

Model Predictive Control (MPC) Project

The Model

The state contains the x position, y position, vehicle orientation, velocity, cross track error or **cte**, which express the error between the center of the road and the vehicle's position, and the orientation error or **epsi**.

It also has two actuators: the steering wheel, and the throttle and brake pedals considered as a single actuator (negative values signifies braking, and positive values signifies accelerating). Therefore, we have two control inputs, the steering angle δ and the acceleration **a**.

The model we have chosen in the one explained in the course, with the following update equations:

$$\begin{aligned}x_{[t+1]} &= x[t] + v[t] * \cos(\psi[t]) * dt \\y_{[t+1]} &= y[t] + v[t] * \sin(\psi[t]) * dt \\\psi_{[t+1]} &= \psi[t] + v[t] / L_f * \delta[t] * dt \\v_{[t+1]} &= v[t] + a[t] * dt \\cte[t+1] &= f(x[t]) - y[t] + v[t] * \sin(\epsilon[t]) * dt \\\epsilon[t+1] &= \psi[t] - \psi_{sides}[t] + v[t] * \delta[t] / L_f * dt\end{aligned}$$

Please notice that **Lf** measures the distance between the front of the vehicle and its center of gravity.

Our constraints are $[\delta, a]$, with steering angle $\delta \in [-25, 25]$ degrees (or $\delta \in [-0.436332, 0.436332]$ in radians) and acceleration $a \in [-1, 1]$.

In my model, I am trying to minimize the predicted distance of the vehicle from the trajectory (cte). Also, I try to minimize the predicted difference between the vehicle orientation and trajectory orientation (epsi).

Timestep Length and Elapsed Duration (N & dt)

The duration over which future predictions are made is the prediction horizon or **T**.

N is the number of timesteps in the horizon. **dt** is how much time elapses between actuations.

$$T = N \times dt.$$

In my final model, I have chosen $N=10$ and $dt=0.1$, which gives a prediction horizon equals 1 second. I expect that in 1 second, the environment does not change too much.

I have tried other combination of values, such as $\{N=10, dt=0.5\}$ and $\{N=20, dt=0.1\}$, but the one I have noticed better results is the one I mentioned at the beginning $\{N=10, dt=0.1\}$.

Polynomial Fitting and MPC Preprocessing

I calculate waypoints by using the following formula:

```
waypoints_x[i] = cos_psi * (ptsx[i] - px) + sin_psi * (ptsy[i] - py);  
waypoints_y[i] = -sin_psi * (ptsx[i] - px) + cos_psi * (ptsy[i] - py);
```

I use a helper (**polyfit**) to fit a third order polynomial to waypoints, and another helper function (**polyeval**) to calculate the cross track error (**cte**) and orientation error (**epsi**).

The initial state is set with **x**, **y** and **psi** equals to 0. The initial state values for **cte** and **epsi** are the ones obtained the former paragraph. The initial state value for **v** is calculated as described in the next section (**Model Predictive Control with Latency**).

```
// set the initial state, with x, y and psi equals 0  
VectorXd initial_state(6);  
initial_state << 0, 0, 0, v, cte, epsi;
```

Steering angle and throttle are calculated invoking **mpc.Solve()** method as follows:

```
// obtain throttle and steer via mpc  
MPC_Results res = mpc.Solve(initial_state, coeffs);  
double steer_value = -res.steering;  
double throttle_value = res.throttle;
```

Model Predictive Control with Latency

In real cars, an actuation command doesn't execute instantly. There is a delay as the command propagates through the system. This is known as "latency".

To deal with latency, we implement the following equations:

```
// Deal with latency  
px = px + v * cos_psi * latency;  
py = py + v * sin_psi * latency;  
psi = psi - v * steering / 2.67 * latency;  
v = v + throttle * latency;
```

where 2.67 is the L_f . That value was obtained by measuring the radius formed by running the vehicle in the simulator around in a circle with a constant steering angle and velocity on a flat terrain.