user with the most functional information.

2.0.2 Optional Features

The element and search pages aim to present our more detail in the data set. These are less complicated and serve a secondary purpose of which is helpful for evaluating individual formula, but not critical for gauging the error in general.

3 Current Data Structure

3.1 Periodic Data Table

The file ptable.csv (see Figure 1) is the data that we load to create the periodic table view (ptable view). Each row of this file describes an element. The attributes in this table contains symbol, row, column, data, name, count, average residual, average predicted and average actual. Row and column attributes provide the information to allow us to format the periodic table. Symbol and name attributes provide the information that we use for generating classes for each element. These allow us to easily communicate across view. The other attributes are made available for creating heat maps, their values are used to generate the color scale, which dictates the color each element block.

3.2 Predictions Data Table

The file experimental_predictions.csv (see Figure ??) is the data that we load to create the element's residual

- 4	A	В	C	D	E	F	G	H	I
1	symbol	row	column	data	name	count	average_residual	average_predicted	average_actual
2	S	3	16	1	Sulfur	1582	-0. 018450124	2. 029286807	2. 047736932
3	C	2	14	1	Carbon	711	-0. 017141874	2. 121395889	2. 138537763
4	Se	4	16	1	Selenium	687	-0. 022107451	2. 071090942	2. 093198393
5	0	2		1	0xygen	544	-0. 036612011	2. 227308763	2. 263920773
6	В	2	13	1	Boron	519	-0. 019434629	2. 167436367	2. 186870997
7	P	3		1	Phosphorus	473	-0.0488924	1. 950587856	1. 999480256
8	Te	5	16	1	Tellurium	401	-0.04280867	1.850754382	1.893563052
9	I	5			Iodine	397	0.000306056	2. 027968025	2. 027661969
10	Ga	4		1	Gallium	313	-0.006491058	2. 07397963	2. 080470688
11	In	5	13	1	Indium	289	0. 023309962	2. 047781665	2. 024471703
12	Sb	5	15	1	Antimony	266	-0. 01736794	1.844183754	1.861551694
13	N	2	15	1	Nitrogen	238	-0. 045934682	2. 29876152	2. 344696201
14	Ge	4	14	1	Germanium	218	0.065067597	2. 070349413	2. 005281816
15	Cu	4	11	1	Copper	217	-0.000401033	2. 169833656	2. 170234688
16	As	4		1	Arsenic	204	-0.093110865	1.868990186	1.96210105
17	Cd	5	12	1	Cadmium	191	-0.064922956	1. 955095054	2. 02001801
18	Ba	6	2	1	Barium	190	-0. 021764965	2. 373987895	2. 39575286
19	Bi	6	15	1	Bismuth	190	-0. 036584624	1. 930019388	1. 966604012
20	Sn	5	14	1	Tin	184	-0.077443006	2. 088748831	2. 166191837
21	K	4	1	1	Potassium	177	0.050816866	2. 356437768	2. 305620901
22	Pb	6	14	1	Lead	175	-0. 039275034	1. 793590866	1. 832865901
23	H	1	1	1	Hydrogen	173	-0. 075598245	2. 303625155	2. 3792234
24	Cs	6		1	Cesium	165	0.007199795	2. 235948793	2. 228748999
25	Zn	4	12	1	Zinc	158	-0.02406119	1. 970638491	1. 99469968
26	Ag	5	11	1	Silver	124	-0.067895739	2. 052740591	2. 120636331

Fig. 1 Periodic Data Table

view and actual vs prediction view. Each row of this file describes a formula. The attributes in this table contains formula, actual, predicted, elements and residual. We classify tables of each elements based on the elements attributes. Actual and predicted attributes provide the information to allow us to format actual vs prediction view. Residual attribute provides the information to allow us to format residual view.

	A	В	С	D	Е
1	formula	actual	predicted	elements	residual
2	DyIn3S6	2. 43	1. 615021285	Dy In S	0. 814978715
3	K4Ba2Nb4S22	0. 29	0. 957665397	K Ba Nb S	-0. 667665397
4	K2Ho4Cu4S9	1. 926667	1. 78392936	K Ho Cu S	0. 142737307
5	Pb0. 9Mn0. 1Te	0. 278833	0. 254484975	Pb Mn Te	0. 024348358
6	RbInSnS4	2. 96	3. 57878207	Rb In Sn S	-0. 61878207
7	PbGa2GeSe6	1. 31	1. 087782872	Pb Ga Ge Se	0. 222217128
8	EuYb2S4	4. 1	4. 0814794	Eu Yb S	0. 0185206
9	Hg0. 01Cd0. 99S	3. 67	5. 616579075	Hg Cd Se	-1. 946579075
10	V02	3. 26	2. 886051502	V O	0. 373948498
11	InSb0. 2As0. 8	2. 48	2. 085664494	In Sb As	0. 394335506
12	EuIn2S4	1	1. 355621908	Eu In S	-0. 355621908
13	CdIn30Te46	2. 16	1.869877649	Cd In Te	0. 290122351
14	Cu3VS4	1.81	1. 198602672	Cu V S	0. 611397328
15	NaGe3P3	2. 64	2. 495712255	Na Ge P	0. 144287745
16	CsDy9Cd4Se18	2. 3	1. 974589013	Cs Dy Cd Se	0. 325410987
17	Hg0. 77Cd0. 23T	1. 725	1.869572861	Hg Cd Te	-0. 144572861
18	In4S5	1. 18	0. 9668109	In S	0. 2131891
19	BaGa2Se4	3. 4	2. 978371702	Ba Ga Se	0. 421628298
20	Ce2Sn3Se9	4. 22	4. 041873144	Ce Sn Se	0. 178126856
21	Ag20	0. 123333	0. 12148003	Ag O	0. 001853303
22	CuIn5S8	0. 7	0.840249935	Cu In S	-0. 140249935
23	BaGa4S7	1.83	1. 673360331	Ba Ga S	0. 156639669
24	CsCd4In5Se12	0.43	0. 352246184	Cs Cd In Se	0. 077753816
25	Cd4GdB3010	1.08	0.853661206	Cd Gd B O	0. 226338794
26	Ca2Si	2. 2	1. 983242966	Ca Si	0. 216757034
27	Cs2ZnGe3Se8	1. 9	1. 756622402	Cs Zn Ge Se	0. 143377598
28	Rb1. 45Pb3. 1Sb	3. 7	3. 932230091	Rb Pb Sb Se	-0. 232230091
29	AgIn9Te14	1. 95	2. 116740627	Ag In Te	-0. 166740627
30	Rb3CdB5010	2	1. 584567136	Rb Cd B O	0. 415432864

Fig. 2 Predictions Data Table

3.3 Histogram Table

The files in hist_data folder (see Figure ??) are the data that we load to create the element's residual view. Each row of this file describes a formula. The attributes in this table contains formula, actual, predicted, elements and residual. Based on elements attributes, we classify tables of each elements. Actual and predicted attributes provide the information to allow us to format actual vs prediction view. Residual attribute provides the information to allow us to format residual view.

4	A	В	С	D
1	bin_count	bin_freq	bin_range	bin_number
2	14	0. 21875	(-0.142, 0.0165]	13
3	13	0. 203125	(0.0165, 0.175]	14
4	9	0. 140625	(-0.301, -0.142]	12
5	8	0. 125	(0. 175, 0. 333]	15
6	5	0. 078125	(-0. 459, -0. 301]	11
7	3	0. 046875	(0. 333, 0. 492]	16
8	3	0. 046875	(-0.618, -0.459]	10
9	2	0. 03125	(0. 809, 0. 968]	19
10	2	0. 03125	(0. 492, 0. 651]	8
11	2	0. 03125	(-0. 935, -0. 776]	17
12	1	0. 015625	(0.651, 0.809]	7
13	1	0. 015625	(-1.093, -0.935]	0
14	1	0. 015625	(-1.727, -1.569]	18
15	0	0	(-2.044, -1.886]	6
16	0	0	(-1.886, -1.727]	5
17	0	0	(-0. 776, -0. 618]	4
18	0	0	(-1.569, -1.41]	3
19	0	0	(-1.41, -1.252]	2
20	0	0	(-1. 252, -1. 093]	1
21	0	0	(-2. 203, -2. 044]	9

Fig. 3 Histogram Table

3.4 Element Data Table

4 Discussion of Feedback from Peer Review

4.0.1 Comments from Peers (response in Cyan)

- 1. You will need a good explanation of how the data is to be used. This could be a tool tip, or a text box.
 - This is a great idea. I think the text box will be the most appealing for users, as it will be easy to see and doesn't depend on mouse location to give information.
- 2. If you include machine learning features in your figures, you will need to show how those are derived.
 - We will include an info box that will have links to relevant publications, and web pages if the

	A	В	С	D	Е
1	formula	actual	predicted	elements	residual
2	AgAlTe2	0. 035	0. 1279492	Ag Al Te	-0. 0929492
3	A1N	6. 89	6. 033343363	Al N	0.856656637
4	BaA14Se7	4. 76	4. 709375625	Ba Al Se	0. 050624375
5	In0. 6A10. 4P	0. 365	0. 749499896	In Al P	-0. 384499896
6	Ga0. 5A10. 5As	2. 23	2. 080964205	Ga Al As	0. 149035795
7	InO. 99A10. 01P	2. 64	3. 065795527	In Al P	-0. 425795527
8	Li6A12Te8022	0. 236666667	0. 365359098	Li Al Te O	-0. 128692431
9	Cs2A12B2O7	1. 56	1. 519802546	Cs Al B O	0. 040197454
10	Ga0. 01A10. 99P	1. 1	0. 585675597	Ga Al P	0. 514324403
11	Ba8A110B12041	4. 76	4. 232035163	Ba Al B O	0. 527964837
12	A1VTe208	3. 78	4. 370909274	Al V Te O	-0. 590909274
13	CuA1Se2	0. 24	0. 407407173	Cu Al Se	-0. 167407173
14	Ga0. 25A10. 75As	1.86	2. 676783984	Ga Al As	-0. 816783984
15	NaA1GeS4	1. 03	1. 595339969	Na Al Ge S	-0. 565339969
16	In0. 8A10. 2P	6. 443333333	6. 262782046	In Al P	0. 180551288
17	Ga0. 85A10. 15As	2	1. 826215518	Ga Al As	0. 173784482
18	A12S3	2	2. 021122155	Al S	-0. 021122155
19	AgA102	0. 2695	0. 468579571	Ag Al O	-0. 199079571
20	Ga0. 7A10. 3As	2. 54	2. 349350999	Ga Al As	0. 190649001
21	Cd0. 01Te0. 01A10.	3. 68	3. 693911035	Cd Te Al Sb	-0. 013911035
22	Li4. 5A10. 5Te06	0. 783333333	0. 784428831	Li Al Te O	-0. 001095497
23	Ga0. 4A10. 6As	2. 79	3. 64249763	Ga Al As	-0. 85249763

Fig. 4 Element Data Table

user wants to learn about the specifics of this data.

- 3. You need to ensure that the elements are very clearly marked in each data view.
 - This is a great idea. It will probably be useful to have figure captions similar to a publication.
- 4. It will be important to label charts and figures. Make sure that the user can understand each figure from the labeling.
 - We agree labeling will be important. However we do not want to present to much test to the user.
- 5. You need to add a full description on what the tool can do. Perhaps a question mark that has a tool tip on hover. Regardless, you need to provide A full description of what this tool uses.
 - We will provide a link in the general info box that fully describes how the data was generated, and gives commentary (if there is any) on specific trends that are interesting.
- 6. You should include a introduction to the issue for those who are not in materials science
 - We will try to have a link in generate info box "Click here if new to materials informative" (or something like that)
- 7. You need to make sure that the heat map is clearly explained and useful. It is the first point of contact for the user.
 - This is extremely important. We have added a legend that explains the cut-ff used for the different displayed colors. We will also try to add buttons that allows the user to explicit select a material property (and inherently show what property is displayed).
- 8. Focus on story telling. Perhaps you can include a small tutorial that shows the user how it works. You

could also put the tool in a particular state at start up.

- We are not quite ready to handle this step yet. This is a tool that is designed to help with the data analysis. Once the tool is more mature, we can look for an interesting story and tailor things in a way that highlights the fact.
- 9. Add a way for people to see selected compounds on the main page.
 - This is a great feature. We will implement this once the main data views are properly communicating with each other.
- 10. Add brush or hover to highlight compounds and make specific space to display results.
 - This brings up a good point about displaying data. Currently we have a too tip, but that can hide the data and is not always visible. We will consider adding a box superficially dedicated to displaying values of interest
- 11. One second page. Make it so that there is explicit explanation of how the combining elements will work
 - Hahaha the second page will probably not be added as a part of this project
- 12. You can probably drop the TSNE and the histogram if there is not enough time.
 - The TSNE should be a relatively simple figure to generate. Interaction with the TSNE is likely to provides an interesting aspect of "the story".
 This comes from exploration of similar (though less functional) tool provided by Citrine Informatics.
- 13. If you can only show one thing on the heat map, it should be the residual.
 - This is an intersting comment. It makes a lot of sense to show residual. On the other hand, showing the relative frequency of data makes interaction with the data easier.
- 14. You can probably get away with not having the brushing. Instead show a list of all the formula that have the currently selected elements.
 - This will almost certainly be the solution we implement.
- 15. All of it is too aggressive. Probably just a part of the first page is enough.
 - Agreed.
- 16. The visualization techniques are boiler plate. The way that it works is useful, but necessarily novel. Not very innovative. Maybe have to reduce the amount of data that can be explored.
 - The original data has been dropped for a subsection of data (44,000 to 2,500) that only includes

examples with experimental band gap information.

- 17. If you have too much data, you can only plot things that are clicked on.
 - This a good idea, and has been added to the current iteration of the act_vs_pred data view.

5 Project Status: 11/8/2018

The ptable view was the first view implemented. This is the main tool for interacting with the data (see Figure 5). This provides the user with the ability to investigate the data on an element-by-element basis. This form of the ptable view allows the user to hover and click on individual elements. On hover, the act_vs_pred view displayes formulae with those elements. On click, the data is updated to only show formulae with that element (as seen in Figure 6). We have currently implemented "or" logic (graph shows formulae with "Al" or "Ag") if two or more elements are clicked. This means that you only add new formulae with each subsequent element click. We hope to eventually add "and" logic as well, allowing the user to drill down into subsets of material types.

5.1 Periodic Table

Periodic Table

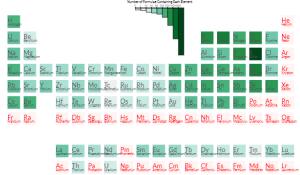


Fig. 5 Version 1 of the ptable view. Colors are not decided, but the heat map and element layout work well for interaction.

There is currently no interactivity with heat map specifically. The heat map is also limited to showing the relative frequency of formulae that contain the specific constituent element (eg. Ag is a part of 10-40 elements). Currently, the ptable does communicate with the act_vs_pred data view. This allows us to load the proper element data on selection making for a smooth and fast user experience. The current color scheme on

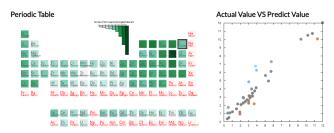


Fig. 6 When elements are clicked on, they are classed as 'selected'. This allows the other views to read to appropriate data and update to only show formulae specified by the user.

ptable is a place holder until we get a better overall feel for the web page. The green squares all have representative data. The red squares indicate that there are no examples of that element in the data set for the user to interact with.

5.2 Actual vs Predicted Values

This view gives the user a soft understanding of error in the data set. The figure will be labeled to indicate that more accurate data lies on the 45° line (which will be implemented soon). The residual error is encoded with color to help the user understand the relative error at a glance. This essentially acts as the main display while the user explores the data (Figure 7). This view dynamically changes as the user interacts with the ptable view. Figure 8 shows the click and highlight function both in use. The click function reduces the displayed data to those containing silicon. The hover element then highlights the subset that also contains phosphorus.

Actual Value VS Predict Value

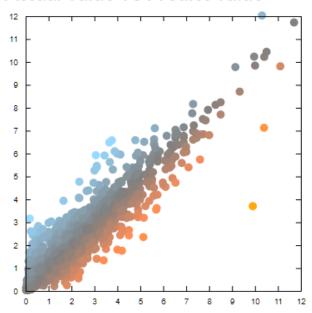


Fig. 7 The actual band gap vs the predicted values are shown here. This allows for quick feed back while the user explores their data.

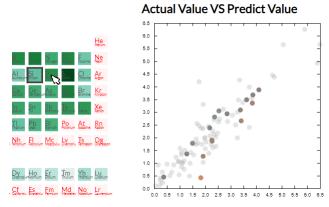


Fig. 8 The "highlight on hover" feature allows the user to preview data without removing data from the current selection. This will likely extend into all data views; however, the exact functionality is still being explored.