

## Homework 2

X[, 1] = variety, X[, 2] = feedback, X[, 3] = autonomy

> smlm

Career:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	3.13428	23.42280	0.134	0.8962
X[, 1]	-0.07783	0.21807	-0.357	0.7286
X[, 2]	0.36484	0.17407	2.096	0.0625
X[, 3]	0.65943	0.34497	1.912	0.0850

Residual standard error: 16.6 on 10 degrees of freedom  
Multiple R-squared: 0.4912, Adjusted R-squared: 0.3385  
F-statistic: 3.218 on 3 and 10 DF, p-value: 0.06994

Supervisor:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-82.2718	23.0723	-3.566	0.00513
X[, 1]	-0.1363	0.2148	-0.634	0.54006
X[, 2]	0.5273	0.1715	3.075	0.01174
X[, 3]	1.5164	0.3398	4.463	0.00121

Residual standard error: 16.35 on 10 degrees of freedom  
Multiple R-squared: 0.7874, Adjusted R-squared: 0.7236  
F-statistic: 12.34 on 3 and 10 DF, p-value: 0.001067

Finance:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	2.35168	3.16314	0.743	0.474
X[, 1]	0.02639	0.02945	0.896	0.391
X[, 2]	-0.00976	0.02351	-0.415	0.687
X[, 3]	0.03133	0.04659	0.672	0.517

Residual standard error: 2.242 on 10 degrees of freedom  
Multiple R-squared: 0.2077, Adjusted R-squared: -0.02994  
F-statistic: 0.874 on 3 and 10 DF, p-value: 0.4866

- H.2.1:

- (a) Overall F-Test

- i. Career,  $j = 1$ :

- I. We can see that response career (Y) has an  $R^2$  value of 49%. This states that 49% of the variability in career is explained by the predictor's variety, feedback and autonomy.
      - II.  $H_0: \beta_{k1} = 0$  for all  $k = 1, 2, 3$ ,  $H_1: \beta_{k1} \neq 0$  for some  $k = 1, 2, 3$
      - III. Since  $F(3, 10) = 3.22$  with a p-value  $> 0.05$ , we fail to reject  $H_0$  at the 0.05 level. We cannot declare  $\beta_{k1} \neq 0$  for some  $k =$

1,2,3. Thus, there is no evidence of a linear association in the population between control and at least one of the predictors variety, feedback and autonomy.

ii. Supervisor,  $j = 2$ :

- I. We can see that response career (Y) has an  $R^2$  value of 79%. This states that 79% of the variability in career is explained by the predictor's variety, feedback and autonomy.
- II.  $H_0: \beta_{k2} = 0$  for all  $k = 1, 2, 3$ ,  $H_1: \beta_{k2} \neq 0$  for some  $k = 1, 2, 3$
- III. Since  $F(3, 10) = 12.34$  with a p-value  $< 0.05$ , we can reject  $H_0$  at the 0.05 level in favor of  $H_1$ . We will declare  $\beta_{k2} \neq 0$  for some  $k = 1, 2, 3$ . Thus, there is a linear association in the population between supervisor and at least one of the predictors variety, feedback and autonomy.

iii. Finance,  $j = 3$ :

- I. We can see that response career (Y) has an  $R^2$  value of 21%. This states that 21% of the variability in career is explained by the predictor's variety, feedback and autonomy.
- II.  $H_0: \beta_{k3} = 0$  for all  $k = 1, 2, 3$ ,  $H_1: \beta_{k3} \neq 0$  for some  $k = 1, 2, 3$
- III. Since  $F(3, 10) = 0.874$  with a p-value  $> 0.05$ , we fail to reject  $H_0$  at the 0.05 level. We cannot declare  $\beta_{k3} \neq 0$  for some  $k = 1, 2, 3$ . Thus, there is no evidence of a linear association in the population between control and at least one of the predictors variety, feedback and autonomy.

Term: X[, 1] = variety

	career	supervisor	finance
career	35.09822	61.45477	-11.902832
supervisor	61.45477	107.60342	-20.841109
finance	-11.90283	-20.84111	4.036599

	Df	test stat	approx F	num Df	den Df	Pr(>F)
Pillai	1	0.1271423	0.3884322	3	8	0.7646
Wilks	1	0.8728577	0.3884322	3	8	0.7646
Hotelling-Lawley	1	0.1456621	0.3884322	3	8	0.7646
Roy	1	0.1456621	0.3884322	3	8	0.7646

Term: X[, 2] = feedback

	career	supervisor	finance
career	1210.46476	1749.33620	-32.3801474
supervisor	1749.33620	2528.10097	-46.7950541
finance	-32.38015	-46.79505	0.8661747

	Df	test stat	approx F	num Df	den Df	Pr(>F)
Pillai	1	0.6248958	4.442469	3	8	0.040722
Wilks	1	0.3751042	4.442469	3	8	0.040722
Hotelling-Lawley	1	1.6659258	4.442469	3	8	0.040722
Roy	1	1.6659258	4.442469	3	8	0.040722

Term: X[, 3] = autonomy

	career	supervisor	finance
career	1006.86284	2315.3990	47.831668
supervisor	2315.39903	5324.5313	109.994522
finance	47.83167	109.9945	2.272274

	Df	test stat	approx F	num Df	den Df	Pr(>F)
Pillai	1	0.7336599	7.345596	3	8	0.010981
Wilks	1	0.2663401	7.345596	3	8	0.010981
Hotelling-Lawley	1	2.7545985	7.345596	3	8	0.010981
Roy	1	2.7545985	7.345596	3	8	0.010981

(b) Multivariate test:

i. Variety,  $k = 1$ :

- I.  $H_0 : \beta_{1j} = 0$  for all  $j = 1, 2, 3$ ,  $H_1 : \beta_{1j} \neq 0$  for some  $j = 1, 2, 3$
- II. Since  $F(3, 8) = 0.39$  with a p-value = 0.76, we fail to reject  $H_0$  at the 0.05 level and not in favor of  $H_1$ . We cannot declare  $\beta_{1j} \neq 0$  for some  $j = 1, 2, 3$ . Thus, there is no evidence of a linear association in the population between variety and at least one of the responses career, supervisor and finance.

ii. Feedback,  $k = 2$ :

- I.  $H_0 : \beta_{2j} = 0$  for all  $j = 1, 2, 3$ ,  $H_1 : \beta_{2j} \neq 0$  for some  $j = 1, 2, 3$
- II. Since  $F(3, 8) = 4.44$  and a p-value = 0.04, we can reject  $H_0$  at the 0.05 level in favor of  $H_1$ . We can declare  $\beta_{2j} \neq 0$  for some  $j = 1, 2, 3$ . Thus, there is a linear association in the population between feedback and at least one of the responses career, supervisor and finance.
- iii. Autonomy,  $k = 3$ :
  - I.  $H_0 : \beta_{3j} = 0$  for all  $j = 1, 2, 3$ ,  $H_1 : \beta_{3j} \neq 0$  for some  $j = 1, 2, 3$
  - II. Since  $F(3, 8) = 7.35$  and a p-value = 0.01, we can reject  $H_0$  at the 0.05 level in favor of  $H_1$ . We can declare  $\beta_{3j} \neq 0$  for some  $j = 1, 2, 3$ . Thus, there is a linear association in the population between autonomy and at least one of the responses career, supervisor and finance.

#### F Test for Canonical Correlations (Rao's F Approximation)

	Corr	F	Num df	Den df	Pr(>F)	
CV 1	0.919412	Inf	0.000000	9.4971	NA	#Reject NA = 0#
CV 2	0.418649	2.282996	1.000000	10.0000	0.1617	#Fail to reject#
CV 3	0.113366	0.029198	4.000000	18.0000	0.9982	#fail to reject#

#### Canonical Correlations:

	CV 1	CV 2	CV 3
	0.9194120	0.4186491	0.1133658

#### X Coefficients:

	CV 1	CV 2	CV 3
variety	0.1108295	0.8095098	-0.9071112
feedback	-0.5519543	-0.7721632	-0.4194377
autonomy	-0.8402945	0.1019873	0.8296945

#### Y Coefficients:

	CV 1	CV 2	CV 3
career	-0.30284133	-0.5416140	-1.0407753
supervisor	-0.78536978	0.1305349	0.9084518
finance	-0.05377069	0.9754208	-0.3329223

#### Structural Correlations (Loadings) - X Vars:

	CV 1	CV 2	CV 3
variety	-0.4863184	0.6591844	-0.5735594
feedback	-0.6215686	-0.5452117	-0.5624915
autonomy	-0.8459188	0.4450690	0.2938283

**Structural Correlations (Loadings) - Y Vars:**

	CV 1	CV 2	CV 3
career	<u>-0.7499135</u>	-0.2503382	<u>-0.6123402</u>
supervisor	<u>-0.9644439</u>	0.0361891	0.2617981
finance	-0.2873325	<u>0.8813524</u>	<u>-0.3750441</u>

**Aggregate Redundancy Coefficients (Total Variance Explained):**

X | Y: 0.4345932

Y | X: 0.4954371

	CV 1	CV 2	CV 3
Career	<u>-0.6894795</u>	-0.10480386	-0.06941846
supervisor	<u>-0.8867213</u>	0.01515053	0.02967896
finance	-0.2641769	0.36897740	-0.04251718

	CV 1	CV 2	CV 3
variety	-0.4471269	0.2759670	-0.06502204
feedback	<u>-0.5714777</u>	-0.2282524	-0.06376731
finance	<u>-0.7777478</u>	0.1863277	0.03331009

• H.2.2:

- (a) From the data above we can see that the first canonical correlation value is 0.92. This value represents that there is a strong correlation between are sets of X and Y.
- (b) Test results of canonical correlations:
  - i.  $H_0 : p(1) = p(2) = p(3) = 0, H^{(1)}_1 : p(1) \neq 0, p(2) \neq 0, \text{ or } p(3) \neq 0$
  - ii. (1) Reject  $H^{(1)}_0$ , (2) Fail to Reject  $H^{(2)}_0$ , (3) Fail to Reject  $H^{(3)}_0$
  - iii. We declare 1 population canonical correlation not 0 at the 0.05 level.
- (c) The first canonical variate  $u_1$  consists of the combination of career (-0.30) and supervisor (-0.79). The variate  $u_1$  is higher for employee satisfaction with lower career and supervisor. The first canonical variable  $v_1$  consists of feedback (-0.55) and autonomy (-0.84). The variate  $v_1$  is higher for job characteristics with lower feedback and autonomy.
- (d) The first canonical variable  $V_{(1)}$ , associated with a negative of feedback and autonomy) has a strong negative sample correlation with supervisor (-0.89). The first canonical variable  $U_{(1)}$  (associated with negative of career and supervisor) has moderate negative

sample correlations with feedback (-0.57) and a strong correlation with autonomy (-0.77)

### R Code:

```
> datv = scan()
1: 72 26 9 10 11 70
7: 63 76 7 85 22 93
13: 96 31 7 83 63 73
19: 96 98 6 82 75 97
25: 84 94 6 36 77 97
31: 66 10 5 28 24 75
37: 31 40 9 64 23 75
43: 45 14 2 19 15 50
49: 42 18 6 33 13 70
55: 79 74 4 23 14 90
61: 39 12 2 37 13 70
67: 54 35 3 23 74 53
73: 60 75 5 45 58 83
79: 63 45 5 22 67 53
85:
Read 84 items

> dat = matrix(datv,14,6,byrow=T)
> Y = as.matrix(dat[,1:3]);
> colnames(Y) = c("career","supervisor","finance")
> X = as.matrix(dat[,4:6]);
> colnames(X) = c("variety","feedback","autonomy")
> n = nrow(dat); p = ncol(Y); m = ncol(X);
> R = cor(dat)
> mlm = lm(Y~X[,1]+X[,2]+X[,3])
> smlm = summary(mlm)
> MA = Manova(mlm,test='Wilks')
> SA = summary(MA)

Y = as.matrix(dat[,1:3]);
> Y = as.matrix(dat[,1:3]);
> X = as.matrix(dat[,4:6]);
> n = row(Y); p = ncol(Y); m = ncol(X)
> R = cor(dat); R2 = R^2
> smlm.Y = summary(lm(Y~X))
> smlm.X = summary(lm(X~Y))
> cc = cca(X,Y,xscale=T,yscale=T)
> Ryv = cc$ycrosscorr
> Rxu = cc$xcrosscorr
```