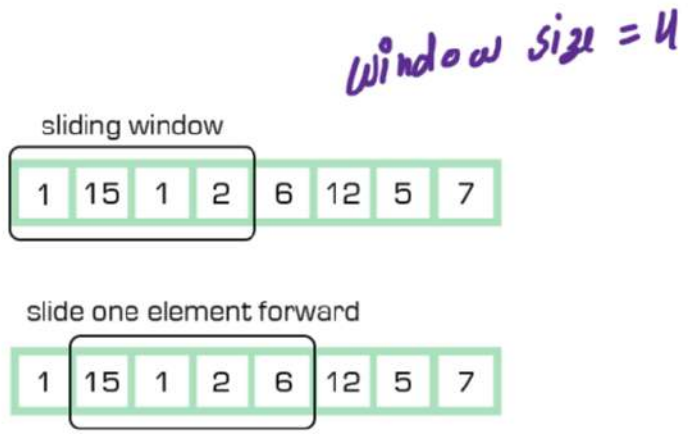
Sliding Window Technique

Table of Contents



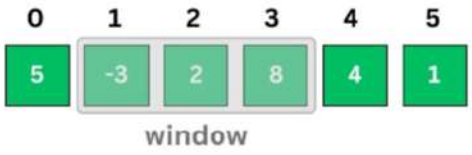
1. What is sliding window technique?

The sliding window is a problem-solving technique that's designed to transform two nested loops into a single loop. It applies to arrays or lists. These problems are painless to solve using a brute force approach in $O(n^2)$ or $O(n^3)$. However, the sliding window technique can reduce the time complexity to $O(n)$.

📝 **Sliding window variants:**

1. Fixed size window
2. Variable size window
3. Two pointer approach
4. Optimization approach

📝 **Master sliding window through this resource:**
https://leetcode.com/discuss/general-discussion/1122776/summary-of-sliding-window-patterns-for-subarray-substring



Sliding Window Algorithm

2. Fixed size window

Problem 1: Sliding Window Maximum (Leetcode-239)
Problem 2: Max Sum Subarray of size K (GFG)

Fixed Size Sliding Window Approach:

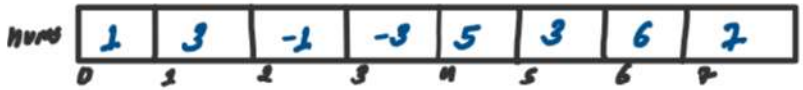
***Note**: Determine window size*
Fixed Size 'K' Window

***Step 1:** Process first 'K' elements*
Initial State

***Step 2:** Process remaining window*
- ***Remove***
- ***Addition***
- ***Store***

1. Sliding Window Maximum (Leetcode-239)

Ex

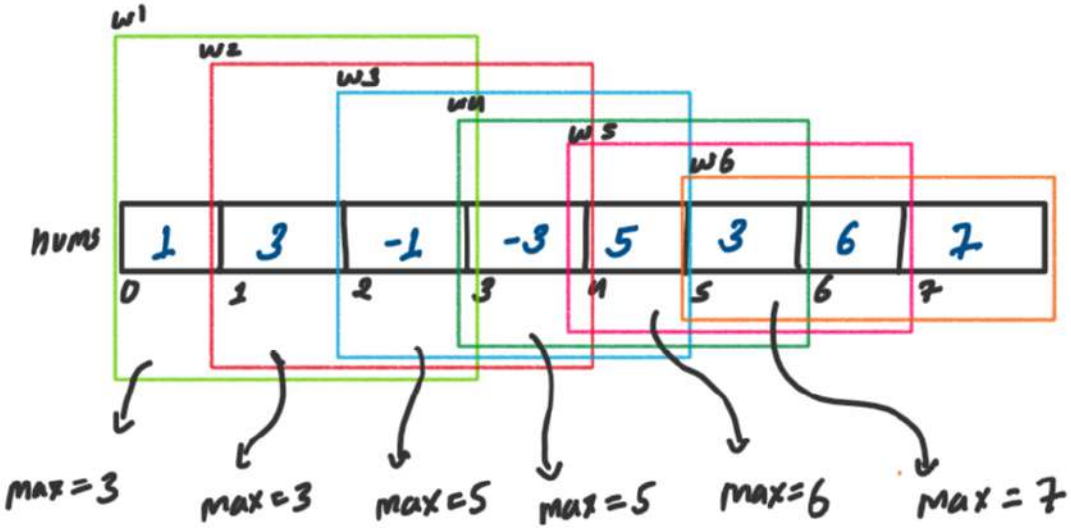


K=3

Output

Fixed size window

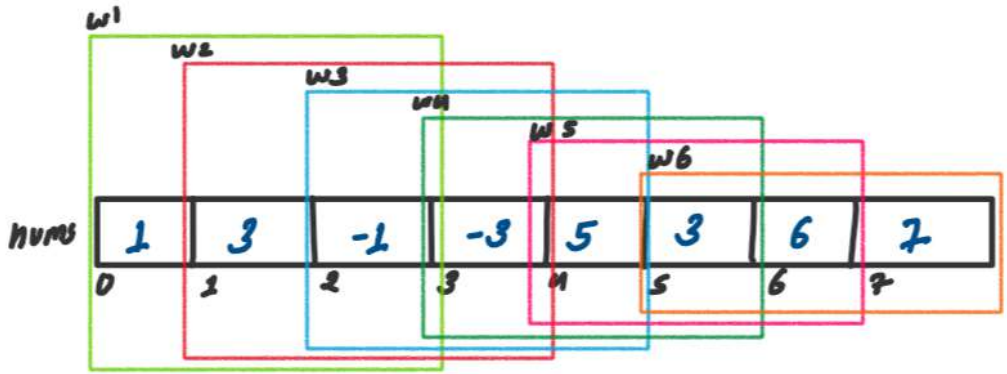
Explanation



K=3

N=size=8

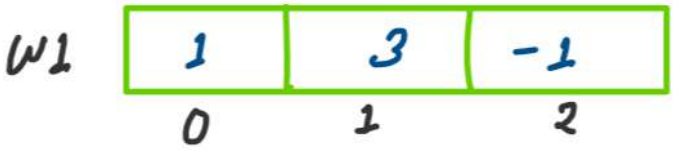
DRY RUN

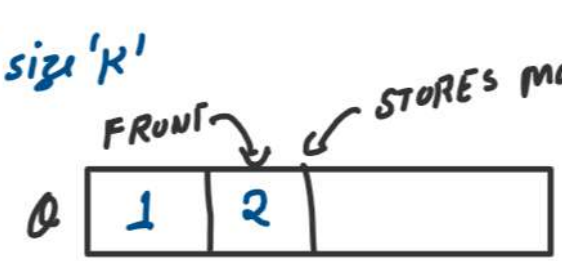


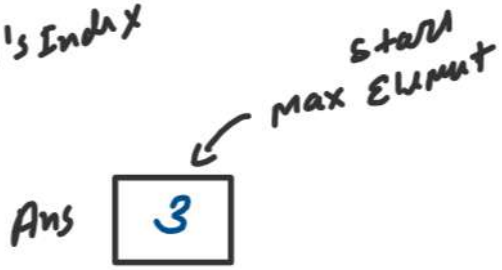
K = 3

N = size = 8

STEP1 Process first window of size 'K'

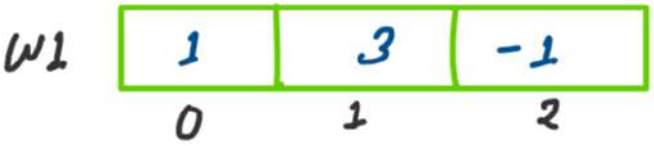


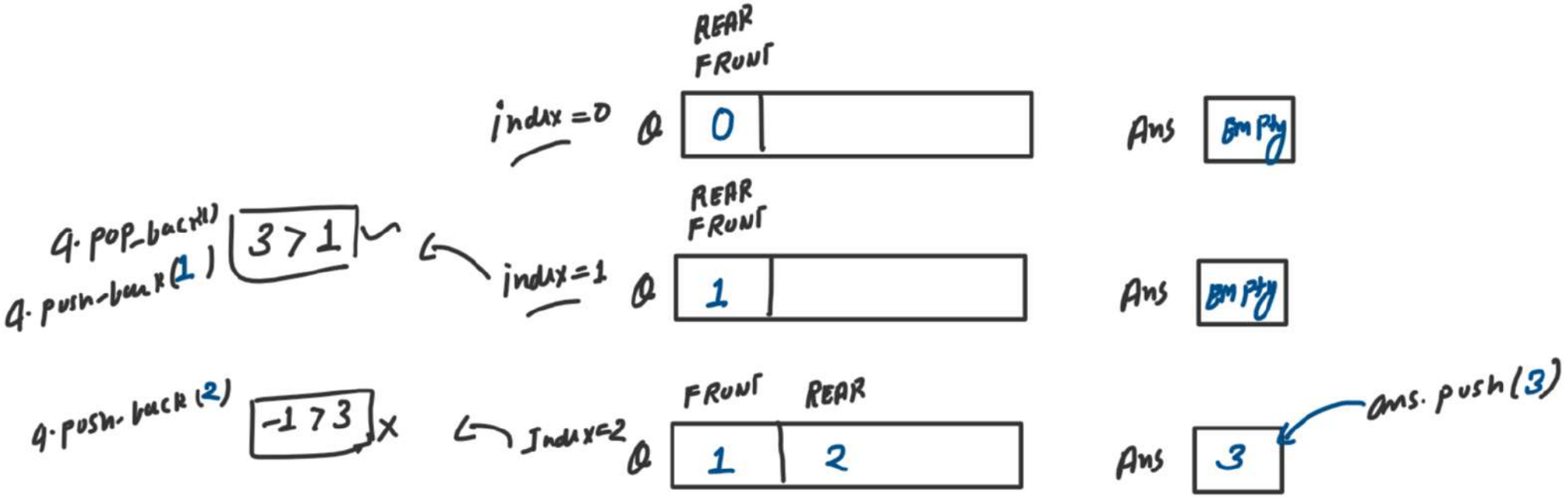




YEH KAISE FILL HO GYA?

STEP1 Process first window of size 'K'

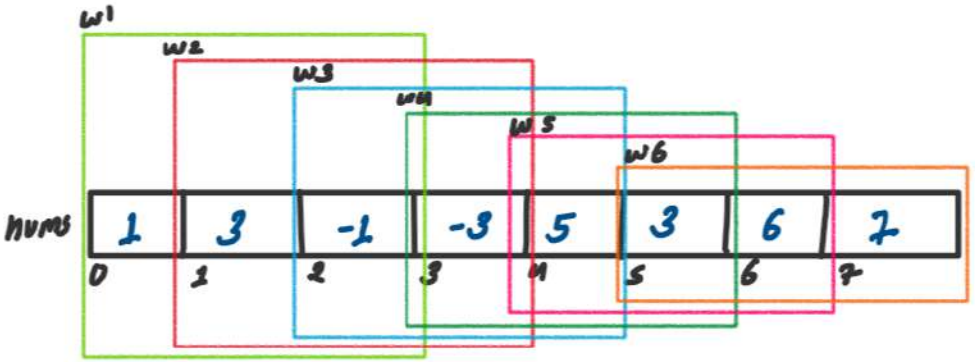




STEP2 Process Remaining windows

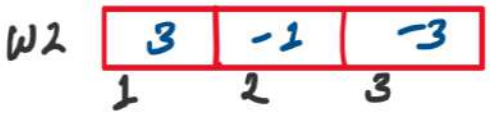
↳ Removal

Insertion



K = 3

N = size = 8



REMOVE (in queue)

(I) Out of Range [0, 1, 2]

(II) Chotta Element Removed

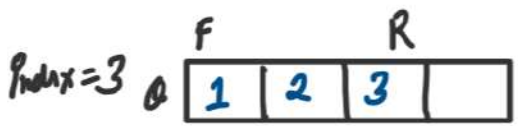
Index - q.front() >= K

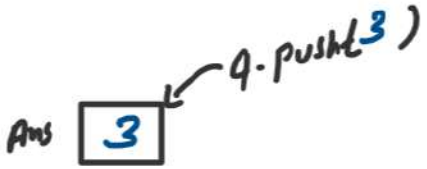
↳ q.pop_front();

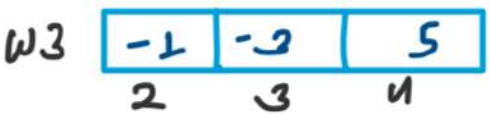
q.pop_back()

✗ (I) 3 - 1 >= 3

✗ (II) -3 > -1

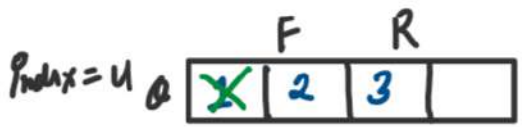


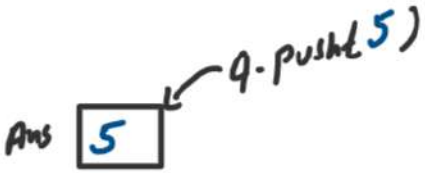




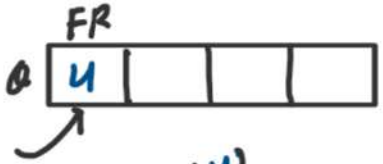
✓ (I) 4-1 >=3

✓ (II) 5 7-1





✓ (II) 5 7-3



REMOVE (inqueue)

(I) Out of Range [0,1,2]

(II) Chotta Element Revolved

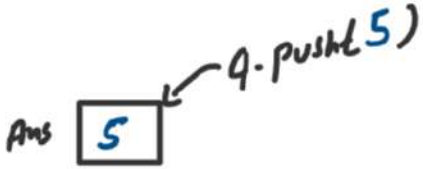
Index-q.front() >= K

↳ q.pop_front();

q.pop_back();

✗ (I) 5-4 >=3

✗ (II) 3 >= 5



REMOVE (in queue)

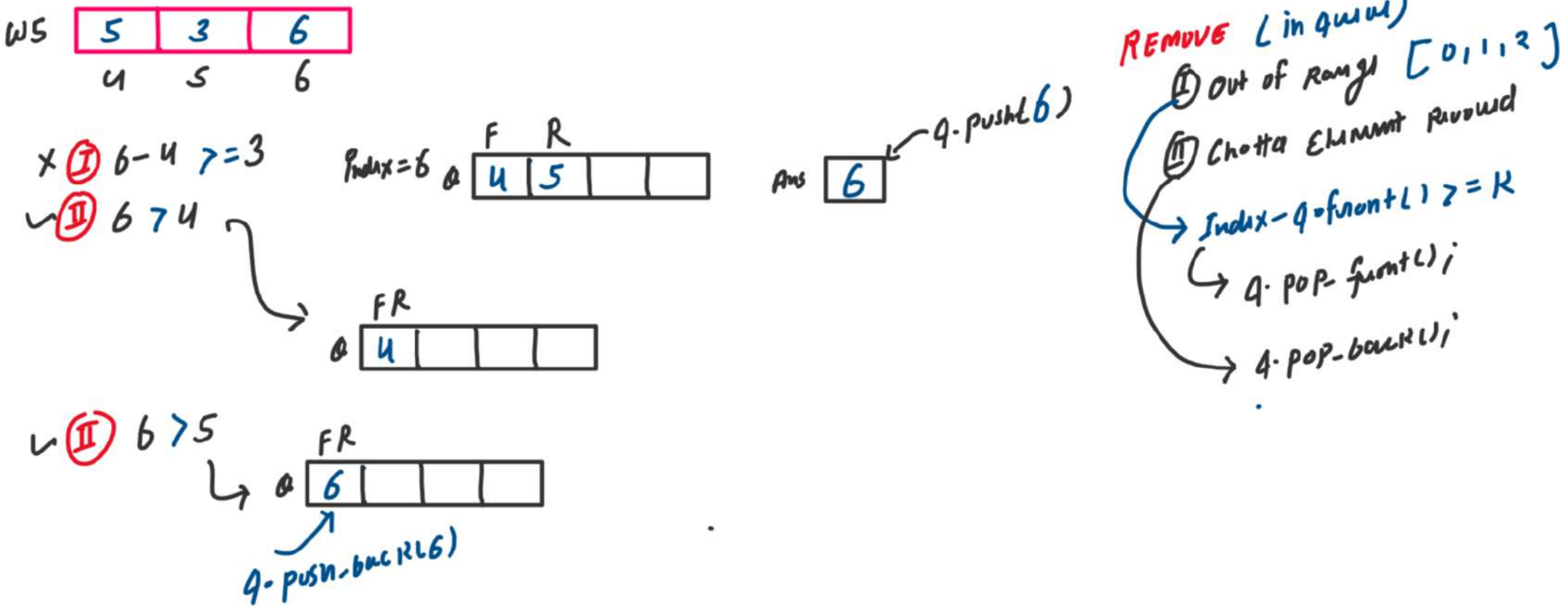
(I) Out of Range [0,1,2]

(II) Chotta Element Revoved

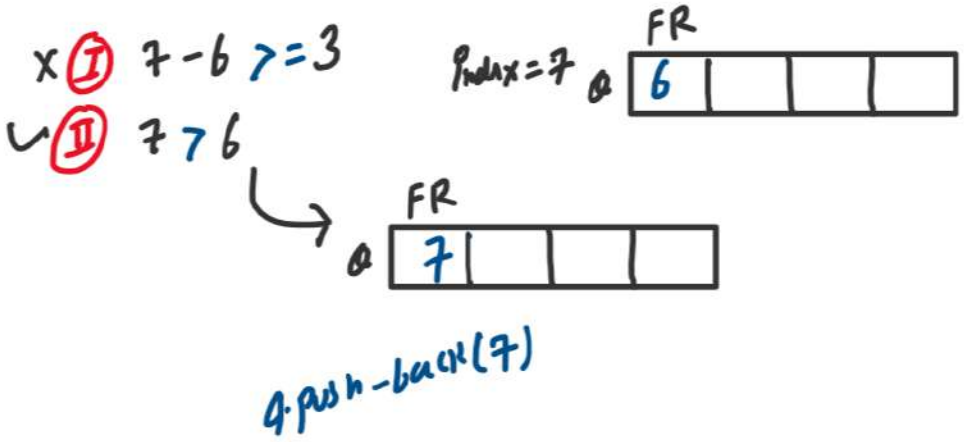
Index - q.front() >= K

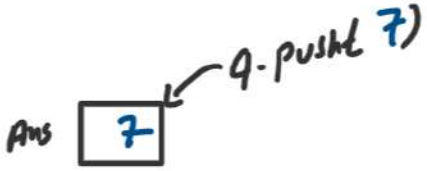
q.pop_front();

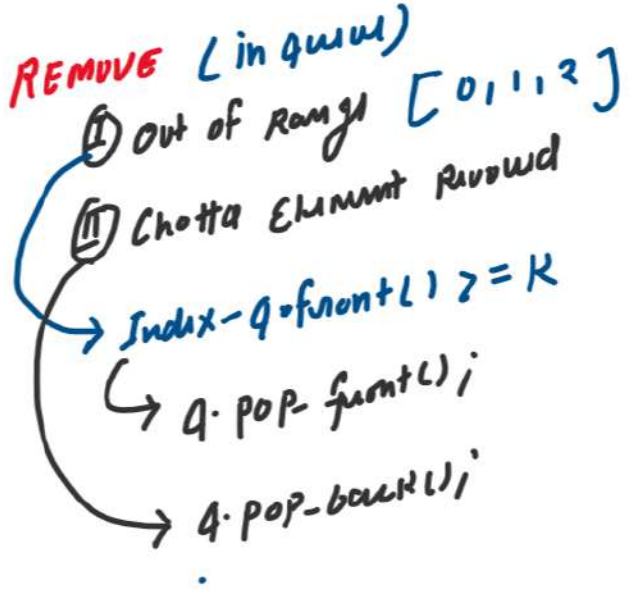
q.pop_back();


WS
5
3
6
4
5
6
x (I) 6-4 >=3
(II) 6 > 4
Index=6
Q
F
R
4
5
FR
Q
4
(II) 6 > 5
FR
Q
6
q.push_back(6)
Ans
6
q.push(6)
REMOVE (in queue)
(I) Out of Range [0,1,2]
(II) Chotta Element Removed
Index-q.front()>=K
q.pop_front();
q.pop_back();


WG
3
6
7
5
6
7


x (I) 7-6 >=3
(II) 7 > 6
Index=7
FR
Q
6
FR
Q
7
q.push_back(7)


q.push(7)
Ans
7


REMOVE (inQueue)
(I) Out of Range [0,1,2]
(II) Chotta Element Revoked
Index-q.front() >= K
q.pop_front();
q.pop_back();

```cpp
// 3. Sliding Window Maximum (Leetcode-239)

class Solution {
public:
    vector<int> maxSlidingWindow(vector<int>& nums, int k) {
        deque<int> q; // store the max element's index
        vector<int> ans; // store the max element

        // Step 1: process the first window for "k time"
        for(int index = 0; index < k; index++){
            int element = nums[index];

            // Agar queue me element chotta hai
            while(!q.empty() && element > nums[q.back()]){
                q.pop_back();
            }

            // Yanha tabhi pahuch skta hu
            // Ya to queue me element chotta nhi hai
            // Ya queue empty ho chuka hai
            q.push_back(index);
        }

        // Step 2: process remaning windows
    }
};
```

```cpp
    // Step 2: process remaning windows
    for(int index = k; index < nums.size(); index++){
        // Purani window ka ans store kardo
        ans.push_back(nums[q.front()]);

        // Remove
        // I -> remove the out of range index from queue
        if(!q.empty() && index - q.front() >= k){
            q.pop_front();
        }

        // II -> remove chotta index from queue
        // Agar queue me element chotta hai
        while(!q.empty() && nums[index] > nums[q.back()]){
            q.pop_back();
        }

        // Addition
        // Yanha tabhi pahuch skta hu
        // Ya to queue me element chotta nhi hai
        // Ya queue empty ho chuka hai
        q.push_back(index);
    }

    // Last window ka ans store karlo
    ans.push_back(nums[q.front()]);

    return ans;
```

Time Complexity: *O(N),*
where N is size of array

Space Complexity: *O(K),*
where K is the size of the window

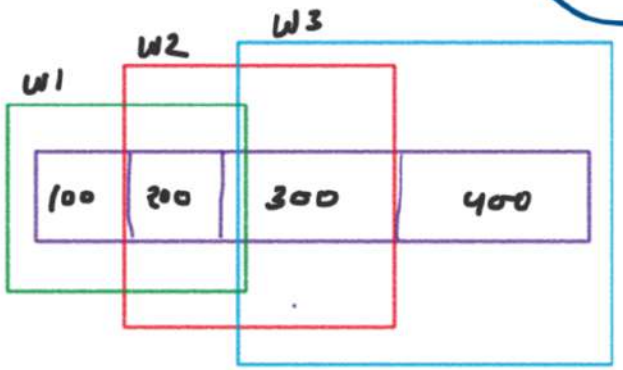
2. Max Sum Subarray of Size K (GFG)

Problem Statement:
Given an array of integers **Arr** of size **N** and a number **K**. Return the **maximum sum** of a subarray of **size K**.

Fixed size window

NOTE: A subarray is a contiguous part of any given array.

Example 1:
Input: N = 4, K = 2, Arr = [100, 200, 300, 400]
Output: 700
Explanation: Arr3 + Arr4 =700, which is maximum.



Example 2:
Input: N = 4, K = 4, Arr = [100, 200, 300, 400]
Output: 1000
Explanation: Arr1 + Arr2 + Arr3 + Arr4 =1000, which is maximum.

sum of
W1 = 100 + 200
W2 = 200 + 300
W3 = 300 + 400

max sum
= 300 + 400
= 700

```cpp
class Solution{
public:
    long maximumSumSubarray(int K, vector<int> &Arr , int N){
        long long maxSum = INT_MIN;
        long long windowSum = 0;

        // Step 1: process the first window for "K time"
        for(long long index = 0; index < K; index++){
            windowSum += Arr[index];
        }

        // Initialize maxSum with the sum of the first window
        maxSum = windowSum;

        // Step 2: process remaning windows
        for(long long index = K; index < N; index++){
                windowSum += Arr[index] - Arr[index - K];
                maxSum = max(maxSum, windowSum);
        }

        return maxSum;
    }
};
```

Time Complexity: *O(N)*
Space Complexity: *O(1)*