

3. Variable size window

Problem 1: Minimum Size Subarray Sum (Leetcode-209)

Problem 2: Binary Subarrays With Sum (Leetcode-930)

Variable Size Sliding Window Approach:

Note: Determine window size

Variable Size Window

Step 1: Start by initializing the **start** and **end** pointers to the first element of the sequence or array

Step 2: Find the answer

- **Valid Ans:** minimize start++
- **Store Ans:** Perform the required calculations or operations to obtain the answer
- **Invalid Ans:** explore end++



<u>window</u>	<u>size</u>
w1	2
w2	4
w3	7

} different sizes of each windows

1. Minimum Size Subarray Sum (Leetcode-209)

Problem Statement:

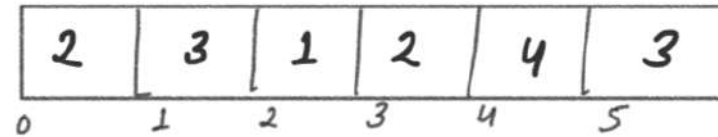
Given an array of positive integers nums and a positive integer **target**, return the **minimal length** of a subarray whose sum is greater than or equal to **target**. If there is no such subarray, return **0** instead.

Example 1:

Input: target = 7, nums = [2,3,1,2,4,3]

Output: 2

Explanation: The subarray [4,3] has the minimal length under the problem constraint.



Example 2:

Input: target = 4, nums = [1,4,4]

Output: 1

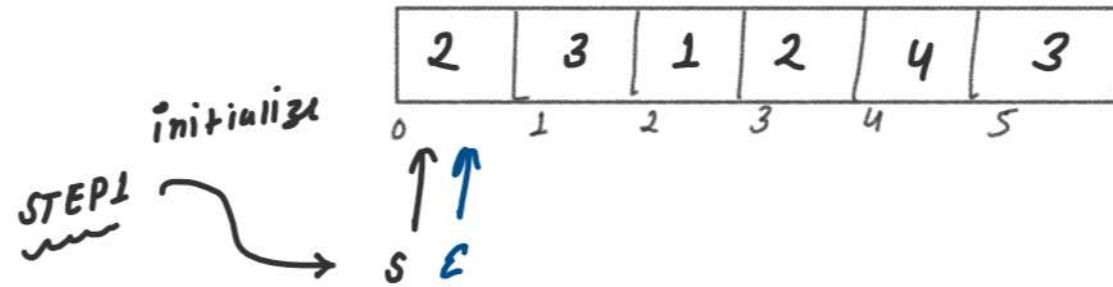
Example 3:

Input: target = 11, nums = [1,1,1,1,1,1,1,1]

Output: 0

possible
subarrays = 2^6

Target = 7



STEP2 Find Ans
if (windowSum \geq target)
start ++
else
end --

why this logic?

return the smallest window length is correct Ans degi.

logic

DRY RUN

Target = 7

S	E	Sum	>= Target	
0	0	2	>= 7 X	End ++
0	1	5	>= 7 X	End ++
0	2	6	>= 7 X	End ++
0	3	7	>= 7 ✓	Start ++
1	3	5	>= 7 X	End ++
1	4	10	>= 7 ✓	Start ++
2	4	7	>= 7 ✓	Start ++
3	4	6	>= 7 X	End ++
3	5	9	>= 7 ✓	Start ++
4	5	7	>= 7 ✓	Start ++
5	5	3	>= 7 X	End ++
5	6			

stop End < size
6 < 6 X

2	3	1	2	4	3
0	1	2	3	4	5

↑ ↑
S E

ANS

4	3
4	5

length = 2
output

```

// Problem 01: Minimum Size Subarray Sum (Leetcode-209)

class Solution {
public:
    int minSubArrayLen(int target, vector<int>& nums) {
        // Step 1: Initializing the start and end
        int start = 0;
        int end = 0;
        int windowLength = INT_MAX;
        int windowSum = 0;

        // Step 2: Find the answer
        while(end < nums.size()){
            // Store the value in windowSum
            windowSum = windowSum + nums[end];

            while(windowSum >= target){
                // Minimize the window
                if(windowSum >= target){
                    int currLength = end - start + 1;
                    windowLength = min(windowLength, currLength);
                }
                // Current element, pointed by start, should be remove from the new window
                windowSum = windowSum - nums[start];
                start++;
            }

            // Loop se bahar tabhi aa skte hai jab windowSize < target hoga
            // Explore the window
            end++;
        }

        // Edge case: me hamesha yeha galti karta hu
        if(windowLength == INT_MAX){
            // Apply for example 3
            return 0;
        }
        return windowLength;
    }
};

```

Time Complexity: $O(N)$
Space Complexity: $O(1)$

2. Binary Subarrays with Sum (Leetcode-930)

Problem Statement:

Given a binary array nums and an integer **goal**, return the number of non-empty subarrays with a sum **goal**.
A **subarray** is a contiguous part of the array.

Example 1:

Input: nums = [1,0,1,0,1], goal = 2
Output: 4

1	0	1	0	1
0	1	2	3	4

Example 2:

Input: nums = [0,0,0,0,0], goal = 0
Output: 15

Initial state

start = 0
end = 0
prefixZero = 0
sum = 0
count = 0

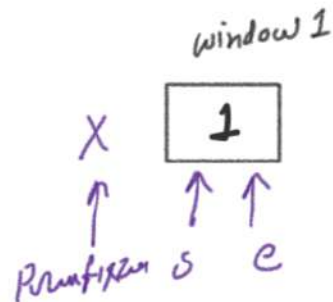
Explanation: The 4 subarrays are

[1,0,1,_,_] = 2
[1,0,1,0,_] = 2
[_,0,1,0,1] = 2
[_,_,1,0,1] = 2

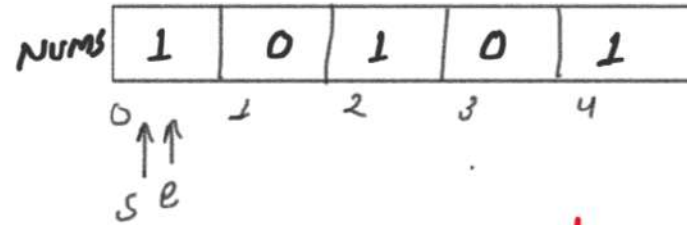
DR + RUN goal = 2

1

start = 0
end = 0
prefixZero = 0
sum = 0
count = 0



sum += num[e]
sum = 0 + 1
= 1



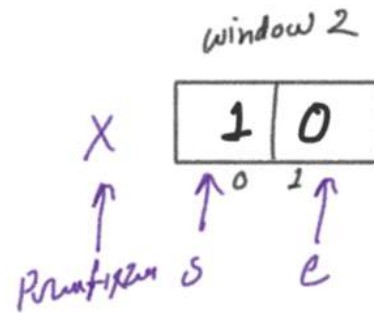
Invalid
(sum < goal)
1 < 2 ✓
→ End++

Unification
(sum == goal) ¹ ₂ X
→ count += prefix + 1;

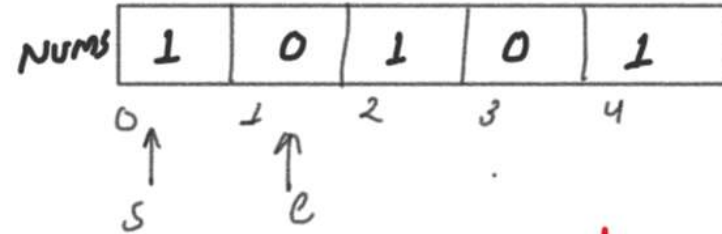
goal = 2

2

start = 0
end = 1
prefixZero = 0
sum = 1
count = 0



sum += num[e]
sum = 1 + 0
= 1



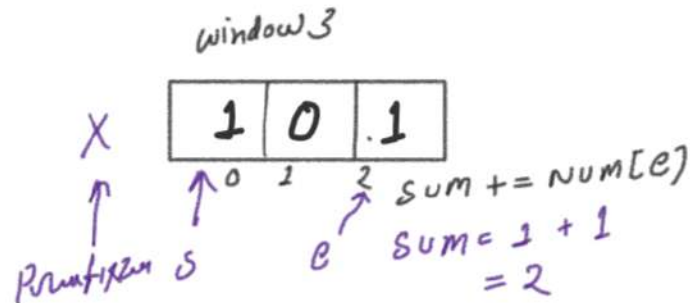
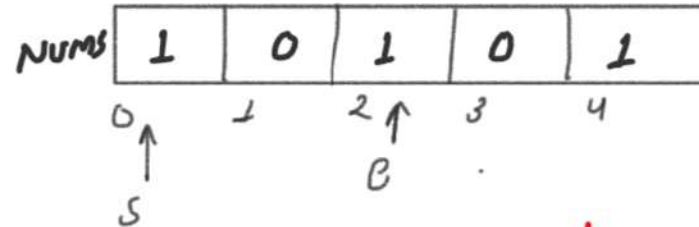
Invalid
(sum < goal)
1 < 2 ✓
→ End++

unification
(sum == goal) X
→ count += prefix + 1;

goal = 2

3

start = 0
end = 2
PrefixZero = 0
sum = 1
count = 0



valid
(sum == goal)
2 < 2 ✓
→ End++

Unification
(sum == goal)
count += PrefixZero + 1;
= 0 + 0 + 1
count = 1



Window 4

1	0	1	0
---	---	---	---

0 1 2 3

X
↑
Printer S

↑
e

valid
(sum == goal)
2 2 2 ✓
→ End++

unification

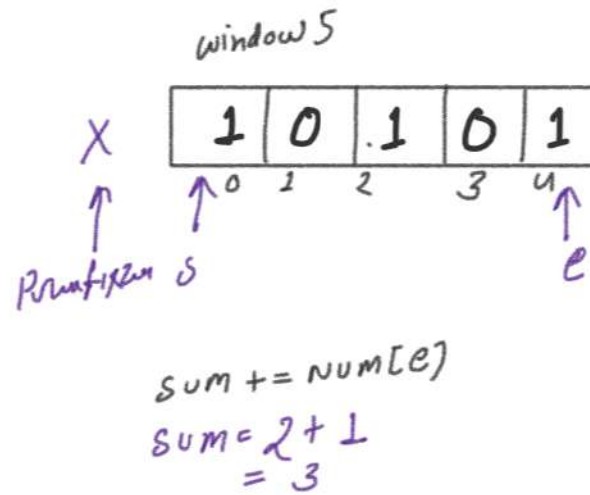
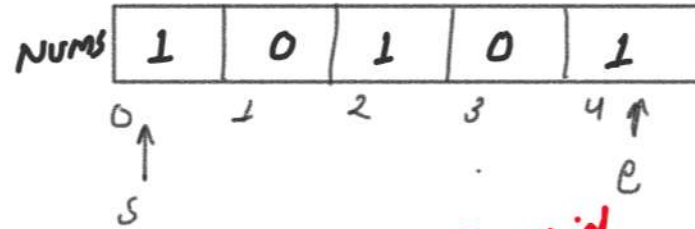
$(sum == goal) \times$
 $count += prefix + 1;$
 $= 1 + 0 + 1$

count = 2

goal = 2

5

$start = 0$
 $end = 5$
 $prefixZero = 0$
 $sum = 2$
 $count = 2$



Invalid

$(sum > goal)$
 $3 > 2$

$if (num[s] == 1)$
 $prefixZero = 0$
 $else$
 $prefixZero += 1$

$sum = sum - num[s];$
 $s++;$ // minimize
 $s = 1$

goal = 2

5

start = 1
end = 5
PrefixZero = 0
sum = 2
count = 2

nums	1	0	1	0	1
	0	1	2	3	4
		↑			↑
		s			e

window

X
↑
PrefixZero

0	1	0	1
1	2	3	4
↑			↑
s			e

valid
(nums[s] == 0)
0 0 ✓

if (nums[s] == 1) {
PrefixZero = -1 X

else {
PrefixZero += 1 → sum = 1

sum = sum - nums[s]; → 2 - 0
s++; // minimize = 2
→ s = 2

goal = 2

5

start = 2

end = 5

prefixZero = 1

sum = 2

count = 2

Nums	1	0	1	0	1
	0	1	2	3	4
			↑		↑
			5		e

window 7

1	0	1
2	3	4
↑		↑
5		e

invalid
(sum == target)
2 2

$$\begin{aligned} \text{count} &= \text{count} + \text{prefix} + 1 \\ &= 2 + 1 + 1 \\ &= 4 \end{aligned}$$

End++

goal = 2

5

start = 2

end = 6 **stop**

PrefixZero = 1

sum = 2

count = 4

output

Nums	1	0	1	0	1
	0	1	2	3	4
			↑		↑
			s		e

Window B

1	0	1
2	3	4
↑		↑
s		e

$e > \text{size}$

size = 5

if (num[s] == 0 ||
sum > goal)

↳ s++

if (sum <= goal)

↳ e++



```

// Problem 02: Binary Subarrays With Sum (Leetcode-930)

class Solution {
public:
    int numSubarraysWithSum(vector<int>& nums, int goal) {
        // Step 1: Initializing the start and end
        int start = 0;
        int end = 0;
        int windowSum = 0;
        int prefixZero = 0;
        int count = 0;

        // Step 2: Find the answer
        while(end < nums.size()){
            // Store the value in windowSum
            windowSum = windowSum + nums[end];

            // Minimise the window
            while(start < end && (windowSum > goal || nums[start] == 0)){
                if(nums[start] == 1){
                    prefixZero = 0;
                }
                else{
                    prefixZero += 1;
                }
                // Current element, pointed by start, should be remove from the new window
                windowSum = windowSum - nums[start];
                start++;
            }
            // Verification
            if(windowSum == goal){
                count += prefixZero + 1;
            }
            // Explore the window
            end++;
        }
        return count;
    }
};

```

Time Complexity: $O(N)$
Space Complexity: $O(1)$