

# BLG456E

## Robotics

### Intro to Localisation (Without Probability)

#### Lecture Contents:

- Intro to perceptual reconstruction.
- Localisation problem & sub-problems.
- Representations.
- Localisation from features.
- Triangulation.

<b>Lecturer:</b>	Damien Jade Duff
<b>Email:</b>	<a href="mailto:djduff@itu.edu.tr">djduff@itu.edu.tr</a>
<b>Office:</b>	EEBF 2316
<b>Schedule:</b>	<a href="http://djduff.net/my-schedule">http://djduff.net/my-schedule</a>
<b>Coordination:</b>	<a href="http://ninoa.itu.edu.tr/Ders/4709">http://ninoa.itu.edu.tr/Ders/4709</a>

# Towards cognitive robotics

*Reactive robots* have huge potential:

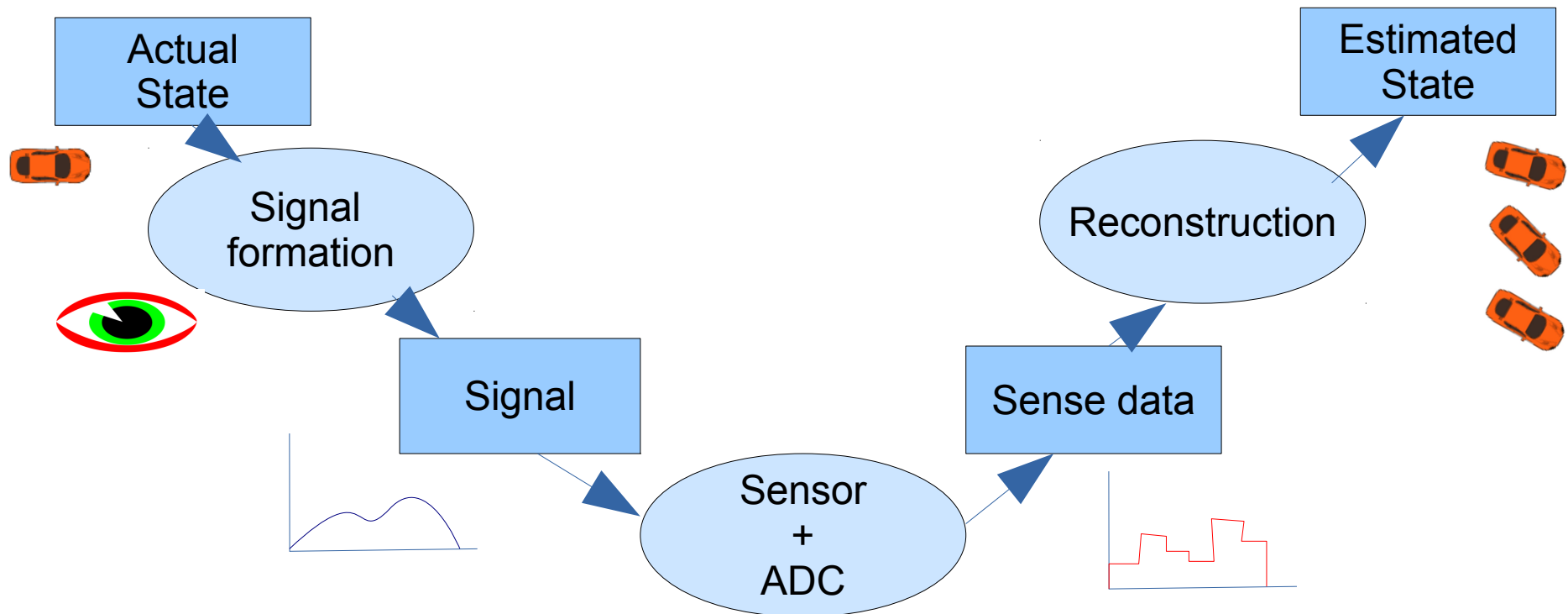
- Learning.
- Evolving.
- ...

*Cognitive robotics* is a good engineering shortcut.

- Representing world information and computing on it → engineering solution.
- BUT:
  - Be careful about *reification*.
  - The world is still *out there*.
  - Don't be fooled by false introspection.

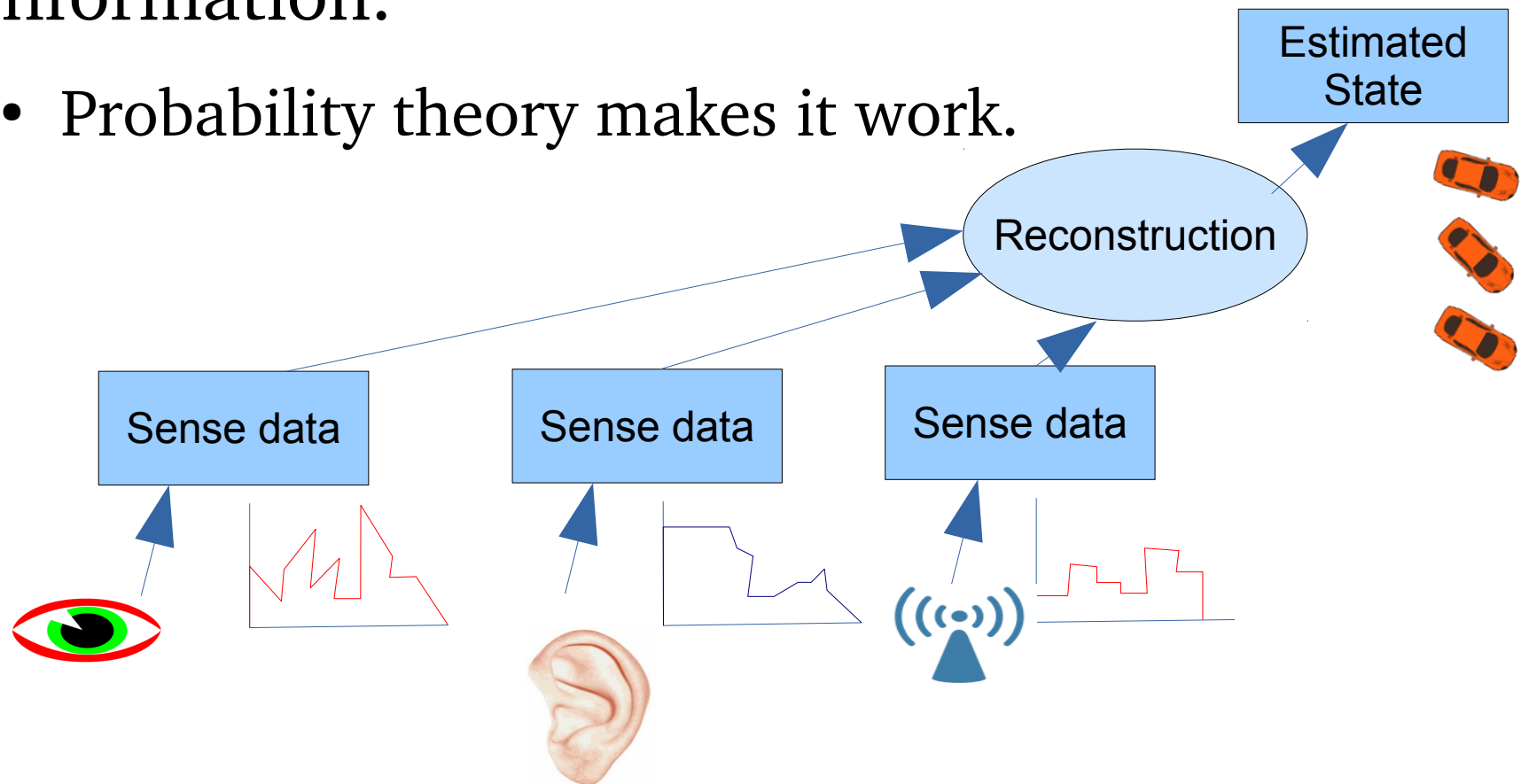
# Reconstruction from sense data

"What must the world be like to get these readings?"



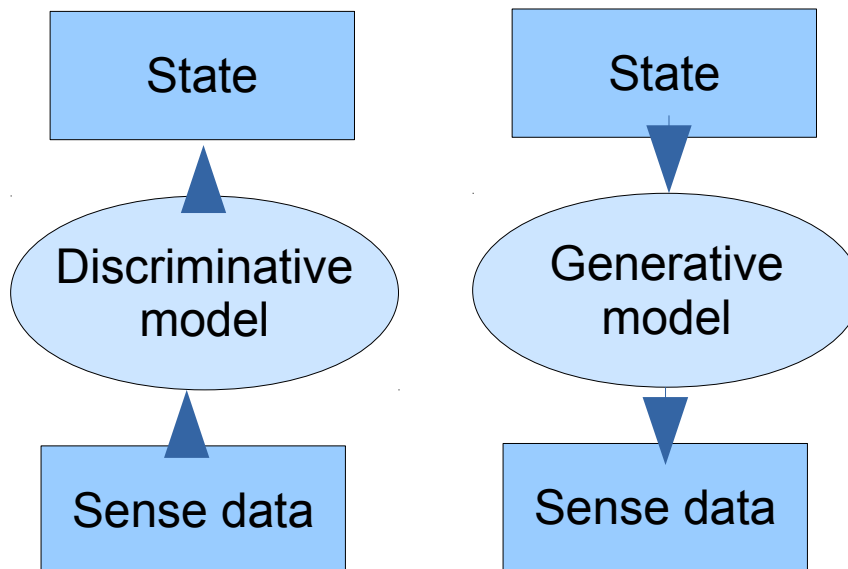
# Sensor fusion

- Combine multiple sources of (sense) information.
  - Probability theory makes it work.



# Discriminative vs. generative models

- Reconstruction usually uses **observation model**.
- **Discriminative model**: How to reconstruct state from sense data.
- **Generative model**: How sense data generated.
  - Extra step to get discriminative model.
  - Easier to understand (e.g. causal models, optic models).



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# Localisation Problem

- Determine robot pose.
- With respect to environment representation (s).
  - e.g. 2D v. 3D.
  - e.g. Coordinates v. grid entry v. location label.
  - e.g. Workspace coordinates v. configuration.
- Use sensors + prediction.

# Open loop localisation

1. Send motor command.
  2. Guess new position.
- Simplest approach.
  - No sensing!



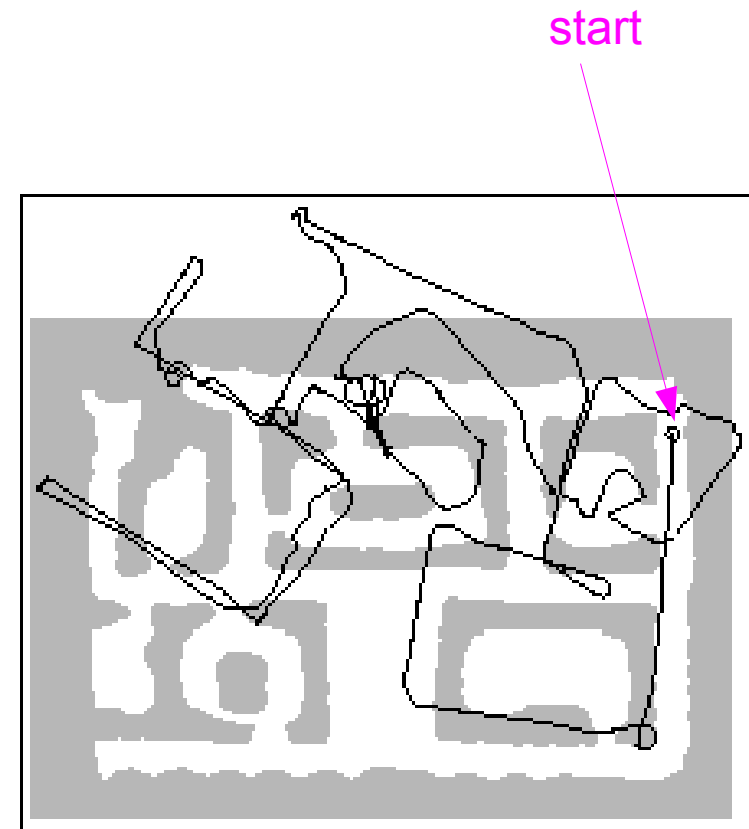
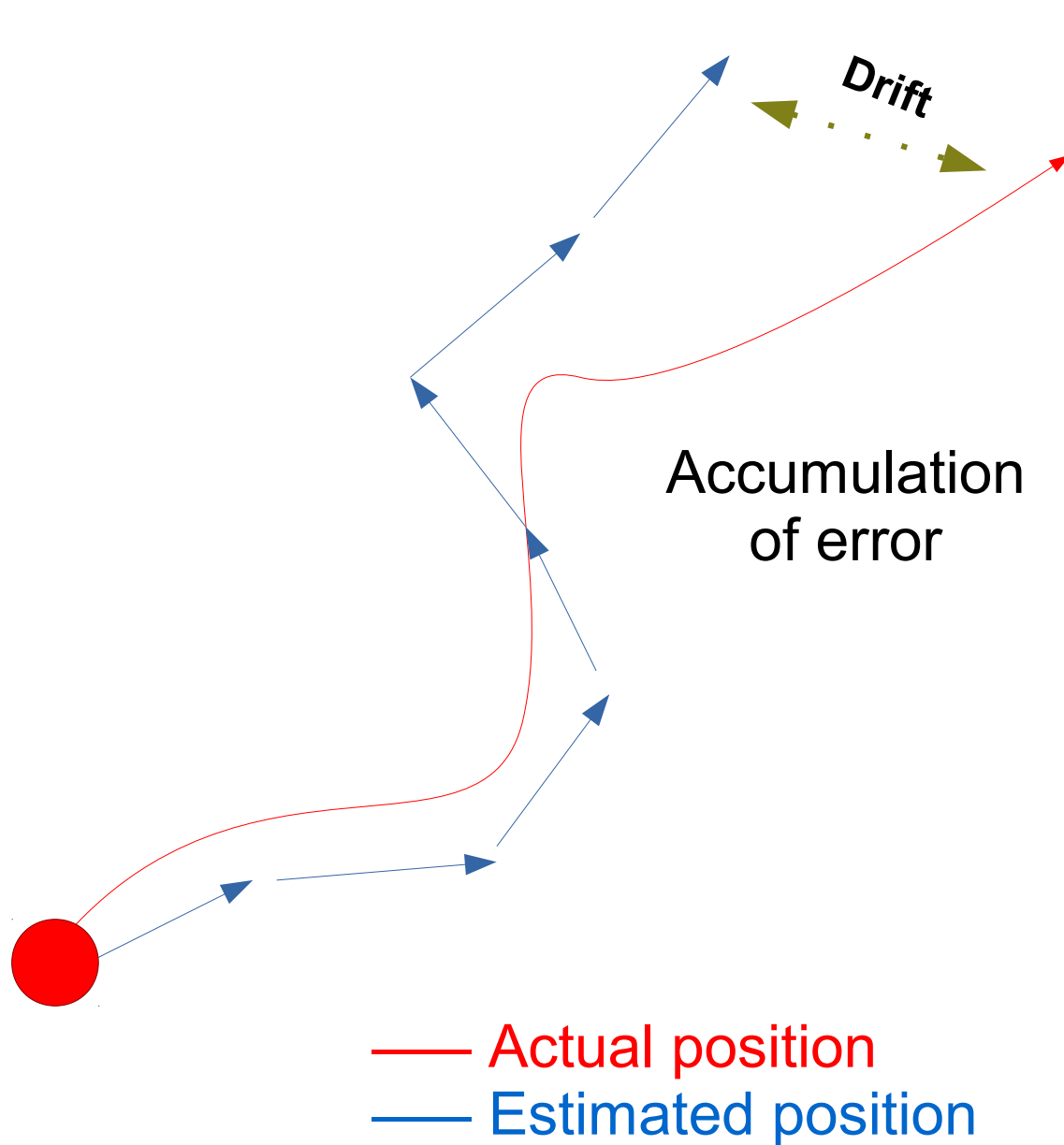


# Dead reckoning

- Only standard odometry (proprioceptive).
- Can estimate change in location.
- Many error sources:
  - Slip, inaccuracy, noise, quantisation errors, kidnapping, etc.
- Error accumulates:
  - Range error.
  - Turn error.



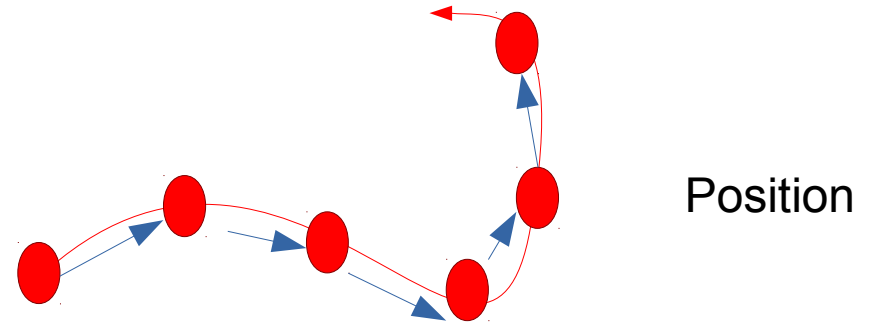
# Dead reckoning



# Localisation sub-problems

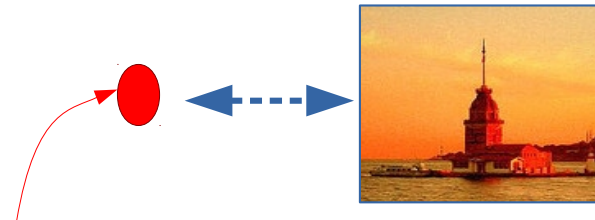
## Position tracking:

- Pose wrt last known point.
- Also "odometry" (e.g. visual odometry).



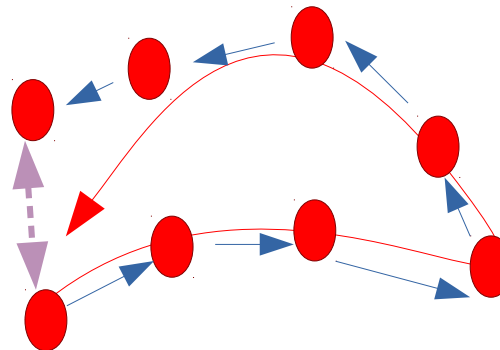
## Global localisation:

- Pose wrt known locations.
- (see "robot kidnapping problem")



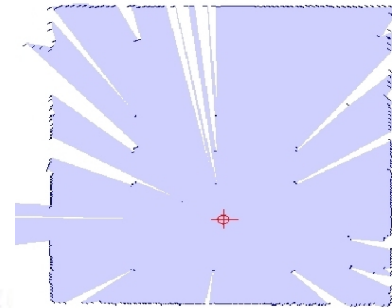
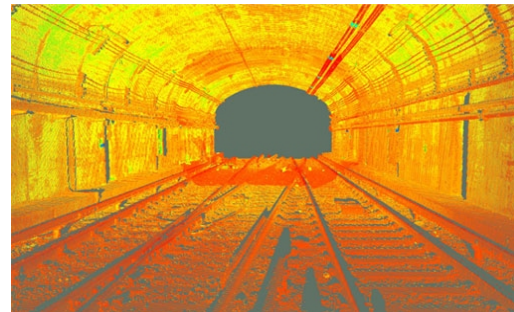
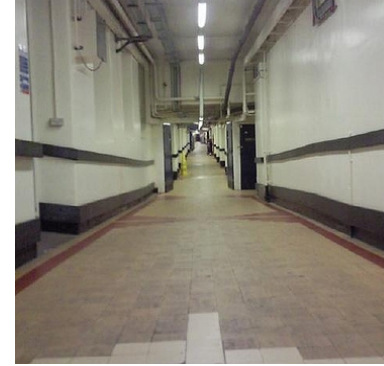
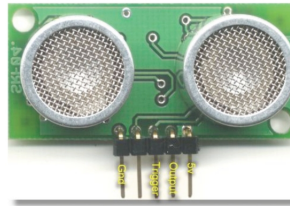
## Loop closing:

- Fixing position track when re-reaching known location.
- Solve "drift".



# Localisation sensors: examples

- Vision.
- Sonar distance.
- Laser distance scans.
- GPS.
- Compass.
- WLAN signal strength.
- Depth and RGBD cameras.



# Active v. Passive Localisation

*Passive:*

In parallel:

- Complete task.
- Localise from sensors.

*Active:*

Simultaneously:

- Complete task.
- Localise from sensors.
- Act to localise.

Acting must satisfy both immediate task and perceptual needs



# Considerations

- Map representation?
  - E.g. occupancy grid, polygonal, landmark-based.
- Data used.
  - E.g. optical flow, wi-fi signal, odometry.
- Map-data mapping.
  - E.g. Prediction/likelihood, RANSAC.
- Position prediction.
  - E.g. velocity based.
- Data expectations.
  - E.g. predicted feature locations.

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# Map representation

Continuous metric.

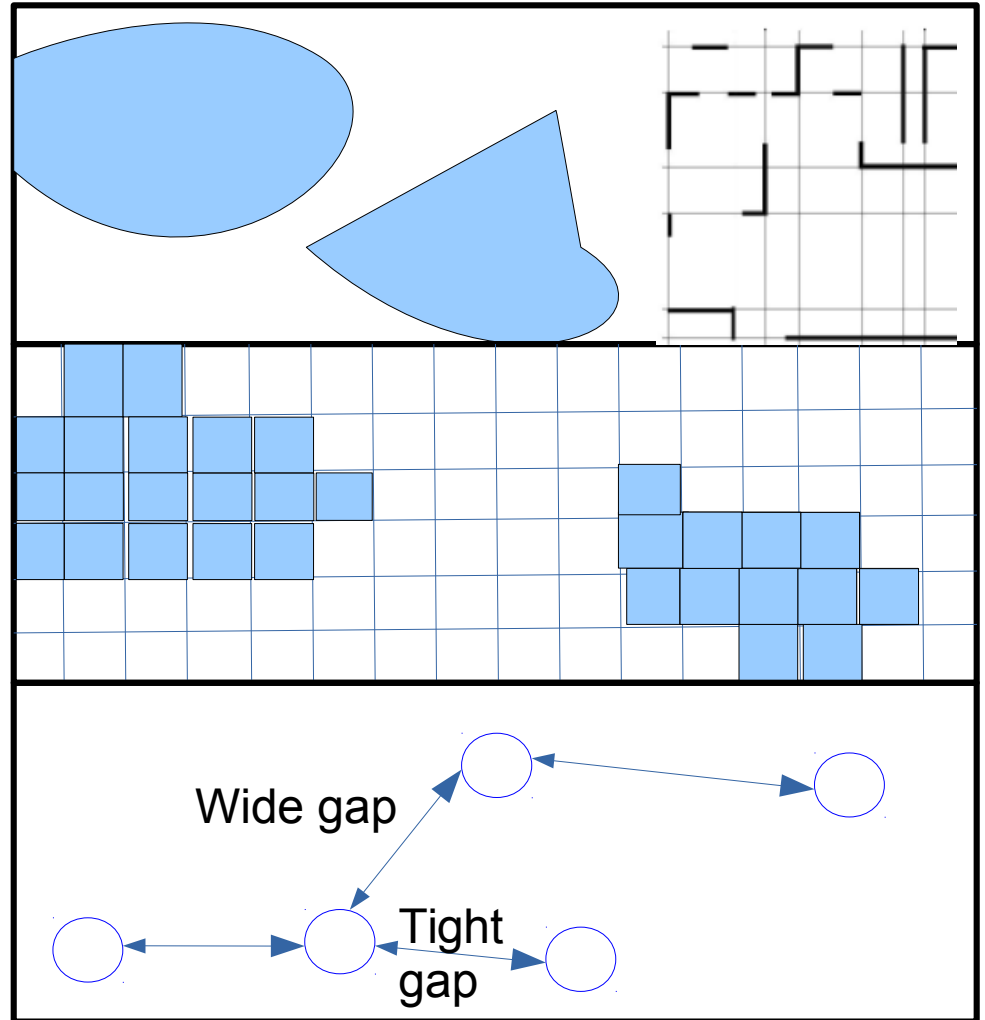
- Parametric curves/lines/surfaces.
- $O(\text{primitives})$

Discrete metric.

- Grids/adaptive occupancy grids.
- $O(\text{size}^2)$

Topological.

- Waypoints and edges.
- $O(\text{places} + \text{ways})$

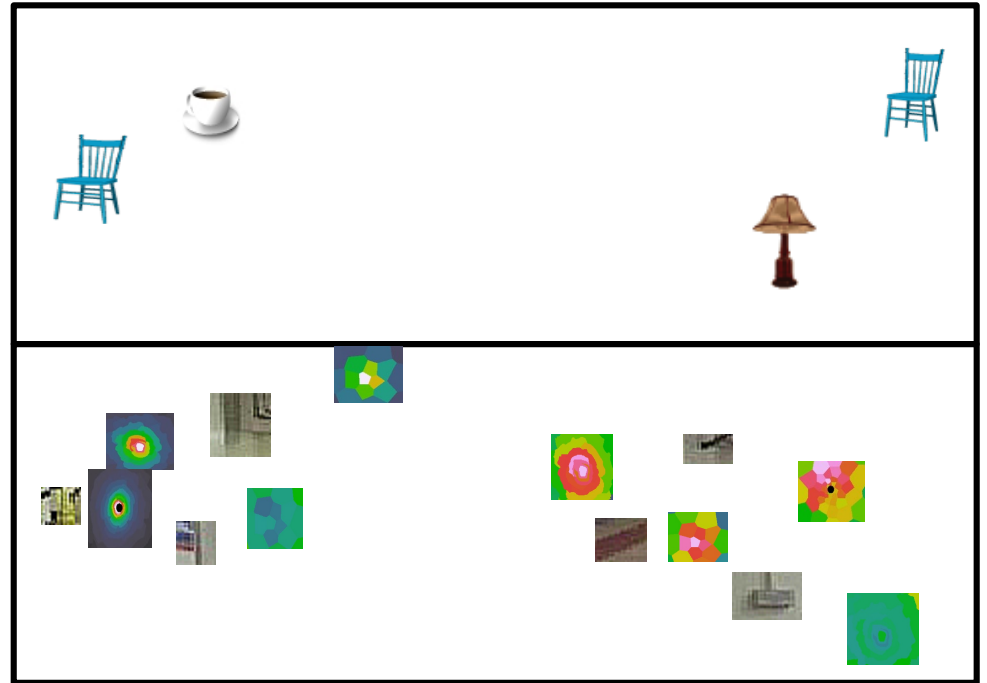




# Map representation

Landmarks/feature maps.

- Known locations/visual elements.
- $O(\text{features})$



Mixed maps.

- Topology + metric + etc.
- More tractable, more complicated.

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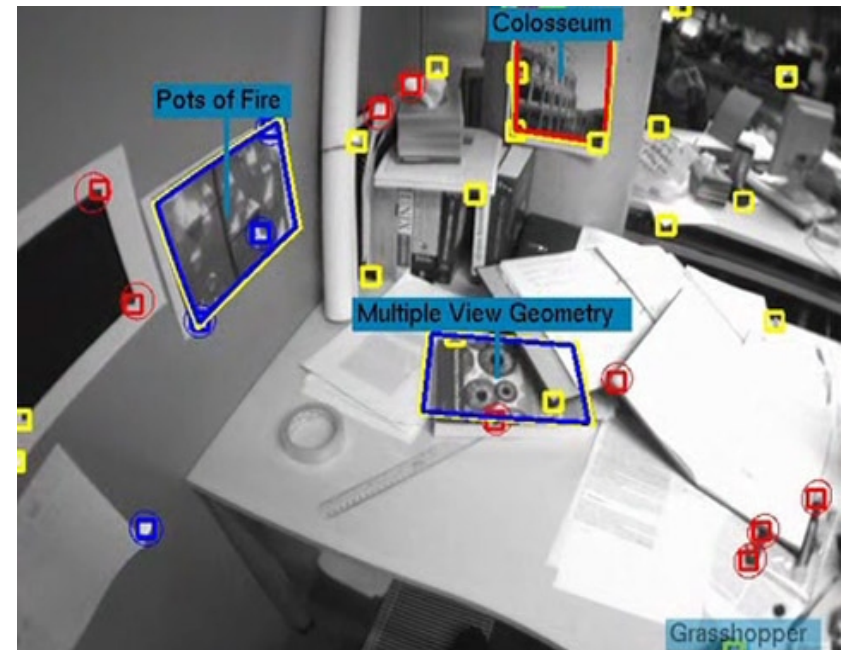
# Features: image features

“Monoslam”



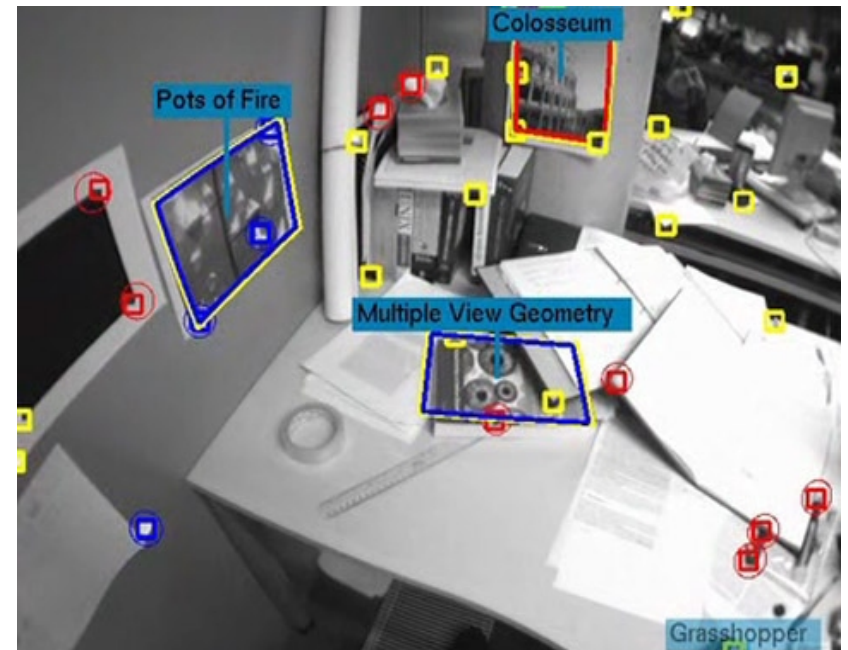
# Qualities of good features

- Detectable.
  - Looks different from background.
    - E.g. `corner detection`.
- Repeatably detectable.
  - Same features detected reliably.
    - E.g. the same points tend to be detected as corners.



# Qualities of good features

- Identifiable.
  - Can recognize it again.
    - E.g. Invariant to angle.
    - E.g. A human face, specific pattern of grays.
- Fusable.
  - Suitable for combining.
    - E.g. Audio source + visual have direction in common?

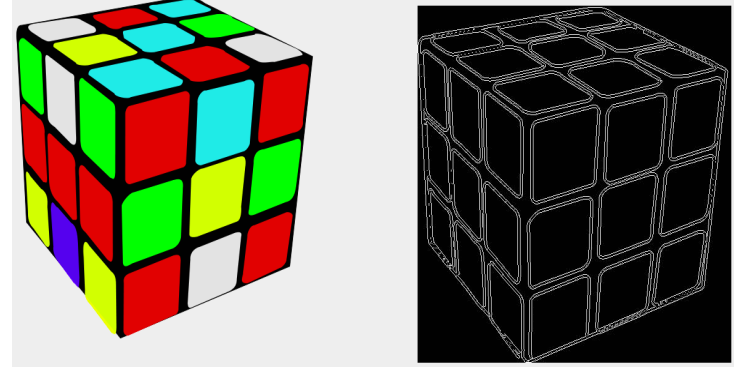


# Levels of features

Raw data / templates.



- Low level features.



High level features.



# Levels of features

Raw data / templates.

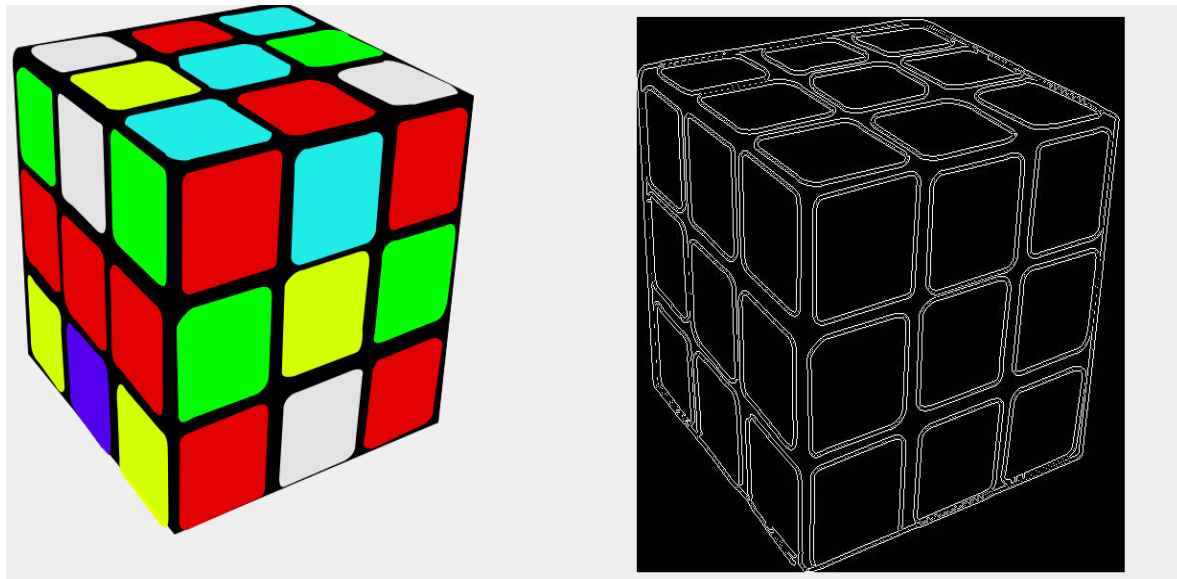
- e.g. laser data, image pixel regions.
- Makes use of all info.
- Lots of extra info → low distinctiveness.
- Usually not invariant (to e.g. angle).



# Levels of features

Low level features.

- e.g. lines, edges, corners, NARF, SIFT, FPH.
- Aim is discriminability, tractable ambiguity.





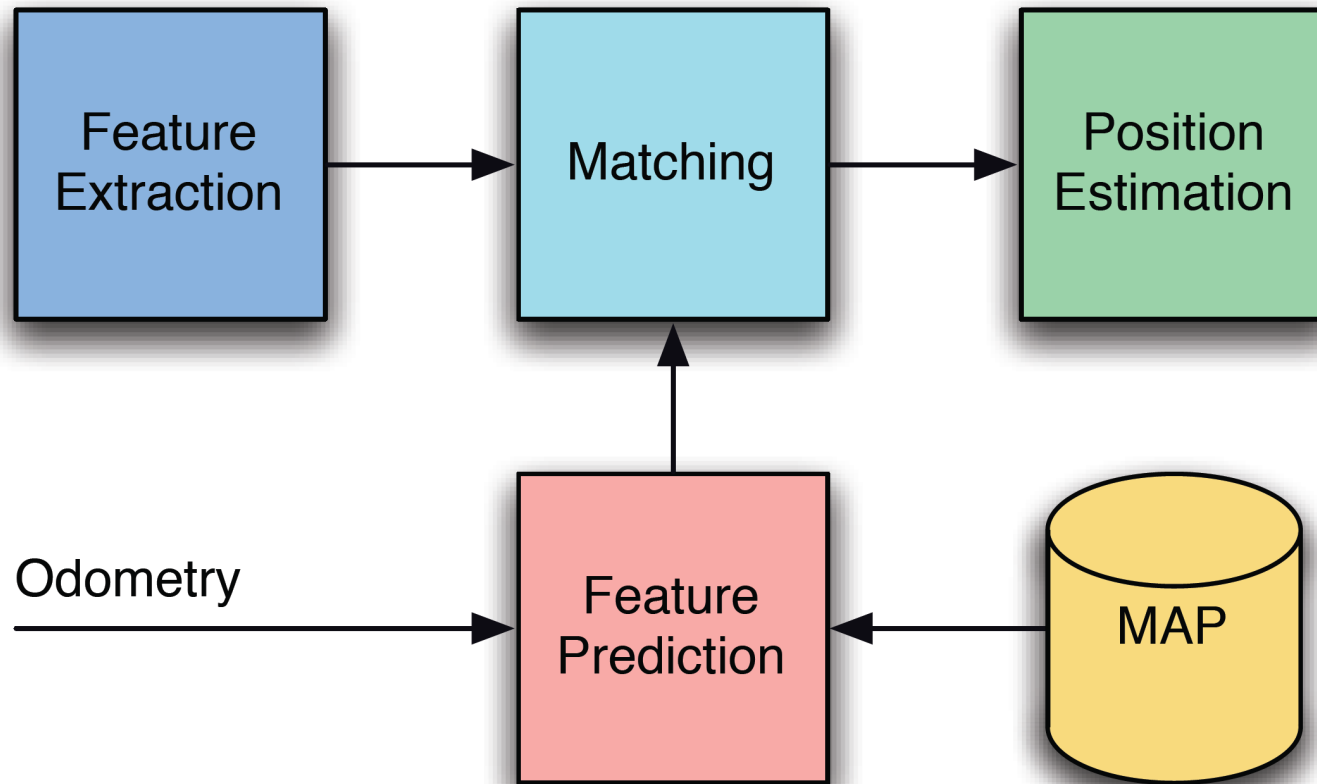
# Levels of features

High level features.

- e.g. faces, objects.
- Semantic level or full object surfaces.
- Much information removed.
- Discriminability is low.



# A landmark-based localisation framework



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# Triangulation from landmarks/features

- From multiple features:
  - Range  $\rightarrow$  location.
- Bearing  $\rightarrow$  location.
- Range + bearing  $\rightarrow$  location.



500m



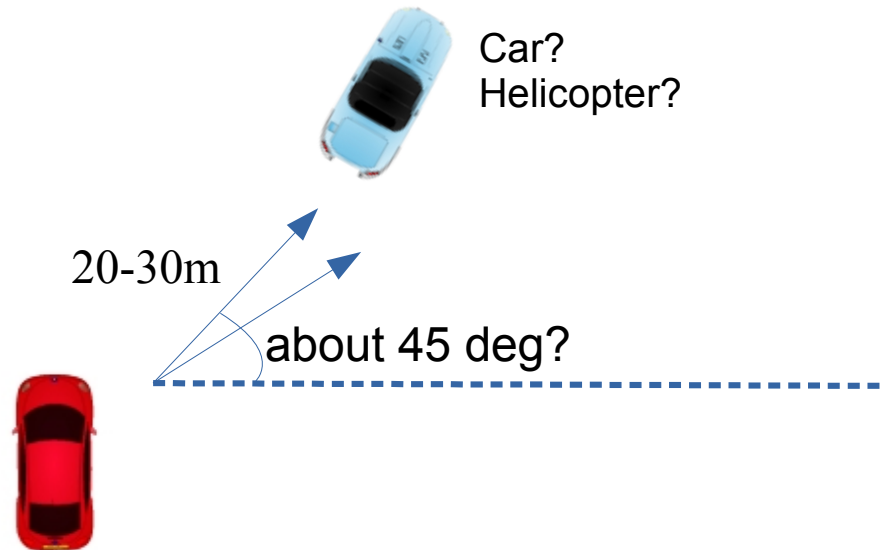
1000m



45 degrees  
(North by North East)

# Note on partial observability

- World is partially observable.
- Features are partially observable:
  - Range.
  - Bearing.
  - Semantics.
  - ...

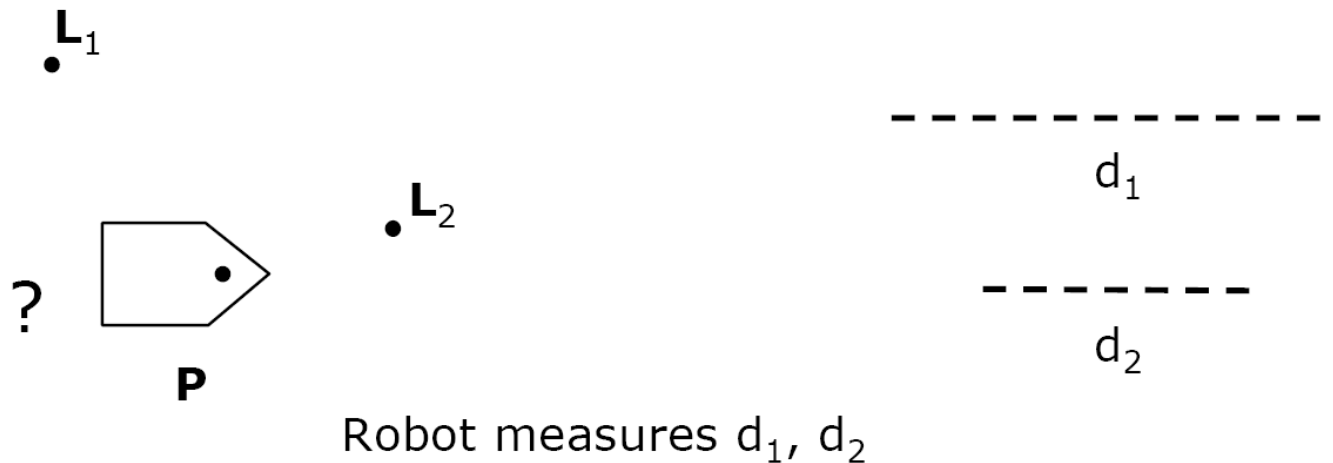


This lecture does not utilise probability for dealing with this – that is the topic of “estimation”.

# Triangulation from ranges

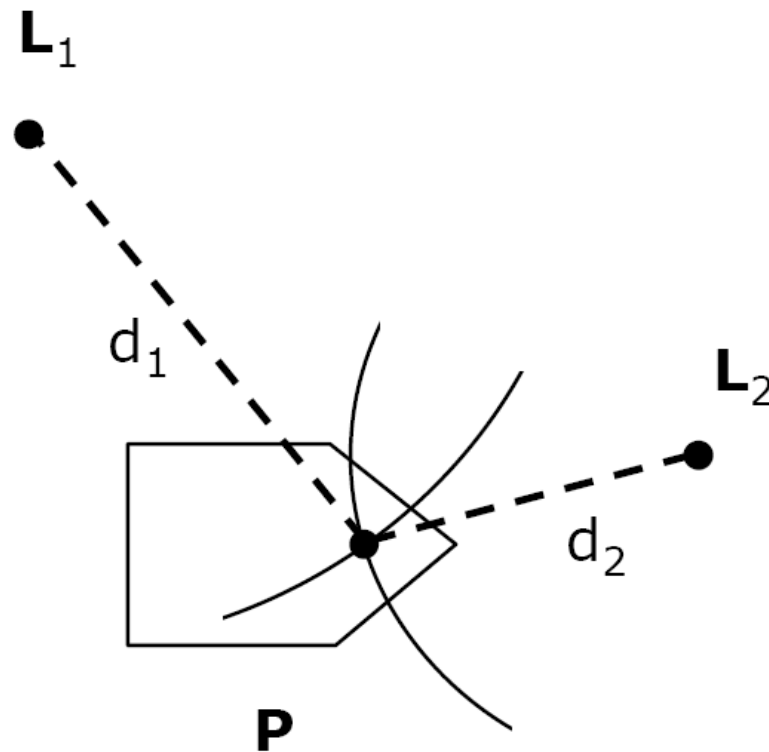
Robot at P.

Measures distances  $d_1$  and  $d_2$  to  $L_1$  and  $L_2$ .



# Triangulation from ranges

Robot must be on circles from  $L_1$ ,  $L_2$ , radii  $d_1$  and  $d_2$ .

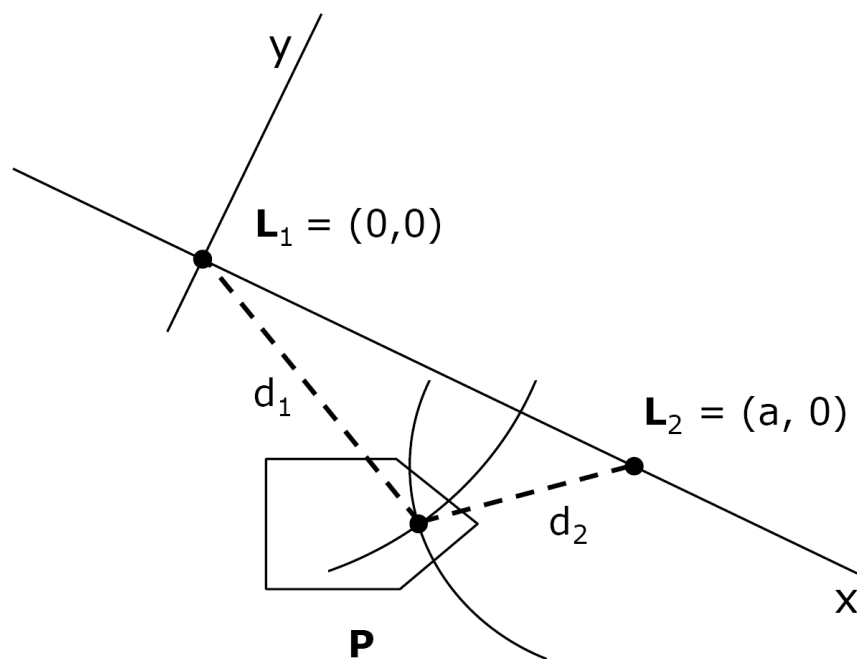


# Triangulation from ranges

Make a coordinate frame from landmarks.

$L_1$  at origin.

$L_2$  at  $(a,0)$  ( $a$  is  $L_1$ - $L_2$  distance).



$$x = (a^2 + d_1^2 - d_2^2) / 2a$$

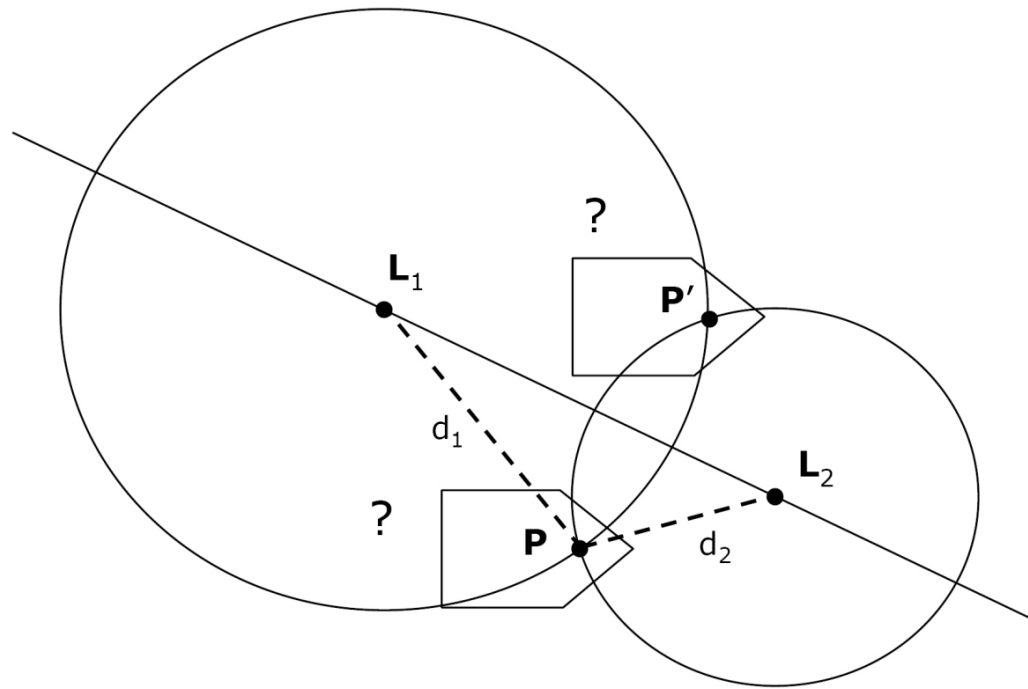
$$y = \pm \sqrt{(d_1^2 - x^2)}$$

(Try e.g. setting  $d_1 = a$ ,  $d_2 = 0$ )



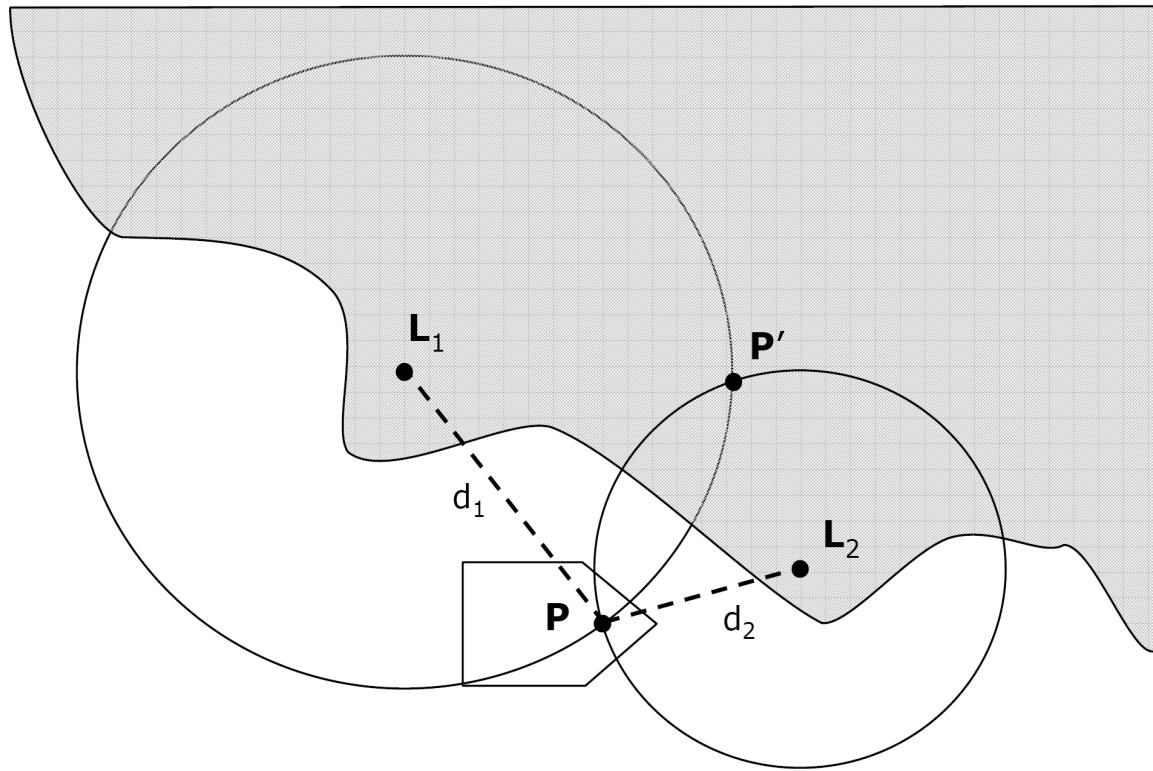
# Disambiguating between solution candidates

Two possible solutions.



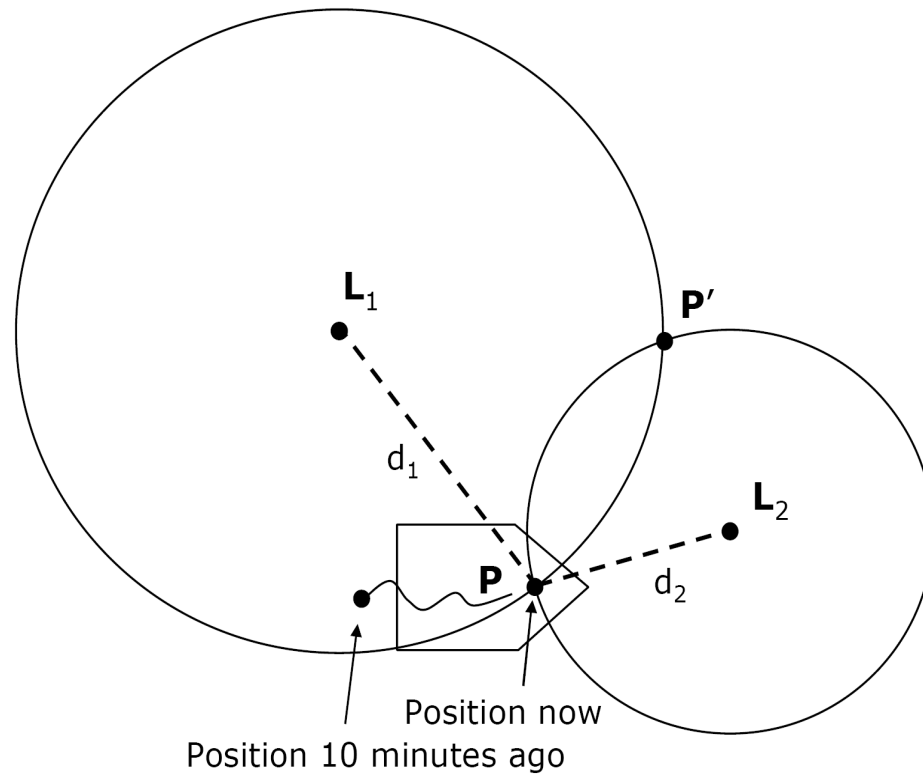
# Disambiguating between solution candidates

A priori/known information.



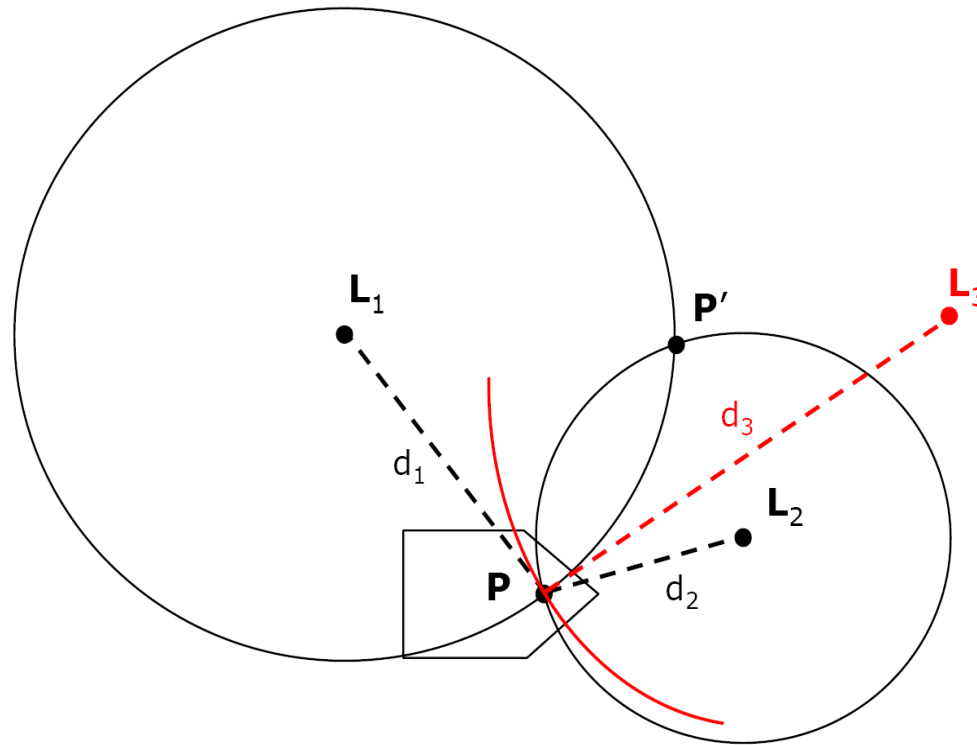
# Disambiguating between solution candidates

Continuity (spatio-temporal info).



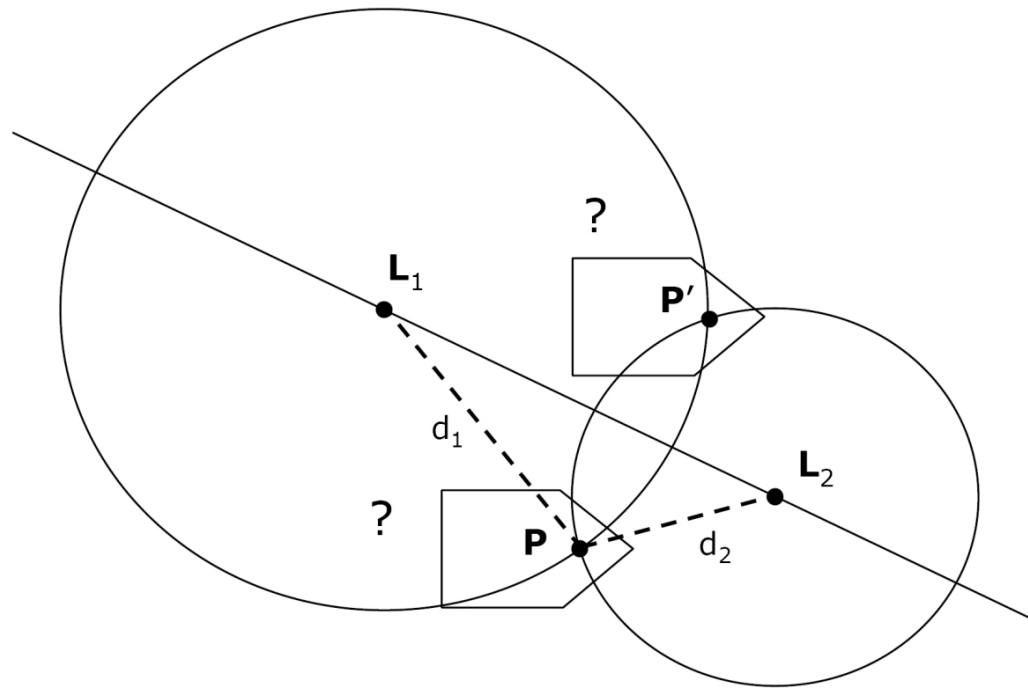
# Disambiguating between solution candidates

Additional landmarks.



# Disambiguating between solution candidates

Can you think of any other information that  
might disambiguate  $P$  from  $P'$ ?



# Triangulation from bearings

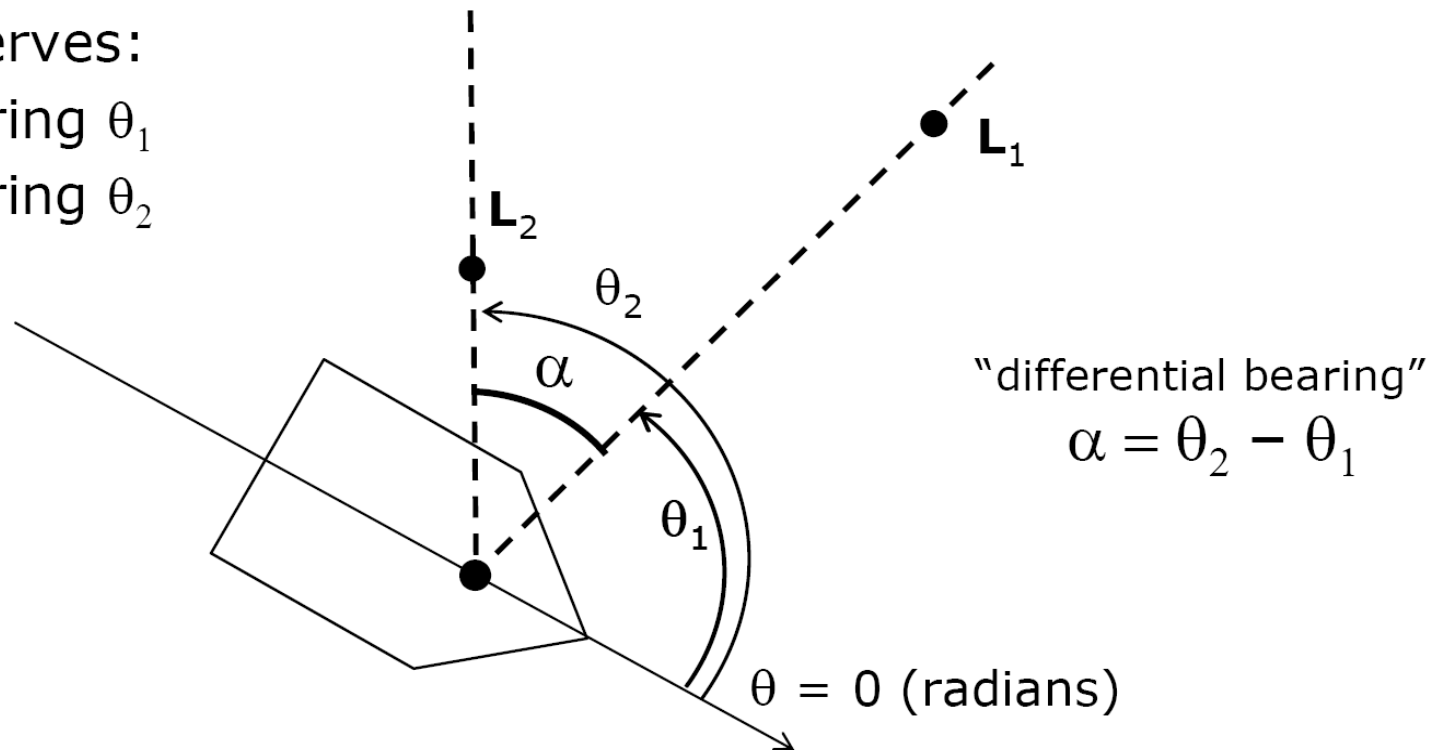
**2 bearings:** restrict pose to an arc.

**3 bearings:** restrict pose to a point.

Robot observes:

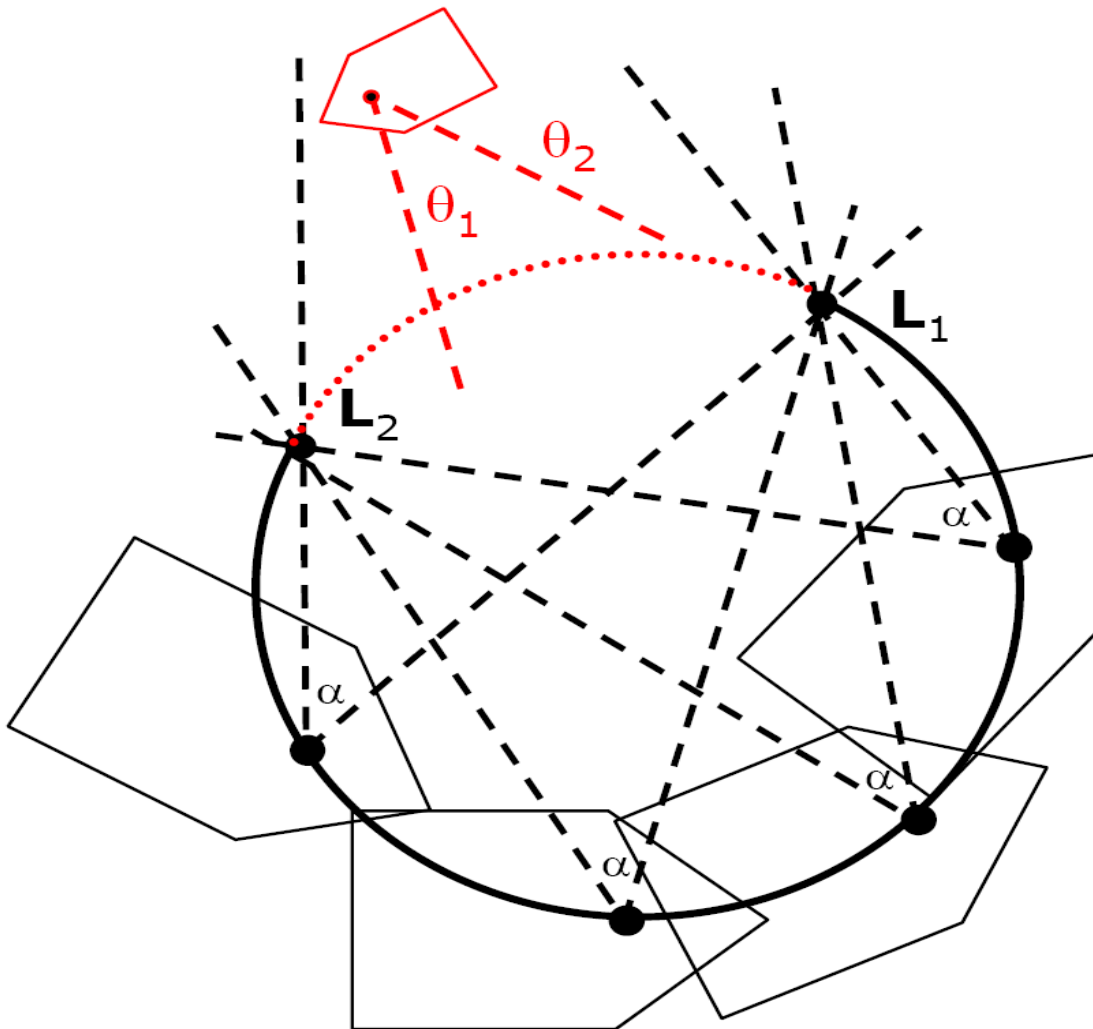
$L_1$  at bearing  $\theta_1$

$L_2$  at bearing  $\theta_2$



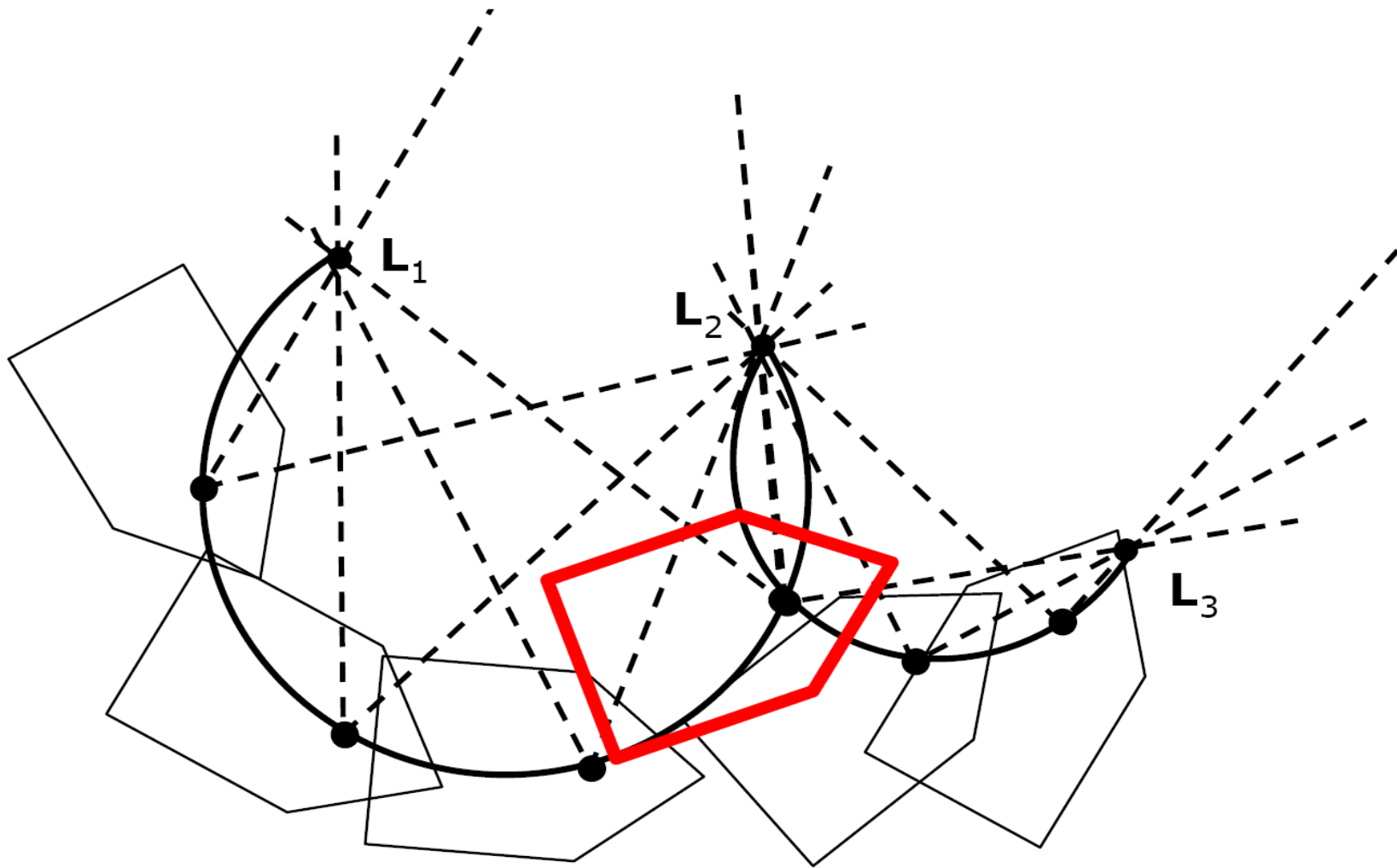
# Triangulation from bearings

2 bearings disambiguate to an arc:



# Triangulation from bearings

3 bearings disambiguate to a pose:





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# Reading

- **Chapter 5. Mobile Robot Localization.**

