

Dated:

Histogram Equalization

- Used for image Enhancement.

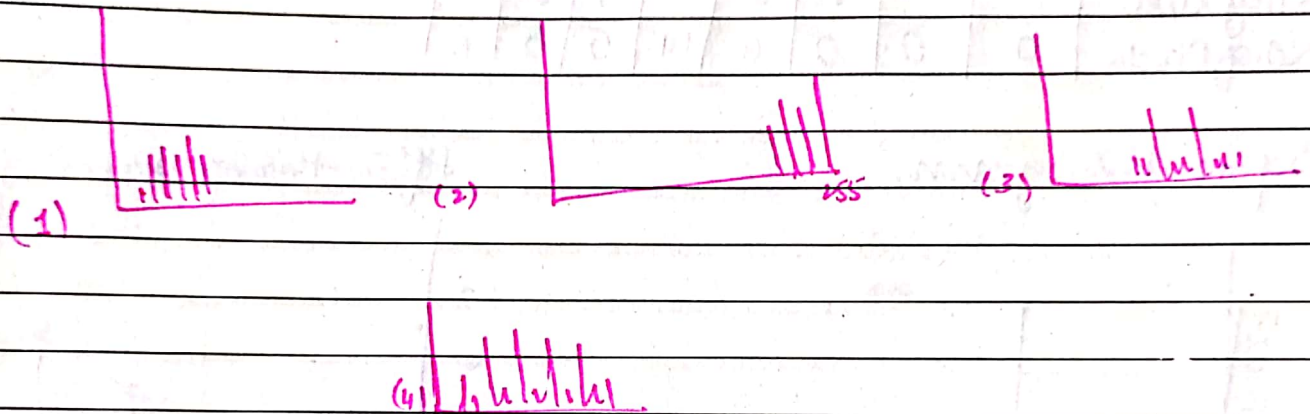
- Used for Brightness & Contrast

1. If graph is towards $(0-1)$ left then more of a black image.

2. If graph is towards (255) - right then it's image is white.

3 - low contrast \rightarrow histogram is at centre.

4 - high contrast \rightarrow entire image.



- controls the quality of image by Normalizing histogram value to flat profile.

7	7	7	7	7
2	6	7	6	2
2	7	7	7	2
2	6	7	6	2
7	7	7	7	7

\rightarrow converted matrix.

Dated: 0

$$F(x,y) =$$

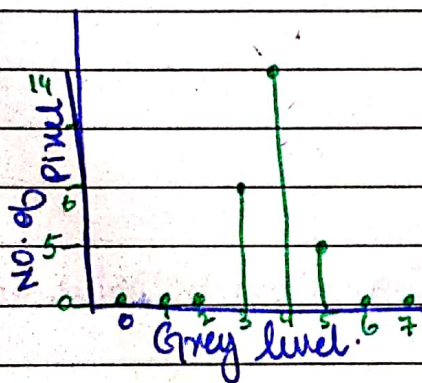
4	4	4	4	4
3	4	5	4	3
3	5	5	5	3
3	4	5	4	3
4	4	4	4	4

→ highest grey level Value = 5
 → bits = $2^3 = 8$.
 (0-7)

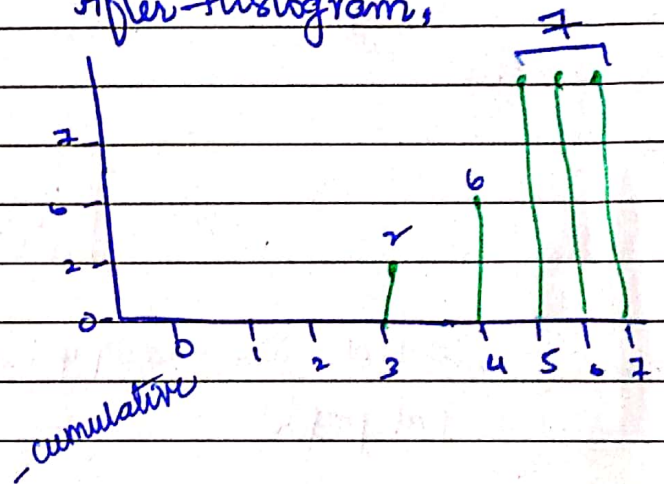
→ No. of Pixel.

Grey level	0	1	2	3	4	5	6	7
NO. of Pixels	0	0	0	6	14	5	0	0

Before Histogram,



After Histogram,



Gray level	NO. of Pixel. (NK)	PDF. $NK / \sum(NK)$	CDF SK.	$SK \times 7$	Histogram Eq. Level.
0	0	$0/25 = 0$	0	$0 \times 7 = 0$	0
1	0	$0/25 = 0$	0	$0 \times 7 = 0$	0
2	0	$0/25 = 0$	0	$0 \times 7 = 0$	0
3	6	$6/25 = 0.24$	0.24	1.68	2
4	14	$14/25 = 0.56$	0.8	5.6	6
5	5	$5/25 = 0.2$	1	7	7
6	0	$0/25 = 0$	1	7	7
7	0	$0/25 = 0$	1	7	7

$\sum 25$

← Transformed Matrix.

Dated:

1 row ka hige 0 (w1, w2, b = 1)
2nd → w1, w2, b = (1st row) goes on.

x_1	x_2	t	y_{in}	y	Δw_1	Δw_2	Δb	w_1	w_2	b
1	1	1	0	0	1	1	1	1	1	1
-1	1	-1	1	1	1	-1	-1	2	0	0
1	-1	-1	2	1	-1	1	-1	1	1	-1
-1	-1	-1	-3	-1	0	0	0	1	1	-1

$$w_1, w_2, b = 0$$

$$\alpha = 1.$$

$$w_1 = 1, w_2 = 1, b = 1, \alpha = 1$$

(1)

$$y_{in} = b + \{w_1 x_1 + w_2 x_2\}.$$

$$y_{in} = 0 + \{0 \times 1\} + \{0 \times 1\}$$

$$0 + 0$$

$$= 0.$$

$$\Delta w_1 = \alpha t x_1$$

$$1 \times 1 \times 1 = 1.$$

$$\Delta w_2 = \alpha t x_2$$

$$1 \times 1 \times 1 = 1$$

$$\Delta b = \alpha t$$

$$1 \times 1 = 1$$

$$w_1 = w_{old} + (\alpha t x_1)$$

$$w_1 = 0 + 1 = 1$$

$$w_2 = 0 + 1 = 1$$

$$b = b_{old} + (\alpha t)$$

$$= 0 + 1$$

$$= 1$$

$$y = w_1 \cdot 1 + w_2 \cdot 1 + b = 1 + 1 + 1 = 3$$

$$-1 + 1 + 1 = 1$$

$$-1 + 1 + 1 = 1$$

$$(2) = 1 + \{1 \times (-1) + (1 \times 1)\}$$

$$1 \neq 0$$

$$= 1.$$

$$\Delta w_1 = \alpha t x_1$$

$$1 \times -1 \times 1 = -1.$$

$$\Delta w_2 = 1 \times -1 \times 1 = -1.$$

$$b = \alpha t$$

$$1 \times -1 = -1.$$

$$w_1 = \text{old} + (\alpha t x_1)$$

$$1 + 1 = 2.$$

$$w_2 = 1 + (-1) = 0.$$

$$b = 1 + (-1) = 0.$$

$$(3) w_1 = 2, w_2 = 0, b = 0, \alpha = 1.$$

$$y_{in} = 0 + \{2 \times 1\} + \{0 \times (-1)\}$$

$$= 0 + 2 = 2.$$

$$\Delta w_1 = \alpha t x_1 = 1 \times 1 \times 1 = 1.$$

$$\Delta b = -1$$

$$\Delta w_2 = 1 \times -1 \times 1 = -1.$$

$$b = -1$$

$$w_1 = 2 + 1 = 3$$

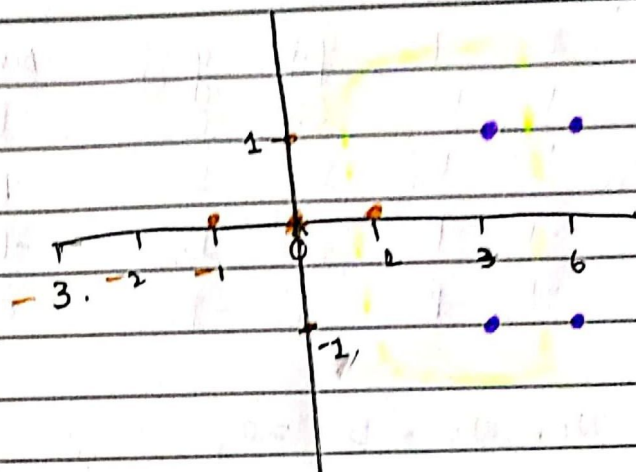
$$w_2 = 0 + 1 = 1.$$

ted:

SYM:-

$$(+)\begin{pmatrix} 3 \\ 1 \end{pmatrix} \begin{pmatrix} 3 \\ -1 \end{pmatrix} \begin{pmatrix} 6 \\ 1 \end{pmatrix} \begin{pmatrix} 6 \\ -1 \end{pmatrix}$$

$$(-)\begin{pmatrix} 1 \\ 0 \end{pmatrix} \begin{pmatrix} 0 \\ 1 \end{pmatrix} \begin{pmatrix} 0 \\ -1 \end{pmatrix} \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$



Supporting vectors

$$s_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix} \quad s_2 = \begin{pmatrix} 3 \\ 1 \end{pmatrix} \quad s_3 = \begin{pmatrix} 3 \\ -1 \end{pmatrix}$$

Now add bias

$$\Rightarrow \tilde{s}_1 = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} \quad \tilde{s}_2 = \begin{pmatrix} 3 \\ 1 \\ 1 \end{pmatrix} \quad \tilde{s}_3 = \begin{pmatrix} 3 \\ -1 \\ +1 \end{pmatrix}$$

$$\begin{aligned} \alpha_1 \tilde{s}_1 \cdot \tilde{s}_1 + \alpha_2 \tilde{s}_2 \cdot \tilde{s}_1 + \alpha_3 \tilde{s}_3 \cdot \tilde{s}_1 \\ \alpha_1 \tilde{s}_1 \cdot \tilde{s}_2 + \alpha_2 \tilde{s}_2 \cdot \tilde{s}_2 + \alpha_3 \tilde{s}_3 \cdot \tilde{s}_2 \\ \alpha_1 \tilde{s}_1 \cdot \tilde{s}_3 + \alpha_2 \tilde{s}_2 \cdot \tilde{s}_3 + \alpha_3 \tilde{s}_3 \cdot \tilde{s}_3 \end{aligned}$$

$$= \alpha_1 \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} + \alpha_2 \begin{pmatrix} 3 \\ 1 \\ 1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} + \alpha_3 \begin{pmatrix} 3 \\ -1 \\ 1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} = -1.$$

$$\alpha_1 \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} \begin{pmatrix} 3 \\ 1 \\ 1 \end{pmatrix} + \alpha_2 \begin{pmatrix} 3 \\ 1 \\ 1 \end{pmatrix} \begin{pmatrix} 3 \\ 1 \\ 1 \end{pmatrix} + \alpha_3 \begin{pmatrix} 3 \\ -1 \\ 1 \end{pmatrix} \begin{pmatrix} 3 \\ 1 \\ 1 \end{pmatrix} = 1$$

$$\alpha_1 \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} \begin{pmatrix} 3 \\ -1 \\ 1 \end{pmatrix} + \alpha_2 \begin{pmatrix} 3 \\ 1 \\ 1 \end{pmatrix} \begin{pmatrix} 3 \\ -1 \\ 1 \end{pmatrix} + \alpha_3 \begin{pmatrix} 3 \\ -1 \\ 1 \end{pmatrix} \begin{pmatrix} 3 \\ -1 \\ 1 \end{pmatrix} = 1$$

Dated:

$$\alpha_1 \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} + \alpha_2 \begin{pmatrix} 3 \\ 0 \\ 1 \end{pmatrix} + \alpha_3 \begin{pmatrix} 3 \\ 0 \\ 1 \end{pmatrix} = \alpha_1 (2) + 4\alpha_2 + 4\alpha_3 = -1$$

$$\alpha_1 \begin{pmatrix} 3 \\ 0 \\ 1 \end{pmatrix} + \alpha_2 \begin{pmatrix} 9 \\ 1 \\ 1 \end{pmatrix} + \alpha_3 \begin{pmatrix} 9 \\ -1 \\ 1 \end{pmatrix} = 4\alpha_1 + 11\alpha_2 + 9\alpha_3 = 1.$$

$$\alpha_1 \begin{pmatrix} 3 \\ 0 \\ 1 \end{pmatrix} + \alpha_2 \begin{pmatrix} 9 \\ -1 \\ 1 \end{pmatrix} + \alpha_3 \begin{pmatrix} 9 \\ 1 \\ 1 \end{pmatrix} = 4\alpha_1 + 9\alpha_2 + 11\alpha_3 = 1.$$

$$2\alpha_1 + 4\alpha_2 + 4\alpha_3 = -1$$

$$4\alpha_1 + 11\alpha_2 + 9\alpha_3 = 1$$

$$4\alpha_1 + 9\alpha_2 + 11\alpha_3 = 1$$

$$\alpha_1 = (-1 - 4\alpha_2 - 4\alpha_3) / 2 \quad -1$$

$$-2 - 8\alpha_2 - 8\alpha_3 + 11\alpha_2 + 9\alpha_3 = 1$$

$$3\alpha_2 + \alpha_3 = 3$$

$$\alpha_3 = 3 - 3\alpha_2 \quad -2$$

Putting value of α_3 & α_1 in eq 3.

$$\alpha_1 = -1 - 4(0.75) - 4(0.75) \quad -2 - 8\alpha_2 - 8\alpha_3 + 9\alpha_2 + 33 - 33\alpha_2 = 1 \quad -3$$

$$= \alpha_1 = -3.5$$

$$\alpha_2 - 8\alpha_3 + 30 - 33\alpha_2 =$$

$$2\alpha_2 = 30 - 8\alpha_3$$

$$= \alpha_2 = 15 - 4\alpha_3$$

$$\alpha_3 = 3 - 3(15 - 4\alpha_3)$$

$$\alpha_3 = 3 - 45 + 12\alpha_3$$

$$11\alpha_3 = 42$$

$$= -33\alpha_2 - 8\alpha_2 + 9\alpha_2 + 30 - 8\alpha_3 = 0$$

$$-32\alpha_2 = 8\alpha_3 - 30$$

$$8\alpha_2 = 30 - 8\alpha_3 - 3 \text{ into } 2$$

$$\alpha_2 = 30 - 6/32$$

$$0.75$$

$$\alpha_3 = 3 - 3 \left(\frac{30 - 8\alpha_3}{32} \right)$$

$$\alpha_3 = 3 - \frac{90 + 24\alpha_3}{32} = \frac{96 - 90 + 24\alpha_3}{32} = \frac{6 + 24\alpha_3}{32}$$

$$8\alpha_3 = 6 \quad \alpha_3 = 0.75$$

