

Problem 1

Authors: Tony Okeke
Nick Corrado
Ben Jennings
Gabriella Grym

Calculate Temperature at Four Locations

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Team: A_03

Script Description

- This script determines the temperatures at different locations based on the model :

$$y(t) = R.\sin(2*\pi/24*(t-t_0)) + B$$

- It returns plots of temperature against time at these locations.

```
% Define time variable
t_data = (0:24)';

% Define cnsts table containing constants at different locations
location = {'Philadelphia, PA','Panama City, FL','Brewster, MA',...
            'Enugu, Nigeria'}';
eq_cnst = [25 9 55 ; 10 9 72 ; 15 9 59 ; 13 9 73];
% eq_cnst(:,1) -> R (oF)
% eq_cnst(:,2) -> t0 (hrs)
% eq_cnst(:,3) -> B (oF)
cnsts = table(location,eq_cnst);
```

cnsts = 4x2 table

	location	eq_cnst		
1	'Philadelphia...	25	9	55
2	'Panama City, FL'	10	9	72
3	'Brewster, MA'	15	9	59
4	'Enugu, Nigeria'	13	9	73

Use `ca1_fun1` to determine temperatures and plot Temperature vs Time graphs for each location.

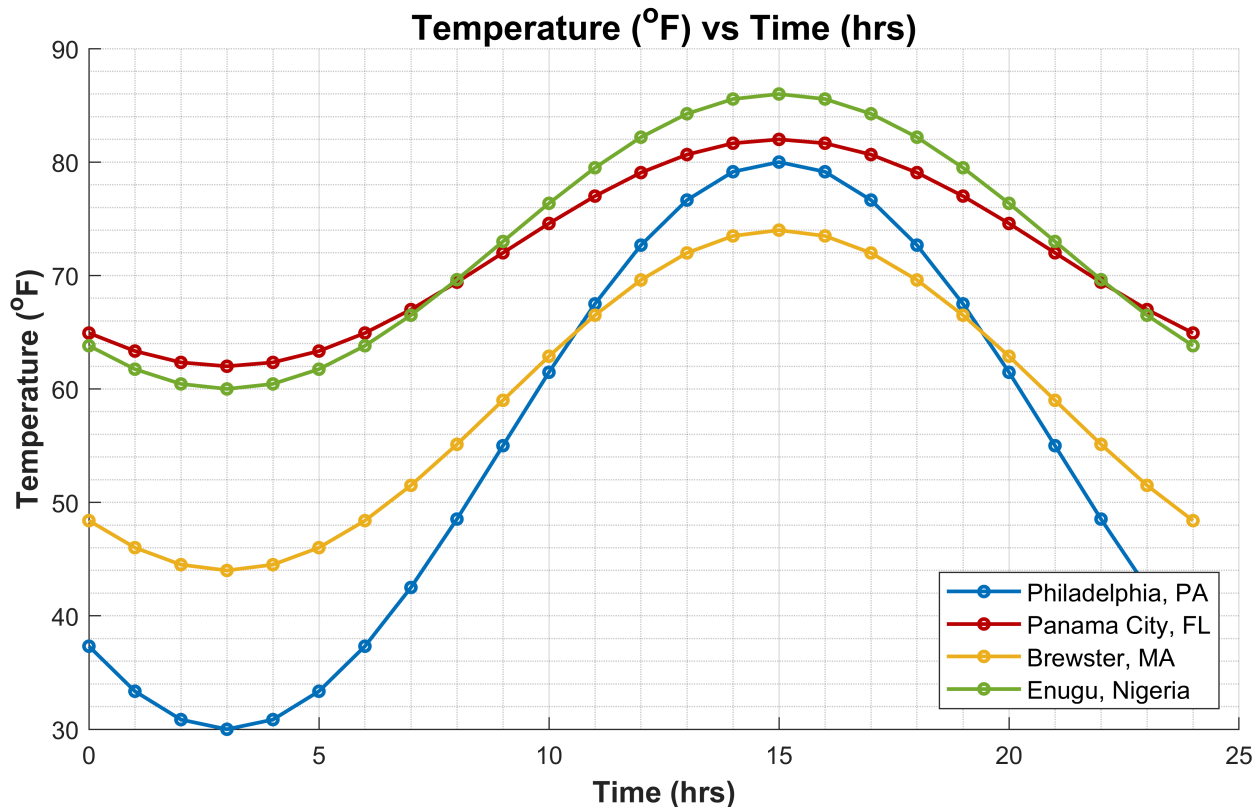
```
% Configure Plot Area
figure
ax = axes;
% Color order for the various graphs
ax.ColorOrder = [0 0.447058823529412 0.741176470588235;0.729411764705882 0 0;...
                 0.929411764705882 0.694117647058824 0.125490196078431;...
                 0.466666666666667 0.674509803921569 0.188235294117647];
% Adjust plot settings
ax.XGrid = 'on';
ax.XMinorGrid = 'on';
ax.YMinorGrid = 'on';
ax.Parent.Position = [900 450 800 450]; % window size
hold on
title('Temperature (^oF) vs Time (hrs)','FontWeight','bold','FontSize',14)
xlabel('Time (hrs)','FontWeight','bold','FontSize',12)
ylabel('Temperature (^oF)','FontWeight','bold','FontSize',12)

% Generate Graphs
for i = 1:numel(location)
```

```

% Calculate yt_data
yt_data = cal_fun1(cnsts.eq_cnst(i,:),t_data);
% Plot Results
plot(t_data,yt_data, '-o', 'LineWidth',1.5, 'MarkerSize',4)
end
legend(location, 'Location', 'southeast', 'FontSize',10)
hold off

```



Determining Constants for Figure 1 (In Problem Statement)

Define Constants and t_data .

From Figure 1 (Problem Statement)

- Max Temp - Min Temp = 40 oF
- Range, $R = 40/2 = \pm 20$ oF
- Bias, $B = \text{Max Temp} - R = 60$ oF

To determine the appropriate t_0 value, we test all possible values and select the one that produces a graph matching figure 1

```

R = 20;
t0 = (0:24)'; % range of values for testing
B = 60;

t_data = (0:24)';

```

Calculate yt_data , and plot graphs for each potential t_0 value in a 5 x 5 subplot grid.

```

figure
clf
for i = 1:numel(t0)
    % Calculate temperature
    yt_data = cal_fun1([R t0(i) B],t_data);

    % Plot Graphs
    subplot(5,5,i)
    hold on
    title(sprintf('t0 = %i',t0(i)))
    plot(t_data,yt_data,'-r')
    plot([15 15],[40 80],'-k') % Identifies peak from problem statement
    xticks(15)
    yticks([])
    hold off
end

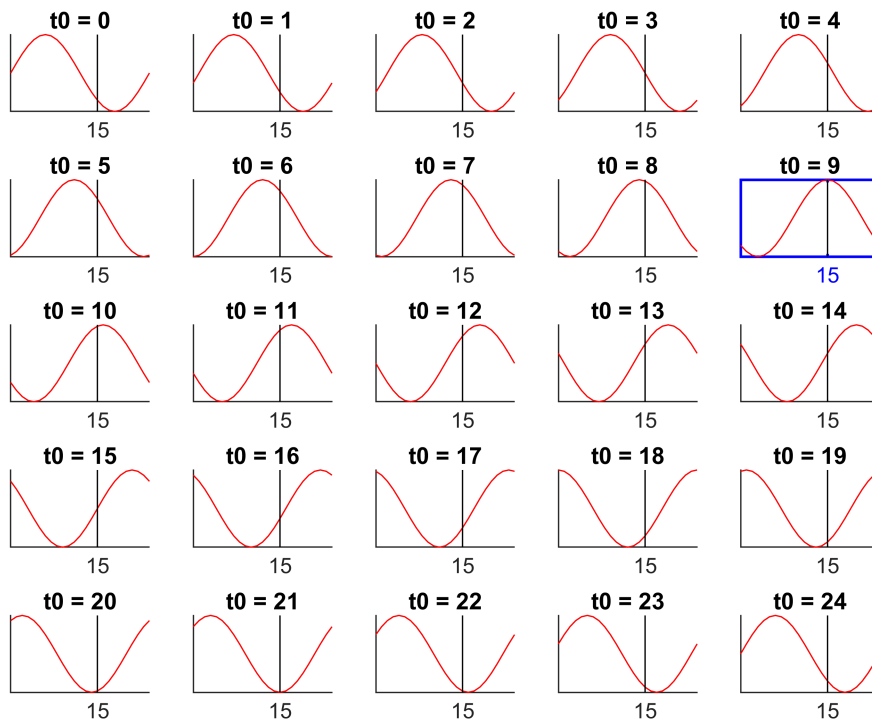
```

The graph $t_0 = 9$ best matches figure 1 as it has the same peak at 15 hrs, as well as matching the shape of figure 1.

```

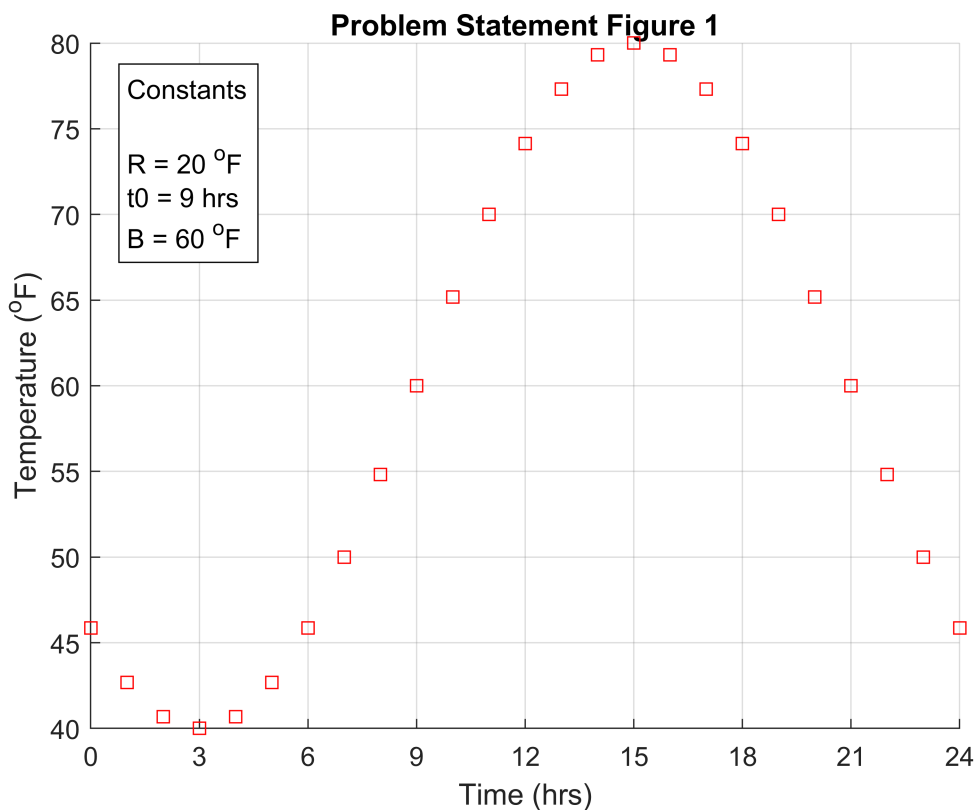
% Emphasize the plot t0 = 9
ax = subplot(5,5,10);
box on
ax.LineWidth = 1;
ax.XColor = 'blue';
ax.YColor = 'blue';

```



Generate Figure 1 From The Problem Statement

```
% Plot Graph
figure
ax = axes;
hold on
plot(t_data,ca1_fun1([R t0(10) B],t_data),'sr');
ax.XGrid = 'on';
ax.YGrid = 'on';
title('Problem Statement Figure 1')
xlabel('Time (hrs)')
ylabel('Temperature (^oF)')
xlim([0 24])
xticks([0 3 6 9 12 15 18 21 24])
% Include a text box containing the determined constants
txt = sprintf('Constants\n\nR = %i ^oF \nt0 = %i hrs \nB = %i ^oF',...
    R,t0(10),B);
a = text(1,73,txt);
a.EdgeColor = 'k';
a.BackgroundColor = 'white';
hold off
```



Problem 2

Calculate Heart-rate Decays for Three Subjects

Script Description

- This function models how the heart rate slows as it returns to 'normal' after exercise based on the model: $y(t) = D \cdot \exp(-t/\tau) + B$
- It plots the return to baseline for three subjects (fit,average,unfit).

```
% Define time variable
t_data = (0:60)';

% Define cnsts table containing constants for the different subjects
fitness = {'Unfit','Average','Fit'}';
eq_cnst = [120 20 75;60 10 60;40 5 40];
% eq_cnst(:,1) -> D (BPM)
% eq_cnst(:,2) -> tau (sec)
% eq_cnst(:,3) -> B (BPM)
cnsts = table(fitness,eq_cnst);
```

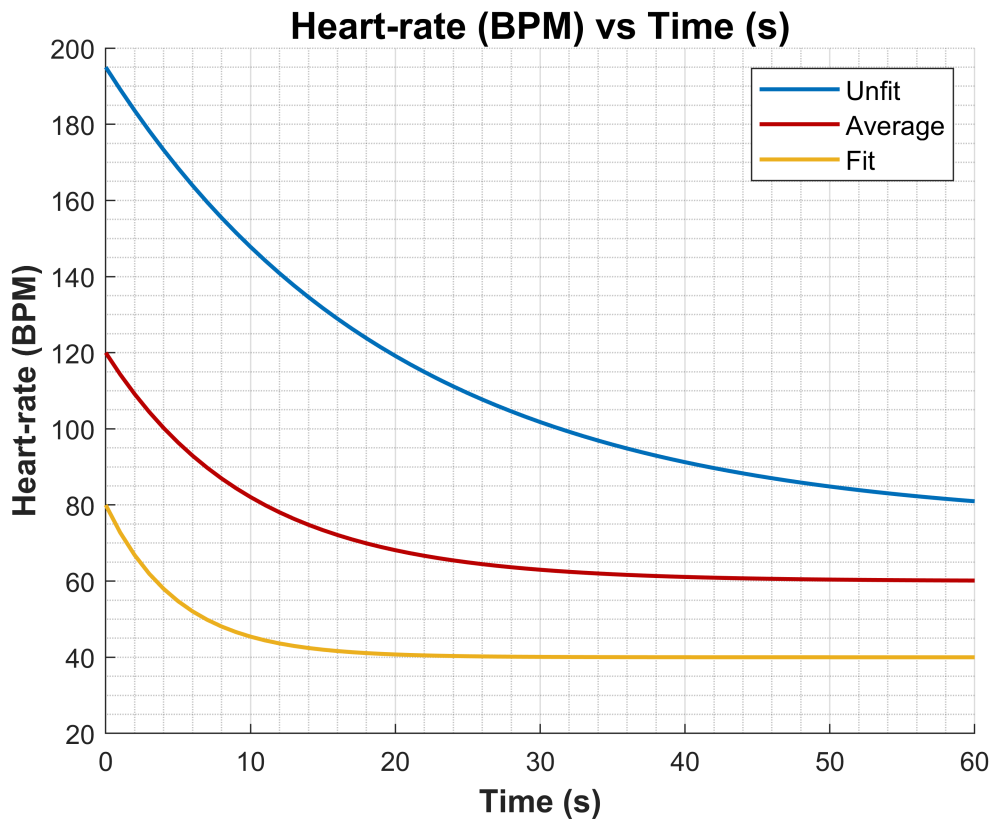
```
cnsts = 3x2 table
```

	fitness	eq_cnst		
1	'Unfit'	120	20	75
2	'Average'	60	10	60
3	'Fit'	40	5	40

Use `ca1_fun2` to determine heart-rates and plot Heart-rate vs Time graphs for each subject.

```
% Configure Plot
figure
ax = axes;
% Color order for the various graphs
ax.ColorOrder = [0 0.447058823529412 0.741176470588235;0.729411764705882 0 0;...
0.929411764705882 0.694117647058824 0.125490196078431];
% Adjust plot settings
ax.XGrid = 'on';
ax.XMinorGrid = 'on';
ax.YMinorGrid = 'on';
hold on
title('Heart-rate (BPM) vs Time (s)','FontWeight','bold','FontSize',14)
xlabel('Time (s)','FontWeight','bold','FontSize',12)
ylabel('Heart-rate (BPM)','FontWeight','bold','FontSize',12)
yticks([20 40 60 80 100 120 140 160 180 200 220])

% Generate Graphs
for i = 1:numel(fitness)
    % Calculate yt_data
    yt_data = ca1_fun2(cnsts.eq_cnst(i,:),t_data);
    % Plot Results
    plot(t_data,yt_data,'-','LineWidth',1.5)
end
ylim([20 200])
legend(fitness,'Location','northeast','FontSize',10)
hold off
```



Determining Constants for Figure 2 (In Problem Statement)

Define Constants and t_data.

From Figure 2 (Problem Statement)

- Increase in HR, $D = \text{Max HR} - \text{Min HR} = 120 \text{ BPM}$
- Base-line HR, $B = \text{Min HR} = 60 \text{ BPM}$

To determine the appropriate tau value, we test four different tau values (based on the values for fit, unfit, and average subjects). The tau value that produces a graph matching figure 2 is then selected.

```
D = 120;
tau = (5:5:20)'; % t0 contains a range of values for testing
B = 60;

t_data = (0:60)';
```

Calculate yt_data, and plot graphs for each potential tau value overlaying figure 2 in a 2 x 2 subplot grid.

```
figure
clf
for i = 1:numel(tau)
    % Calculate heart rate
    yt_data = ca1_fun2([D tau(i) B],t_data);

    % Plot Graphs
    subplot(2,2,i)
```

```

hold on
title(sprintf('tau = %i',tau(i)))
plot(t_data,yt_data,'-r','LineWidth',1.5)
ylim([40 200])

% Add graph from fig.2 to the background of the plots
I = imread('Figure2.png');
h = image([0 60],[200 40],I);
uistack(h,'bottom')
xticks([0 60])
yticks([50 200])
hold off
end

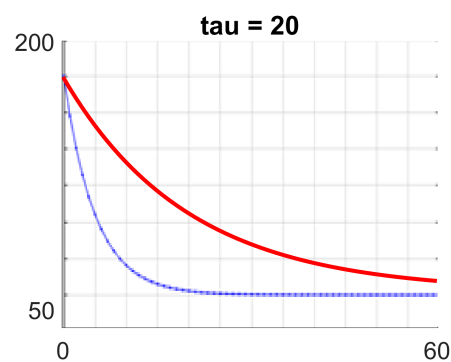
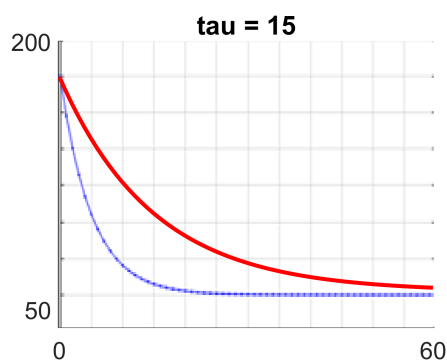
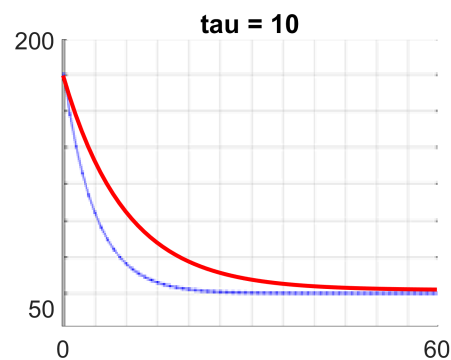
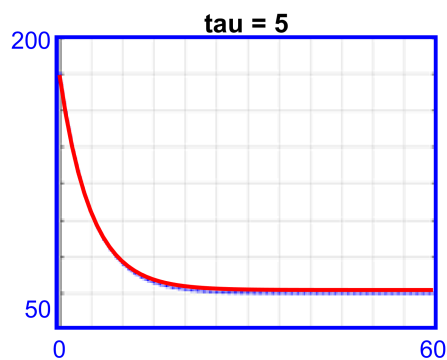
```

The graph $\tau = 5$ matches fig.2 the best out of all values tested.

```

% Emphasize the plot tau = 5
ax = subplot(2,2,1);
box on
ax.LineWidth = 3;
ax.XColor = 'blue';
ax.YColor = 'blue';

```



Generate Figure 2 From The Problem Statement

```

% Plot Graph
figure
ax = axes;
hold on

```

```

plot(t_data,ca1_fun2([D tau(1) B],t_data),'-r','LineWidth',1.5);
ax.XGrid = 'on';
ax.YGrid = 'on';
title('Problem Statement Figure 2')
xlabel('Time (s)')
ylabel('Heart-rate (BPM)')
ylim([40 200])
% Include a text box containing the determined constants
txt = sprintf('Constants\n\nD = %i BPM \n\tau = %i s \nB = %i BPM',...
              D,tau(1),B);
a = text(45,170,txt);
a.EdgeColor = 'k';
a.BackgroundColor = 'white';
hold off

```

