# Multiple Sequence Alignment

by Ahmet Sacan

# Multiple alignment

- Improve confidence in homology
- Correct an alignment
- Find conserved residues and regions
- Predict protein secondary/tertiary structures

### Multiple sequence alignment

• Given k sequences, find an alignment that maximizes the alignment score.

VSLSCTGSSSNIGAGNHVKWYQQLPG
VTISCTGTSSNIGSITVNWYQQLPG
ATLVCLISDFYPGASVTVAWKADS
AALGCLVKDYFPEPVTVSWNSG
LTCLVKGFYPSDIAVEWESNG



VSLSCTGSSSNIGAG-NHVKWYQQLPG
VTISCTGTSSNIG--SITVNWYQQLPG
ATLVCLISDFYPGA-SVTVAWKADS-AALGCLVKDYFPEP--VTVSWNSG----LTCLVKGFYPSD--IAVEWESNG--

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# Multiple Alignment Score

Column score = Sum of all-pairs:

$$S_{VV} + S_{VA} + S_{VA} + S_{V-} + S_{VA} + S_{V-} + S_{VA} + S_{V-} + S_{AA} + S_{A-} + S_{A-}$$

 Multiple Alignment score = Sum of all column scores

### Multiple Alignment Score

 Pairwise sequence alignment score:

$$S_{ab} = S_{VV} + S_{ST} + S_{LI} + S_{SS} + \cdots$$

 Multiple Alignment Score: sum of all pairwise alignments

$$S_{ab} + S_{ac} + S_{ad} + S_{ae} + S_{bc} + S_{bc} + S_{bd} + S_{be} + S_{cd} + S_{ce} + S_{de}$$

a: VSLSCTGSSSNIGAG-NHVKWYQQLPG

**b**: VTISCTGTSSNIG--SITVNWYQQLPG

c: ATLVCLISDFYPGA-SVTVAWKADS--

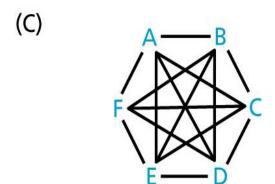
1: AALGCLVKDYFPEP--VTVSWNSG---

e: --LTCLVKGFYPSD--IAVEWESNG--

### Multiple Alignment Score

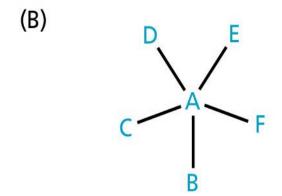
• Sum of scores of pairwise alignments:

#### All-pairs



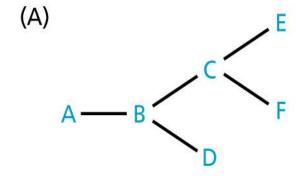
score = 
$$S_{AB} + S_{AC} + S_{AD} + S_{AE} + S_{AF}$$
  
+  $S_{BC} + S_{BD} + S_{BE} + S_{BF} + S_{CD}$   
+  $S_{CE} + S_{CF} + S_{DE} + S_{DF} + S_{EF}$ 

#### Star



score = 
$$S_{AB} + S_{AC} + S_{AD} + S_{AE} + S_{AE}$$

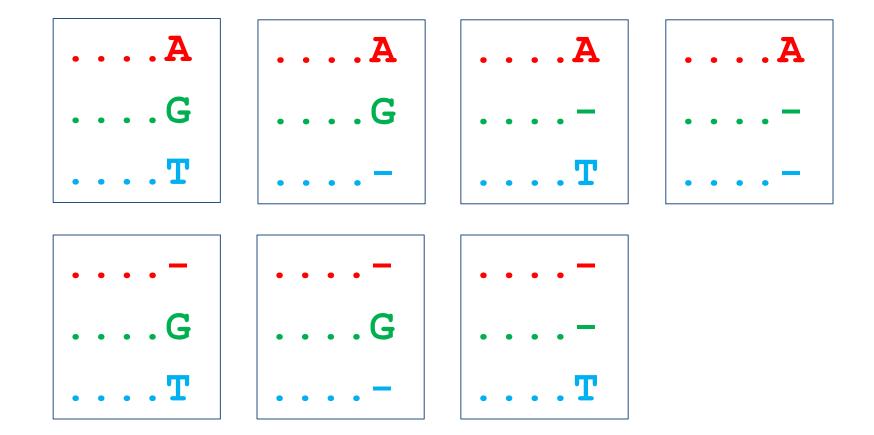
#### Phylogenetic-tree



score = 
$$S_{AB} + S_{BC} + S_{BD} + S_{CE} + S_{CE}$$

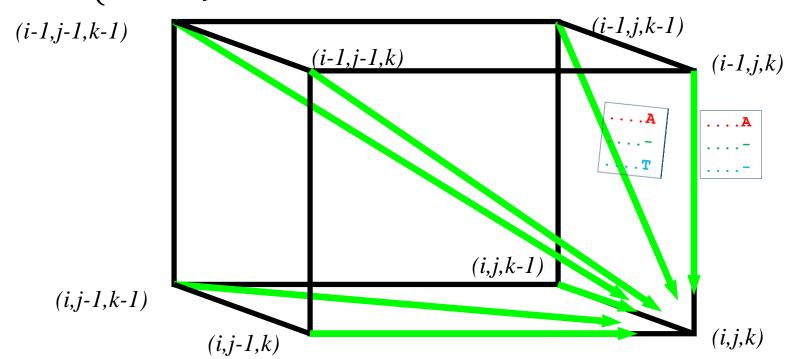
### Aligning 3 sequences

 The last column of the alignment could be one of:



#### Dynamic Programming Multiple alignment

$$S_{i,j,k} = max \begin{cases} S_{i-1,j-1,k-1} + \delta(a_i,b_j,c_k) & \text{cube diagonal: no indels} \\ S_{i,j-1,k-1} + \delta(\_,b_j,c_k) & \\ S_{i-1,j,k-1} + \delta(a_i,\_,c_k) & \text{face diagonal: one indel} \\ S_{i-1,j-1,k} + \delta(a_i,b_j,\_) & \\ S_{i,j,k-1} + \delta(\_,b_j,\_) & \\ S_{i,j-1,k} + \delta(\_,b_j,\_) & \\ S_{i-1,j,k} + \delta(a_i,\_,\_) & \text{edge diagonal: two indels} \end{cases}$$



### Dynamic Programming Multiple alignment: Computational Complexity

• For 3 sequences of length n, run time is:  $O(7n^3)$ 

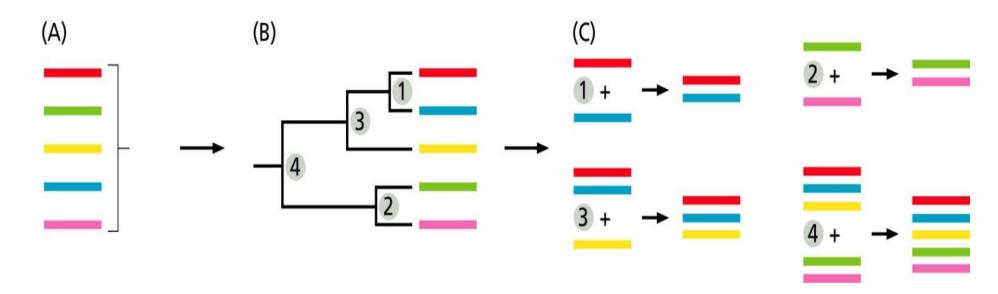
• For 4 sequences:  $O(15n^4)$ 

• For k sequences:

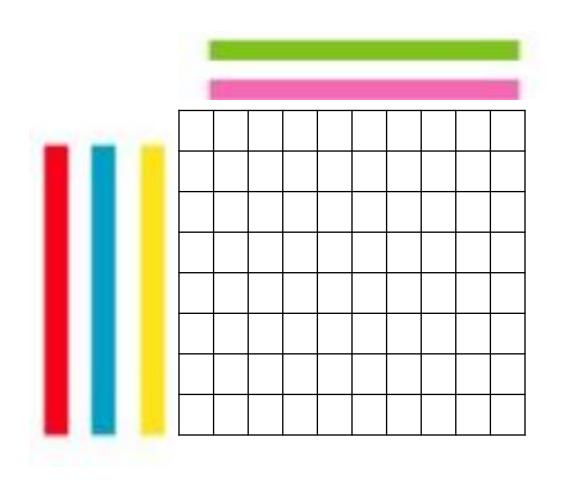
$$-O((2^k-1)n^k) = O(2^k n^k)$$

### Progressive alignment

- · Do pairwise alignment at each step
  - Align a sequence to a sequence
  - Align a sequence to a multiple-alignment
  - Align a multiple alignment to a multiple alignment



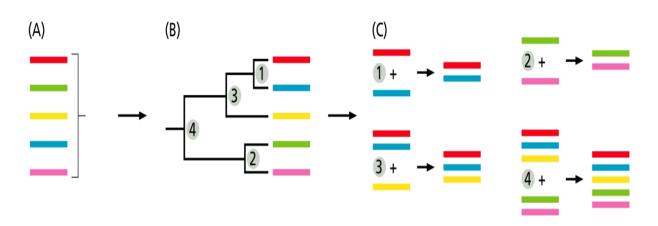
### Dynamic Programming to Align Alignments



### Progressive alignment: Computational Complexity

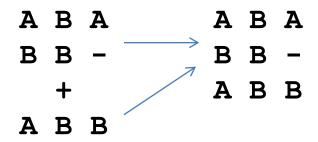
- · k sequences, each with length n
- Each pairwise alignment:  $O(n^2)$
- Building the phylogenetic tree
  - $-O(k^2)$  pairwise comparisons
  - $-O(k^2n^2)$  time
  - Done once, to construct a phylogenetic tree
- Number of merge steps
  - -O(k) steps
  - $-O(k n^2)$  time
- Overall time:

$$-O(k^2n^2 + kn^2) = O(k^2n^2)$$

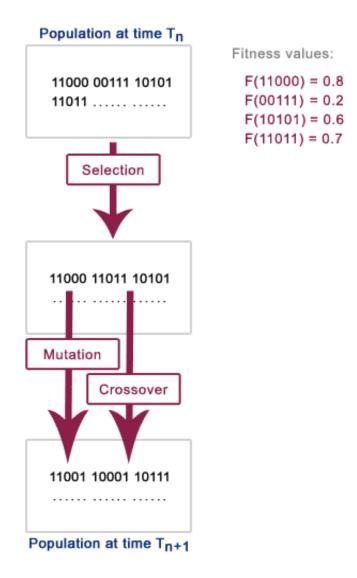


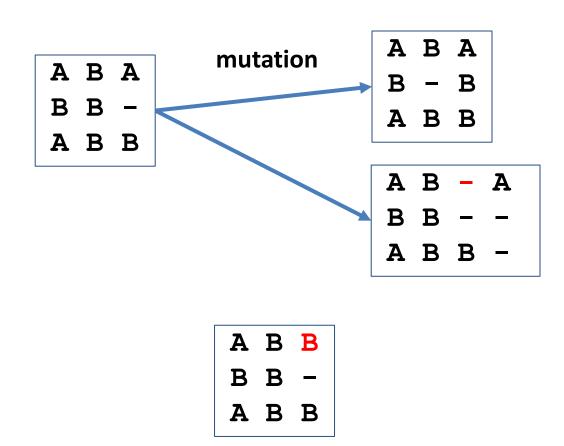
### The order of alignment matters

- Align ABA, BB, and ABB
- If we align ABA and BB, we may get:



 If we align ABA and ABB first, we don't have this problem:





(B)

```
WGKVN---VDEVGGEAL-
WDKVNEEE---VGGEAL-
WGKVG--AHAGEYGAEAL
WSKVGGHA--GEYGAEAL
```

WD--WGK

--WGKVNVDEVG-GEAL WD--KVNEEEVG-GEAL WGKVGA-HAGEYGAEAL WSKVGGHAGE-YGAEAL

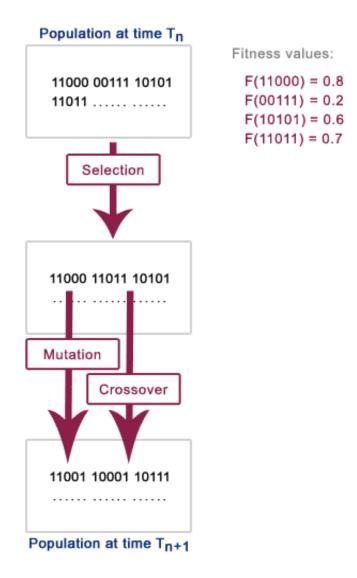
one-point crossover

new offspring

--WGKVN---VDEVGGEAL-WD--KVNEEE---VGGEAL-WGKV--G--AHAGEYGAEAL WSKV--GGHA--GEYGAEAL

selection

WGKV--NVDEVG-GEAL WDKV--NEEEVG-GEAL WGKVGA-HAGEYGAEAL WSKVGGHAGE-YGAEAL



### Summary

- Multiple sequence alignment is more accurate than pairwise alignment
  - Used to create sequence profiles
- Multiple Alignment is a computationally difficult problem
  - Finding optimal solution is not feasible
- Heuristic approaches find an answer efficiently, but do not guarantee it is the best one
- Optimization methods can be employed to obtain better solutions.