

COMP6771

Week 7.2 – Generic Programming

# Concepts

*“Somewhat more formally, a concept is a description of requirements on one or more types stated in terms of the existence and properties of procedures, type attributes, and type functions defined on the types.*

— *Elements of Programming*, by Alexander Stepanov and Paul McJones.

# What's in a requirement?

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We say that we *satisfy* the requirements if all the constraints evaluate as true. We *model* the concept if, and only if, we satisfy the requirements and meet the axioms and complexity requirements.

# Hello, concepts!

```
1 template<typename T>
2 concept type = true;
3
4 template<typename T>
5 requires type<T>
6 void hello(T)
7 {
8     std::cout << "Permissive, base-case\n";
9 }
10
11 int main()
12 {
13     hello(0);
14     hello(0.0);
15     hello("base-case");
16 }
```

Try it on Compiler Explorer!

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```

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1 template<typename T>
2 concept type = true;
3
4 template<type T> // same as using `typename` right now
5 void hello(T)
6 {
7     std::cout << "Permissive, base-case\n";
8 }
9
10 int main()
11 {
12     hello(0);
13     hello(0.0);
14     hello("base-case");
15 }
```

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# Hello, concepts!

```
1 template<typename T>
2 concept integral = std::is_integral_v<T>;
3
4 template<integral T>
5 void hello(T)
6 {
7     std::cout << "Integral case\n";
8 }
9
10 int main()
11 {
12     hello(0);
13     //hello(0.0);
14     //hello("base-case");
15 }
```

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# Hello, concepts!

```
1 template<typename T>
2 concept floating_point = std::is_floating_point_v<T>;
3
4 void hello(floating_point auto)
5 {
6     std::cout << "Floating-point case\n";
7 }
8
9 int main()
10 {
11     // hello(0);
12     hello(0.0);
13     // hello("base case");
14 }
```

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# Hello, concepts!

```
1 void hello(integral auto)      { std::cout << "Integral case\n"; }
2 void hello(floating_point auto) { std::cout << "Floating-point case\n"; }
3 void hello(auto)              { std::cout << "Base-case\n"; }
4
5 int main()
6 {
7     hello(0);                  // prints "Integral case"
8     hello(0.0);                // prints "Floating-point case"
9     hello("base case"); // prints "Base-case"
10 }
```

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# Refining and weakening concepts

A concept C2 *refines* a concept C1, if whenever C2 is modelled, C1 is also modelled.

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A concept C2 *refines* a concept C1, if whenever C2 is modelled, C1 is also modelled.

A concept C2 *weakens* C1, if its requirements are a proper subset of C1.

# Hello, concepts!

```
1 void hello(integral auto) { std::cout << "Integral case\n"; }
2
3 template<typename T>
4 concept signed_integral = integral<T> and std::is_signed_v<T>;
5
6 void hello(signed_integral auto) { std::cout << "Signed integral case\n"; }
7
8 int main()
9 {
10    hello(0); // prints "Signed integral case"
11    hello(0U); // prints "Integral case"
12 }
```

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# Hello, concepts!

```
signed_integral refines integral  
1 void hello(integral auto) { std::cout << "Integral case\n"; }  
2  
3 template<typename T>  
4 concept signed_integral = integral<T> and std::is_signed_v<T>;  
5  
6 void hello(signed_integral auto) { std::cout << "Signed integral case\n"; }  
7  
8 int main()  
9 {  
10    hello(0); // prints "Signed integral case"  
11    hello(0U); // prints "Integral case"  
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signed_integral refines integral  
1 void hello(integral auto) { std::cout << "Integral case\n"; }  
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3 template<typename T>  
4 concept signed_integral = integral<T> and std::is_signed_v<T>;  
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7  
8 int main()  
9 {  
10    hello(0); // prints "Signed integral case"  
11    hello(0U); // prints "Integral case"  
12 }
```

Try it on Compiler Explorer!

# Library concepts

C++20 not only introduced concepts as a language feature, but also three families of highly usable concepts.

Due to many reasons they are available in GCC 10, but not Clang with libc++ (which is what we use in the course).

There's a 1:1 mapping between concepts in range-v3 and what's in the standard library (namespaces aside).

Concepts family	Relevant header	CMakeLists LINK:	Namespace:
<a href="#">C++ Reference: Concepts library</a>	<concepts/concepts.hpp>	range-v3-concepts	concepts
<a href="#">C++ Reference: Iterators library</a>	<range/v3/iterator.hpp>	range-v3	ranges
<a href="#">C++ Reference: Ranges library</a>	<range/v3/range.hpp>	range-v3	ranges

# Motivation

```
1 struct equal_to {  
2     template<typename T, typename U>  
3     auto operator()(T const& t, U const& u) const -> bool  
4     {  
5         return t == u;  
6     }  
7 };
```

# Motivation

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1 struct equal_to {  
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3     auto operator()(T const& t, U const& u) const -> bool  
4     {  
5         return t == u;  
6     }  
7 };
```

equal_to{}(0, 0)	// okay, returns true
equal_to{}(std::vector{0}, std::vector{1})	// okay, returns false
equal_to{}(0, 0.0)	// okay, returns true
equal_to{}(0.0, 0)	// okay, returns true
equal_to{}(0, std::vector<int>{})	// error: `int == vector` not defined

# Motivation

```
1 struct equal_to {  
2     template<typename T, std::equality_comparable_with<T> U>  
3     auto operator()(T const& t, U const& u) const -> bool  
4     {  
5         return t == u;  
6     }  
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# Motivation

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equal_to{}(0, 0)	// okay, returns true
equal_to{}(std::vector{0}, std::vector{1})	// okay, returns false
equal_to{}(0, 0.0)	// okay, returns true
equal_to{}(0.0, 0)	// okay, returns true
equal_to{}(0, std::vector<int>{})	// still error, but makes more sense

# Regularity

```
1 template<typename T>
2 concept movable = std::is_object_v<T>
3         and std::move_constructible<T>
4         and std::assignable_from<T&, T>
5         and std::swappable<T>;
```

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2 concept movable = std::is_object_v<T>
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```

```
1 template<typename T>
2 concept copyable = std::copy_constructible<T>
3         and std::movable<T>
4         and std::assignable_from<T&, T const&>;
```

# Regularity

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1 template<typename T>
2 concept movable = std::is_object_v<T>
3           and std::move_constructible<T>
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```

```
1 template<typename T>
2 concept semiregular = std::copyable<T> and std::default_initializable<T>;
```

# Regularity

```
1 template<typename T>
2 concept movable = std::is_object_v<T>
3             and std::move_constructible<T>
4             and std::assignable_from<T&, T>
5             and std::swappable<T>;
6
7 template<typename T>
8 concept copyable = std::copy_constructible<T>
9             and std::movable<T>
10            and std::assignable_from<T&, T const&>;
11
12 template<typename T>
13 concept semiregular = std::copyable<T> and std::default_initializable<T>;
14
15 template<typename T>
16 concept regular = std::semiregular<T> and std::equality_comparable<T>;
```

Previously on COMP6771...

A range is an ordered sequence of elements  
with a designated start and rule for finishing

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`std::string("Hello, world!")`

`std::vector<std::string>{ "Hello", "world!" }`

$\mathbb{N}$     $\mathbb{Z}^+$     $\mathbb{Q}^+$     $\mathbb{R}^+$

Exercise: how can  $\mathbb{C}$  be made into a range?

`for (auto i = 0; std::cin >> i;) { ... }`

# Iterators and pointers

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*“ Iterators are a generalization of pointers that allow a C++ program to work with different data structures... in a uniform manner.*

—Working Draft, Standard for Programming Language C++

```
1 template<typename T, std::equality_comparable_with<T> U>
2 auto find(std::vector<T> const& r, U const& value) -> std::vector<T>::size_type {
3     for (auto i = typename std::vector<T>::size_type{0}; i < r.size(); ++i) {
4         if (r[i] == value) {
5             return i;
6         }
7     }
8     return r.size();
9 }
```

```
1 template<typename T, std::equality_comparable_with<T> U>
2 auto find(std::deque<T> const& r, U const& value) -> std::deque<T>::size_type {
3     for (auto i = typename std::deque<T>::size_type{0}; i < r.size(); ++i) {
4         if (r[i] == value) {
5             return i;
6         }
7     }
8     return r.size();
9 }
```

$x$  sequence containers

$\times$

$y$  sequence algorithms (e.g. find)

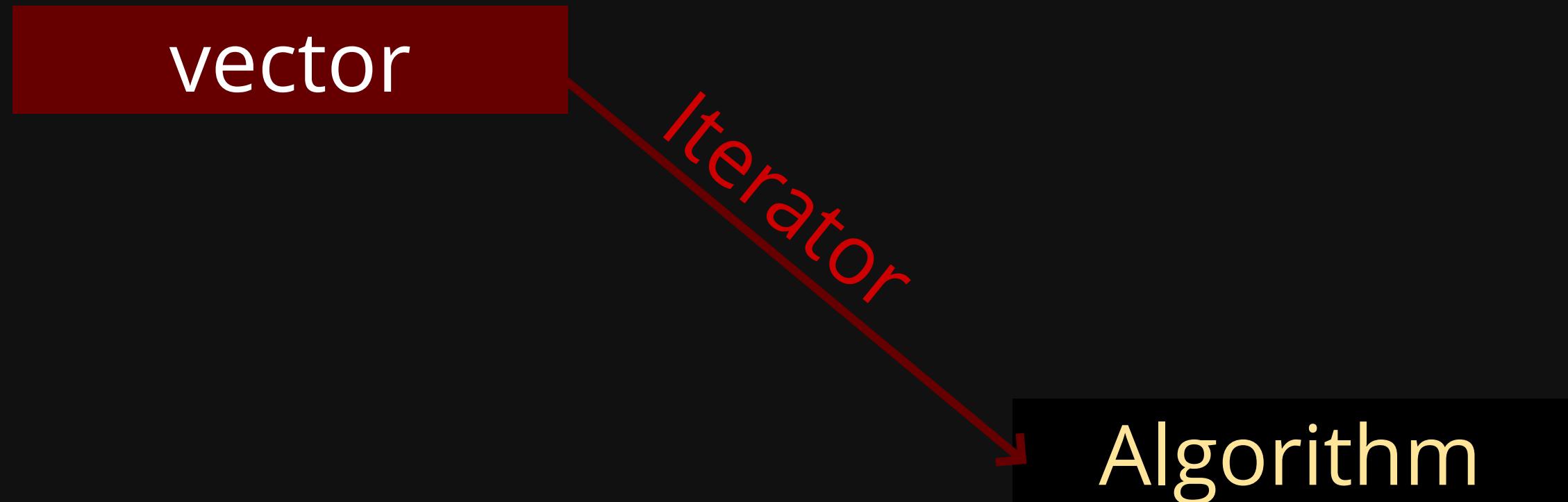
$\approx$

$xy$  algorithm implementations

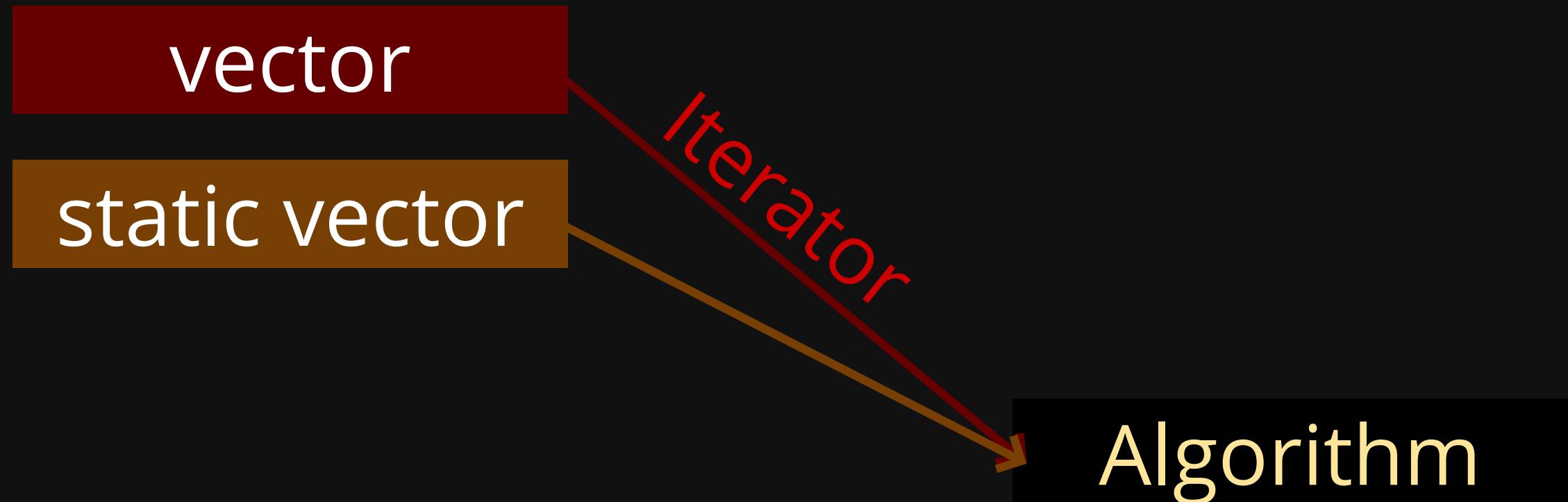
# We need an intermediate representation

Algorithm

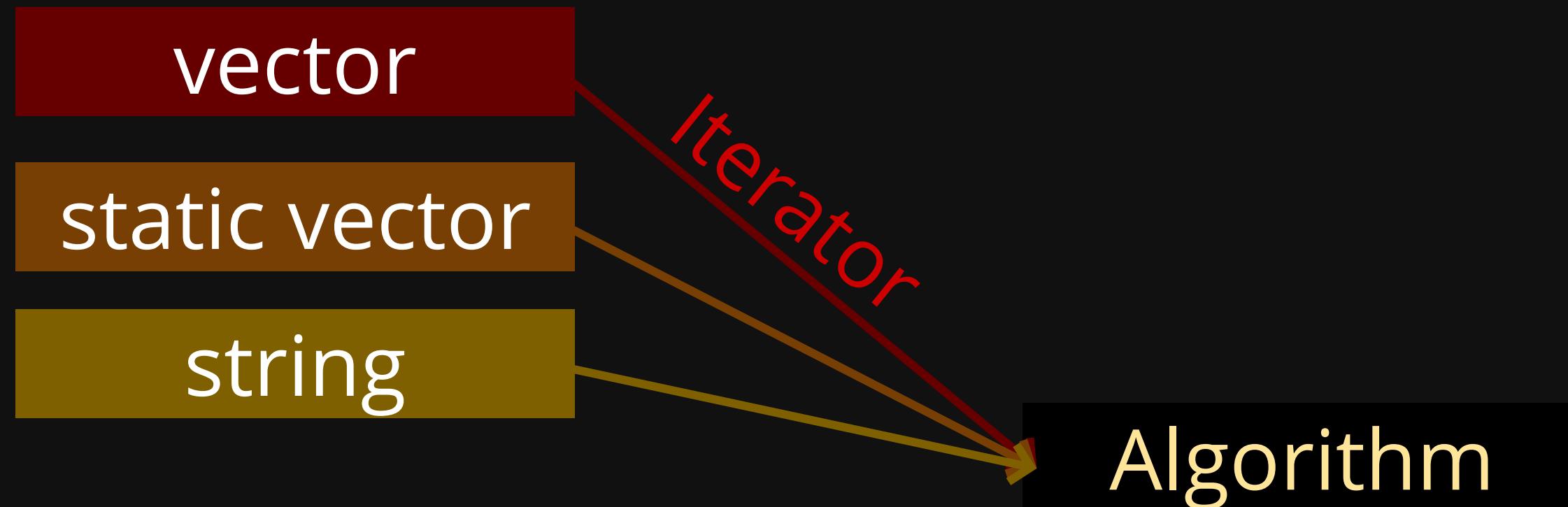
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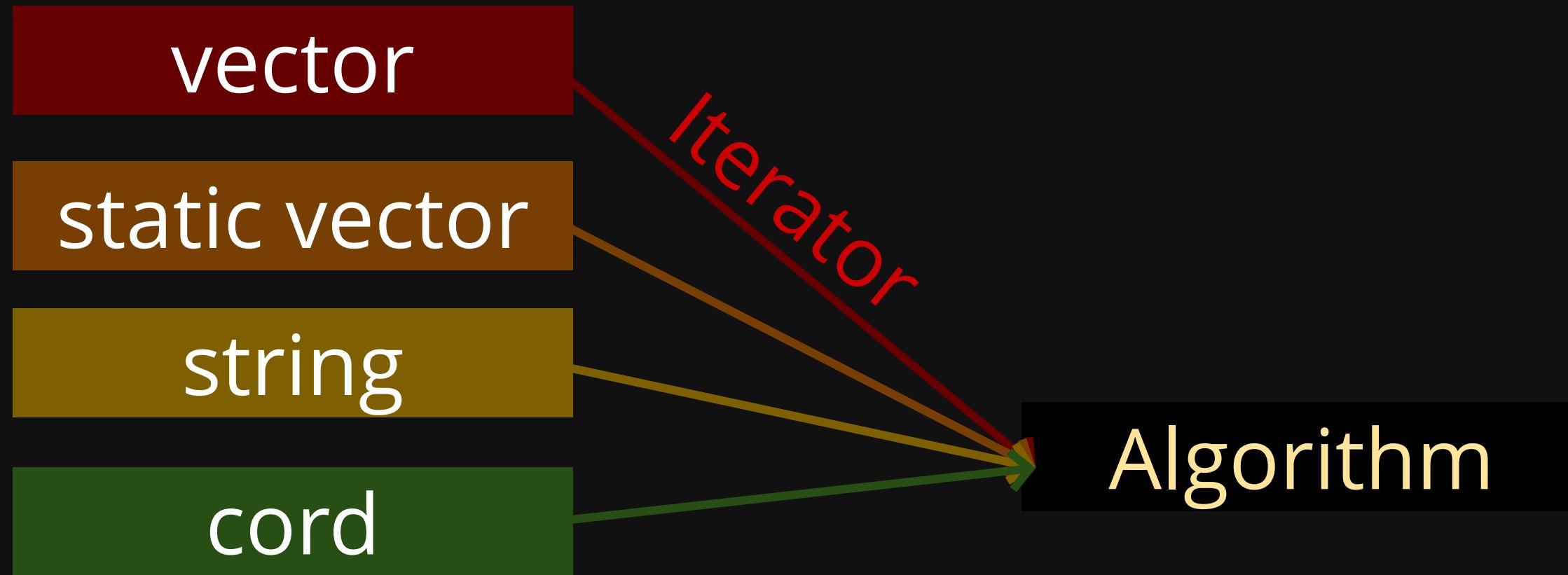
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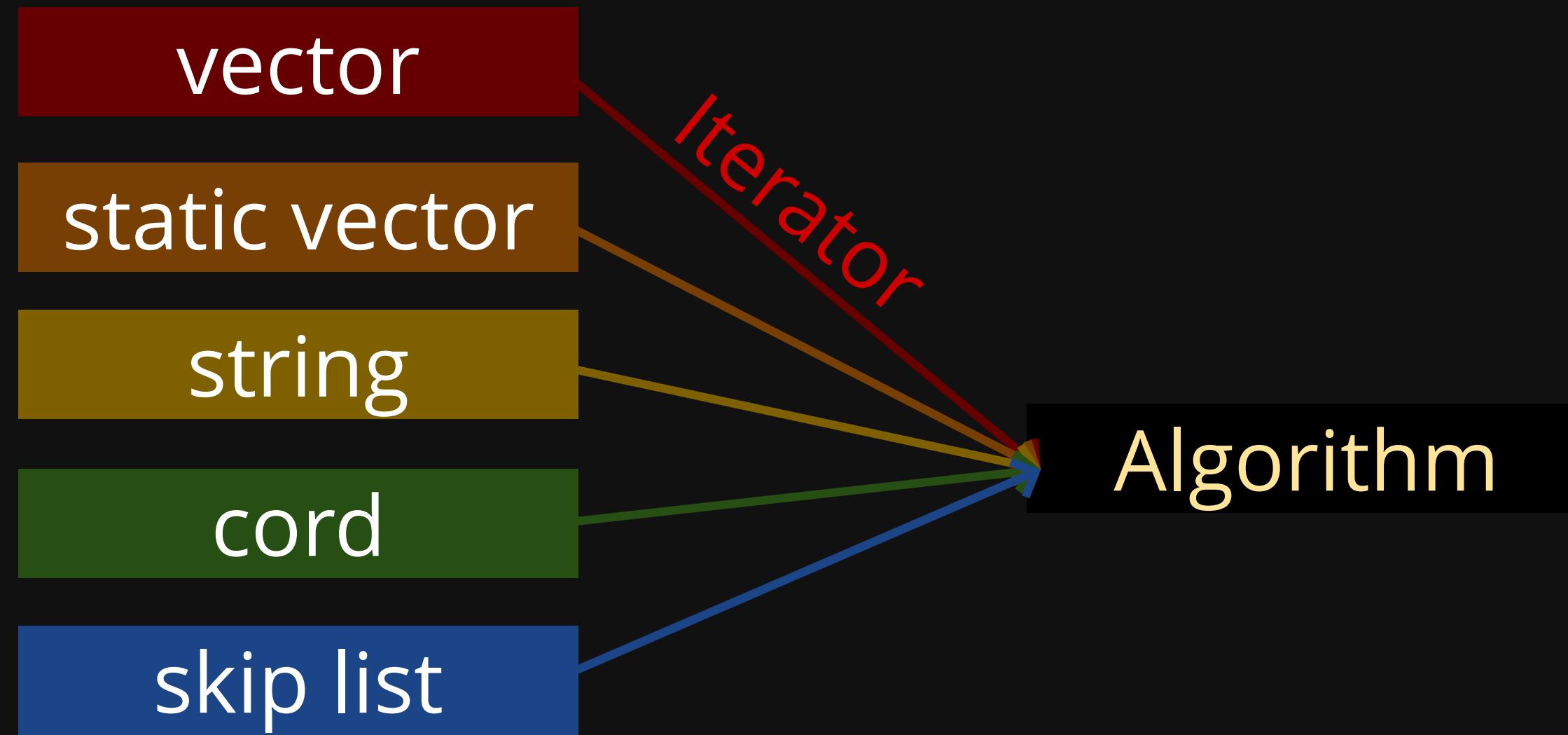
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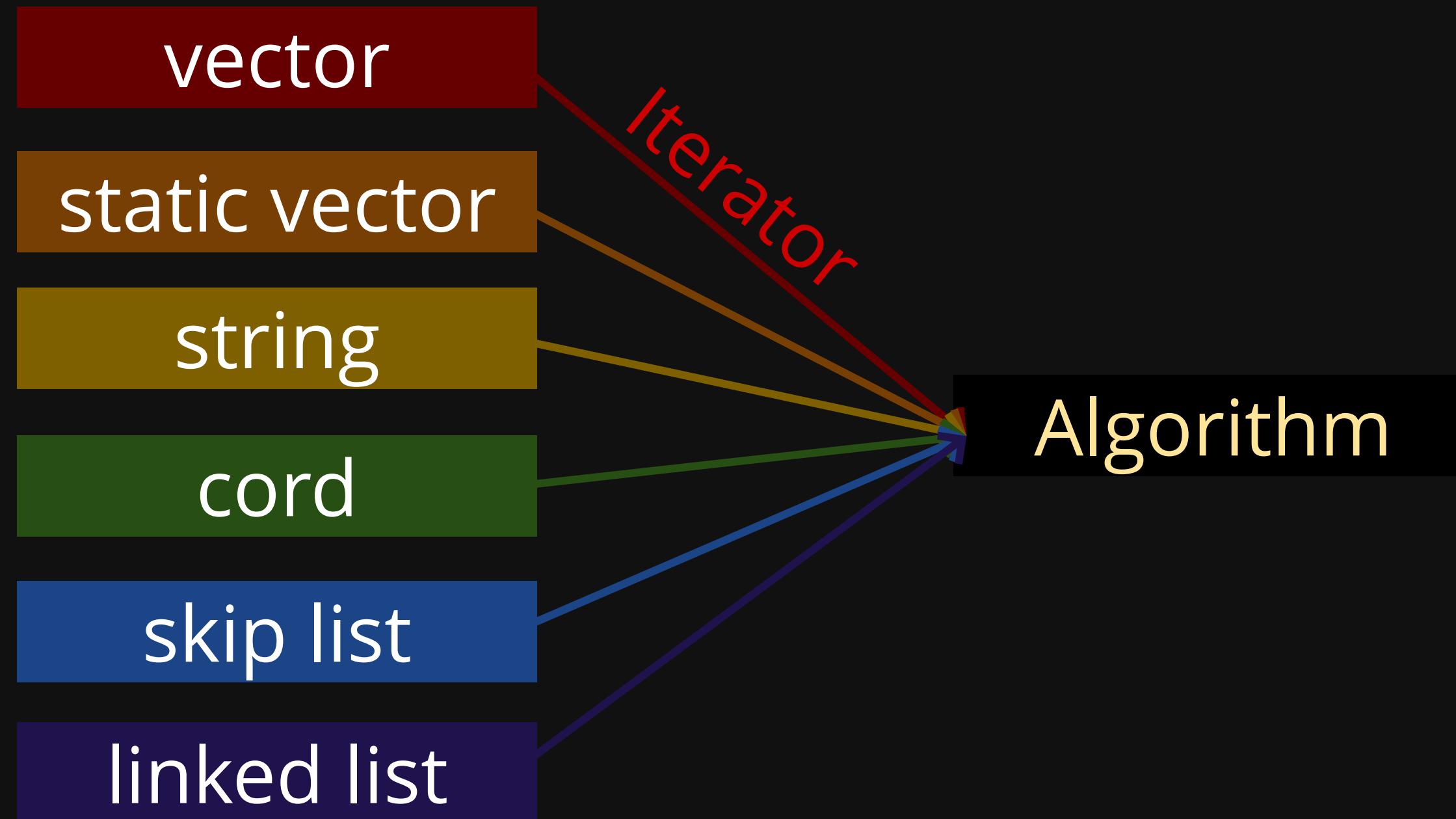
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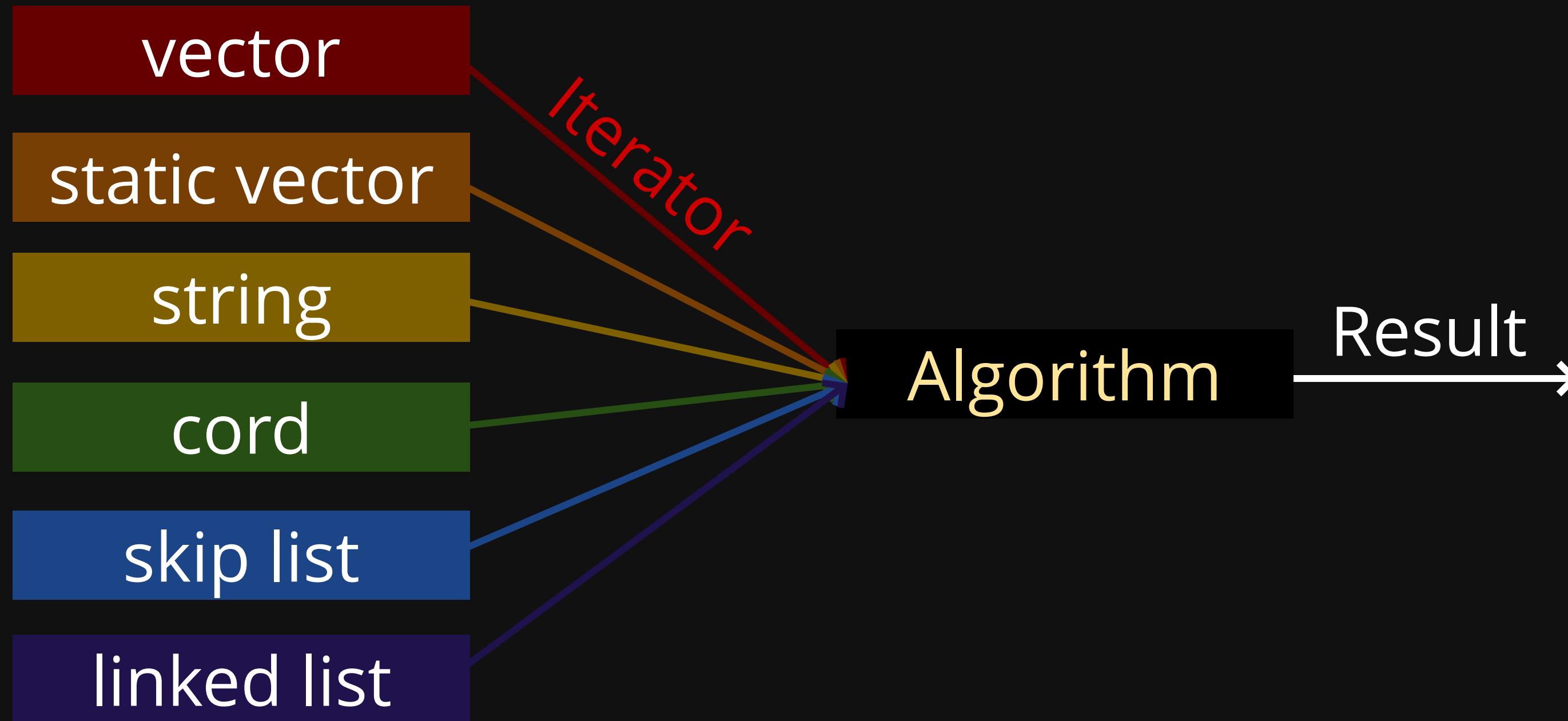
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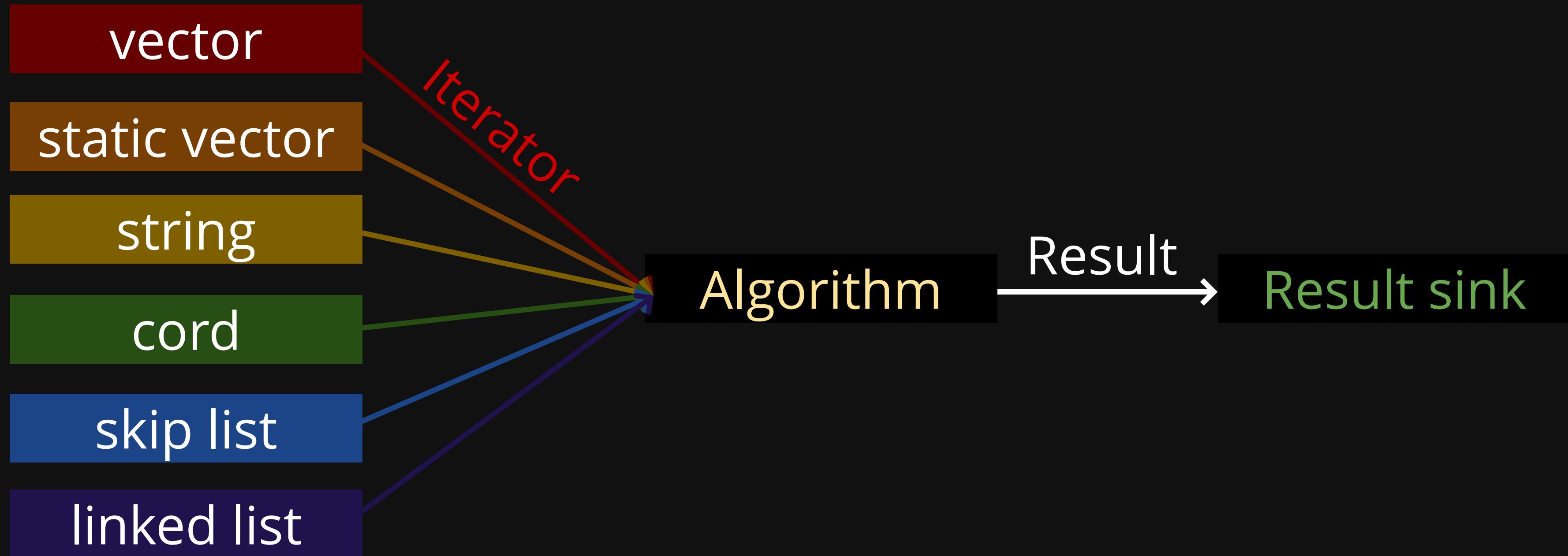


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The result may be a one or more iterators, a scalar value, or some combination of both.

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$x$  sequence containers

+

$y$  sequence algorithms (e.g. find)

≈

$x + y$  total implementations

# What makes an iterator tick?

# Iterators let us write a generic find

```
1 {
2     auto const v = std::deque<int>{0, 1, 2, 3, 4, 5, 6, 7, 8, 9};
3     auto result = ranges::find(v.begin(), v.end(), 6);
4     if (result != v.end()) {
5         std::cout << "Found 6!\n";
6     }
7     else {
8         std::cout << "Didn't find 6.\n";
9     }
10 }
```

# Iterator invalidation

- Iterator is an abstract notion of a **pointer**
- What happens when we modify the container?
  - What happens to iterators?
  - What happens to references to elements?
- Using an invalid iterator is undefined

```
1 auto v = std::vector<int>{1, 2, 3, 4, 5};
2 // Copy all 2s
3 for (auto it = v.begin(); it != v.end(); ++it) {
4     if (*it == 2) {
5         v.push_back(2);
6     }
7 }
8 // Erase all 2s
9 for (auto it = v.begin(); it != v.end(); ++it) {
10    if (*it == 2) {
11        v.erase(it);
12    }
13 }
```

# Iterator invalidation - push\_back

- Think about the way a vector is stored
- "If the new `size()` is greater than `capacity()` then all iterators and references (including the past-the-end iterator) are invalidated. Otherwise only the past-the-end iterator is invalidated."

```
1 auto v = std::vector<int>{1, 2, 3, 4, 5};  
2 // Copy all 2s  
3 for (auto it = v.begin(); it != v.end(); ++it) {  
4     if (*it == 2) {  
5         v.push_back(2);  
6     }  
7 }
```

# Iterator invalidation - erase

- "Invalidates iterators and references at or after the point of the erase, including the `end()` iterator."
- For this reason, `erase` returns a new iterator

```
1 std::vector v{1, 2, 3, 4, 5};  
2 // Erase all even numbers  
3 for (auto it = v.begin(); it != v.end(); ) {  
4     if (*it % 2 == 0) {  
5         it = v.erase(it);  
6     } else {  
7         ++it;  
8     }  
9 }
```

# Iterator invalidation - general

- Containers generally don't invalidate when you modify values
- But they may invalidate when removing or adding elements
- `std::vector` invalidates everything when adding elements
- `std::unordered_(map/set)` invalidates all iterators when adding elements
- `std::map/std::set` doesn't invalidate iterators upon insertion (why?)

# Iterator adaptors

Wrapper around a type to grant that type iterator properties.

or

Wrapper around an iterator type to grant additional or different iterator properties.

## Example: std::reverse\_iterator

std::reverse\_iterator is an iterator adaptor that transforms an existing iterator's operator++ to mean "move backward" and operator-- to mean "move forward".

```
std::reverse_iterator<std::vector<int>::iterator>
```

# Readable iterators

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Read element	<code>v[i]</code>	<code>i-&gt;value</code>	<code>*i</code>
Successor	<pre>j = i + n &lt; ranges::distance(v) ? i + n : ranges::distance(v);</pre>	<code>j = i-&gt;successor(n)</code>	<code>ranges::next(i, s, n)</code>

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Successor	<code>j = i + n &lt; ranges::distance(v)</code> <code>? i + n</code> <code>: ranges::distance(v);</code>	<code>j = i-&gt;successor(n)</code>	<code>ranges::next(i, s, n)</code>
Advance fwd	<code>++i</code>	<code>i = i-&gt;next</code>	<code>++i</code>

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Read element	<code>v[i]</code>	<code>i-&gt;value</code>	<code>*i</code>
Successor	<code>j = i + n &lt; ranges::distance(v)</code> <code>? i + n</code> <code>: ranges::distance(v);</code>	<code>j = i-&gt;successor(n)</code>	<code>ranges::next(i, s, n)</code>
Advance fwd	<code>++i</code>	<code>i = i-&gt;next</code>	<code>++i</code>
Comparison	<code>i &lt; ranges::distance(v)</code>	<code>i != nullptr</code>	<code>i != s</code>

# Indirectly readable

A type  $I$  models the concept `std::indirectly_readable` if:

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`std::iter_value_t<I>`

A type we can create an lvalue from.

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The type `I::operator*` returns.

`std::iter_rvalue_reference_t<I>`

The type `ranges::iter_move(i)` returns.

2. These type pairs share a "relationship":

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`std::iter_value_t<I>&`

// Approximately  
`std::move(*i)`

`std::iter_reference_t<I>`

`std::iter_rvalue_reference_t<I>`

`std::iter_rvalue_reference_t<I>`

`std::iter_value_t<I> const&`

3. Given an object `i` of type `I`, `*i` outputs the same thing when called with the same input.

# Generating those iter\_ types (preamble)

```
1 template<typename T>
2 class linked_list {
3 public:
4     class iterator;
5 private:
6     struct node {
7         T value;
8         std::unique_ptr<node> next;
9         node* prev;
10    };
11
12    std::unique_ptr<node> head_;
13 }
```

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# Generating those iter\_ types (preamble)

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9         return pointee_->value;
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Let `i` be an object of type `I`.

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# Generating `std::iter_difference_t<I>`

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1 template<typename T>
2 class linked_list<T>::iterator {
3 public:
4     using value_type = T;
5     using difference_type = std::ptrdiff_t; // std::iter_difference_t<iterator> is difference_type
6
7     iterator() = default;
8
9     auto operator*() const noexcept -> value_type const& { ... }
10
11    auto operator++() -> iterator& {
12        pointee_ = pointee_->next.get();
13        return *this;
14    }
15
16    auto operator++(int) -> void { ++*this; }
17 private:
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# Iterator basis

`std::input_or_output_iterator` is the root concept for all six iterator categories.

A type `I` models the concept `std::input_or_output_iterator` if:

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A type `I` models the concept `std::input_or_output_iterator` if:

1. `I` models `std::weakly_incrementable`
2. `*i` is a valid expression returns a reference to an object.

# Input iterators

`std::input_iterator` describes the requirements for an iterator that can be read from.

A type  $\mathcal{I}$  models the concept `std::input_iterator` if:

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# Input iterators

`std::input_iterator` describes the requirements for an iterator that can be read from.

A type `I` models the concept `std::input_iterator` if:

1. `I` models `std::input_or_output_iterator`
2. `I` models `std::indirectly_readable`
3. `I::iterator_category` is a type alias derived from `std::input_iterator_tag`

# Input iterators let us write an generic find

```
1 template<std::input_iterator I, typename T>
2 requires std::indirect_binary_predicate<ranges::equal_to, I, T const*>
3 auto find(I first, I last, T const& value) -> I {
4     for (; first != last; ++first) {
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10    return last;
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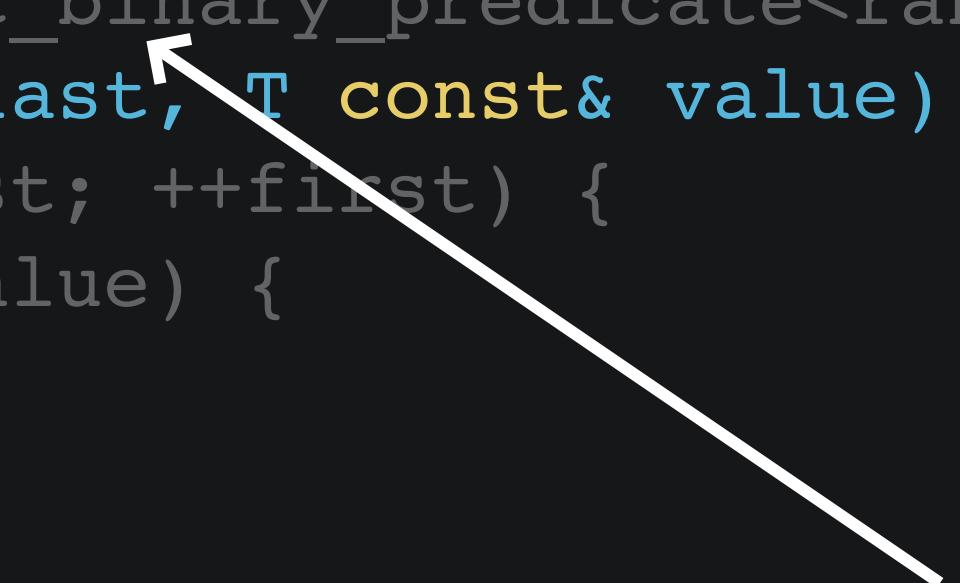


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This is how we check `*first == value` is valid.

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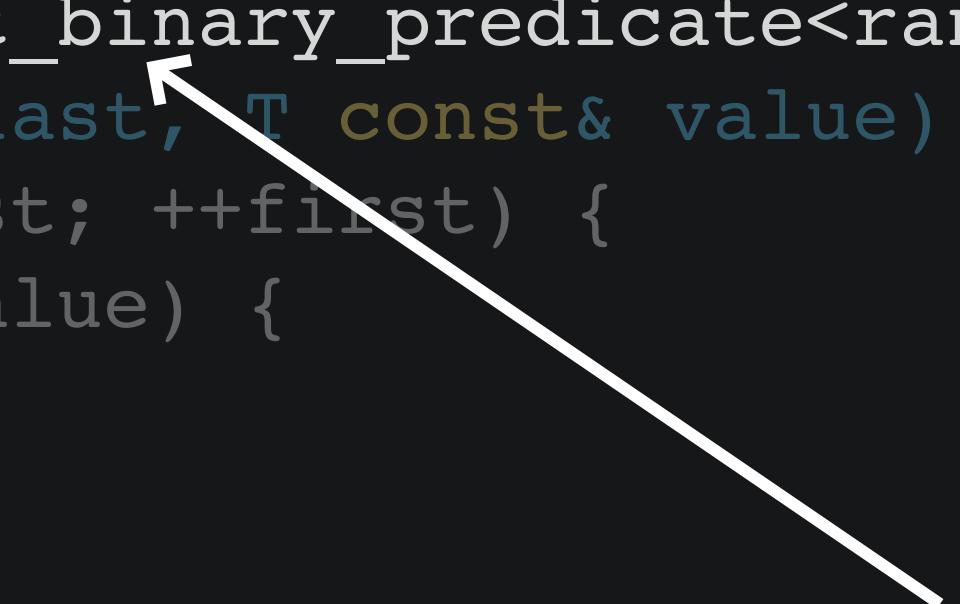


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This is how we check `*first == value` is valid.



# Modelling std::input\_iterator<I>

```
1 template<typename T>
2 class linked_list<T>::iterator {
3 public:
4     using value_type = T;
5     using difference_type = std::ptrdiff_t;
6     using iterator_category = std::input_iterator_tag;
7
8     iterator() = default;
9
10    auto operator*() const noexcept -> value_type const& { ... }
11
12    auto operator++() -> iterator& { ... }
13    auto operator++(int) -> void { ++*this; }
14 private:
15     //...
16 };
17
18 static_assert(std::input_iterator<linked_list<int>::iterator>);
```

# tl;dr

`std::weakly_incrementable<I>`

Requires:

`I::difference_type` is a signed integer  
`++i` and `i++` move `i` to next element in  $O(1)$  time  
`++i` returns a reference to itself

`std::input_or_output_iterator<I>`

Requires:

`*i` return type can be a reference

`std::input_iterator<I>`

Requires:

`I::iterator_category` is derived from `std::input_iterator_tag`

`std::indirectly_readable<I>`

Requires:

`I::value_type` exists  
`*i` always outputs the same thing given the same input

Type of `*i` and `I::value_type` have a type in common

# Design problem?

```
1 // real find
2 template<std::input_iterator I, typename T>
3 auto find(I first, I last, T const& value) -> I;
4
5 // bounded find
6 template<std::input_iterator I, typename T>
7 auto find_n(I first, std::iter_difference_t<I> n, T const& value) -> I {
8     for (; n > 0; ++first, (void)--n) {
9         if (*first == value) {
10             return first;
11         }
12     }
13     return first;
14 }
```

There are >100 algorithms. Do you *really* want to define copy\_n, lower\_bound\_n, sort\_n, etc.?

# Counted iterators

```
// We leverage this through range-v3 in 20T2
// (it's available as std:: in GCC 10)
template<std::input_iterator I>
counted_iterator<I>::counted_iterator(I first, std::iter_difference_t<I> n);
```

```
1 std::ranges::find(
2     std::counted_iterator{first, 10},
3     ???,
4     value)
```

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1 std::ranges::find(
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3     std::counted_iterator<int>(), // well, that's a bit weird
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It's weird because we are giving meaning to an arbitrary value, and it doesn't really express intentions to the reader.

It's also limiting, because we can't express any additional information. What if we wanted to also stop on the first even int?

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# Introducing sentinels

A sentinel is a type that denotes the end of a range. It might be an iterator of the same type (like with containers), or it might be a completely different type.

Types `S` and `I` model the concept `std::sentinel_for<S, I>` if:

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Let `i` be an object of type `I` and `s` be an object of type `S`.

1. `i == s` is well-defined (i.e. it returns `bool` and we have the other three).
2. If `i != s` is true, then `i` is dereferenceable.

# std::default\_sentinel

The default sentinel is type-based a way of deferring the comparison rule to the iterator when there's no meaningful definition for an end *value*.

```
1 std::ranges::find(  
2     std::counted_iterator{first, 10},  
3     std::default_sentinel,  
4     value)
```

```
1 template<std::input_iterator I>  
2 auto counted_iterator<I>::operator==(std::default_sentinel) const -> bool {  
3     return n_ == 0;  
4 }
```

# std::unreachable\_sentinel

The unreachable sentinel is a way of saying "there is no end to this range".

```
1 struct unreachable_sentinel_t {
2     template<std::weakly_incrementable I>
3     friend constexpr bool operator==(unreachable_sentinel_t, I const&) noexcept {
4         return false;
5     }
6 };
```

# Completing our implementation of find

```
1 template<std::input_iterator I, std::sentinel_for<I> S, typename T>
2 requires std::indirect_binary_predicate<ranges::equal_to, I, T const*>
3 auto find(I first, S last, T const& value) -> I {
4     for (; first != last; ++first) {
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# Relationship between iterators and ranges

Let's say there's an object `r` of type `R`

## std::ranges::begin

```
template<typename R>
std::input_or_output_iterator auto std::ranges::begin(R&& r);
```

Returns an object that models `std::input_or_output_iterator`.

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Works on lvalues and sometimes on rvalues.

## std::ranges::begin

```
template<typename R>
std::input_or_output_iterator auto std::ranges::begin(R&& r);
```

Returns an object that models `std::input_or_output_iterator`.

Works on lvalues and sometimes on rvalues.

Works on types that use `r.begin()` (e.g. `std::vector`)

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```
using std::begin;
auto i = begin(r);
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```
using std::begin;
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```

Example usage:

```
auto i = std::ranges::begin(r);
```

# `std::ranges::begin`

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std::input_or_output_iterator auto std::ranges::begin(R&& r);
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Returns an object that models `std::input_or_output_iterator`.

Works on lvalues and sometimes on rvalues.

Works on types that use `r.begin()` (e.g. `std::vector`)

Works on types that use `begin(r)` without needing to do this insanity in every scope:

```
using std::begin;
auto i = begin(r);
```

Example usage:

```
auto i = std::ranges::begin(r);
```

`std::iterator_t<R>` is defined as the deduced return type for  
`std::ranges::begin(r)`.

## std::ranges::end

```
template<typename R>
std::sentinel_for<std::ranges::iterator_t<R>> auto
std::ranges::end(R&& r);
```

Returns an object that models `std::sentinel_for<std::ranges::iterator_t<R>>`.

## std::ranges::end

```
template<typename R>
std::sentinel_for<std::ranges::iterator_t<R>> auto
std::ranges::end(R&& r);
```

Returns an object that models `std::sentinel_for<std::ranges::iterator_t<R>>`.

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template<typename R>
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Works on lvalues and sometimes on rvalues.

Works on types that use `r.end()` (e.g. `std::vector`)

Works on types that use `end(r)` without needing to do this insanity in every scope:

```
using std::end;
auto i = end(r);
```

## std::ranges::end

```
template<typename R>
std::sentinel_for<std::ranges::iterator_t<R>> auto
std::ranges::end(R&& r);
```

Returns an object that models `std::sentinel_for<std::ranges::iterator_t<R>>`.

Works on lvalues and sometimes on rvalues.

Works on types that use `r.end()` (e.g. `std::vector`)

Works on types that use `end(r)` without needing to do this insanity in every scope:

```
using std::end;
auto i = end(r);
```

Example usage:

```
auto s = std::ranges::end(r);
```

## std::ranges::end

```
template<typename R>
std::sentinel_for<std::ranges::iterator_t<R>> auto
std::ranges::end(R&& r);
```

Returns an object that models `std::sentinel_for<std::ranges::iterator_t<R>>`.

Works on lvalues and sometimes on rvalues.

Works on types that use `r.end()` (e.g. `std::vector`)

Works on types that use `end(r)` without needing to do this insanity in every scope:

```
using std::end;
auto i = end(r);
```

Example usage:

```
auto s = std::ranges::end(r);
```

`std::sentinel_t<R>` is defined as the deduced return type for `std::ranges::end(r)`.

# std::ranges::range

R models the concept range when:

- R is a valid type parameter for both std::ranges::begin and std::ranges::end, where std::ranges::end ranges::begin(r) returns an iterator in amortised  $O(1)$  time.
- ranges::end(r) returns a sentinel in amortised  $O(1)$  time.
- [ranges::begin(r), ranges::end(r)) denotes a valid range (i.e. there's a finite number of iterations between the two).

```
template<typename T>
concept range = requires(R& r) {
    std::ranges::begin(r); // returns an iterator
    std::ranges::end(r); // returns a sentinel for that iterator
};
```

Note: std::ranges::begin(r) is not required to return the same result on each call.

## std::ranges::input\_range

Refines range to make sure ranges::begin(r) returns an input iterator.

```
template<typename T>
concept input_range =
    std::ranges::range<T> and
    std::input_iterator<std::ranges::iterator_t<T>>;
```

# A range-based find

```
1 template<ranges::input_range R, typename T>
2 requires std::indirect_binary_predicate<ranges::equal_to,
3                                         ranges::iterator_t<R>>, const T*>
4 auto find(R&& r, const T& value) -> ranges::borrowed_iterator_t<R> {
5     return comp6771::find(ranges::begin(r), ranges::end(r), value)
6 }
```

The range-based find simply defers to the iterator-based find. We prefer this algorithm when we need both begin and end, as opposed to arbitrary iterators, so that we don't mix iterators up and create invalid ranges (it's also more readable).

# A range-based find

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1 template<ranges::input_range R, typename T>
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The range-based find simply defers to the iterator-based find. We prefer this algorithm when we need both begin and end, as opposed to arbitrary iterators, so that we don't mix iterators up and create invalid ranges (it's also more readable).

`ranges::borrowed_iterator_t<R>` is the same as `ranges::iterator_t<R>` if `R` is an lvalue reference or a reference to a borrowed range (not discussed), and a non-iterator otherwise.

# A range-based find

```
1 template<ranges::input_range R, typename T>
2 requires std::indirect_binary_predicate<ranges::equal_to,
3                                         ranges::iterator_t<R>>, const T*>
4 auto find(R&& r, const T& value) -> ranges::borrowed_iterator_t<R> {
5     return comp6771::find(ranges::begin(r), ranges::end(r), value)
6 }
```

The range-based find simply defers to the iterator-based find. We prefer this algorithm when we need both begin and end, as opposed to arbitrary iterators, so that we don't mix iterators up and create invalid ranges (it's also more readable).

`ranges::borrowed_iterator_t<R>` is the same as `ranges::iterator_t<R>` if `R` is an lvalue reference or a reference to a borrowed range (not discussed), and a non-iterator otherwise.

```
auto v = std::vector<int>{0, 1, 2, 3};
ranges::find(v, 2); // returns an iterator
ranges::find(views::iota(0, 100), 2); // returns an iterator

ranges::find(std::vector<int>{0, 1, 2, 3}, 2); // returns ranges::dangling which is more useful
                                                // than void (better compile-time diagnostic info)
```

# Turning our list into a range

```
1 template<typename T>
2 class linked_list {
3 public:
4     class iterator;
5
6     auto begin() const -> iterator { return head_; }
7     auto end() const -> iterator { return tail_; }
8 private:
9     struct node {
10         T value;
11         std::unique_ptr<node> next;
12         node* prev;
13     };
14
15     std::unique_ptr<node> head_;
16     node* tail_;
17 }
```

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12         node* prev;
13     };
14
15     std::unique_ptr<node> head_;
16     node* tail_;
17 }
```

# Find last

```
1 template<std::input_iterator I, std::sentinel_for<I> S, class Val>
2 requires std::indirect_relation<ranges::equal_to, I, Val const*>
3 auto find_last(I first, S last, Val const& value) -> I {
4     auto cache = std::optional<I>();
5     for (; first != last; ++first) {
6         if (*first == value) {
7             cache = first;
8         }
9     }
10
11     return cache.value_or(std::move(first));
12 }
```

# Find last

```
1 template<std::input_iterator I, std::sentinel_for<I> S, class Val>
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7             cache = first;
8         }
9     }
10    return cache.value_or(std::move(first));
11 }
12 }
```

I isn't guaranteed to model std::copyable

Even if it were, I is only guaranteed to work for a single-pass

What if we are reading input from a network socket?

# Incrementable

Refines `std::weakly_incrementable` so you can copy and iterate over the same sequence of values multiple times.

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A type `I` models the concept `std::incrementable` if:

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2. `I` models `std::regular`

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Refines `std::weakly_incrementable` so you can copy and iterate over the same sequence of values multiple times.

A type `I` models the concept `std::incrementable` if:

1. `I` models `std::weakly_incrementable`
2. `I` models `std::regular`
3. `i++` is equivalent to

```
auto I::operator++(int) -> I {
    auto temp = i;
    ++i;
    return temp;
}
```

# Modelling std::incrementable<I>

```
1 template<typename T>
2 class linked_list<T>::iterator {
3 public:
4     using value_type = T;
5     using difference_type = std::ptrdiff_t;
6     using iterator_category = std::input_iterator_tag;
7
8     iterator() = default;
9
10    auto operator*() const noexcept -> value_type const& { ... }
11
12    auto operator++() -> iterator& { ... }
13    auto operator++(int) -> iterator {
14        auto temp = *this;
15        **this;
16        return temp;
17    }
18 private:
19     //...
20 };
21
22 static_assert(std::incrementable<linked_list<int>::iterator>);
```

# Forward iterators

Refines input iterators so you can copy and iterate over the same sequence of values multiple times.

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2. `I` models `std::incrementable`

# Forward iterators

Refines input iterators so you can copy and iterate over the same sequence of values multiple times.

A type `I` models the concept `std::forward_iterator` if:

1. `I` models `std::input_iterator`
2. `I` models `std::incrementable`
3. `I::iterator_category` is derived from `std::forward_iterator_tag`
4. `I` can be its own sentinel

# Modelling std::forward\_iterator<I>

```
1 template<typename T>
2 class linked_list<T>::iterator {
3 public:
4     using value_type = T;
5     using difference_type = std::ptrdiff_t;
6     using iterator_category = std::forward_iterator_tag;
7
8     iterator() = default;
9
10    auto operator*() const noexcept -> value_type& { ... }
11
12    auto operator++() -> iterator& { ... }
13    auto operator++(int) -> iterator { ... }
14
15    auto operator==(iterator const&) const -> bool = default;
16 private:
17     //...
18 };
19
20 static_assert(std::forward_iterator<linked_list<int>::iterator>);
```

# Find last

```
1 template<std::forward_iterator I, std::sentinel_for<I> S, class Val>
2 requires std::indirect_relation<ranges::equal_to, I, Val const*>
3 auto find_last(I first, S last, Val const& value) -> I {
4     auto cache = std::optional<I>();
5     for (; first != last; ++first) {
6         if (*first == value) {
7             cache = first;
8         }
9     }
10    return cache.value_or(std::move(first));
11 }
12 }
```

Can we optimise this algorithm further?

# Forward range

Refines `input_range` to make sure `ranges::begin(r)` returns a forward iterator.

`ranges::begin(r)` now returns the same value given the same input.

```
template<typename T>
concept forward_range =
    std::ranges::input_range<T> and
    std::forward_iterator<std::ranges::iterator_t<T>>;
```

# tl;dr

## std::input\_iterator<I>

(See previous tl;dr)

## std::incrementable<I>

Requires:

std::weakly\_incrementable<I>  
std::regular<I>

```
1 auto I::operator++(int) -> I {
2     auto temp = *this;
3     ++*this;
4     return temp;
5 }
```

## std::forward\_iterator<I>

Requires:

I::iterator\_category is derived from std::forward\_iterator\_tag  
auto operator==(I, I) -> bool;  
auto operator!=(I, I) -> bool; (before C++20)

# Bidirectional iterators

Refines forward iterators so you can iterate in reverse order.

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A type `I` models the concept `std::bidirectional_iterator` if:

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1. `I` models `std::forward_iterator`
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3. `--i` is valid and returns a reference to itself.

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1. `I` models `std::forward_iterator`
2. `I::iterator_category` is derived from `std::bidirectional_iterator_tag`
3. `--i` is valid and returns a reference to itself.
4. `i--` is valid and has the same domain as `--i`

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3. `--i` is valid and returns a reference to itself.
4. `i--` is valid and has the same domain as `--i`
5. `--i` and `i--` both decline `i` in constant time complexity

# Bidirectional iterators

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A type `I` models the concept `std::bidirectional_iterator` if:

1. `I` models `std::forward_iterator`
2. `I::iterator_category` is derived from `std::bidirectional_iterator_tag`
3. `--i` is valid and returns a reference to itself.
4. `i--` is valid and has the same domain as `--i`
5. `--i` and `i--` both decline `i` in constant time complexity
6. `i--` is equivalent to

```
1 auto I::operator--(int) -> I {  
2     auto temp = i;  
3     --i;  
4     return temp;  
5 }
```

# Modelling std::bidirectional\_iterator<I>

```
1 template<typename T>
2 class linked_list<T>::iterator {
3 public:
4     using value_type = T;
5     using difference_type = std::ptrdiff_t;
6     using iterator_category = std::bidirectional_iterator_tag;
7
8     iterator() = default;
9
10    auto operator*() const noexcept -> value_type const& { ... }
11
12    auto operator++() -> iterator& { ... }
13    auto operator++(int) -> iterator { ... }
14
15    auto operator--() -> iterator& {
16        pointee_ = pointee_->prev;
17        return *this;
18    }
19
20    auto operator--(int) -> iterator {
21        auto temp = *this;
22        --*this;
23        return temp;
24    }
25
26    auto operator==(iterator const&) const -> bool = default;
27 private:
28     //...
29 };
30
31 static_assert(std::bidirectional_iterator<linked_list<int>::iterator>);
```

# Find last

```
1 template<std::bidirectional_iterator I, class Val>
2 requires std::indirect_relation<ranges::equal_to, I, Val const*>
3 auto find_last(I first, I last, Val const& value) -> I {
4     while (first != last) {
5         --last;
6         if (*last == value) {
7             return last;
8         }
9     }
10    return first;
11 }
12 }
```

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2 requires std::indirect_relation<ranges::equal_to, I, Val const*>
3 auto find_last(I first, I last, Val const& value) -> I {
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4     while (first != last) {
5         --last;
6         if (*last == value) {
7             return last;
8         }
9     }
10    return first;
11 }
12 }
```

# We keep both implementations

```
1 template<std::forward_iterator I, std::sentinel_for<I> S, class Val>
2 requires std::indirect_relation<ranges::equal_to, I, Val const*>
3 auto find_last(I first, S last, Val const& value) -> I {
4     auto cache = std::optional<I>();
5     for (; first != last; ++first) {
6         if (*first == value) {
7             cache = first;
8         }
9     }
10
11     return cache.value_or(std::move(first));
12 }
13
14 template<std::bidirectional_iterator I, class Val>
15 requires std::indirect_relation<ranges::equal_to, I, Val const*>
16 auto find_last(I first, I last, Val const& value) -> I {
17     while (first != last--) {
18         if (*last == value) {
19             return last;
20         }
21     }
22
23     return first;
24 }
```

# tl;dr

`std::forward_iterator<I>`

(See previous tl;dr)

`std::bidirectional_iterator<I>`

Requires:

`I::iterator_category` is derived from `std::bidirectional_iterator_tag`

`--i` and `i--` move to the previous element, with  $O(1)$  time complexity

`--i` returns a reference to itself

```
1 auto I::operator--(int) -> I {
2     auto temp = *this;
3     --*this;
4     return temp;
5 }
```

# A new example type

Our `linked_list` has been a good friend up until now.

It's sadly run its course for the lecture content and we can't use it any more.

Let's now define something similar to `ranges::views::iota`

# simple\_iota\_view

```
1 template<std::integral I>
2 class simple_iota_view {
3     class iterator;
4 public:
5     simple_iota_view() = default;
6
7     simple_iota_view(I first, I last)
8     : start_(std::move(first))
9     , stop_(std::move(last)) {}
10
11    auto begin() const -> iterator { return iterator(*this, start_); }
12    auto end() const -> iterator { return iterator(*this, stop_); }
13 private:
14     I start_ = I();
15     I stop_ = I();
16 };
```

# simple\_iota\_view

```
1 template<std::integral I>
2 class simple_iota_view {
3     class iterator;
4 public:
5     simple_iota_view() = default;
6
7     simple_iota_view(I first, I last)
8     : start_(std::move(first))
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10
11    auto begin() const -> iterator { return iterator(*this, start_); }
12    auto end() const -> iterator { return iterator(*this, stop_); }
13 private:
14     I start_ = I();
15     I stop_ = I();
16 };
```

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14     I start_ = I();
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```

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14     I start_ = I();
15     I stop_ = I();
16 };
```

# Simple\_iota\_view::iterator

```
1 template<std::integral I>
2 class simple_iota_view<I>::iterator {
3 public:
4     using value_type = I;
5     using difference_type = std::iter_difference_t<I>;
6     using iterator_category = iterator_category_helper_t<I>;
7
8     iterator() = default;
9
10    explicit iterator(simple_iota_view const& base, I const& value)
11        : base_(std::addressof(base))
12        , current_(value) {}
13
14    auto operator*() const -> I { return current_; }
15
16    auto operator++() -> iterator& { ++current_; return *this; }
17    auto operator++(int) -> iterator { ... }
18
19    auto operator--() -> iterator& { --current_; return *this; }
20    auto operator--(int) -> iterator { ... }
21
22    auto operator==(iterator) const -> bool = default;
23 private:
24     simple_iota_view const* base_ = nullptr;
25     I current_ = I();
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19    auto operator--() -> iterator& { --current_; return *this; }
20    auto operator--(int) -> iterator { ... }
21
22    auto operator==(iterator) const -> bool = default;
23 private:
24     simple_iota_view const* base_ = nullptr;
25     I current_ = I();
26 };
```

# Check if two ranges meet some predicate, element-wise

```
1 template<std::input_iterator I1, std::sentinel_for<I1> S1,
2           std::input_iterator I2, std::sentinel_for<I2> S2,
3           std::indirect_binary_predicate<Pred, I1, I2> Pred = ranges::equal_to>
4     bool comp6771::equal(I1 first1, S1 last1, I2 first2, S2 last2, Pred pred = {})
5 {
6     auto result = ranges::mismatch(std::move(first1), last1,
7                                     std::move(first2), last2,
8                                     std::ref(pred));
9     return (result.in1 == last1) and (result.in2 == last2);
10 }
11 }
```

A good starting point, but `ranges::mismatch` isn't designed to short-circuit.

What might we be able to do to optimise this?

# An optimisation

If ranges don't have the same distance, then complexity should be constant!

Checking the distance of a range is currently a linear operation...

```
1 template<std::input_iterator I1, std::sentinel_for<I1> S1,
2     std::input_iterator I2, std::sentinel_for<I2> S2,
3     std::indirect_binary_predicate<Pred, I1, I2> Pred = ranges::equal_to>
4 bool comp6771::equal(I1 first1, S1 last1, I2 first2, S2 last2, Pred pred = {})
5 {
6     auto result = ranges::mismatch(std::move(first1), last1,
7                                     std::move(first2), last2,
8                                     std::ref(pred));
9     return (result.in1 == last1) and (result.in2 == last2);
10
11 }
```

# Sized sentinels

Refines `std::sentinel` so that we can compute the distance between two elements in constant time.

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Given an iterator type `I`, A type `S` models the concept `std::sized_sentinel_for<I>` if:

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1. `S` models `std::sentinel_for<I>`

# Sized sentinels

Refines `std::sentinel` so that we can compute the distance between two elements in constant time.

Given an iterator type `I`, A type `S` models the concept `std::sized_sentinel_for<I>` if:

1. `S` models `std::sentinel_for<I>`

2. `ranges::disable_sized_sentinel_for<S, I>` is `false`

Used to opt *out* of being a sized sentinel for `I` if `s - i` doesn't evaluate in  $O(1)$  time (i.e. this is `false` by default).

# Sized sentinels

Refines `std::sentinel` so that we can compute the distance between two elements in constant time.

Given an iterator type `I`, A type `s` models the concept `std::sized_sentinel_for<I>` if:

1. `s` models `std::sentinel_for<I>`
  2. `ranges::disable_sized_sentinel_for<s, I>` is `false`
  3. `s - i` returns the number of elements between the iterator and sentinel, as an object of type `std::iter_difference_t<I>`, in constant time
  4. `i - s` is equivalent to `-(s - i)`
- Used to opt *out* of being a sized sentinel for `I` if `s - i` doesn't evaluate in  $O(1)$  time (i.e. this is `false` by default).

# An optimisation

```
1 template<std::input_iterator I1, std::sentinel_for<I1> S1,
2         std::input_iterator I2, std::sentinel_for<I2> S2,
3         std::indirect_binary_predicate<Pred, I1, I2> Pred = ranges::equal_to>
4     bool comp6771::equal(I1 first1, S1 last1, I2 first2, S2 last2, Pred pred = {}) {
5     if constexpr (std::sized_sentinel_for<S1, I1> and std::sized_sentinel_for<S2, I2>) {
6         if (last1 - first1 != last2 - first2) {
7             return false;
8         }
9     }
10
11     auto result = ranges::mismatch(std::move(first1), last1,
12                                     std::move(first2), last2,
13                                     std::ref(pred));
14
15     return (result.in1 == last1) and (result.in2 == last2);
16
17 }
```

# Modelling std::sized\_sentinel\_for<S, I>

```
1 template<std::integral I>
2 class simple_iota_view<I>::iterator {
3 public:
4     using value_type = I;
5     using difference_type = std::iter_difference_t<I>;
6     using iterator_category = iterator_category_helper_t<I>;
7
8     iterator() = default;
9
10    explicit iterator(simple_iota_view const& base, I const& value);
11
12    auto operator*() const -> I;
13    auto operator++() -> iterator&;
14    auto operator++(int) -> iterator;
15    auto operator--() -> iterator&;
16    auto operator--(int) -> iterator;
17
18    auto operator==(iterator) const -> bool = default;
19
20    friend auto operator-(iterator const x, iterator const y) -> difference_type {
21        assert(x.base_ == y.base_);
22        return x.current_ - y.current_;
23    }
24 private: // ...
25 };
26 static_assert(std::sized_sentinel_for<simple_iota_view<int>::iterator, simple_iota_view<int>::iterator>);
```

# Partition point

0 2 7 6 8 1 3 7 5

# Partition point

0 2 7 6 8 1 3 7 5

^

# Partition point

```
1 template<std::forward_iterator I, std::sentinel_for<I> S,
2         std::indirect_unary_predicate<I> Pred>
3     auto partition_point(I first, S last, Pred pred) -> I {
4         auto end = ranges::next(first, last);
5         while (first != end) {
6             auto middle = ranges::next(first, ranges::distance(first, end) / 2);
7             if (std::invoke(pred, *middle)) {
8                 first = std::move(middle);
9                 ++first;
10                continue;
11            }
12            end = std::move(middle);
13        }
14
15        return first;
16    }
```

What is the complexity of this partition\_point?

# Partition point

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1 template<std::forward_iterator I, std::sentinel_for<I> S,
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3     auto partition_point(I first, S last, Pred pred) -> I {
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7             if (std::invoke(pred, *middle)) {
8                 first = std::move(middle);
9                 ++first;
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11            }
12            end = std::move(middle);
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What is the complexity of this `partition_point`?

$O(\log(\text{last} - \text{first}))$  applications of `pred`

# Partition point complexity

$O(\log(\text{last} - \text{first}))$  applications of pred

But there's currently  $O(n)$  steps through the range.

Wouldn't it be great for the applications and steps to be the same?

# Random-access iterators

Refines bidirectional iterators so you can make arbitrary steps in constant time

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1.  $\mathbf{I}$  models `std::bidirectional_iterator`

# Random-access iterators

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A type `I` models the concept `std::random_access_iterator` if:

1. `I` models `std::bidirectional_iterator`
2. `I::iterator_category` is derived from `std::random_access_iterator_tag`

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3. `I` models `std::totally_ordered`

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4. `I` is a sized sentinel for itself

Let `i` and `j` be objects of type `I` and `n` be an object of type `iter_difference_t<I>`.

1. `i += n` and `i -= n` are valid and return references to the same object.
2. `i ±= n` advances/declines `i` by `n` elements in constant time.

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A type  $\mathbb{I}$  models the concept `std::random_access_iterator` if:

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Let  $i$  and  $j$  be objects of type  $\mathbb{I}$  and  $n$  be an object of type `iter_difference_t<I>`.

1.  $i += n$  and  $i -= n$  are valid and return references to the same object.
2.  $i \pm= n$  advances/declines  $i$  by  $n$  elements in constant time.
3.  $j \pm n$  advances/declines a copy of  $j$  by  $n$  elements in constant time.
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4.  $n + j$  is the same as  $j + n$ .
5.  $j[n]$  is the same as  $* (j + n)$ .

# Modelling std::random\_access\_iterator<I>

```
1 template<std::integral I>
2 class simple_iota_view<I>::iterator {
3 public:
4     using value_type = I;
5     using difference_type = std::iter_difference_t<I>;
6     using iterator_category = std::random_access_iterator_tag;
7
8     // stuff from previous slides
9
10    auto operator<=>(iterator) const -> std::strong_ordering = default;
11
12    auto operator+=(difference_type const n) -> iterator& {
13        current_ += n;
14        return *this;
15    }
16
17    auto operator-=(difference_type const n) -> iterator& { return *this += -n; }
18    auto operator[](difference_type const n) const -> value_type { return *(*this + n); }
19
20    friend auto operator+(iterator j, difference_type const n) -> iterator { return j += n; }
21    friend auto operator+(difference_type const n, iterator j) -> iterator { return j += n; }
22    friend auto operator-(iterator j, difference_type const n) -> iterator { return j -= n; }
23    friend auto operator-(iterator const x, iterator const y) -> difference_type { ... }
24 };
25
26 static_assert(std::random_access_iterator<simple_iota_view<int>::iterator>);
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24 };
25
26 static_assert(std::random_access_iterator<simple_iota_view<int>::iterator>);
```

# tl;dr

`std::bidirectional_iterator<I>`  
(See previous tl;dr)

`std::sized_sentinel_for<I, I>`  
Requires:  
`std::sentinel_for<I, I>`  
`std::disable_sentinel_for<I, I> == false`  
`s - i` returns the number of elements between `i` and `s` in  $O(1)$  time  
`i - s` is equivalent to `s - i`

`std::random_access_iterator<I>`

Requires:

`std::totally_ordered<I>` (i.e. has all traditional comparison operators)  
`I::iterator_category` is derived from `std::random_access_iterator_tag`  
`i += n` and `i -= n` advance/decline `i` by `n` elements in  $O(1)$  time  
`j + n, n + j` and `j - n` advance/decline a copy of `j` by `n` elements in  $O(1)$  time  
`j[n]` is equivalent to `* (j + n)`

# What happens if we want to write to a range?

```
template<std::input_iterator I, std::sentinel_for<I> S,  
        ??? O>  
auto copy(I first, S last, O result) -> copy_result<I, O> {  
    for (; first != last; ++first, (void)++result) {  
        *result = *first;  
    }  
    return {std::move(first), std::move(result)};  
}
```

What do O and I need to model?

```
template<typename T,  
        ??? O,  
        std::sentinel_for<O> S>  
auto fill(O first, S last, T const& value) -> O {  
    for (first != last) {  
        *first++ = value;  
    }  
    return first;  
}
```

What does O need to model?

# Writable iterators

Operation	Array-like	Node-based	Iterator
Iteration type	<code>gsl_lite::index</code>	<code>node*</code>	<i>unspecified</i>
Write to element	<code>v[i] = x</code>  <code>j = i + n &lt; ranges::distance(v)</code> <code>? i + n</code> <code>: ranges::distance(v);</code>	<code>i-&gt;value = x</code>  <code>j = i-&gt;successor(n)</code>	<code>*i = x</code>  <code>ranges::next(i, s, n)</code>
Successor			
Advance fwd	<code>++i</code>	<code>i = i-&gt;next</code>	<code>++i</code>
Comparison	<code>i &lt; ranges::distance(v)</code>	<code>i != nullptr</code>	<code>i != s</code>

# Indirectly writable

The concept `indirectly_writable` determines if we can write a value to whatever the iterator is referencing.

Let `o` be a possibly-constant object of type `O` and `val` be an object of type `T`. A type `O` models the concept `std::indirectly_writable<T>` if:

1. `*o = val` is possible regardless of whether `o` is const-qualified
2. These expressions are possible for `o&` and `o&&:`
  - `*o = std::move(val)`
  - `*std::move(o) = std::move(val)`
3. All forms of `*o = val` result in `*o` returning a reference.

# Modelling std::indirectly\_writable<O, T>

```
1 template<typename T>
2 class linked_list<T>::iterator {
3 public:
4     using value_type = T;
5     using difference_type = std::ptrdiff_t;
6     using iterator_category = std::bidirectional_iterator_tag;
7
8     iterator() = default;
9
10    auto operator*() const noexcept -> value_type& { return pointee_->data; }
11
12    auto operator++() -> iterator& { ... }
13    auto operator++(int) -> iterator { ... }
14    auto operator--() -> iterator& { ... }
15    auto operator--(int) -> iterator { ... }
16
17    auto operator==(iterator) const -> bool = default;
18 private:
19     //...
20 };
21
22 static_assert(std::indirectly_writable<linked_list<int>::iterator, int);
```

# Applying this to copy

```
1 template<std::input_iterator I, std::sentinel_for<I> S,>
2     std::weakly_incrementable O>
3 requires std::indirectly_copyable<I, O>
4 auto copy(I first, S last, O result) -> copy_result<I, O> {
5     for (; first != last; ++first, (void)++result) {
6         *result = *first;
7     }
8     return {std::move(first), std::move(result)};
9 }
```

# Applying this to copy

```
1 template<std::input_iterator I, std::sentinel_for<I> S,  
2           std::weakly_incrementable O>  
3 requires std::indirectly_copyable<I, O>  
4 auto copy(I first, S last, O result) -> copy_result<I, O> {  
5     for (; first != last; ++first, (void)++result) {  
6         *result = *first;  
7     }  
8     return {std::move(first), std::move(result)};  
9 }
```

Where `std::indirectly_copyable<I, O>` means "we can copy the value we've read from `I` into `O`". In other words:

```
template<typename In, typename Out>  
concept indirectly_copyable =  
    std::indirectly_readable<In> and  
    std::indirectly_writable<Out, std::iter_reference_t<In>>;
```

# Output iterators

The concept `output_iterator` refines the base iterator concept by requiring the iterator models `indirectly_writable`.

Let `o` be a possibly-constant object of type `O` and `val` be an object of type `T`. A type `O` models the concept `std::output_iterator<T>` if:

1. `O` models `std::input_or_output_iterator`
2. `O` models `std::indirectly_writable<T>`
3. • `* (o++) = val` is valid, if `T` is an lvalue, and is equivalent to

```
*o = val;  
++o;
```

- `* (o++) = std::move(val)` is valid, if `T` is an rvalue, and is equivalent to

```
*o = std::move(val);  
++o;
```

# Modelling std::output\_iterator<O, T>

```
1 template<typename T>
2 class linked_list<T>::iterator {
3 public:
4     // ...
5 private:
6     //...
7 };
8
9 static_assert(std::bidirectional_iterator<linked_list<int>::iterator>);
10 static_assert(std::output_iterator<linked_list<int>::iterator, int>);
```

Iterators that model both `std::bidirectional_iterator<I>` and `std::indirectly_writable<O, T>` model `std::output_iterator<O, T>` by default.

There isn't a concept for these kinds of iterators, but they're known as *mutable* iterators in generic programming theory.

# Applying this to fill

```
1 template<typename T,  
2         std::output_iterator<T const&> O,  
3         std::sentinel_for<O> S>  
4 auto fill(O first, S last, T const& value) -> O {  
5     while (first != last)  
6         *first++ = value;  
7     }  
8     return first;  
9 }
```

Non-mutable output iterators are write-once-then-advance.

# Iterators and const

Mutable iterators are always `indirectly_writable`, even when const-qualified.

```
void write_access(linked_list<int>::iterator const i) {
    *i = 42; // okay, changes what *i refers to
    i = {};// error: can't change i itself
}
```

This is the same problem as `T* const`: we have a constant iterator, not an iterator pointing-to-const.

# const\_iterators

A `const_iterator` is the iterator-equivalent of `T const*`.

```
void no_write_access(linked_list<int>::const_iterator i) {  
    i = {};  
    // okay  
  
    *i = 42;  
    // error: can't indirectly write to i  
}
```

# How do we make `const_` iterators?

# Attempt 1: Two types

```
1 template<typename T>
2 class linked_list<T>::iterator {
3 public:
4     using value_type = T;
5     using difference_type = std::ptrdiff_t;
6     using iterator_category = std::bidirectional_iterator_tag;
7
8     iterator() = default;
9
10    auto operator*() const noexcept -> value_type& {
11        return pointee_>data;
12    }
13
14    auto operator++() -> iterator& { ... }
15    auto operator++(int) -> iterator { ... }
16    auto operator--() -> iterator& { ... }
17    auto operator--(int) -> iterator { ... }
18
19    auto operator==(iterator) const -> bool = default;
20 private:
21     //...
22 };
23
24 static_assert(
25     std::indirectly_writable<linked_list<int>::iterator, int>);
26
27
28 template<typename T>
29 class linked_list<T>::const_iterator {
30 public:
31     using value_type = T;
32     using difference_type = std::ptrdiff_t;
33     using iterator_category = std::bidirectional_iterator_tag;
34
35     iterator() = default;
36
37     auto operator*() const noexcept -> value_type const& {
38         return pointee_>data;
39     }
40
41     auto operator++() -> iterator& { ... }
42     auto operator++(int) -> iterator { ... }
43     auto operator--() -> iterator& { ... }
44     auto operator--(int) -> iterator { ... }
45
46     auto operator==(iterator) const -> bool = default;
47 private:
48     //...
49 };
50
51 static_assert(
52     not std::indirectly_writable<linked_list<int>::const_iterator,
53     int>);
```

Why might this be a bad approach?

# Attempt 2: Parameterise on constness

```
1 template<typename T>
2 class linked_list {
3     template<bool is_const>
4         class iterator_impl;
5 public:
6     using iterator = iterator_impl<false>;
7     using const_iterator = iterator_impl<true>;
8
9     // ...
10};
```

We define one template class `iterator_impl` and *parameterise* it based on constness.

Then we add metadata to `iterator_impl` to help it understand what `is_const` means.

# Attempt 2: Parameterise on constness

```
1 template<typename T>
2 template<bool is_const>
3 class linked_list<T>::iterator_impl {
4 public:
5     using value_type = T;
6     using difference_type = std::ptrdiff_t;
7     using iterator_category = std::bidirectional_iterator_tag;
8
9     iterator_impl() = default;
10
11    auto operator*() const noexcept -> value_type const&
12    requires is_const {
13        return pointee_->data;
14    }
15
16    auto operator*() const noexcept -> value_type&
17    requires (not is_const) {
18        return pointee_->data;
19    }
20
21    auto operator++() -> iterator_impl& { ... }
22    auto operator++(int) -> iterator_impl { ... }
23    auto operator--() -> iterator_impl& { ... }
24    auto operator--(int) -> iterator_impl { ... }
25    auto operator==(iterator_impl) const -> bool = default;
26 private:
27     maybe_const_t<is_const, T*>* pointee_;
28
29     iterator_impl(maybe_const_t<is_const, T*>* ptr) { ... }
30     friend class linked_list<T>;
31 };
```

# Attempt 2: Parameterise on constness

```
1 template<typename T>
2 template<bool is_const>
3 class linked_list<T>::iterator_impl {
4 public:
5     using value_type = T;
6     using difference_type = std::ptrdiff_t;
7     using iterator_category = std::bidirectional_iterator_tag;
8
9     iterator_impl() = default;
10
11    auto operator*() const noexcept -> value_type const&
12    requires is_const {
13        return pointee_->data;
14    }
15
16    auto operator*() const noexcept -> value_type&
17    requires (not is_const) {
18        return pointee_->data;
19    }
20
21    auto operator++() -> iterator_impl& { ... }
22    auto operator++(int) -> iterator_impl { ... }
23    auto operator--() -> iterator_impl& { ... }
24    auto operator--(int) -> iterator_impl { ... }
25    auto operator==(iterator_impl) const -> bool = default;
26 private:
27     maybe_const_t<is_const, T>* pointee_;
28
29     iterator_impl(maybe_const_t<is_const, T>* ptr) { ... }
30
31 };
```

```
1 template<bool is_const, typename T>
2 struct maybe_const {
3     using type = T;
4 }
5
6 template<typename T>
7 struct maybe_const<true, T> {
8     using type = T const;
9 }
10
11 template<bool is_const, typename T>
12 using maybe_const_t =
13     typename maybe_const<is_const, T>;
```

This is **partial template specialisation**, which we cover in Week 8. For now, you can think of it like a switch on constness, based on some compile-time property.

# Attempt 2: Parameterise on constness

```
1 template<typename T>
2 template<bool is_const>
3 class linked_list<T>::iterator_impl {
4 public:
5     using value_type = T;
6     using difference_type = std::ptrdiff_t;
7     using iterator_category = std::bidirectional_iterator_tag;
8
9     iterator_impl() = default;
10
11    auto operator*() const noexcept -> value_type const&
12    requires is_const {
13        return pointee_->data;
14    }
15
16    auto operator*() const noexcept -> value_type&
17    requires (not is_const) {
18        return pointee_->data;
19    }
20
21    auto operator++() -> iterator_impl& { ... }
22    auto operator++(int) -> iterator_impl { ... }
23    auto operator--() -> iterator_impl& { ... }
24    auto operator--(int) -> iterator_impl { ... }
25    auto operator==(iterator_impl) const -> bool = default;
26 private:
27     maybe_const_t<is_const, T>* pointee_;
28
29     iterator_impl(maybe_const_t<is_const, T>* ptr) { ... }
30
31 };
```

```
1 template<bool is_const, typename T>
2 struct maybe_const {
3     using type = T;
4 }
5
6 template<typename T>
7 struct maybe_const<true, T> {
8     using type = T const;
9 }
10
11 template<bool is_const, typename T>
12 using maybe_const_t =
13     typename maybe_const<is_const, T>;
```

This is **partial template specialisation**, which we cover in Week 8. For now, you can think of it like a switch on constness, based on some compile-time property.

# Attempt 2: Parameterise on constness

```
1 template<typename T>
2 template<bool is_const>
3 class linked_list<T>::iterator_impl {
4 public:
5     using value_type = T;
6     using difference_type = std::ptrdiff_t;
7     using iterator_category = std::bidirectional_iterator_tag;
8
9     iterator_impl() = default;
10
11    auto operator*() const noexcept -> value_type const&
12    requires is_const {
13        return pointee_->data;
14    }
15
16    auto operator*() const noexcept -> value_type&
17    requires (not is_const) {
18        return pointee_->data;
19    }
20
21    auto operator++() -> iterator_impl& { ... }
22    auto operator++(int) -> iterator_impl { ... }
23    auto operator--() -> iterator_impl& { ... }
24    auto operator--(int) -> iterator_impl { ... }
25    auto operator==(iterator_impl) const -> bool = default;
26 private:
27     maybe_const_t<is_const, T>* pointee_;
28
29     iterator_impl(maybe_const_t<is_const, T>* ptr) { ... }
30
31 };
```

```
1 template<bool is_const, typename T>
2 struct maybe_const {
3     using type = T;
4 }
5
6 template<typename T>
7 struct maybe_const<true, T> {
8     using type = T const;
9 }
10
11 template<bool is_const, typename T>
12 using maybe_const_t =
13     typename maybe_const<is_const, T>;
```

This is **partial template specialisation**, which we cover in Week 8. For now, you can think of it like a switch on constness, based on some compile-time property.

# Getting the right kind of iterator

Either way, you'll need to have two overloads for begin and for end. We don't want linked\_list<int> const to return mutable iterators!

```
1 template<typename T>
2 class linked_list {
3     template<bool is_const>
4         class iterator_impl;
5     public:
6         using iterator = iterator_impl<false>;
7         using const_iterator = iterator_impl<true>;
8
9         auto begin() -> iterator { return iterator(head_); }
10        auto end() -> iterator { return iterator(tail_); }
11
12        auto begin() const -> const_iterator { return iterator(head_); }
13        auto end() const -> const_iterator { return iterator(tail_); }
14    };
```

How might you improve this code?

# Getting the right kind of iterator

Either way, you'll need to have two overloads for begin and for end. We don't want linked\_list<int> const to return mutable iterators!

```
1 template<typename T>
2 class linked_list {
3     template<bool is_const>
4         class iterator_impl;
5     public:
6         using iterator = iterator_impl<false>;
7         using const_iterator = iterator_impl<true>;
8
9         auto begin() -> iterator { return iterator(head_); }
10        auto end() -> iterator { return iterator(tail_); }
11
12        auto begin() const -> const_iterator { return iterator(head_); }
13        auto end() const -> const_iterator { return iterator(tail_); }
14    };
```

How might you improve this code?

# Getting the right kind of iterator DRY style

```
1 template<typename T>
2 class linked_list {
3 public:
4     using iterator = iterator_impl<false>;
5     using const_iterator = iterator_impl<true>;
6
7     auto begin() -> iterator { begin_impl(*this); }
8     auto end() -> iterator { return end_impl(*this); }
9
10    auto begin() const -> const_iterator { return begin_impl(*this); }
11    auto end() const -> const_iterator { return end_impl(*this); }
12 private:
13     template<typename T>
14     static auto begin_impl(T& t) -> decltype(t.begin()) {
15         return iterator_impl<std::is_const_v<T>>(head_);
16     }
17
18     template<typename T>
19     static auto end_impl(T& t) -> decltype(t.end()) {
20         return iterator_impl<std::is_const_v<T>>(tail_);
21     }
22 };
```

# Getting the right kind of iterator DRY style

```
1 template<typename T>
2 class linked_list {
3 public:
4     using iterator = iterator_impl<false>;
5     using const_iterator = iterator_impl<true>;
6
7     auto begin() -> iterator { begin_impl(*this); }
8     auto end() -> iterator { return end_impl(*this); }
9
10    auto begin() const -> const_iterator { return begin_impl(*this); }
11    auto end() const -> const_iterator { return end_impl(*this); }
12 private:
13     template<typename T>
14     static auto begin_impl(T& t) -> decltype(t.begin()) {
15         return iterator_impl<std::is_const_v<T>>(head_);
16     }
17
18     template<typename T>
19     static auto end_impl(T& t) -> decltype(t.end()) {
20         return iterator_impl<std::is_const_v<T>>(tail_);
21     }
22 };
```

# Getting the right kind of iterator DRY style

```
1 template<typename T>
2 class linked_list {
3 public:
4     using iterator = iterator_impl<false>;
5     using const_iterator = iterator_impl<true>;
6
7     auto begin() -> iterator { begin_impl(*this); }
8     auto end() -> iterator { return end_impl(*this); }
9
10    auto begin() const -> const_iterator { return begin_impl(*this); }
11    auto end() const -> const_iterator { return end_impl(*this); }
12 private:
13     template<typename T>
14     static auto begin_impl(T& t) -> decltype(t.begin()) {
15         return iterator_impl<std::is_const_v<T>>(head_);
16     }
17
18     template<typename T>
19     static auto end_impl(T& t) -> decltype(t.end()) {
20         return iterator_impl<std::is_const_v<T>>(tail_);
21     }
22 };
```

# When to have differently-qualified overloads

Is the iterator `indirectly_writable`?

Yes

Then you should use

`begin()`  
`end()`

No

`begin() const`  
`end() const`

No, but the range does housekeeping (e.g. keeps a  
cache)

`begin()`  
`end()`

# What about `cbegin` and `cend`?

Standard containers ship with `cbegin` and `cend` as member functions.

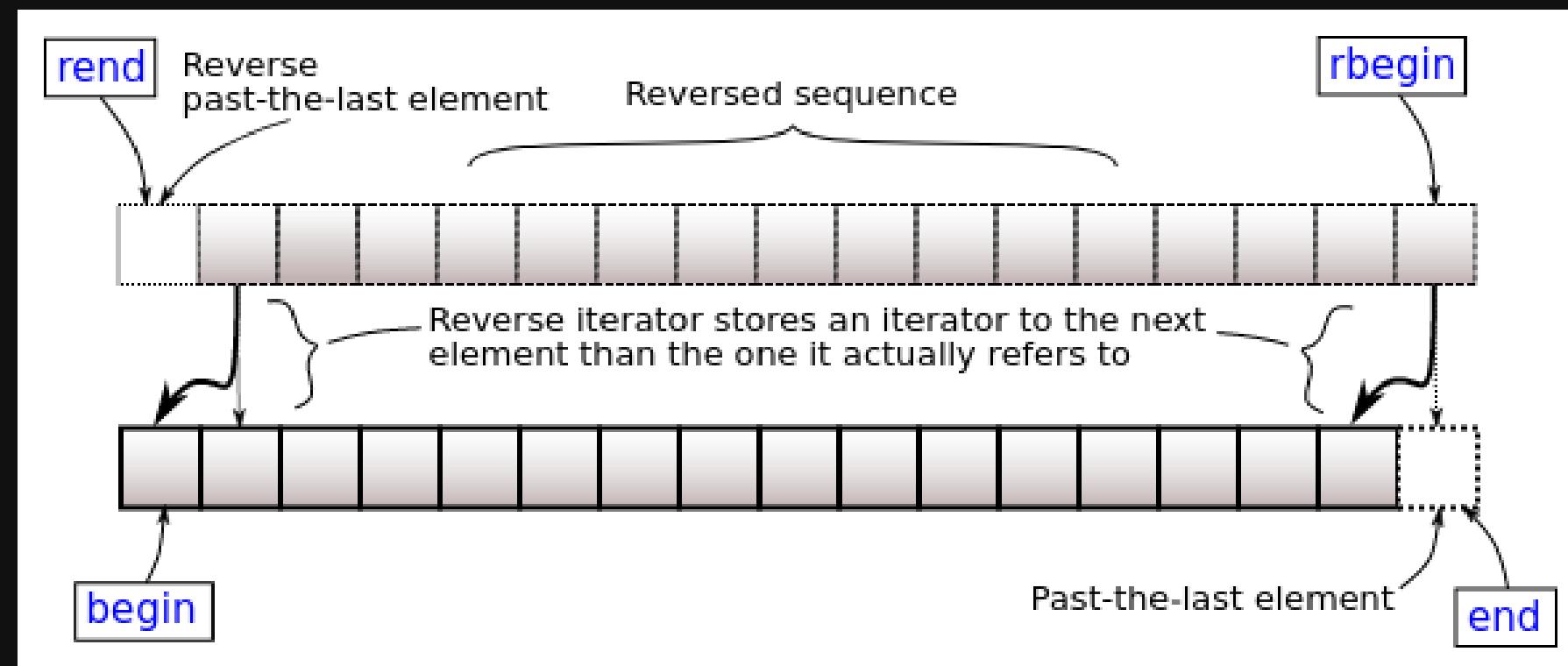
While they *might* be handy, they're not *necessary*.

`ranges::cbegin(r)` and `ranges::cend(r)` will Do The Right Thing™ if you have a `const`-qualified `begin` member function. (Try it on our `linked_list` and see if it works!)

Not all ranges will have `cbegin/cend` member functions, so the only reliable way to get an iterator to a constant range is to use one of the above.

# rbegin and rend

rbegin and rend **idiomatically return reverse\_iterator<iterator>s.**



Unlike `cbegin/cend`, you'll probably want to define `rbegin/rend` as members for backwards-compatibility reasons.

`crbegin/crend` are in the same category as `cbegin/cend`.

# Video Resources



*Generic Programming*, by Sean Parent



- *Concepts in 60: Everything You Need to Know and Nothing You Don't*, by Andrew Sutton
- *Concepts: A Day in the Life*, by Saar Raz
- *An Overview of Standard Ranges*, by Tristan Brindle
- *Algorithm Intuition*, by Conor Hoekstra
- *Range Algorithms, Views and Actions: A Comprehensive Guide*, by Dvir Yitzchacki
- *From STL to Ranges: Using Ranges Effectively*, by Jeff Garland
- *What a View! Building Your own (Lazy) Range Adaptors*, by Christopher Di Bella

# Written Resources

*From Mathematics to Generic Programming*, by Alexander Stepanov and Daniel Rose

*Elements of Programming*, by Alexander Stepanov and Paul McJones